

# **OTAP REFERENCE MANUAL: VERSION 1.0**

**AERODYNAMIC HEATING & THERMAL ANALYSIS DIVISION  
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# AERODYNAMIC HEATING EVALUATION AND THERMAL PROTECTION SYSTEM DESIGN FOR SPACE VEHICLES

## Abstract

*This report brings out features of the TPS design code OTAP (One-dimensional Thermal Analysis Package). This code uses engineering methods for calculating the aerodynamic heat flux over space vehicles during their atmospheric flight. Thermal response of the structure is evaluated by solving one dimensional conduction equation locally for a multi layer structure with suitable boundary conditions, with provisions for charring/ablation/melting at the surface. This code can be used as a tool for the design of thermal protection system for ascent vehicles and re-entry modules.*

## 1. INTRODUCTION

During atmospheric flight which includes ascent as well as re-entry into atmosphere, space vehicles encounter severe thermal environment. The kinetic energy of air is converted into thermal energy and part of this energy is transferred to the body by viscous diffusion. This is known as **Aerodynamic heating**. It is important that the structure, payload and other sensitive equipments are protected from excessive heating by means of a suitable Thermal Protection System (TPS). Design of TPS is a critical aspect of re-entry vehicle design.

Aerodynamic heating analysis involves evaluation of heat flux on the body due to air flow and the thermal response of the structure to this heat flux. These two problems are strictly coupled since the wall conditions affect the flow and vice versa. In practice, these two problems are solved separately in an iterative manner, till the process converges to a consistent solution.

## **2. CONVECTIVE HEAT TRANSFER**

Theoretically, convective heat transfer can be estimated by solving the Navier-Stokes equations, which completely describe the flow field over a body using the conservation laws of mass, momentum and energy. These equations are extremely complex and their numerical solution requires large computer resources. Alternately, when the viscous-inviscid interactions are not strong, one can obtain the flow field from an inviscid, Euler code [1] and use this as input to a Boundary layer code [2] to evaluate the heat flux. These solutions have to be iteratively solved when interactions are predominant. However for design purposes, one can employ approximate methods based on Boundary Layer Theory. These methods give fairly accurate and conservative estimates of heat transfer over a wide range of flow conditions.

### **2.1 Thermal Design of Reentry Vehicles**

Reentry vehicles experience very high velocities and heating rates compared to ascent vehicles. Hypersonic flows are characterized by the following features:

#### **a) Real gas effects**

Gas temperatures after the shock are very high. The perfect gas relations can be used for temperatures up to 1500 K. Beyond this temperature, molecular excitations start. Dissociation of oxygen starts around 2000 K and that of nitrogen starts around 4000 K. Around 4000 K, ionization of oxygen atoms starts and ionization of nitrogen starts around 8000 K. In between certain recombination reactions also take place. A lot of energy changes take place along with these reactions. The constituent gases of the air are in dissociated or ionized state. The flow can be in a chemically equilibrium (infinite reaction rates) or non equilibrium (finite reaction rates) or frozen (no reactions) state depending on the air density and temperature. Roughly the flow may be in chemically frozen state above 80 km. It may be in non-equilibrium state between 80 and 60 km and in equilibrium state between 60 and 40 km. The actual conditions depend on configuration and trajectory. At these elevated temperatures, the thermo physical and transport properties of a gas mixture vary drastically with temperature and pressure. Perfect gas assumptions are no longer valid.

**b) Viscous shock layer**

The entire shock layer becomes viscous. There is no clear demarcation between inviscid and viscous (boundary layer) regions.

**c) Slip conditions**

At high altitudes, the flow becomes rarefied. Continuum hypothesis is strictly not valid. Velocity and temperature show a jump close to the wall. A similar jump occurs at the shock also. Numerical solution of the conservation equations should include the effect of slip boundary conditions. Alternately, one can use Monte-Carlo simulations for estimating the heat transfer in the rarefied regime.

**d) Radiation**

Radiation from the hot gases in the shock layer to the body is significant for high speed flows (velocities more than 10 km/s). This radiation is likely to heat the free stream and changes free stream conditions. Radiation from the shock layer is significant for planetary entry bodies (like Jupiter) or earth reentry bodies from outer planets. At these entry velocities, the gases in the shock layer are in chemically and thermally non-equilibrium state.

**e) Wall catalysis**

A fully catalytic wall promotes recombination reactions, enhancing the wall heat transfer considerably. Therefore re-entry vehicles are generally provided non-catalytic coating to bring down the wall heat transfer.

**f) Diffusion**

Molecular diffusion also plays a role in changing the concentrations of the various species of gases.

All these effects influence the process of heat transfer to the wall significantly. To estimate the heat transfer accurately, one can use a viscous shock layer code [3] or non-equilibrium N-S Code [4]. But these codes cannot be used for routine design computations, as they require a lot of computer time. In the present formulation, simple, reasonably accurate engineering methods are used.

### **3. FORMULATION**

In the present formulation, aerodynamic heating rates are computed using engineering methods based on the local inviscid flow properties. Where ever possible, the inviscid flow field obtained from CFD or wind tunnel measurements is read as an input. Where ever such inputs are not available, approximate inviscid flow properties are computed by the code.

#### **3.1 Shock Relations**

At supersonic speeds, a shock wave is formed over the body, causing an abrupt change in the flow properties. An attached oblique shock is formed in the case of sharp nosed bodies (up to a certain value of the vertex angle) like wedges and cones. A detached bow shock is formed in the case of blunt bodies. Rankine-Hugoniot relations are used to compute the properties across the shock when perfect gas assumptions hold good. For high temperature flows, one dimensional conservation equations are solved using equilibrium air properties from Hansen's tables. In the case of blunt bodies, normal shock relations may be assumed in the vicinity of the stagnation point. Since the heat transfer to the body depends on the properties of the body streamlines, this assumption is justified. Once the properties across the normal shock are known, flow variables on the body are estimated by using isentropic relations along the body streamline. This assumption may not strictly hold for hypersonic flows, since entropy changes occur over the body.

#### **3.2 Approximate Inviscid Flow Field Calculation Methods**

- i. For supersonic flows over blunt bodies, normal shock relating (with equilibrium air properties) are used for computing the stagnations conditions ( $P_o$ ,  $T_o$ ). Newtonian pressure distributions are used along with isentropic relations to get the local flow properties ( $P_e$ ,  $T_e$ ,  $M_e$ ) ([Appendix-A1](#)).
- ii. For subsonic flows, potential flow is assumed for calculating the pressure distribution over the spherical cap and cylinder. Elsewhere free stream conditions are assumed ([Appendix-A2](#)).

- iii. For supersonic flow over sharp wedges, oblique shock relations are used to get the local properties ( $P_e$ ,  $T_e$ ,  $M_e$ ) ([Appendix-A3](#)). If the shock is detached, Newtonian pressure distribution is used to get the local properties.
- iv. For supersonic flows over cones, the inviscid pressure is obtained from curve fits for the cone tables ([Appendix-A2](#)). Local Mach number is calculated from the stagnation pressure (after normal shock) and the local pressure using isentropic relations..

### **3.3 Engineering Heat Transfer Calculation Methods**

- i. Stagnation point heat transfer is calculated using the Fay and Riddell formula [\[5\]](#) ([Appendix-A4](#)). This formula requires the velocity gradient at the stagnation point. This formula is based on boundary layer method for flows in chemical equilibrium/non-equilibrium. This formula also accounts for the molecular diffusion taking place within the boundary layer. The velocity gradient at the stagnation point is an important parameter in this formula. For supersonic flows over a sphere or cylinder, it can be based on Newtonian pressure distribution. For highly blunt body configurations, the experimental velocity gradients can be used [\[6\]](#). Velocity gradient at the stagnation point of the blunt bodies is shown in [Fig. 1, 2 & 3](#). For highly blunt bodies like re-entry capsules (where  $R \gg r$ ), stagnation point velocity gradient is shown in [Fig. 4](#). It is seen from the [Fig. 5](#) that for large values of  $R$ , the velocity gradient reaches the value for flat headed cylinder asymptotically.
- ii. Laminar heat transfer in the stagnation region is calculated using the Lees formula ([Appendix-A5](#)) [\[7\]](#). This formula is applicable for the spherical and conical regions.
- iii. Heat transfer on the cone and cylinder are computed using the Van-Driest formulas for laminar and turbulent flows based on the local Reynolds number ([Appendix-A6](#)) [\[8\]](#). This formula is based on boundary layer flow over a flat plate. Cone rule is applied for correcting the Van-Driest formula for conical flow. The local Reynolds number is reduced by a factor of 3 for laminar flow and a factor of 2 for turbulent flow. No correction is given for the cylindrical part. The heat transfer

rates from Van-Driest formula generally compare well with boundary layer or Navier-Stokes solutions. For re-entry heat flux estimation on cone and flare regions (aft-bodies), Eckert formula [\(Appendix-A7\) \[9\]](#) is used.

- iv. Transition is assumed to begin when the local Reynolds number exceeds  $10^6$  (or the Reynolds number based on momentum thickness  $Re_\theta$  exceeds  $300^\circ$ ). Chen and Thyson correlation [\(Appendix-A8\) \[10\]](#) is used for calculating the transitional phase between laminar and turbulent flow. A weighted average is taken based on the intermittency factor. For ascent vehicles, the flow becomes turbulent right on the nose cap and remains fully turbulent roughly up to 50 km. For reentry vehicles, the flow is laminar from 120 km to about 30 km. Transition studies are more important for re-entry vehicles which experience very high heating rates.
- v. For flows with angle of incidence, the body is treated as an infinite swept cylinder. Heat transfer along the windward generator is calculated using Beckwith and Gallagher's formula [\(Appendix-A9\) \[11\]](#). The laminar formula involves  $\cos \lambda$  factor. The turbulent formula involves a product of  $\cos \lambda$  and  $\sin \lambda$  factors. Both the formula gives zero heat transfer as  $\lambda \rightarrow 90^\circ$ . The turbulent formula gives a peak value for  $\lambda = 30^\circ$ . When the sweep angle  $\lambda = 0$  and flow is laminar, heating is maximum. But the turbulent formula gives zero heat transfer when  $\lambda = 0$ . Therefore in the computations, care must be taken to switch over to the laminar formula when  $\lambda < 10$ .
- vi. For rarefied flows, heat transfer is computed by taking a weighted average between continuum and free molecular values, the weighing factor being based on the Knudsen number. Continuum values are used for  $Kn < 0.01$ , Free molecular formula is used for  $Kn > 10$  and transitional flow is assumed in between [\(Appendix-A10\) \[12, 13\]](#). This approach covers the slip regime also.

### **3.4 Heat transfer in the shock-boundary layer interaction zone and over protrusions**

Whenever shocks interact with the boundary layer (eg: Strap-on core region of launch vehicles, fuselage wing junctions in RLV, fin body interface in sounding rockets, wing elevon interface) the local heat transfer coefficient needs to be augmented. From the literature, it is seen these augmentation factors can be used for design.

$$\frac{h}{h_o} = \begin{cases} \left( \frac{P_1}{P_2} \right)^{0.5}, & \text{Laminar flow} \\ \left( \frac{P_1}{P_2} \right)^{0.8}, & \text{Turbulent flow} \end{cases}$$

where  $\frac{P_1}{P_2}$  is the static pressure ratio across such shocks. Similar factors can be used for protrusions also.

## **4. RADIATION HEAT TRANSFER**

The net heat transfer to the body is computed by subtracting the radiation loss to the surroundings, from the convective heat transfer. Heat loss to the ambient is given by  $q_{\text{rad}} = \epsilon \sigma (T_w^4 - T_{\text{amb}}^4)$ , where  $\epsilon$  is the emissivity of the wall and  $\sigma$  is Stefan-Boltzmann constant.  $T_{\text{amb}}$  is the ambient temperature.

Solar radiation also gives heat input for the body, especially in the upper atmosphere or during orbital phase of a space vehicle; where there is practically no convective heating. The radiative equilibrium temperature attained by the vehicle is given by,  $\epsilon \sigma T^4 = \alpha_s (E_s + E_r + E_d)$  where  $E_s$  is the solar radiation ( $0.1353 \text{ W/cm}^2$ ),  $E_r$  is the reflected solar radiation ( $0.0234 \text{ W/cm}^2$ ) and  $E_d$  is the Earth's re-radiation ( $0.0208 \text{ W/cm}^2$ ). Thus the radiative equilibrium temperature is dependent on the absorptivity  $\alpha_s$  and the emissivity  $\epsilon$ .

At speeds more than the orbital velocities, (as in the case of re-entry from other planets), radiation from the hot gases of the shock layer to the body becomes significant. The radiation from the gases is given by the empirical formulae [14].

$$q_{rad} = 100r_N \left( \frac{V}{10,000} \right)^{8.5} \left( \frac{\rho_{\infty}}{\rho_{SL}} \right)^{1.6} \text{ BTU} / \text{ft}^2 / \text{sec}$$

where  $r_N$  is the nose radius in feet,  $V$  is the free stream velocity ft/s,  $\rho_{\infty}$  is the free stream density and  $\rho_{SL}$  is the sea level density.

## 5. FREE CONVECTION HEAT TRANSFER

While computing the thermal response of the structure, convective heat transfer from the inner surface is to be considered. The following free convection formula is used for estimating the heat transfer coefficient on the inner boundary [\(Appendix-A11\)](#) [15].

$$Nu = \begin{cases} 0.59 (Gr Pr)^{1/4} & (Gr Pr < 10^9) \\ 0.13 (Gr Pr)^{1/3} & (Gr Pr > 10^9) \end{cases}$$

$$Gr = \frac{g \Delta T L^3 \rho^2}{\bar{T} \mu^2}$$

$$\text{where } \Delta T = T - T_{amb} \text{ and } \bar{T} = \frac{(T + T_{amb})}{2}$$



## 6. CONDUCTION HEAT TRANSFER

Aerodynamic heating analysis involves evaluation of heat flux on the body due to air flow and the thermal response of the structure to this heat flux. These two problems are strictly coupled since the wall conditions affect the flow and vice versa. In practice, these two problems are solved separately in an iterative manner, till the process converges to a consistent solution.

### 6.1 One dimensional thermal response of a multi-layer Thermal Protection System with Charring/ Ablation at the surface

The governing equation for the **Char layer** is

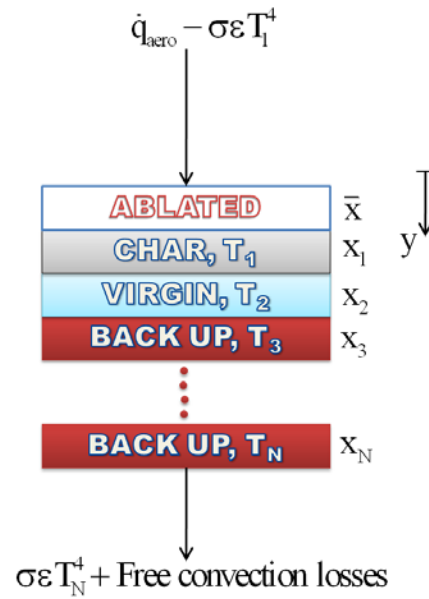
$$\rho_1 C_1 \frac{\partial T_1}{\partial t} = \frac{\partial}{\partial y} \left( k_1 \frac{\partial T_1}{\partial y} \right) + \dot{m}_p C_1 \frac{\partial T_1}{\partial y} \quad (1)$$

$$(\bar{x} \leq y \leq \bar{x} + x_1)$$

Boundary conditions are

$$y = \bar{x} = \int_0^t \frac{\dot{m}_a dt}{\rho_1} \quad (2)$$

$$\dot{q}_{aero} = \sigma \epsilon T_1^4 - k_1 \frac{\partial T_1}{\partial y} + U(T_1 - T_A) \dot{m}_a H_a \quad (3)$$



where  $T_A$  is the ablation temperature and  $U$  is the unit step function.

$$U = \begin{cases} 0, & \text{when } T_1 < T_A \\ 1, & \text{when } T_1 \geq T_A \end{cases}$$

From equation (3),  $\dot{m}_a$  is calculated and from equation (2)  $\bar{x}$  is calculated.

$H_a$  is the heat of ablation.

$\dot{m}_a$  is the ablation mass rate/area.

$$\text{At } y = \bar{x} + x_1, T_1 = T_2 = T_p \quad (4)$$

$T_p$  is the pyrolysis temperature at the Char/virgin interface. Since the interfaces move with time during the process of ablation/charring, the governing equation is written in moving co-ordinate system so that interface conditions are specified easily. Char thickness is given by

$$x_1 = x_1(t=0) + \int_0^t \frac{\dot{m}_p dt}{(\rho_2 - \rho_1)} - \int_0^t \frac{\dot{m}_a dt}{\rho_1} \quad (5)$$

$$-k_1 \frac{\partial T_1}{\partial y} = -k_2 \frac{\partial T_2}{\partial y} + U(T_2 - T_p) \dot{m}_p H_p \quad (6)$$

where  $T_p$  is the pyrolysis temperature and  $H_p$  is the heat of pyrolysis.  $U$  is the unit step function.  $\dot{m}_p$  is calculated from equation (5) and  $x_1$  is calculated from (4)

Virgin thickness is given by

$$x_2 = x_2(t=0) - \int_0^t \frac{\dot{m}_p}{(\rho_2 - \rho_1)} dt \quad (7)$$

The governing equation for the **virgin layer** is

$$\rho_2 C_2 \frac{\partial T_2}{\partial t} = \frac{\partial}{\partial y} \left( k_2 \frac{\partial T_2}{\partial y} \right) \quad (\bar{x} + x_1 \leq y \leq \bar{x} + x_1 + x_2) \quad (8)$$

Boundary Conditions are

At  $y = \bar{x} + x_1$ ,  $T_1 = T_2 = T_p$

$$-k_1 \frac{\partial T_1}{\partial y} = -k_2 \frac{\partial T_2}{\partial y} + U(T_2 - T_p) \dot{m}_p H_p \quad (9)$$

$$\text{At } y = \bar{x} + x_1 + x_2, \quad k_2 \frac{\partial T_2}{\partial y} = k_3 \frac{\partial T_3}{\partial y} \quad (10)$$

The governing equation for **other layers** is

$$\rho_i C_i \frac{\partial T_i}{\partial t} = \frac{\partial}{\partial y} \left( k_i \frac{\partial T_i}{\partial y} \right) \quad (i = 3, \dots, N) \quad (11)$$

with the interface conditions:

$$T_i = T_{i-1} \quad \text{and} \quad k_{i-1} \frac{\partial T_{i-1}}{\partial y} = k_i \frac{\partial T_i}{\partial y}$$

At the last layer, free convection and radiation conditions are imposed at the inner boundary.

The boundary conditions are put in the general form

$$A_1 \frac{\partial T}{\partial x} + A_2 \frac{\partial T}{\partial t} + A_3 T = A_4 \quad (12)$$

By defining A1, A2, A3 and A4 appropriately boundary conditions of the various forms can be obtained (convective, radiative, temperature specified and mixed).

The governing equations for all layers are solved together along with the interface and boundary conditions using implicit central difference scheme [16]. The resulting discretized algebraic equations are tri-diagonal in nature and are solved by a standard procedure (forward sweep and backward substitution) [17, 18].

## 7. Design Cycle

The inputs required for the thermal design and analysis are:

- a) Vehicle configuration (geometry).
- b) Inviscid flow field data (whenever applicable).
- c) Trajectory (Variation of altitude and relative velocity with time).
- d) Material properties.
- e) Nominal Indian Atmosphere 2002 (Table 1) [19].
- f) Equilibrium air properties: The air properties in general depend on the state of the chemical reactions that are taking place. However in the present formulation, only equilibrium heating rates are computed, as they are expected to give conservative estimates for design. Hansen's equilibrium air property model [20] which gives various thermodynamic and transport properties of air as function of temperature and pressure is built into the program. The data is presented in Tables 2, 3, 4, 5, 6, 7 and 8. External TPS design criteria adopted is described in Annexure –B1:

## **8. PROGRAM OTAP**

**Figures 6 & 7** show the flow chart of OTAP program for heat flux computation and thermal response & TPS design respectively. This section gives details on various input variables, subroutines and output variables for OTAP program.

### **8.1 Input Variables**

Input variables include input cards, geometry description variables, trajectory variables, solution parameters and perturbation/augmentation factors. The significance of all input variables to carry out thermal response analysis is discussed in [Appendix A12](#).

### **8.2 List of Subroutines**

OTAP software consists of a main program with various subroutines. The functions performed by various modules are described in [Appendix A13](#).

### **8.3 Output Variables**

The output variables are described in [Appendix A14](#).

A sample of input and output files is given in [Appendix A15](#).

## **9. VALIDATION**

In order to check the validity of the methods for predicting heat transfer rates, cold wall heat flux distribution computed using the design code 'OTAP' has been compared with those obtained from various sources. The wall temperature is taken as 300 K, for purposes of comparison. The details of these validations are given in the following sections [21, 22]:

### **9.1 Published Data from Calspan 96-in Shock Tunnel**

A laboratory measurements program, performed in the Calspan 96-in Hypersonic Shock Tunnel, provides a database for a re-entry sphere cone configuration with a nose radius of 43.2 mm and a cone angle of 7.8 degrees. The test conditions are : Total temperature of 6000 K, total pressure of 500 atmospheres and Mach Number of 9.3. **Figure 6** gives the comparison of Calspan Shock Tunnel data with the data computed using the present program. The agreement is fairly good.

### **9.2 CFD Computations Using 'UNS2D'**

Laminar heat flux distribution over SRE Module for various flow conditions were computed using a Navier-Stokes solver 'UNS2D' where equilibrium air properties were considered. The results computed using 'OTAP' and 'UNS2D' are compared. Figure 7 shows the comparison of heat flux for  $M = 15$  and altitude 42 km and there is fairly good agreement between the results.

### **9.3 CFD Computations Using 'PARAS-3D'**

Heat flux distribution over SRE for  $M=20.0$  and altitude 51 km computed using 'OTAP' and 'PARAS-3D' is compared in figure 8. It is seen that 'OTAP' heat flux values are marginally higher than fully catalytic heat flux values computed using 'PARAS-3D', on the spherical cap whereas these are marginally lower on the cone and flare.

### **9.4 Comparison with various flight measurements**

Design software code OTAP has been used for estimation of heat flux and thermal response on Heat Shield of GSLV FO4 and silica tile of SRE 1 mission. A fairly

good comparison between the measured and computed temperatures as shown in [Figures 9, 10, 11 and 12](#) validates design code OTAP.

## **10. CONCLUDING REMARKS**

A detailed reference manual for OTAP (One-dimensional Thermal Analysis Package) has been brought out. It includes details on different engineering methods used for heat flux estimation for various geometries. Thermal response of a multi-layer TPS (charring/ablating surface) with boundary conditions is described with mathematical formulation.

Design cycle and the philosophy adopted for TPS design of launch vehicles and re-entering modules are also addressed in this manual.

List of different subroutines used in the program along with significance of input variables, output variables is described. Sample input and sample output calculations using the program are also included in this reference manual.

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**TABLE - 1**  
**Nominal Indian Atmosphere 2002**

| Altitude<br>(km) | Temperature<br>(K) | Pressure<br>(Pa) | Density<br>(kg/m <sup>3</sup> ) | Altitude<br>(km) | Temperature<br>(K) | Pressure<br>(Pa) | Density<br>(kg/m <sup>3</sup> ) |
|------------------|--------------------|------------------|---------------------------------|------------------|--------------------|------------------|---------------------------------|
| 0                | 300.7              | 1.01E+05         | 1.17E+00                        | 39               | 254.2              | 3.48E+02         | 4.77E-03                        |
| 1                | 294.6              | 9.00E+04         | 1.06E+00                        | 40               | 256.6              | 3.05E+02         | 4.14E-03                        |
| 2                | 288.4              | 8.01E+04         | 9.67E-01                        | 41               | 258.9              | 2.68E+02         | 3.60E-03                        |
| 3                | 283.6              | 7.11E+04         | 8.73E-01                        | 42               | 260.6              | 2.35E+02         | 3.14E-03                        |
| 4                | 278.4              | 6.30E+04         | 7.88E-01                        | 43               | 262                | 2.07E+02         | 2.75E-03                        |
| 5                | 272.9              | 5.57E+04         | 7.11E-01                        | 44               | 262.9              | 1.82E+02         | 2.41E-03                        |
| 6                | 267.2              | 4.91E+04         | 6.40E-01                        | 45               | 263.8              | 1.60E+02         | 2.12E-03                        |
| 7                | 261.4              | 4.31E+04         | 5.75E-01                        | 46               | 264.4              | 1.41E+02         | 1.86E-03                        |
| 8                | 254.9              | 3.78E+04         | 5.17E-01                        | 47               | 264.7              | 1.24E+02         | 1.64E-03                        |
| 9                | 247.9              | 3.30E+04         | 4.64E-01                        | 48               | 264.6              | 1.09E+02         | 1.44E-03                        |
| 10               | 240.4              | 2.87E+04         | 4.17E-01                        | 49               | 264.1              | 9.64E+01         | 1.27E-03                        |
| 11               | 232.4              | 2.49E+04         | 3.73E-01                        | 50               | 263.5              | 8.49E+01         | 1.12E-03                        |
| 12               | 224.2              | 2.15E+04         | 3.33E-01                        | 51               | 262.5              | 7.47E+01         | 9.92E-04                        |
| 13               | 215.9              | 1.84E+04         | 2.97E-01                        | 52               | 261                | 6.57E+01         | 8.78E-04                        |
| 14               | 207.7              | 1.57E+04         | 2.63E-01                        | 53               | 258.9              | 5.78E+01         | 7.78E-04                        |
| 15               | 200.8              | 1.33E+04         | 2.30E-01                        | 54               | 256.4              | 5.07E+01         | 6.89E-04                        |
| 16               | 195.6              | 1.12E+04         | 1.99E-01                        | 55               | 253.6              | 4.45E+01         | 6.11E-04                        |
| 17               | 194.2              | 9.40E+03         | 1.69E-01                        | 56               | 251.1              | 3.90E+01         | 5.41E-04                        |
| 18               | 197.3              | 7.90E+03         | 1.40E-01                        | 57               | 248.5              | 3.41E+01         | 4.78E-04                        |
| 19               | 201.7              | 6.67E+03         | 1.15E-01                        | 58               | 245.3              | 2.98E+01         | 4.23E-04                        |
| 20               | 206.6              | 5.65E+03         | 9.53E-02                        | 59               | 241.7              | 2.59E+01         | 3.74E-04                        |
| 21               | 209.1              | 4.80E+03         | 7.99E-02                        | 60               | 238                | 2.26E+01         | 3.30E-04                        |
| 22               | 212.2              | 4.09E+03         | 6.71E-02                        | 61               | 234.1              | 1.96E+01         | 2.91E-04                        |
| 23               | 215.5              | 3.49E+03         | 5.64E-02                        | 62               | 230.3              | 1.70E+01         | 2.57E-04                        |
| 24               | 218.8              | 2.99E+03         | 4.75E-02                        | 63               | 226.9              | 1.47E+01         | 2.25E-04                        |
| 25               | 221.3              | 2.56E+03         | 4.03E-02                        | 64               | 223.5              | 1.26E+01         | 1.97E-04                        |
| 26               | 223.8              | 2.20E+03         | 3.42E-02                        | 65               | 220.4              | 1.09E+01         | 1.72E-04                        |
| 27               | 226                | 1.89E+03         | 2.92E-02                        | 66               | 217.3              | 9.33E+00         | 1.50E-04                        |
| 28               | 228                | 1.63E+03         | 2.49E-02                        | 67               | 213.9              | 7.99E+00         | 1.30E-04                        |
| 29               | 230.3              | 1.41E+03         | 2.13E-02                        | 68               | 210.2              | 6.83E+00         | 1.13E-04                        |
| 30               | 232.4              | 1.22E+03         | 1.82E-02                        | 69               | 207.3              | 5.82E+00         | 9.78E-05                        |
| 31               | 234.4              | 1.05E+03         | 1.56E-02                        | 70               | 204.8              | 4.95E+00         | 8.42E-05                        |
| 32               | 236.3              | 9.12E+02         | 1.34E-02                        | 71               | 203.5              | 4.20E+00         | 7.20E-05                        |
| 33               | 238.4              | 7.91E+02         | 1.16E-02                        | 72               | 201.7              | 3.57E+00         | 6.16E-05                        |
| 34               | 240.7              | 6.87E+02         | 9.95E-03                        | 73               | 199.5              | 3.02E+00         | 5.28E-05                        |
| 35               | 243.4              | 5.98E+02         | 8.56E-03                        | 74               | 197                | 2.56E+00         | 4.49E-05                        |
| 36               | 246.1              | 5.21E+02         | 7.38E-03                        | 75               | 194.4              | 2.16E+00         | 3.87E-05                        |
| 37               | 248.9              | 4.55E+02         | 6.36E-03                        | 76               | 193.4              | 1.82E+00         | 3.27E-05                        |
| 38               | 251.7              | 3.98E+02         | 5.50E-03                        | 77               | 191.4              | 1.53E+00         | 2.78E-05                        |

| Altitude<br>(km) | Temperature<br>(K) | Pressure<br>(Pa) | Density<br>(kg/m <sup>3</sup> ) |
|------------------|--------------------|------------------|---------------------------------|
| 78               | 190.6              | 1.28E+00         | 2.35E-05                        |
| 79               | 188.4              | 1.08E+00         | 1.99E-05                        |
| 80               | 187.1              | 9.03E-01         | 1.68E-05                        |
| 81               | 185.6              | 8.51E-01         | 1.48E-05                        |
| 82               | 184.1              | 7.18E-01         | 1.25E-05                        |
| 83               | 182.8              | 6.06E-01         | 1.06E-05                        |
| 84               | 181.5              | 5.11E-01         | 9.01E-06                        |
| 85               | 180.3              | 4.30E-01         | 7.64E-06                        |
| 86               | 179.2              | 3.62E-01         | 6.47E-06                        |
| 87               | 178.2              | 3.04E-01         | 5.48E-06                        |
| 88               | 177.3              | 2.55E-01         | 4.64E-06                        |
| 89               | 176.5              | 2.14E-01         | 3.92E-06                        |
| 90               | 175.7              | 1.79E-01         | 3.32E-06                        |
| 91               | 175                | 1.49E-01         | 2.80E-06                        |
| 92               | 174.5              | 1.24E-01         | 2.36E-06                        |
| 93               | 174                | 1.04E-01         | 1.99E-06                        |
| 94               | 173.6              | 8.60E-02         | 1.67E-06                        |
| 95               | 173.3              | 7.14E-02         | 1.40E-06                        |
| 96               | 173.1              | 5.92E-02         | 1.16E-06                        |
| 97               | 173                | 4.90E-02         | 9.67E-07                        |
| 98               | 172.9              | 4.07E-02         | 8.00E-07                        |
| 99               | 173.4              | 3.37E-02         | 6.60E-07                        |
| 100              | 174.8              | 2.81E-02         | 5.43E-07                        |
| 101              | 177.1              | 2.34E-02         | 4.45E-07                        |
| 102              | 180.4              | 1.96E-02         | 3.65E-07                        |
| 103              | 184.7              | 1.65E-02         | 2.99E-07                        |
| 104              | 189.9              | 1.39E-02         | 2.45E-07                        |
| 105              | 196                | 1.18E-02         | 2.01E-07                        |
| 106              | 203                | 1.01E-02         | 1.65E-07                        |
| 107              | 210.9              | 8.70E-03         | 1.36E-07                        |
| 108              | 219.8              | 7.54E-03         | 1.13E-07                        |
| 109              | 229.5              | 6.58E-03         | 9.39E-08                        |
| 110              | 239.9              | 5.78E-03         | 7.85E-08                        |
| 111              | 251                | 5.11E-03         | 6.61E-08                        |
| 112              | 262.7              | 4.54E-03         | 5.59E-08                        |
| 113              | 275                | 4.06E-03         | 4.76E-08                        |
| 114              | 288                | 3.65E-03         | 4.07E-08                        |
| 115              | 301.6              | 3.30E-03         | 3.50E-08                        |
| 116              | 315.8              | 3.00E-03         | 3.02E-08                        |
| 117              | 330.5              | 2.74E-03         | 2.63E-08                        |
| 118              | 345.8              | 2.51E-03         | 2.29E-08                        |
| 119              | 361.4              | 2.31E-03         | 2.01E-08                        |
| 120              | 377.3              | 2.14E-03         | 1.78E-08                        |
| 121              | 393.3              | 1.98E-03         | 1.58E-08                        |

| Altitude<br>(km) | Temperature<br>(K) | Pressure<br>(Pa) | Density<br>(kg/m <sup>3</sup> ) |
|------------------|--------------------|------------------|---------------------------------|
| 122              | 409.1              | 1.85E-03         | 1.40E-08                        |
| 123              | 424.6              | 1.72E-03         | 1.26E-08                        |
| 124              | 439.7              | 1.61E-03         | 1.13E-08                        |
| 125              | 454.4              | 1.51E-03         | 1.03E-08                        |
| 126              | 468.7              | 1.42E-03         | 9.31E-09                        |
| 127              | 482.6              | 1.34E-03         | 8.49E-09                        |
| 128              | 496.2              | 1.26E-03         | 7.77E-09                        |
| 129              | 509.4              | 1.19E-03         | 7.13E-09                        |
| 130              | 522.3              | 1.13E-03         | 6.57E-09                        |
| 131              | 534.8              | 1.07E-03         | 6.06E-09                        |
| 132              | 547.1              | 1.02E-03         | 5.61E-09                        |
| 133              | 559                | 9.67E-04         | 5.20E-09                        |
| 134              | 570.6              | 9.20E-04         | 4.84E-09                        |
| 135              | 581.9              | 8.76E-04         | 4.51E-09                        |
| 136              | 592.9              | 8.35E-04         | 4.21E-09                        |
| 137              | 603.6              | 7.97E-04         | 3.94E-09                        |
| 138              | 614.1              | 7.62E-04         | 3.69E-09                        |
| 139              | 624.3              | 7.28E-04         | 3.46E-09                        |
| 140              | 634.2              | 6.97E-04         | 3.25E-09                        |
| 141              | 643.9              | 6.68E-04         | 3.06E-09                        |
| 142              | 653.3              | 6.40E-04         | 2.88E-09                        |
| 143              | 662.5              | 6.14E-04         | 2.72E-09                        |
| 144              | 671.4              | 5.89E-04         | 2.57E-09                        |
| 145              | 680.1              | 5.66E-04         | 2.43E-09                        |
| 146              | 688.6              | 5.44E-04         | 2.30E-09                        |
| 147              | 696.9              | 5.23E-04         | 2.18E-09                        |
| 148              | 705                | 5.03E-04         | 2.07E-09                        |
| 149              | 712.8              | 4.84E-04         | 1.96E-09                        |
| 150              | 720.5              | 4.66E-04         | 1.87E-09                        |
| 151              | 727.9              | 4.49E-04         | 1.78E-09                        |
| 152              | 735.2              | 4.33E-04         | 1.69E-09                        |
| 153              | 742.3              | 4.17E-04         | 1.61E-09                        |
| 154              | 749.2              | 4.03E-04         | 1.54E-09                        |
| 155              | 755.9              | 3.89E-04         | 1.47E-09                        |
| 156              | 762.5              | 3.75E-04         | 1.40E-09                        |
| 157              | 768.8              | 3.62E-04         | 1.34E-09                        |
| 158              | 775.1              | 3.50E-04         | 1.28E-09                        |
| 159              | 781.1              | 3.39E-04         | 1.23E-09                        |
| 160              | 787                | 3.27E-04         | 1.17E-09                        |
| 161              | 792.8              | 3.17E-04         | 1.13E-09                        |
| 162              | 798.4              | 3.06E-04         | 1.08E-09                        |
| 163              | 803.9              | 2.97E-04         | 1.03E-09                        |
| 164              | 809.2              | 2.87E-04         | 9.93E-10                        |
| 165              | 814.4              | 2.78E-04         | 9.53E-10                        |

| Altitude<br>(km) | Temperature<br>(K) | Pressure<br>(Pa) | Density<br>(kg/m <sup>3</sup> ) |
|------------------|--------------------|------------------|---------------------------------|
| 166              | 819.4              | 2.69E-04         | 9.15E-10                        |
| 167              | 824.4              | 2.61E-04         | 8.80E-10                        |
| 168              | 829.2              | 2.53E-04         | 8.46E-10                        |
| 169              | 833.9              | 2.45E-04         | 8.14E-10                        |
| 170              | 838.4              | 2.38E-04         | 7.83E-10                        |
| 171              | 842.9              | 2.31E-04         | 7.54E-10                        |
| 172              | 847.2              | 2.24E-04         | 7.26E-10                        |
| 173              | 851.4              | 2.17E-04         | 7.00E-10                        |
| 174              | 855.5              | 2.11E-04         | 6.75E-10                        |
| 175              | 859.6              | 2.05E-04         | 6.51E-10                        |
| 176              | 863.5              | 1.99E-04         | 6.27E-10                        |
| 177              | 867.3              | 1.93E-04         | 6.05E-10                        |
| 178              | 871                | 1.88E-04         | 5.84E-10                        |
| 179              | 874.6              | 1.82E-04         | 5.64E-10                        |
| 180              | 878.1              | 1.77E-04         | 5.45E-10                        |
| 181              | 881.6              | 1.72E-04         | 5.27E-10                        |
| 182              | 884.9              | 1.67E-04         | 5.09E-10                        |
| 183              | 888.2              | 1.63E-04         | 4.92E-10                        |
| 184              | 891.4              | 1.58E-04         | 4.76E-10                        |
| 185              | 894.5              | 1.54E-04         | 4.60E-10                        |
| 186              | 897.5              | 1.50E-04         | 4.45E-10                        |
| 187              | 900.4              | 1.46E-04         | 4.31E-10                        |
| 188              | 903.3              | 1.42E-04         | 4.17E-10                        |
| 189              | 906.1              | 1.38E-04         | 4.04E-10                        |
| 190              | 908.8              | 1.35E-04         | 3.91E-10                        |
| 191              | 911.5              | 1.31E-04         | 3.79E-10                        |
| 192              | 914.1              | 1.28E-04         | 3.67E-10                        |
| 193              | 916.6              | 1.24E-04         | 3.56E-10                        |
| 194              | 919.1              | 1.21E-04         | 3.45E-10                        |
| 195              | 921.5              | 1.18E-04         | 3.34E-10                        |
| 196              | 923.8              | 1.15E-04         | 3.24E-10                        |
| 197              | 926.1              | 1.12E-04         | 3.15E-10                        |
| 198              | 928.3              | 1.09E-04         | 3.05E-10                        |
| 199              | 930.5              | 1.06E-04         | 2.96E-10                        |
| 200              | 932.6              | 1.04E-04         | 2.87E-10                        |
| 210              | 951                | 8.07E-05         | 2.15E-10                        |
| 220              | 965.3              | 6.36E-05         | 1.64E-10                        |
| 230              | 976.3              | 5.05E-05         | 1.26E-10                        |
| 240              | 984.9              | 4.04E-05         | 9.79E-11                        |
| 250              | 991.6              | 3.25E-05         | 7.68E-11                        |
| 260              | 996.8              | 2.63E-05         | 6.08E-11                        |
| 270              | 1000.8             | 2.14E-05         | 4.84E-11                        |
| 280              | 1004               | 1.75E-05         | 3.89E-11                        |
| 290              | 1006.4             | 1.43E-05         | 3.13E-11                        |

| Altitude<br>(km) | Temperature<br>(K) | Pressure<br>(Pa) | Density<br>(kg/m <sup>3</sup> ) |
|------------------|--------------------|------------------|---------------------------------|
| 300              | 1008.3             | 1.18E-05         | 2.54E-11                        |
| 310              | 1009.8             | 9.77E-06         | 2.07E-11                        |
| 320              | 1011               | 8.10E-06         | 1.69E-11                        |
| 330              | 1011.9             | 6.74E-06         | 1.39E-11                        |
| 340              | 1012.6             | 5.62E-06         | 1.15E-11                        |
| 350              | 1013.2             | 4.70E-06         | 9.50E-12                        |
| 360              | 1013.6             | 3.94E-06         | 7.89E-12                        |
| 370              | 1014               | 3.31E-06         | 6.57E-12                        |
| 380              | 1014.2             | 2.79E-06         | 5.48E-12                        |
| 390              | 1014.4             | 2.35E-06         | 4.58E-12                        |
| 400              | 1014.6             | 1.99E-06         | 3.84E-12                        |
| 410              | 1014.7             | 1.68E-06         | 3.23E-12                        |
| 420              | 1014.8             | 1.43E-06         | 2.72E-12                        |
| 430              | 1014.9             | 1.21E-06         | 2.29E-12                        |
| 440              | 1015               | 1.03E-06         | 1.94E-12                        |
| 450              | 1015               | 8.78E-07         | 1.64E-12                        |
| 460              | 1015.1             | 7.49E-07         | 1.39E-12                        |
| 470              | 1015.1             | 6.40E-07         | 1.18E-12                        |
| 480              | 1015.1             | 5.49E-07         | 1.00E-12                        |
| 490              | 1015.1             | 4.71E-07         | 8.50E-13                        |
| 500              | 1015.2             | 4.05E-07         | 7.24E-13                        |
| 510              | 1015.2             | 3.48E-07         | 6.18E-13                        |
| 520              | 1015.2             | 3.01E-07         | 5.27E-13                        |
| 530              | 1015.2             | 2.60E-07         | 4.51E-13                        |
| 540              | 1015.2             | 2.25E-07         | 3.86E-13                        |
| 550              | 1015.2             | 1.96E-07         | 3.31E-13                        |
| 560              | 1015.2             | 1.70E-07         | 2.84E-13                        |
| 570              | 1015.2             | 1.49E-07         | 2.44E-13                        |
| 580              | 1015.2             | 1.30E-07         | 2.10E-13                        |
| 590              | 1015.2             | 1.14E-07         | 1.81E-13                        |
| 600              | 1015.2             | 1.00E-07         | 1.56E-13                        |
| 610              | 1015.2             | 8.85E-08         | 1.34E-13                        |
| 620              | 1015.2             | 7.83E-08         | 1.16E-13                        |
| 630              | 1015.2             | 6.95E-08         | 1.01E-13                        |
| 640              | 1015.2             | 6.20E-08         | 8.74E-14                        |
| 650              | 1015.2             | 5.54E-08         | 7.60E-14                        |
| 660              | 1015.2             | 4.97E-08         | 6.62E-14                        |
| 670              | 1015.2             | 4.48E-08         | 5.78E-14                        |
| 680              | 1015.2             | 4.04E-08         | 5.05E-14                        |
| 690              | 1015.2             | 3.67E-08         | 4.43E-14                        |
| 700              | 1015.2             | 3.34E-08         | 3.89E-14                        |
| 710              | 1015.2             | 3.05E-08         | 3.43E-14                        |
| 720              | 1015.2             | 2.80E-08         | 3.03E-14                        |
| 730              | 1015.2             | 2.57E-08         | 2.68E-14                        |

| Altitude<br>(km) | Temperature<br>(K) | Pressure<br>(Pa) | Density<br>(kg/m <sup>3</sup> ) |
|------------------|--------------------|------------------|---------------------------------|
| 740              | 1015.2             | 2.38E-08         | 2.38E-14                        |
| 750              | 1015.2             | 2.20E-08         | 2.12E-14                        |
| 760              | 1015.2             | 2.05E-08         | 1.89E-14                        |
| 770              | 1015.2             | 1.91E-08         | 1.69E-14                        |
| 780              | 1015.2             | 1.79E-08         | 1.52E-14                        |
| 790              | 1015.2             | 1.68E-08         | 1.37E-14                        |
| 800              | 1015.2             | 1.58E-08         | 1.24E-14                        |
| 810              | 1015.2             | 1.49E-08         | 1.12E-14                        |
| 820              | 1015.2             | 1.41E-08         | 1.02E-14                        |
| 830              | 1015.2             | 1.33E-08         | 9.33E-15                        |
| 840              | 1015.2             | 1.27E-08         | 8.55E-15                        |
| 850              | 1015.2             | 1.20E-08         | 7.85E-15                        |
| 860              | 1015.2             | 1.15E-08         | 7.24E-15                        |
| 870              | 1015.2             | 1.10E-08         | 6.70E-15                        |

| Altitude<br>(km) | Temperature<br>(K) | Pressure<br>(Pa) | Density<br>(kg/m <sup>3</sup> ) |
|------------------|--------------------|------------------|---------------------------------|
| 880              | 1015.2             | 1.05E-08         | 6.21E-15                        |
| 890              | 1015.2             | 1.00E-08         | 5.78E-15                        |
| 900              | 1015.2             | 9.63E-09         | 5.39E-15                        |
| 910              | 1015.2             | 9.25E-09         | 5.04E-15                        |
| 920              | 1015.2             | 8.90E-09         | 4.73E-15                        |
| 930              | 1015.2             | 8.57E-09         | 4.45E-15                        |
| 940              | 1015.2             | 8.26E-09         | 4.19E-15                        |
| 950              | 1015.2             | 7.97E-09         | 3.96E-15                        |
| 960              | 1015.2             | 7.69E-09         | 3.75E-15                        |
| 970              | 1015.2             | 7.43E-09         | 3.56E-15                        |
| 980              | 1015.2             | 7.19E-09         | 3.38E-15                        |
| 990              | 1015.2             | 6.96E-09         | 3.21E-15                        |
| 1000             | 1015.2             | 6.74E-09         | 3.06E-15                        |

**TABLE - 2**  
**Variation of Cp (J/kg K) with Pressure & Temperature**

| Temp(K) | PRESSURE (atm) |         |         |         |         |         |         |
|---------|----------------|---------|---------|---------|---------|---------|---------|
|         | 100            | 10      | 1       | 0.1     | 0.01    | 0.001   | 0.0001  |
| 500     | 1030.3         | 1030.3  | 1030.3  | 1030.3  | 1030.3  | 1030.3  | 1030.3  |
| 1000    | 1136.5         | 1136.5  | 1136.5  | 1136.5  | 1136.5  | 1136.5  | 1136.5  |
| 1500    | 1205.4         | 1205.4  | 1205.4  | 1205.4  | 1208.3  | 1214.0  | 1231.2  |
| 2000    | 1245.6         | 1248.4  | 1265.7  | 1311.6  | 1463.7  | 1931.5  | 3320.6  |
| 2500    | 1294.4         | 1360.4  | 1567.0  | 2189.8  | 3897.5  | 6888.0  | 5748.6  |
| 3000    | 1443.6         | 1788.0  | 2760.9  | 4775.7  | 5068.4  | 2261.6  | 1552.7  |
| 3500    | 1799.5         | 2726.5  | 4276.3  | 3533.0  | 1868.4  | 1905.7  | 3068.0  |
| 4000    | 2364.9         | 3578.9  | 3171.4  | 1983.2  | 2436.6  | 4724.0  | 11703.9 |
| 4500    | 2904.4         | 3174.2  | 2189.8  | 2758.1  | 5648.2  | 14080.2 | 29127.6 |
| 5000    | 3022.1         | 2459.6  | 2749.5  | 5447.3  | 13265.1 | 25020.7 | 13629.6 |
| 5500    | 2743.7         | 2600.2  | 4548.9  | 10687.9 | 20864.9 | 12794.5 | 3679.3  |
| 6000    | 2597.4         | 3553.1  | 7734.7  | 16531.2 | 14169.2 | 4350.9  | 3280.4  |
| 6500    | 2884.4         | 5255.0  | 11804.3 | 15604.2 | 5912.2  | 3375.1  | 5490.3  |
| 7000    | 3587.5         | 7605.5  | 14235.2 | 8948.7  | 3699.4  | 4701.1  | 10567.3 |
| 7500    | 4729.8         | 10099.5 | 12252.0 | 4970.8  | 4015.1  | 7754.7  | 20095.7 |
| 8000    | 6147.5         | 11574.7 | 8113.5  | 3926.2  | 5567.8  | 13092.9 | 34899.2 |
| 8500    | 7662.9         | 10946.2 | 5332.5  | 4279.2  | 8279.9  | 21329.8 | 49754.3 |
| 9000    | 8911.4         | 8719.1  | 4256.2  | 5424.3  | 12372.6 | 31989.0 | 49742.8 |
| 9500    | 9442.3         | 6457.5  | 4204.6  | 7249.6  | 17992.0 | 41310.8 | 32993.5 |
| 10000   | 9020.4         | 5011.0  | 4744.1  | 9789.6  | 24805.4 | 42217.7 | 17303.2 |
| 10500   | 7881.0         | 4359.5  | 5699.8  | 13067.1 | 31380.6 | 32936.1 | 9181.1  |
| 11000   | 9419.3         | 4256.2  | 7020.0  | 17004.8 | 34950.9 | 21094.5 | 5717.0  |
| 11500   | 5441.5         | 4508.8  | 8687.5  | 21266.7 | 33142.8 | 12679.7 | 4284.9  |
| 12000   | 4703.9         | 5008.2  | 10685.0 | 25132.6 | 26800.1 | 8010.2  | 3679.3  |
| 12500   | 4307.9         | 5705.6  | 12963.8 | 27554.9 | 19332.3 | 5645.3  | 3412.4  |
| 13000   | 4181.6         | 6569.4  | 15411.9 | 27595.0 | 13302.5 | 4465.7  | 3291.9  |
| 13500   | 4247.6         | 7582.5  | 17828.4 | 25138.3 | 9270.1  | 3871.6  | 3231.6  |
| 14000   | 4454.2         | 8727.7  | 19920.7 | 21071.5 | 6807.6  | 3561.7  | 3202.9  |
| 14500   | 4769.9         | 9979.0  | 21341.3 | 16733.8 | 5355.4  | 3395.2  | 3185.7  |
| 15000   | 5171.7         | 11299.2 | 21797.7 | 12814.6 | 4505.9  | 3303.4  | 3180.0  |

**TABLE-3**  
**Variation of GAMA with Pressure & Temperature**

| Temp(K) | PRESSURE (atm) |       |       |       |       |       |        |
|---------|----------------|-------|-------|-------|-------|-------|--------|
|         | 100            | 10    | 1     | 0.1   | 0.01  | 0.001 | 0.0001 |
| 500     | 1.387          | 1.387 | 1.387 | 1.387 | 1.387 | 1.387 | 1.387  |
| 1000    | 1.337          | 1.337 | 1.337 | 1.337 | 1.337 | 1.337 | 1.337  |
| 1500    | 1.312          | 1.312 | 1.312 | 1.312 | 1.312 | 1.31  | 1.306  |
| 2000    | 1.3            | 1.299 | 1.296 | 1.286 | 1.26  | 1.209 | 1.153  |
| 2500    | 1.288          | 1.277 | 1.249 | 1.202 | 1.161 | 1.152 | 1.157  |
| 3000    | 1.266          | 1.235 | 1.195 | 1.178 | 1.181 | 1.239 | 1.304  |
| 3500    | 1.241          | 1.211 | 1.202 | 1.212 | 1.27  | 1.252 | 1.176  |
| 4000    | 1.23           | 1.223 | 1.23  | 1.26  | 1.213 | 1.15  | 1.133  |
| 4500    | 1.24           | 1.243 | 1.251 | 1.204 | 1.154 | 1.155 | 1.19   |
| 5000    | 1.256          | 1.252 | 1.212 | 1.166 | 1.172 | 1.203 | 1.168  |
| 5500    | 1.262          | 1.231 | 1.183 | 1.182 | 1.214 | 1.183 | 1.257  |
| 6000    | 1.253          | 1.206 | 1.19  | 1.221 | 1.202 | 1.237 | 1.266  |
| 6500    | 1.235          | 1.201 | 1.22  | 1.228 | 1.217 | 1.265 | 1.188  |
| 7000    | 1.223          | 1.217 | 1.246 | 1.216 | 1.258 | 1.21  | 1.155  |
| 7500    | 1.223          | 1.243 | 1.244 | 1.237 | 1.237 | 1.173 | 1.164  |
| 8000    | 1.235          | 1.264 | 1.235 | 1.252 | 1.201 | 1.168 | 1.201  |
| 8500    | 1.255          | 1.267 | 1.243 | 1.235 | 1.183 | 1.188 | 1.242  |
| 9000    | 1.275          | 1.26  | 1.252 | 1.213 | 1.185 | 1.224 | 1.244  |
| 9500    | 1.288          | 1.255 | 1.248 | 1.201 | 1.203 | 1.256 | 1.216  |
| 10000   | 1.291          | 1.259 | 1.236 | 1.201 | 1.232 | 1.263 | 1.211  |
| 10500   | 1.287          | 1.262 | 1.226 | 1.213 | 1.263 | 1.244 | 1.256  |
| 11000   | 1.282          | 1.261 | 1.222 | 1.233 | 1.281 | 1.23  | 1.339  |
| 11500   | 1.28           | 1.256 | 1.226 | 1.258 | 1.28  | 1.243 | 1.427  |
| 12000   | 1.282          | 1.252 | 1.236 | 1.283 | 1.267 | 1.288 | 1.491  |
| 12500   | 1.284          | 1.25  | 1.251 | 1.301 | 1.257 | 1.352 | 1.528  |
| 13000   | 1.285          | 1.251 | 1.271 | 1.307 | 1.263 | 1.419 | 1.548  |
| 13500   | 1.284          | 1.257 | 1.291 | 1.303 | 1.288 | 1.472 | 1.558  |
| 14000   | 1.284          | 1.266 | 1.311 | 1.295 | 1.329 | 1.509 | 1.563  |
| 14500   | 1.284          | 1.278 | 1.326 | 1.29  | 1.377 | 1.532 | 1.565  |
| 15000   | 1.286          | 1.293 | 1.336 | 1.293 | 1.425 | 1.547 | 1.567  |

**TABLE-4**  
**Variation of ENTHALPY (J/kg) with Pressure & Temperature**

| Temp(K) | PRESSURE (atm) |           |           |           |           |           |           |
|---------|----------------|-----------|-----------|-----------|-----------|-----------|-----------|
|         | 100            | 10        | 1         | 0.1       | 0.01      | 0.001     | 0.0001    |
| 500     | 5.051E+05      | 5.051E+05 | 5.051E+05 | 5.051E+05 | 5.051E+05 | 5.051E+05 | 5.051E+05 |
| 1000    | 1.048E+06      | 1.048E+06 | 1.048E+06 | 1.048E+06 | 1.048E+06 | 1.048E+06 | 1.048E+06 |
| 1500    | 1.636E+06      | 1.636E+06 | 1.636E+06 | 1.636E+06 | 1.636E+06 | 1.636E+06 | 1.636E+06 |
| 2000    | 2.250E+06      | 2.250E+06 | 2.250E+06 | 2.256E+06 | 2.279E+06 | 2.336E+06 | 2.531E+06 |
| 2500    | 2.877E+06      | 2.892E+06 | 2.935E+06 | 3.064E+06 | 3.451E+06 | 4.420E+06 | 5.754E+06 |
| 3000    | 3.556E+06      | 3.659E+06 | 3.969E+06 | 4.779E+06 | 6.139E+06 | 6.905E+06 | 7.052E+06 |
| 3500    | 4.360E+06      | 4.771E+06 | 5.776E+06 | 7.112E+06 | 7.654E+06 | 7.805E+06 | 8.066E+06 |
| 4000    | 5.396E+06      | 6.383E+06 | 7.738E+06 | 8.357E+06 | 8.644E+06 | 9.287E+06 | 1.127E+07 |
| 4500    | 6.716E+06      | 8.124E+06 | 9.015E+06 | 9.467E+06 | 1.051E+07 | 1.363E+07 | 2.170E+07 |
| 5000    | 8.223E+06      | 9.500E+06 | 1.019E+07 | 1.142E+07 | 1.504E+07 | 2.394E+07 | 3.367E+07 |
| 5500    | 9.676E+06      | 1.073E+07 | 1.197E+07 | 1.536E+07 | 2.390E+07 | 3.406E+07 | 3.722E+07 |
| 6000    | 1.099E+07      | 1.224E+07 | 1.498E+07 | 2.227E+07 | 3.323E+07 | 3.783E+07 | 3.881E+07 |
| 6500    | 1.235E+07      | 1.440E+07 | 1.985E+07 | 3.071E+07 | 3.796E+07 | 3.962E+07 | 4.091E+07 |
| 7000    | 1.396E+07      | 1.760E+07 | 2.652E+07 | 3.685E+07 | 4.020E+07 | 4.157E+07 | 4.460E+07 |
| 7500    | 1.601E+07      | 2.204E+07 | 3.332E+07 | 4.017E+07 | 4.206E+07 | 4.460E+07 | 5.222E+07 |
| 8000    | 1.874E+07      | 2.753E+07 | 3.841E+07 | 4.232E+07 | 4.440E+07 | 4.971E+07 | 6.578E+07 |
| 8500    | 2.220E+07      | 3.325E+07 | 4.169E+07 | 4.433E+07 | 4.781E+07 | 5.818E+07 | 8.721E+07 |
| 9000    | 2.635E+07      | 3.820E+07 | 4.401E+07 | 4.673E+07 | 5.293E+07 | 7.145E+07 | 1.130E+08 |
| 9500    | 3.097E+07      | 4.199E+07 | 4.611E+07 | 4.987E+07 | 6.045E+07 | 8.997E+07 | 1.340E+08 |
| 10000   | 3.565E+07      | 4.480E+07 | 4.833E+07 | 5.410E+07 | 7.112E+07 | 1.113E+08 | 1.463E+08 |
| 10500   | 3.987E+07      | 4.713E+07 | 5.093E+07 | 5.979E+07 | 8.522E+07 | 1.304E+08 | 1.526E+08 |
| 11000   | 4.347E+07      | 4.925E+07 | 5.410E+07 | 6.728E+07 | 1.020E+08 | 1.439E+08 | 1.562E+08 |
| 11500   | 4.647E+07      | 5.142E+07 | 5.799E+07 | 7.684E+07 | 1.193E+08 | 1.521E+08 | 1.587E+08 |
| 12000   | 4.897E+07      | 5.380E+07 | 6.282E+07 | 8.848E+07 | 1.344E+08 | 1.572E+08 | 1.606E+08 |
| 12500   | 5.123E+07      | 5.647E+07 | 6.874E+07 | 1.017E+08 | 1.459E+08 | 1.605E+08 | 1.624E+08 |
| 13000   | 5.335E+07      | 5.955E+07 | 7.581E+07 | 1.156E+08 | 1.539E+08 | 1.630E+08 | 1.641E+08 |
| 13500   | 5.544E+07      | 6.308E+07 | 8.415E+07 | 1.289E+08 | 1.595E+08 | 1.651E+08 | 1.657E+08 |
| 14000   | 5.762E+07      | 6.714E+07 | 9.358E+07 | 1.405E+08 | 1.635E+08 | 1.669E+08 | 1.673E+08 |
| 14500   | 5.993E+07      | 7.183E+07 | 1.040E+08 | 1.499E+08 | 1.665E+08 | 1.687E+08 | 1.689E+08 |
| 15000   | 6.238E+07      | 7.715E+07 | 1.148E+08 | 1.573E+08 | 1.689E+08 | 1.703E+08 | 1.705E+08 |

**TABLE-5**  
**Variation of Prandtl Number with Pressure & Temperature**

| Temp(K) | PRESSURE (atm) |        |        |        |        |        |        |
|---------|----------------|--------|--------|--------|--------|--------|--------|
|         | 100            | 10     | 1      | 0.1    | 0.01   | 0.001  | 0.0001 |
| 500     | 0.7380         | 0.7380 | 0.7380 | 0.7380 | 0.7380 | 0.7380 | 0.7380 |
| 1000    | 0.7560         | 0.7560 | 0.7560 | 0.7560 | 0.7560 | 0.7560 | 0.7560 |
| 1500    | 0.7670         | 0.7670 | 0.7670 | 0.7670 | 0.7670 | 0.7670 | 0.7670 |
| 2000    | 0.7730         | 0.7730 | 0.7730 | 0.7660 | 0.7240 | 0.6680 | 0.6140 |
| 2500    | 0.7620         | 0.7510 | 0.6960 | 0.6450 | 0.6110 | 0.6540 | 0.7710 |
| 3000    | 0.7400         | 0.6800 | 0.6270 | 0.6360 | 0.7400 | 0.7450 | 0.7140 |
| 3500    | 0.6780         | 0.6310 | 0.6600 | 0.7440 | 0.7370 | 0.6580 | 0.6060 |
| 4000    | 0.6400         | 0.6620 | 0.7620 | 0.7590 | 0.6190 | 0.5800 | 0.5870 |
| 4500    | 0.6540         | 0.7430 | 0.7520 | 0.6100 | 0.5780 | 0.6110 | 0.7640 |
| 5000    | 0.7020         | 0.7670 | 0.6110 | 0.5810 | 0.6240 | 0.7990 | 0.9930 |
| 5500    | 0.7480         | 0.6200 | 0.5830 | 0.6170 | 0.7850 | 0.9890 | 0.8710 |
| 6000    | 0.7630         | 0.5920 | 0.6020 | 0.7360 | 0.9690 | 0.8910 | 0.4550 |
| 6500    | 0.6100         | 0.5920 | 0.6730 | 0.9060 | 0.9550 | 0.4640 | 0.3920 |
| 7000    | 0.5930         | 0.6200 | 0.7960 | 0.9860 | 0.8300 | 0.4040 | 0.3610 |
| 7500    | 0.5950         | 0.6880 | 0.9270 | 0.9690 | 0.4240 | 0.3710 | 0.3420 |
| 8000    | 0.6200         | 0.7880 | 0.9830 | 0.6480 | 0.3870 | 0.3510 | 0.3220 |
| 8500    | 0.6660         | 0.8910 | 0.9430 | 0.4110 | 0.3630 | 0.3550 | 0.2790 |
| 9000    | 0.7300         | 0.9610 | 0.8070 | 0.3820 | 0.3480 | 0.3160 | 0.2000 |
| 9500    | 0.8060         | 0.9660 | 0.4970 | 0.3640 | 0.3360 | 0.2790 | 0.1140 |
| 10000   | 0.8860         | 0.8720 | 0.4290 | 0.3480 | 0.3190 | 0.2160 | 0.0576 |
| 10500   | 0.9370         | 0.5320 | 0.4040 | 0.3390 | 0.2950 | 0.1450 | 0.0314 |
| 11000   | 0.9550         | 0.4630 | 0.3820 | 0.3270 | 0.2540 | 0.0877 | 0.0213 |
| 11500   | 0.9470         | 0.4340 | 0.3690 | 0.3120 | 0.2010 | 0.0524 | 0.0167 |
| 12000   | 0.9080         | 0.4120 | 0.3550 | 0.2920 | 0.1460 | 0.0346 | 0.0143 |
| 12500   | 0.7280         | 0.3960 | 0.3430 | 0.2630 | 0.1010 | 0.0238 | 0.0129 |
| 13000   | 0.5250         | 0.3830 | 0.3330 | 0.2270 | 0.0688 | 0.0190 | 0.0121 |
| 13500   | 0.4380         | 0.3690 | 0.3190 | 0.1850 | 0.0470 | 0.0162 | 0.0110 |
| 14000   | 0.4210         | 0.3600 | 0.3020 | 0.1440 | 0.0345 | 0.0149 | 0.0108 |
| 14500   | 0.4010         | 0.3490 | 0.2770 | 0.0986 | 0.0245 | 0.0130 | 0.0109 |
| 15000   | 0.3940         | 0.3410 | 0.2530 | 0.0819 | 0.0129 | 0.0120 | 0.0110 |



**TABLE-6**  
**Variation of Thermal Conductivity(W/mK) with Pressure & Temperature**

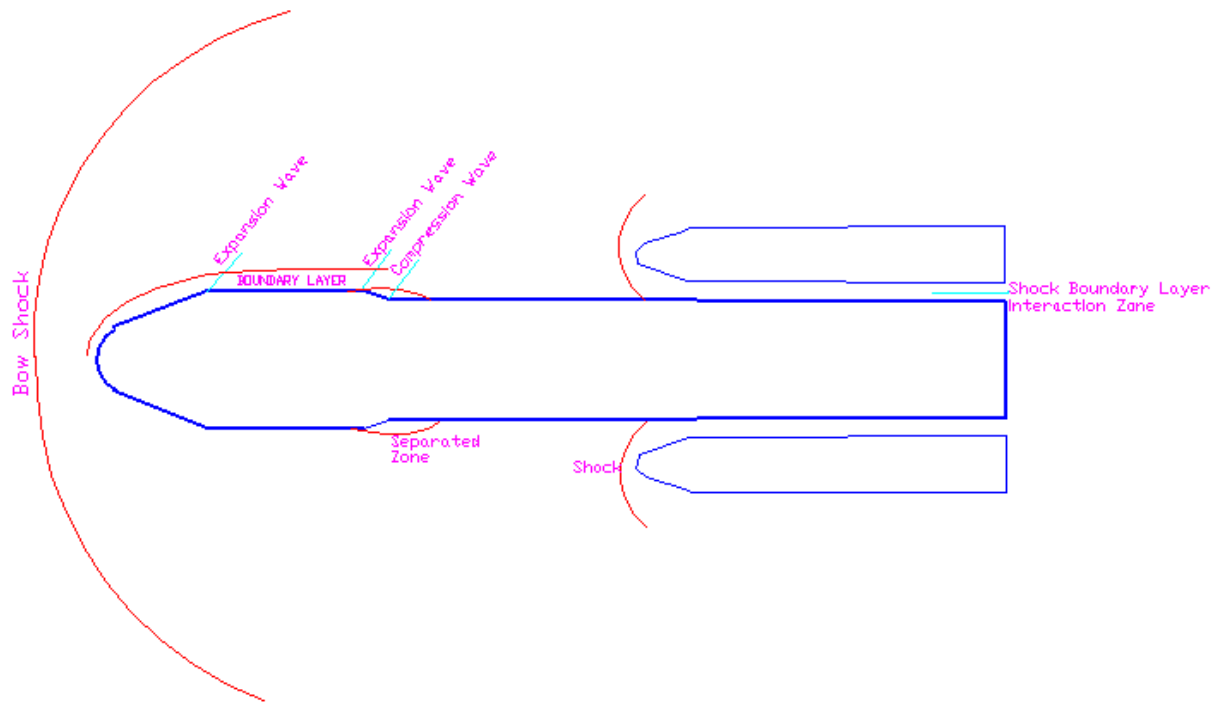
| Temp(K) | PRESSURE (atm) |        |        |        |        |        |        |
|---------|----------------|--------|--------|--------|--------|--------|--------|
|         | 100            | 10     | 1      | 0.1    | 0.01   | 0.001  | 0.0001 |
| 500     | 0.0372         | 0.0372 | 0.0372 | 0.0372 | 0.0372 | 0.0372 | 0.0372 |
| 1000    | 0.0624         | 0.0624 | 0.0624 | 0.0624 | 0.0624 | 0.0624 | 0.0624 |
| 1500    | 0.0826         | 0.0826 | 0.0826 | 0.0826 | 0.0826 | 0.0826 | 0.0826 |
| 2000    | 0.0994         | 0.0994 | 0.0994 | 0.1057 | 0.1233 | 0.1765 | 0.337  |
| 2500    | 0.1199         | 0.1257 | 0.1545 | 0.2386 | 0.4419 | 0.732  | 0.5249 |
| 3000    | 0.1496         | 0.203  | 0.3369 | 0.577  | 0.6339 | 0.2306 | 0.1543 |
| 3500    | 0.2219         | 0.3601 | 0.5396 | 0.4527 | 0.1965 | 0.2412 | 0.4241 |
| 4000    | 0.33           | 0.4834 | 0.3668 | 0.1963 | 0.357  | 0.741  | 1.844  |
| 4500    | 0.4203         | 0.3994 | 0.2237 | 0.4333 | 0.958  | 2.304  | 3.981  |
| 5000    | 0.4234         | 0.2754 | 0.4538 | 0.9903 | 2.294  | 3.558  | 1.633  |
| 5500    | 0.3566         | 0.4218 | 0.8682 | 1.987  | 3.218  | 1.652  | 0.5131 |
| 6000    | 0.2927         | 0.6869 | 1.545  | 2.842  | 1.985  | 0.6005 | 0.9311 |
| 6500    | 0.5295         | 1.103  | 2.292  | 2.432  | 0.8677 | 0.9357 | 2.053  |
| 7000    | 0.7702         | 1.637  | 2.577  | 1.366  | 0.5386 | 1.798  | 4.417  |
| 7500    | 1.074          | 2.124  | 2.083  | 1.007  | 1.467  | 3.398  | 8.831  |
| 8000    | 1.444          | 2.32   | 1.372  | 0.6016 | 2.461  | 6.104  | 14.92  |
| 8500    | 1.789          | 2.096  | 0.9255 | 1.764  | 4.01   | 10.22  | 19.53  |
| 9000    | 2.037          | 1.642  | 0.6092 | 2.622  | 6.372  | 14.72  | 17.53  |
| 9500    | 2.09           | 1.226  | 1.279  | 3.9    | 9.432  | 17.79  | 10.55  |
| 10000   | 1.946          | 0.8026 | 2.159  | 5.561  | 12.78  | 16.72  | 5.049  |
| 10500   | 1.684          | 1.314  | 2.952  | 7.602  | 15.49  | 12.11  | 2.315  |
| 11000   | 1.416          | 1.754  | 3.969  | 10     | 16.27  | 7.288  | 1.203  |
| 11500   | 1.184          | 2.22   | 5.189  | 12.33  | 14.53  | 4.032  | 0.7201 |
| 12000   | 1.037          | 2.805  | 6.688  | 14.15  | 11.17  | 2.327  | 0.4956 |
| 12500   | 0.7381         | 3.436  | 8.176  | 14.87  | 7.69   | 1.346  | 0.3993 |
| 13000   | 1.303          | 4.231  | 9.761  | 14.29  | 5.072  | 0.9197 | 0.3656 |
| 13500   | 2.286          | 5.124  | 11.19  | 12.52  | 3.281  | 0.7307 | 0.3357 |
| 14000   | 2.678          | 6.063  | 12.24  | 10.18  | 2.242  | 0.6461 | 0.3713 |
| 14500   | 3.272          | 7.482  | 12.92  | 7.244  | 1.489  | 0.579  | 0.3979 |
| 15000   | 3.624          | 8.194  | 12.7   | 5.891  | 0.737  | 0.5648 | 0.4252 |

**TABLE-7**  
**Variation of Viscosity(Kg m/s) with Pressure & Temperature**

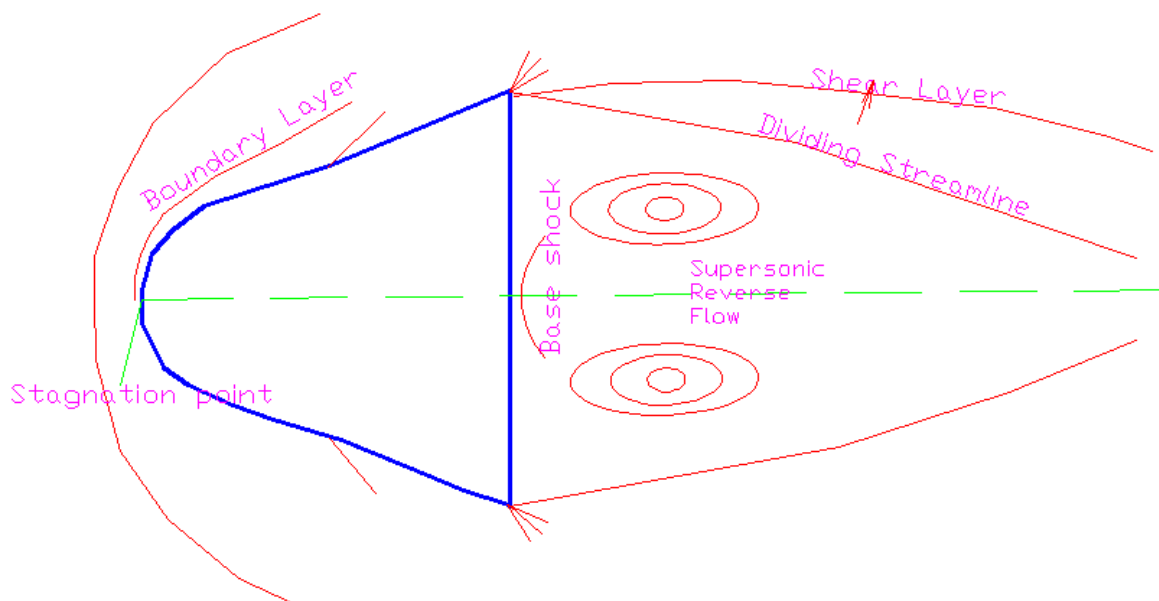
| Temp(K) | PRESSURE (atm) |            |            |            |            |            |            |
|---------|----------------|------------|------------|------------|------------|------------|------------|
|         | 100            | 10         | 1          | 0.1        | 0.01       | 0.001      | 0.0001     |
| 500     | 2.6710E-05     | 2.6710E-05 | 2.6710E-05 | 2.6710E-05 | 2.6710E-05 | 2.6710E-05 | 2.6710E-05 |
| 1000    | 4.1580E-05     | 4.1580E-05 | 4.1580E-05 | 4.1580E-05 | 4.1580E-05 | 4.1580E-05 | 4.1580E-05 |
| 1500    | 5.2690E-05     | 5.2690E-05 | 5.2690E-05 | 5.2690E-05 | 5.2690E-05 | 5.2690E-05 | 5.2690E-05 |
| 2000    | 6.1920E-05     | 6.1920E-05 | 6.1920E-05 | 6.1920E-05 | 6.1920E-05 | 6.1920E-05 | 6.1920E-05 |
| 2500    | 6.9970E-05     | 6.9970E-05 | 6.9970E-05 | 6.9970E-05 | 6.9970E-05 | 6.9970E-05 | 6.9970E-05 |
| 3000    | 7.7190E-05     | 7.7190E-05 | 7.7190E-05 | 7.7190E-05 | 7.7190E-05 | 7.7190E-05 | 7.7190E-05 |
| 3500    | 8.3810E-05     | 8.3890E-05 | 8.4060E-05 | 8.4310E-05 | 8.4650E-05 | 8.4650E-05 | 8.4730E-05 |
| 4000    | 9.0220E-05     | 9.0670E-05 | 9.1390E-05 | 9.1750E-05 | 9.1930E-05 | 9.2110E-05 | 9.2830E-05 |
| 4500    | 9.6650E-05     | 9.7800E-05 | 9.8470E-05 | 9.8850E-05 | 9.9330E-05 | 1.0100E-04 | 1.0490E-04 |
| 5000    | 1.0330E-04     | 1.0470E-04 | 1.0550E-04 | 1.0630E-04 | 1.0860E-04 | 1.0240E-04 | 1.1940E-04 |
| 5500    | 1.1010E-04     | 1.1180E-04 | 1.1260E-04 | 1.1540E-04 | 1.2180E-04 | 1.2850E-04 | 1.3040E-04 |
| 6000    | 1.1670E-04     | 1.1860E-04 | 1.2120E-04 | 1.2760E-04 | 1.3650E-04 | 1.3970E-04 | 1.3960E-04 |
| 6500    | 1.2420E-04     | 1.2630E-04 | 1.3200E-04 | 1.4360E-04 | 1.4790E-04 | 1.4900E-04 | 1.4730E-04 |
| 7000    | 1.3110E-04     | 1.3530E-04 | 1.4540E-04 | 1.5580E-04 | 1.5860E-04 | 1.5690E-04 | 1.5220E-04 |
| 7500    | 1.3870E-04     | 1.4660E-04 | 1.6000E-04 | 1.6620E-04 | 1.6680E-04 | 1.6310E-04 | 1.5090E-04 |
| 8000    | 1.4740E-04     | 1.5960E-04 | 1.7310E-04 | 1.7680E-04 | 1.7370E-04 | 1.6510E-04 | 1.3820E-04 |
| 8500    | 1.5770E-04     | 1.7390E-04 | 1.8440E-04 | 1.8440E-04 | 1.7870E-04 | 1.6060E-04 | 1.0990E-04 |
| 9000    | 1.6960E-04     | 1.8740E-04 | 1.9520E-04 | 1.9120E-04 | 1.8000E-04 | 1.4630E-04 | 7.0830E-05 |
| 9500    | 1.8280E-04     | 1.9970E-04 | 2.0250E-04 | 1.9620E-04 | 1.7620E-04 | 1.2010E-04 | 3.6760E-05 |
| 10000   | 1.9680E-04     | 2.1220E-04 | 2.0890E-04 | 1.9880E-04 | 1.6530E-04 | 8.6030E-05 | 1.7060E-05 |
| 10500   | 2.1020E-04     | 2.2180E-04 | 2.1460E-04 | 1.9790E-04 | 1.4570E-04 | 5.3510E-05 | 8.1530E-06 |
| 11000   | 2.2270E-04     | 2.2780E-04 | 2.1890E-04 | 1.9230E-04 | 1.1870E-04 | 3.0360E-05 | 4.4020E-06 |
| 11500   | 2.3430E-04     | 2.3460E-04 | 2.2110E-04 | 1.8140E-04 | 8.8660E-05 | 1.6770E-05 | 2.7950E-06 |
| 12000   | 2.4580E-04     | 2.4120E-04 | 2.2120E-04 | 1.6500E-04 | 6.1410E-05 | 9.9960E-06 | 1.9040E-06 |
| 12500   | 2.5550E-04     | 2.4560E-04 | 2.1740E-04 | 1.4270E-04 | 4.0340E-05 | 5.8320E-06 | 1.4580E-06 |
| 13000   | 2.6130E-04     | 2.4920E-04 | 2.1060E-04 | 1.1750E-04 | 2.6110E-05 | 3.9670E-06 | 1.3220E-06 |
| 13500   | 2.6850E-04     | 2.5140E-04 | 2.0000E-04 | 9.2150E-05 | 1.6850E-05 | 3.0320E-06 | 1.1790E-06 |
| 14000   | 2.7440E-04     | 2.5190E-04 | 1.8570E-04 | 7.0020E-05 | 1.1500E-05 | 2.5740E-06 | 1.2010E-06 |
| 14500   | 2.7970E-04     | 2.4720E-04 | 1.6420E-04 | 4.6820E-05 | 7.3370E-06 | 2.2710E-06 | 1.3980E-06 |
| 15000   | 2.8510E-04     | 2.4650E-04 | 1.4720E-04 | 3.7680E-05 | 2.8440E-06 | 2.1330E-06 | 1.4220E-06 |

**TABLE-8**  
**Variation of Compressibility with Pressure & Temperature**

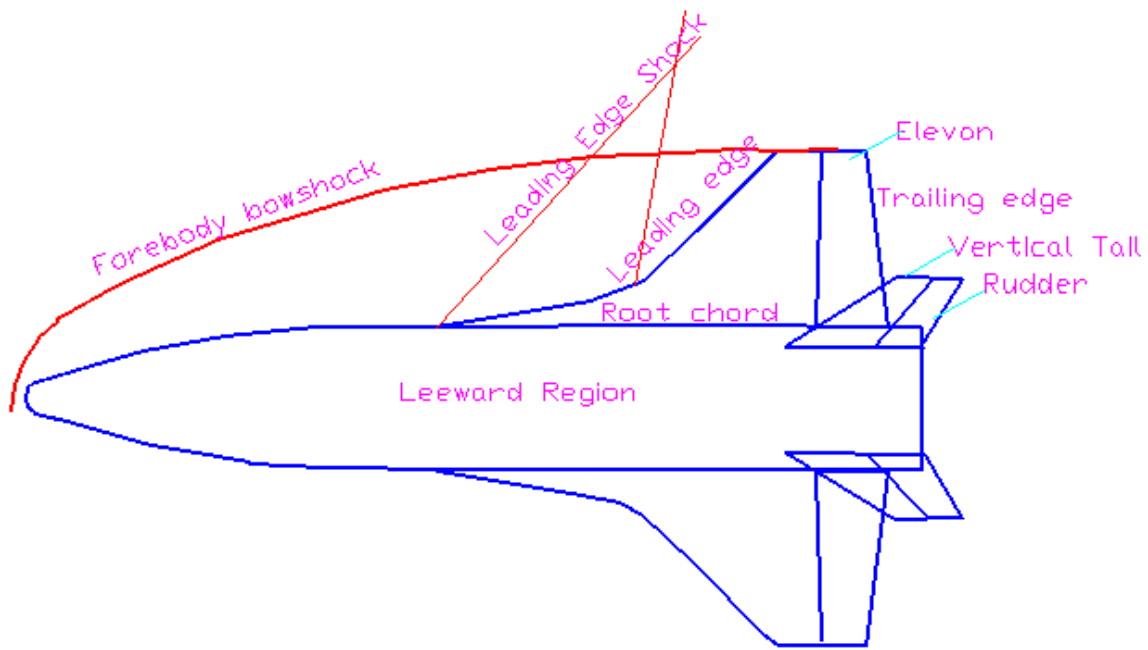
| Temp(K) | PRESSURE (atm) |       |       |       |       |       |        |
|---------|----------------|-------|-------|-------|-------|-------|--------|
|         | 100            | 10    | 1     | 0.1   | 0.01  | 0.001 | 0.0001 |
| 500     | 1.000          | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000  |
| 1000    | 1.000          | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000  |
| 1500    | 1.000          | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000  |
| 2000    | 1.000          | 1.000 | 1.000 | 1.001 | 1.002 | 1.005 | 1.016  |
| 2500    | 1.000          | 1.001 | 1.004 | 1.011 | 1.033 | 1.088 | 1.163  |
| 3000    | 1.003          | 1.009 | 1.026 | 1.072 | 1.149 | 1.192 | 1.200  |
| 3500    | 1.012          | 1.035 | 1.092 | 1.167 | 1.197 | 1.203 | 1.211  |
| 4000    | 1.033          | 1.089 | 1.165 | 1.198 | 1.208 | 1.228 | 1.287  |
| 4500    | 1.071          | 1.149 | 1.196 | 1.213 | 1.245 | 1.337 | 1.577  |
| 5000    | 1.118          | 1.186 | 1.214 | 1.252 | 1.359 | 1.622 | 1.910  |
| 5500    | 1.159          | 1.208 | 1.248 | 1.348 | 1.599 | 1.898 | 1.990  |
| 6000    | 1.189          | 1.235 | 1.316 | 1.529 | 1.849 | 1.983 | 2.008  |
| 6500    | 1.214          | 1.279 | 1.437 | 1.752 | 1.961 | 2.006 | 2.032  |
| 7000    | 1.243          | 1.351 | 1.607 | 1.904 | 1.997 | 2.027 | 2.088  |
| 7500    | 1.284          | 1.457 | 1.778 | 1.971 | 2.017 | 2.067 | 2.210  |
| 8000    | 1.341          | 1.590 | 1.896 | 2.001 | 2.044 | 2.144 | 2.446  |
| 8500    | 1.418          | 1.727 | 1.959 | 2.023 | 2.090 | 2.284 | 2.826  |
| 9000    | 1.512          | 1.838 | 1.993 | 2.050 | 2.166 | 2.510 | 3.282  |
| 9500    | 1.616          | 1.914 | 2.018 | 2.090 | 2.286 | 2.832 | 3.645  |
| 10000   | 1.718          | 1.962 | 2.042 | 2.149 | 2.462 | 3.202 | 3.843  |
| 10500   | 1.807          | 1.993 | 2.071 | 2.234 | 2.700 | 3.526 | 3.932  |
| 11000   | 1.876          | 2.018 | 2.111 | 2.351 | 2.983 | 3.745 | 3.969  |
| 11500   | 1.927          | 2.042 | 2.163 | 2.505 | 3.272 | 3.867 | 3.985  |
| 12000   | 1.965          | 2.067 | 2.232 | 2.694 | 3.520 | 3.931 | 3.993  |
| 12500   | 1.993          | 2.098 | 2.318 | 2.910 | 3.700 | 3.963 | 3.996  |
| 13000   | 2.017          | 2.135 | 2.426 | 3.135 | 3.818 | 3.979 | 3.998  |
| 13500   | 2.039          | 2.180 | 2.553 | 3.347 | 3.889 | 3.988 | 3.999  |
| 14000   | 2.062          | 2.233 | 2.700 | 3.527 | 3.932 | 3.993 | 3.999  |
| 14500   | 2.086          | 2.297 | 2.861 | 3.667 | 3.957 | 3.996 | 4.000  |
| 15000   | 2.113          | 2.372 | 3.028 | 3.769 | 3.973 | 3.997 | 4.000  |



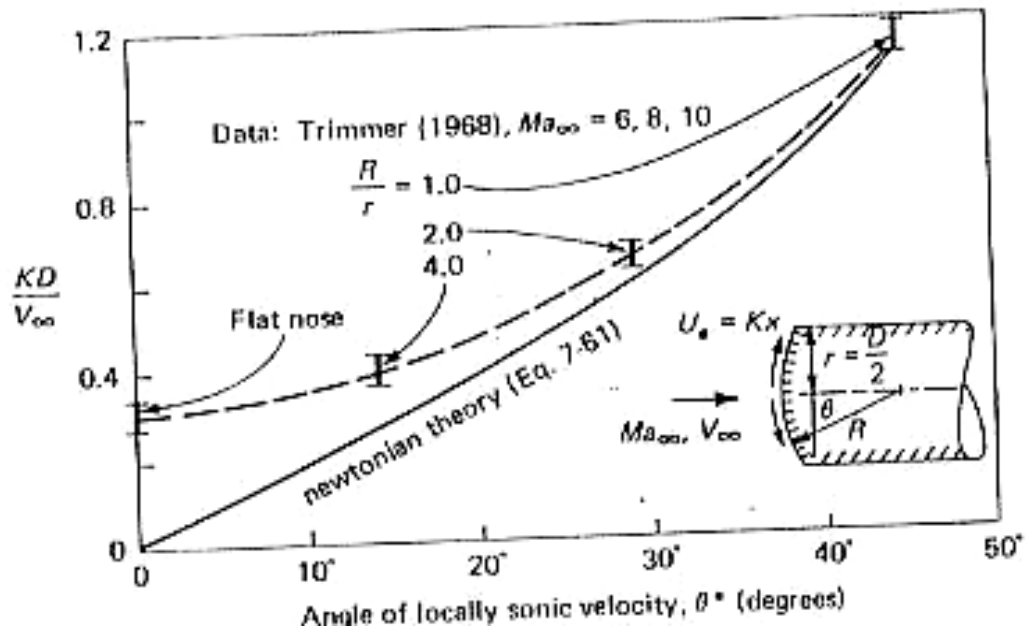
**Fig. 1** Flow past a typical launch vehicle



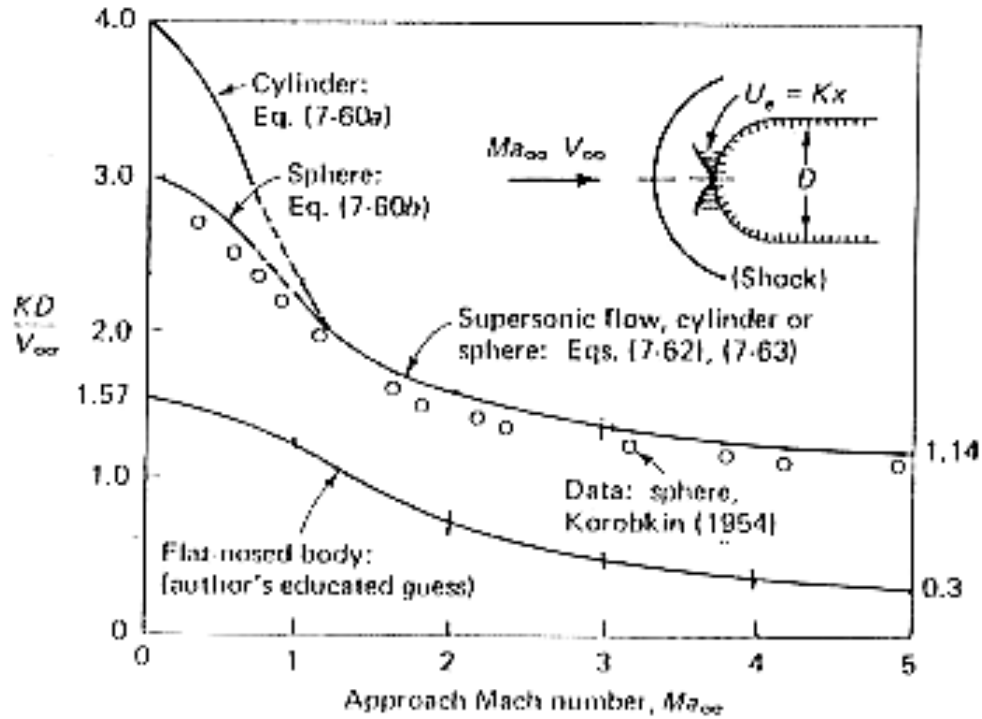
**Fig. 2** Flow past a Reentry module



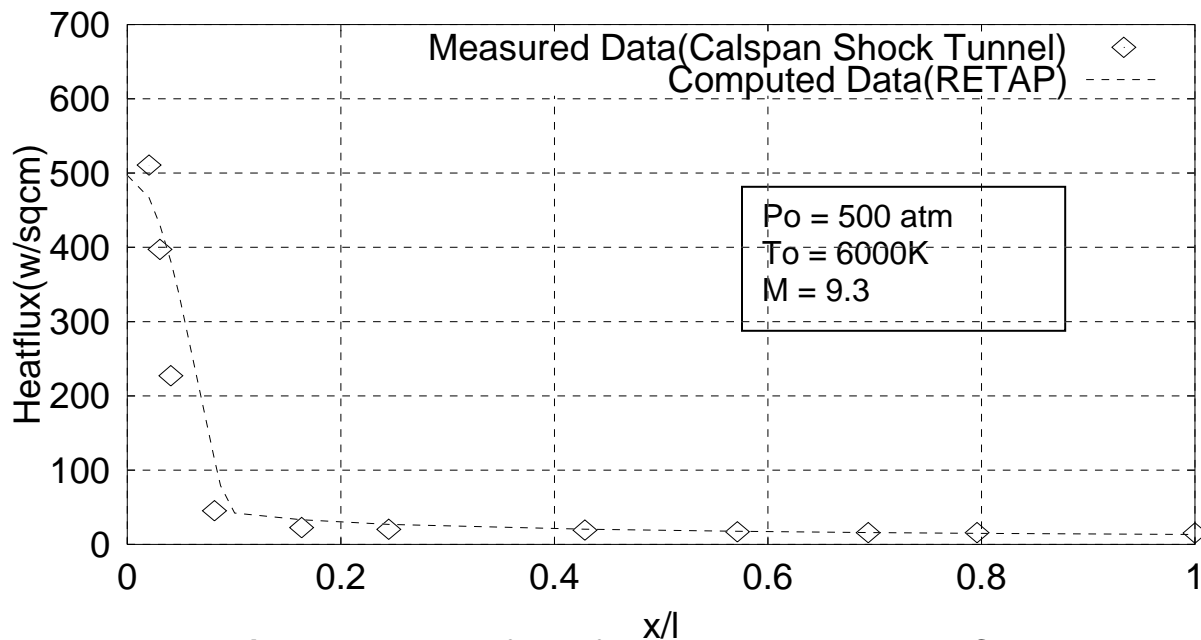
**Fig. 3** Flow past a Reusable Launch Vehicle



**Fig. 4** Comparison of theory and experiment for the stagnation point velocity gradient  $K$  on cylinders with spherical noses



**Fig. 5** Theoretical, experimental and estimated stagnation-point velocity gradients on cylinders, spheres and flat noses



**Fig 6** comparison of heat flux on spherically blunted Cone

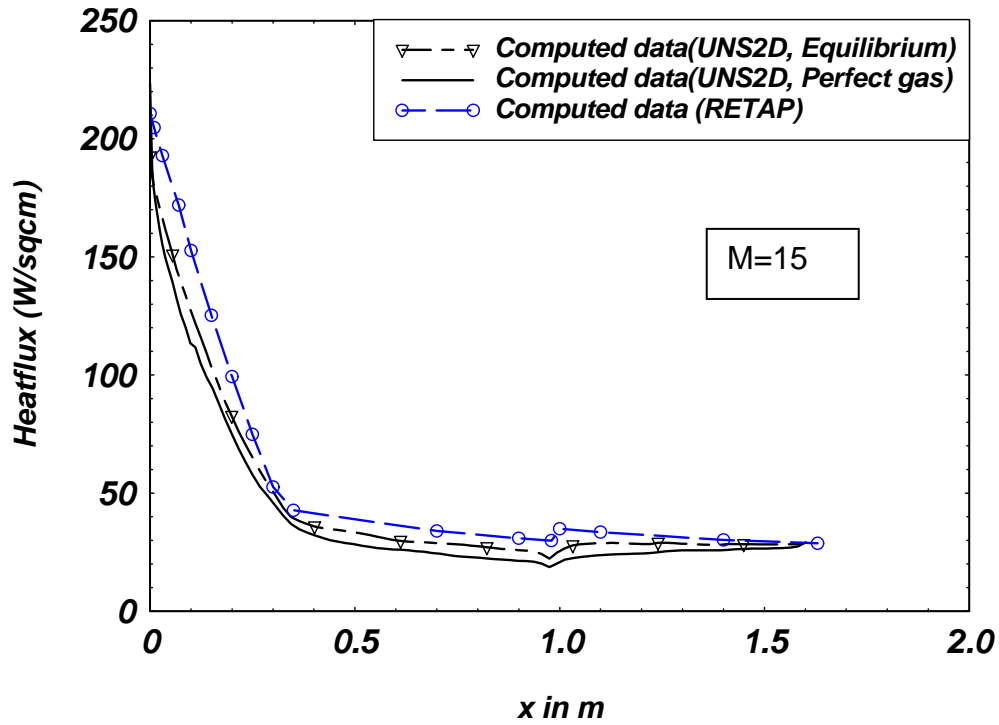


Fig: 7 Comparison of Heat flux between OTAP and UNS2D

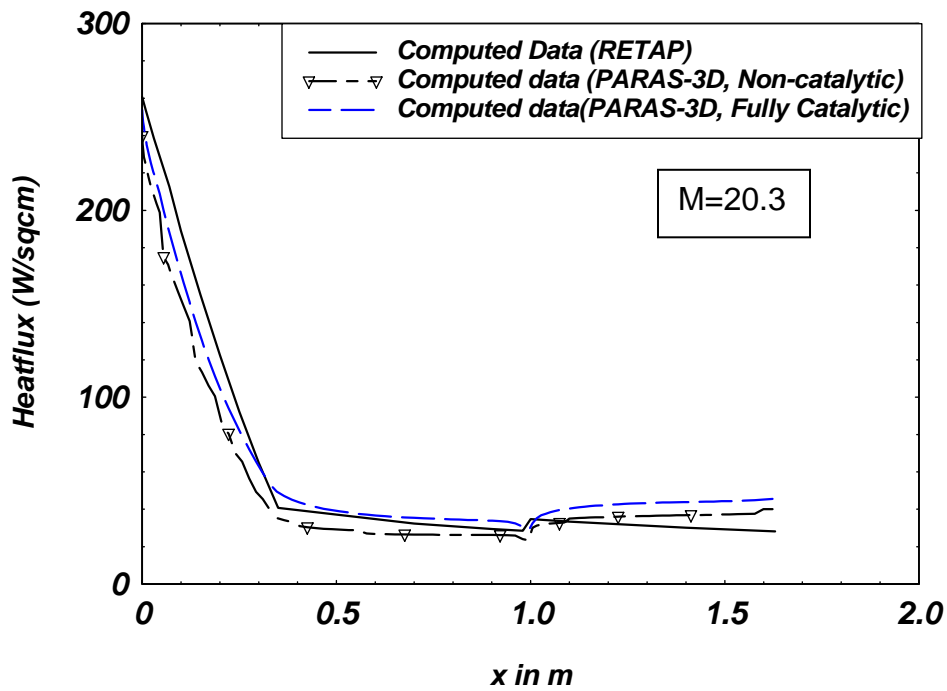


Fig: 8 Comparison of Heat flux between OTAP and PARAS-3D

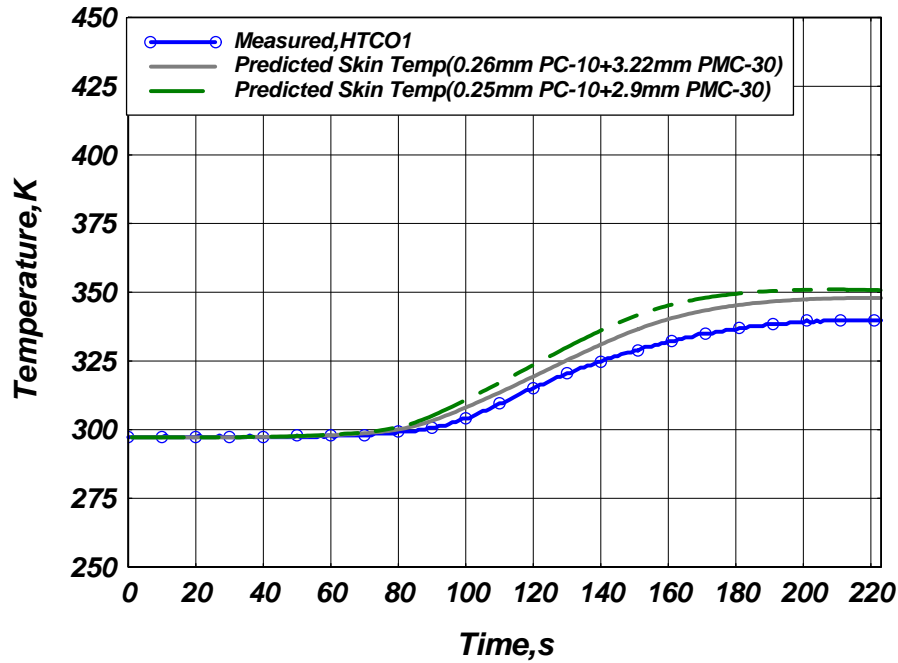


Fig. 9 Comparison between measured and computed temperature histories at cone region for F04 Mission

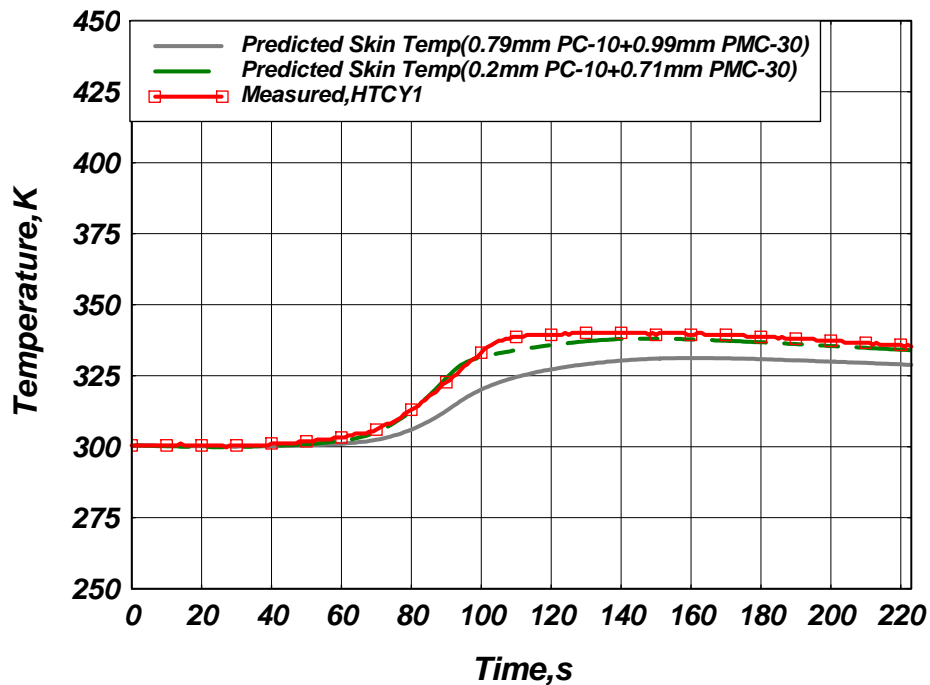


Fig. 10 Comparison between measured and computed temperature histories at cylinder region for F04 Mission



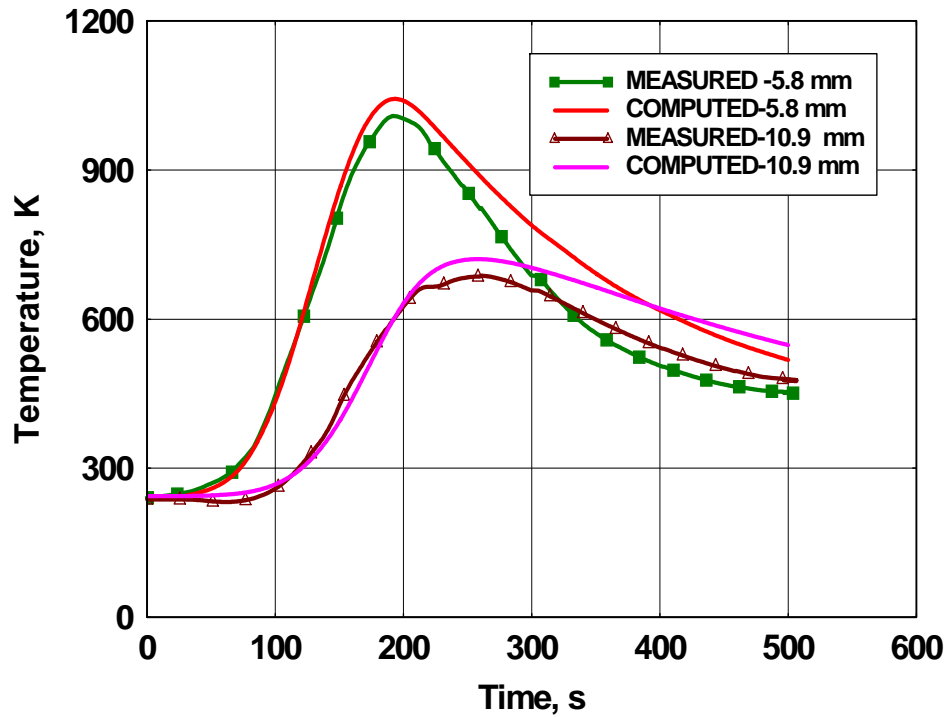


Fig. 11 Thermal Response of Silica Tile in the Conical Region of SRE

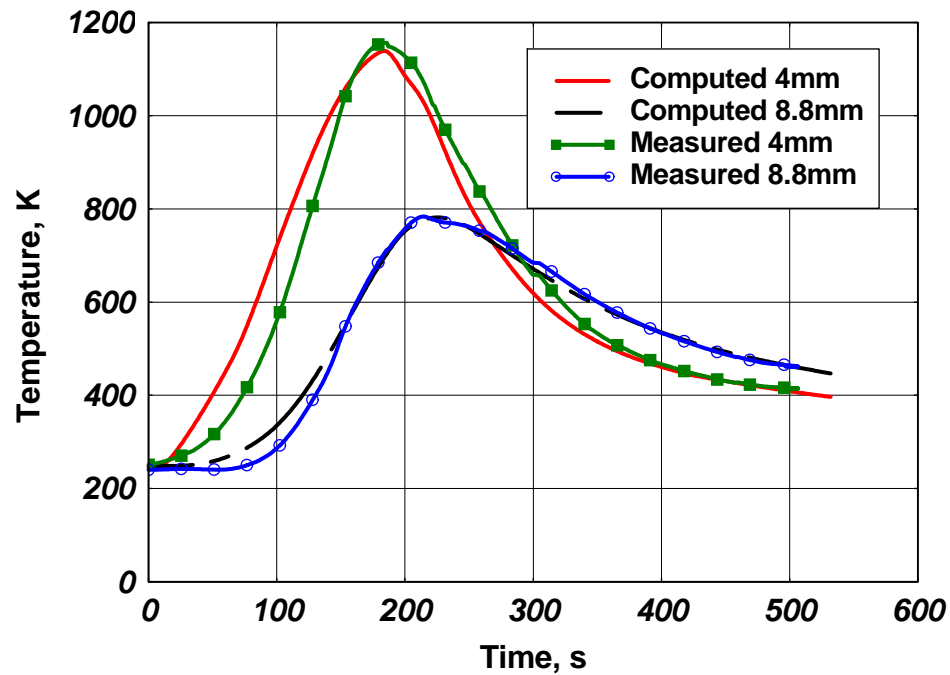


Fig. 12 Thermal Response of Silica Tile in the flare Region of SRE

## APPENDIX – A1

### Normal Shock Relations for Equilibrium Air

Let  $p_\infty, \rho_\infty, u_\infty, T_\infty, h_\infty$  denote the free stream values and  $p_s, \rho_s, u_s, T_s, h_s$  denote the post-shock values.

We have the following conservative equations for one-dimensional flow.

$$\rho_s u_s = \rho_\infty u_\infty \quad (\text{Mass}) \quad (1)$$

$$p_s + \rho_s u_s^2 = p_\infty + \rho_\infty u_\infty^2 \quad (\text{Momentum}) \quad (2)$$

$$h_s + \frac{u_s^2}{2} = h_\infty + \frac{u_\infty^2}{2} \quad (\text{Energy}) \quad (3)$$

$$h_s = f(p_s, T_s) \quad (\text{Enthalpy form}) \quad (4)$$

$$\rho_s = g(p_s, T_s) \quad (\text{Equation of state}) \quad (5)$$

Equations (4) and (5) are obtained from Hansen's tables for the properties of equilibrium air. From these five equations, one can solve for the post shock parameters in iterative manner. Post-shock stagnation conditions can be obtained by using the following isentropic relations:

$$p_0 = p_s \left( 1 + \frac{\gamma-1}{2} M_s^2 \right)^{\frac{\gamma}{\gamma-1}}$$

$$T_0 = T_s \left( 1 + \frac{\gamma-1}{2} M_s^2 \right)$$

Where  $\gamma$  is evaluated at  $(p_s, T_s)$

Local flow conditions can be obtained from the following equations,

$$p_0 = p_e \left( 1 + \frac{\gamma-1}{2} M_e^2 \right)^{\frac{\gamma}{\gamma-1}}$$

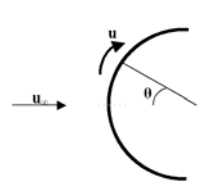
$$T_0 = T_e \left( 1 + \frac{\gamma-1}{2} M_e^2 \right)$$

## APPENDIX – A2

### Inviscid Pressure Distribution

- 1) Subsonic (potential flow over a sphere)

$$\frac{u}{u_{\infty}} = \frac{3}{2} \sin \theta$$



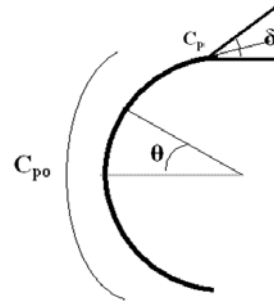
- Subsonic (potential flow over a cylinder)

$$\frac{u}{u_{\infty}} = 2 \sin \theta$$

- Newtonian pressure distribution for supersonic flow

$$C_p' = C_{p0} \sin^2 \delta$$

$$C_p = C_{p0} \cos^2 \theta$$



- 2) Curve fit for cone tables (supersonic flow)

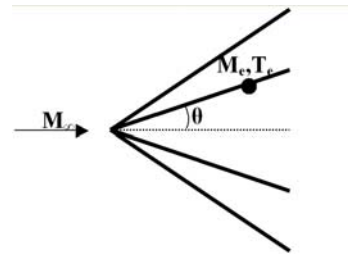
$$\beta = \sqrt{M_{\infty}^2 - 1}$$

$$\frac{T_e}{T_{\infty}} = \begin{cases} 1 + 0.35 (M_{\infty} \sin \theta)^{1.5} \\ \left[ 1 + e^{-(1+1.52 M_{\infty} \sin \theta)} \right] \left[ 1 + \frac{M_{\infty} \sin \theta}{2} \right]^2 \end{cases}$$

for  $0 \leq M_{\infty} \sin \theta \leq 1$

for  $M_{\infty} \sin \theta \geq 1$

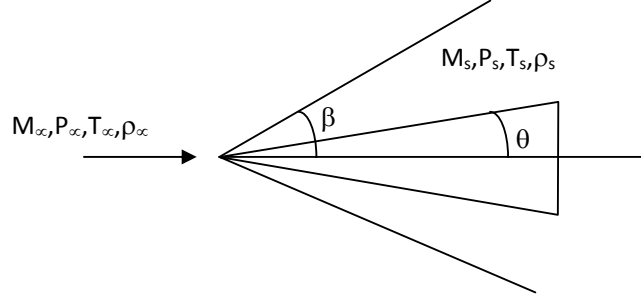
$$\frac{u_e}{u_{\infty}} = \sin \theta \left[ 1 - \frac{\sin \theta}{M_{\infty}} \right]^{1/2}$$



$$C_p = (4 \sin^2 \theta) \frac{(2.5 + 8 \beta \sin \theta)}{(1 + 16 \beta \sin \theta)} = \frac{\frac{P_e}{P_{\infty}} - 1}{\gamma M_{\infty}^2}$$

## APPENDIX – A3

### Oblique Shock Relations



Shock angle  $\beta$  is given in terms of the flow deflection angle  $\theta$  as follows:

$$\tan \theta = \cot \beta - \frac{2[M_\infty^2 \sin^2 \beta - 1]}{M_\infty^2 (\gamma + \cos 2\beta) + 2}$$

For given Mach number, there is a maximum value of  $\theta_{\max}$  for which the shock is attached. Once  $\beta$  is found from the above relation; other parameters are calculated as follows:

$$\frac{\rho_s}{\rho_\infty} = \frac{(\gamma + 1)M_\infty^2 \sin^2 \beta}{(\gamma - 1)M_\infty^2 \sin^2 \beta + 2}$$

$$\frac{P_s - P_\infty}{P_\infty} = \frac{2\gamma}{\gamma + 1} (M_\infty^2 \sin^2 \beta - 1)$$

$$\frac{T_s}{T_\infty} = \frac{a_s^2}{a_\infty^2} = 1 + \frac{2(\gamma - 1)M_\infty^2 \sin^2 \beta - 1}{(\gamma + 1)^2 M_\infty^2 \sin^2 \beta} (\gamma M_\infty^2 \sin^2 \beta + 1)$$

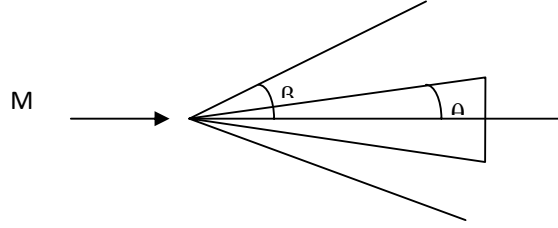
$$M_s^2 \sin^2 (\beta - \theta) = \frac{1 + \frac{(\gamma - 1)}{2} M_\infty^2 \sin^2 \beta}{\gamma M_\infty^2 \sin^2 \beta - \frac{(\gamma - 1)}{2}}$$

## Oblique Shock Relations (Theory)

(Journal of Aircraft, Vol. 35, 1998, p. 647)

$\theta$  = Flow deflection angle

$\beta$  = Shock angle



$$\frac{\tan(\beta - \theta)}{\tan(\beta)} = \frac{(\gamma - 1)M^2 \sin^2 \beta + 2}{(\gamma + 1)M^2 \sin^2 \beta}$$

This can be simplified as

$$\tan \theta = \cot \beta - \frac{M^2 \sin^2 \beta - 1}{1 + \left( \frac{\gamma + 1}{2} - \sin^2 \beta \right) M^2}$$

This can be written as a cubic in  $\tan \beta$  as follows

$$\left( 1 + \frac{(\gamma - 1)}{2} M^2 \right) \tan \theta \tan^3 \beta - (M^2 - 1) \tan^2 \beta + \left( 1 + \frac{(\gamma + 1)}{2} M^2 \right) \tan \theta \tan \beta + 1 = 0$$

This is a cubic in  $\tan \beta$ . If two of the roots are complex, the shock is detached. If all the roots are real,

$$\tan \beta = \left( \frac{b + 9a \tan \mu}{2(1 - 3ab)} - \frac{d(27a^2 \tan \mu + 9ab - 2)}{6a(1 - 3ab)} \right) \tan \left( \frac{n\pi}{3} + \frac{1}{3} \tan^{-1} \left( \frac{1}{d} \right) \right)$$

$$n = \begin{cases} 0, & \text{Weak shock} \\ 1, & \text{Strong shock} \\ -1, & \text{Physically meaningless solution} \end{cases}$$

$$\mu = \text{Mach wave angle} \quad \left( \sin \mu = \frac{1}{M} \right)$$

$$a = \left( \frac{\gamma - 1}{2} + \frac{\gamma + 1}{2} \tan^2 \mu \right) \tan \theta$$

$$b = \left( \frac{\gamma + 1}{2} + \frac{\gamma + 3}{2} \tan^2 \mu \right) \tan \theta$$

$$d = \sqrt{\frac{4(1 - 3ab)^3}{(27a^2c + 9ab - 2)^2}} - 1$$

Only weak shock solution is taken.

### Oblique Shock Relations (SHWAVE PROGRAM)

$$c = \frac{2}{(\gamma - 1) \tan \theta \left( M^2 + \frac{2}{(\gamma - 1)} \right)} \quad \theta = \text{Flow deflection angle} \quad \beta = \text{Shock angle}$$

$$b = \frac{\left( \frac{\gamma + 1}{\gamma - 1} M^2 + \frac{2}{(\gamma - 1)} \right)}{\left( M^2 + \frac{2}{(\gamma - 1)} \right)}$$

$$a = c(1 - M^2)$$

$$p = -\frac{a^2}{3} + b$$

$$q = \frac{2a^3}{27} - \frac{ab}{3} + c$$

$$s = \left( \frac{p}{3} \right)^3 + \left( \frac{q}{2} \right)^2$$

$s < 0$

$$b_1 = \sqrt{\frac{-p}{3}}$$

$$a_1 = \frac{-s}{2b_1^3} \quad \phi = \cos^{-1}(a_1)$$

$$Z_1 = 2b_1 \cos\left(\frac{\phi}{3}\right) - \frac{a}{3}$$

$$Z_2 = -2b_1 \cos\left(\frac{\phi}{3} + \frac{\pi}{3}\right) - \frac{a}{3}$$

$$Z_3 = -2b_1 \cos\left(\frac{\phi}{3} - \frac{\pi}{3}\right) - \frac{a}{3}$$

if  $(\max(Z_1, Z_2, Z_3) < 0)$ , Shock is detached

$$\beta = \tan^{-1}(Z_2) \quad ; \quad M_2 = \frac{(\gamma - 1)x^2 + 2}{2\gamma x^2 - (\gamma - 1)} \quad ; \quad x = M \sin(\beta)$$

$s = 0$

$$a_1 = \sqrt{s} - \frac{q}{2}$$

$$b_1 = -\sqrt{s} - \frac{q}{2}$$

$$z_1 = (a_1 b_1)^{\frac{1}{3}} - \frac{a}{3}$$

$\beta = \tan^{-1}(Z_1)$  if  $(\beta < 0)$ , Shock is detached

## APPENDIX – A4

### Fay and Riddel Formula for Stagnation Point Heat Transfer

$$q = k (Pr)^{-0.6} (\rho_w \mu_w)^{0.1} (\rho_o \mu_o)^{0.4} (H_o - H_w) \sqrt{\left. \frac{du}{ds} \right|_{s=0}} \left\{ 1 + (Le^\beta - 1) \frac{H_D}{H_o} \right\}$$

where  $k = \begin{cases} 0.763 & \text{for axisymmetric flow} \\ 0.57 & \text{for two – dimensional flow} \end{cases}$

$\alpha = \left. \frac{du}{ds} \right|_{s=0}$  is the velocity gradient at the stagnation point.

$\beta = \begin{cases} 0.52 & \text{for frozen flow} \\ 0.63 & \text{for equilibrium flow} \end{cases}$

Le is Lewis number (usually taken as 1.4)

$H_D$  is the energy of dissociation

$H_o$  is the Total stagnation enthalpy

### Velocity gradient for various nose shapes

- ✓ **Thick infinite plate or flat-headed cylinder (D thickness or diameter)**

$$\frac{\alpha D}{u_\infty} = \begin{cases} 1.57 - 0.408M & (M < 2.5) \\ 0.5 - 0.08(M - 2.5) & (2.5 < M < 5) \\ 0.3 & (M > 5) \end{cases}$$

- ✓ **Cylinder**

$$\frac{\alpha D}{u_\infty} = 4 - 1.664 M^2 \quad (M < 1)$$

$$\alpha = \frac{1}{r_N} \sqrt{\frac{2(P_o - P_\infty)}{\rho_o}} \quad (M > 1)$$

- ✓ **Sphere**

$$\frac{\alpha D}{u_\infty} = 3 - 0.756 M^2 \quad (M < 1)$$

$$\alpha = \frac{1}{r_N} \sqrt{\frac{2(P_o - P_\infty)}{\rho_o}} \quad (M > 1)$$

### Energy of Dissociation

$$H_D = 0.79 \sqrt{\frac{F_{N_2}}{1+F_{N_2}}} \cdot E_{N_2} + 0.21 \sqrt{\frac{F_{O_2}}{1+F_{O_2}}} \cdot E_{O_2} \quad (\text{cal/gm})$$

where  $E_{N_2} = 4183$  and  $E_{O_2} = 7023$

$$F_{N_2} = \frac{P_{N_2}}{P} \cdot \frac{T}{T_{N_2}} e^{\left(-\frac{T_{N_2}}{T}\right)} \quad P_{N_2} = 4.5 \times 10^7$$

$$F_{O_2} = \frac{P_{O_2}}{P} \cdot \frac{T}{T_{O_2}} e^{\left(-\frac{T_{O_2}}{T}\right)} \quad P_{O_2} = 2.3 \times 10^7$$

$$T_{N_2} = 113200$$

$$T_{O_2} = 59000$$

P is pressure in atmospheres and T is the temperature in Kelvin.

### Equilibrium Air Composition

Partition functions are given as

$$\ln Q(O) = \frac{5}{2} \ln T + 0.5 + \ln \left( 5 + 3e^{\frac{-228}{T}} + e^{\frac{-326}{T}} + 5e^{\frac{-22800}{T}} + e^{\frac{-48600}{T}} \right) - \ln P$$

$$\ln Q(N) = \frac{5}{2} \ln T + 0.3 + \ln \left( 4 + 10e^{\frac{-27700}{T}} + 6e^{\frac{-41500}{T}} \right) - \ln P$$

$$\ln Q(O^+) = \frac{5}{2} \ln T + 0.5 + \ln \left( 4 + 10e^{\frac{-38600}{T}} + 6e^{\frac{-58200}{T}} \right) - \ln P$$

$$\ln Q(N^+) = \frac{5}{2} \ln T + 0.3 + \ln \left( 1 + 3e^{\frac{-70.6}{T}} + 5e^{\frac{-188.9}{T}} + 5e^{\frac{-22000}{T}} + e^{\frac{-47000}{T}} + 5e^{\frac{-679000}{T}} \right) - \ln P$$

$$\ln Q(e^-) = \frac{5}{2} \ln T - 14.24 - \ln P$$

$$\ln Q(N_2) = \frac{7}{2} \ln T - 0.42 - \ln \left( 1 - e^{\frac{-3390}{T}} \right) - \ln P$$

$$\ln Q(O_2) = \frac{7}{2} \ln T + 0.11 - \ln \left( 1 - e^{\frac{-2270}{T}} \right) - \ln \left( 3 + 2e^{\frac{-11390}{T}} + e^{\frac{-18990}{T}} \right) - \ln P$$



Equilibrium constants for the 4 major reactions are given by

$$\ln K_{p_1}(O_2 \rightarrow 2O) = -\frac{59000}{T} + 2\ln Q_p(O) - \ln Q_p(O_2)$$

$$\ln K_{p_2}(N_2 \rightarrow 2N) = -\frac{113200}{T} + 2\ln Q_p(N) - \ln Q_p(N_2)$$

$$\ln K_p(O \rightarrow O^+ + \bar{e}) = -\frac{158000}{T} + \ln Q_p(O^+) - \ln Q_p(\bar{e}) - \ln Q_p(O)$$

$$\ln K_p(N \rightarrow N^+ + \bar{e}) = -\frac{168000}{T} + \ln Q_p(N^+) - \ln Q_p(\bar{e}) - \ln Q_p(N)$$

$$Q_p = pQ$$

$$\varepsilon_1 = \frac{-0.8 + [0.64 + 0.8(1 + 4p/kp_1)]^{1/2}}{2\left(1 + \frac{4p}{kp_1}\right)}$$

$$\varepsilon_2 = \frac{-0.4 + [0.16 + 3.84(1 + 4p/kp_2)]^{1/2}}{2\left(1 + \frac{4p}{kp_2}\right)}$$

$$\text{where } K_{p_3} = 0.2 K_p(O \rightarrow O^+ + \bar{e}) + 0.8 K_p(N \rightarrow N^+ + \bar{e})$$

The component mole fractions are given by

$$X(O_2) = \frac{0.2 - \varepsilon_1}{Z}$$

$$X(N_2) = \frac{0.8 - \varepsilon_2}{Z}$$

$$X(O) = \frac{2\varepsilon_1 - 0.4\varepsilon_3}{Z}$$

$$X(N) = \frac{2\varepsilon_2 - 1.6\varepsilon_3}{Z}$$

$$X(O^+ + N^+) = X(\bar{e}) = \frac{2\varepsilon_3}{Z} \quad \text{where } Z \text{ is the compressibility factor given by}$$

$$Z = 1 + \varepsilon_1 + \varepsilon_2 + \varepsilon_3$$

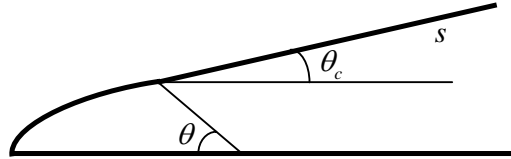
## APPENDIX – A5

### Lees Formula for Laminar Heat Transfer in the Stagnation Region

$$\frac{q}{q_0} = \frac{2\theta \sin\theta \left\{ \left[ 1 - \frac{1}{\gamma M_\infty^2} \right] \cos^2\theta + \frac{1}{\gamma M_\infty^2} \right\}}{[D(\theta)]^{1/2}} \quad [0 \leq \theta \leq (D - \theta_c)]$$

$$D(\theta) = \left( 1 - \frac{1}{\gamma M_\infty^2} \right) \left( \theta^2 - \frac{\theta \sin 4\theta}{2} + \frac{1 - \cos 4\theta}{8} \right) + \frac{4}{\gamma M_\infty^2} \left( \theta^2 - \theta \sin 2\theta + \frac{1 - \cos 2\theta}{8} \right)$$

$q_0$  is the heat transfer at the stagnation point.



In the case of spherically blunted cone, heat transfer on the cone is given by

$$\frac{q}{q_0} = A(\theta_c) + \frac{\left( \frac{s'}{r_N} \right)}{\left[ B(\theta_c) + \left( \frac{s'}{r_N} \right)^2 \right]^{1/2}}$$

Where  $\frac{s'}{r_N} = \cot \theta_c + \left[ \frac{s}{r_N} - \left( \frac{\pi}{2} - \theta_c \right) \right]$

$$A(\theta_c) = \frac{\sqrt{3}}{2} \left[ \left( 1 - \frac{1}{\gamma M_\infty^2} \right) \sin^2 \theta_c + \frac{1}{\gamma M_\infty^2} \right]^{1/2} \sqrt{\left( \frac{\pi}{2} - \theta_c \right)}$$

$$B(\theta_c) = \frac{3/16}{\sin^2 \theta_c \left\{ \left[ 1 - \frac{1}{\gamma M_\infty^2} \right] \sin^2 \theta_c + \frac{1}{\gamma M_\infty^2} \right\}} \left[ \frac{D(\theta)}{\theta} \right] - \cot^3 \theta_c$$

where  $\theta = \frac{\pi}{2} - \theta_c$

## APPENDIX – A6

### Van Driest Formula for Turbulent Flow over Flat Plate

$C_f$  is given by the following equation

$$\frac{0.242}{A \sqrt{C_f \frac{T_w}{T_e}}} (\sin^{-1} \alpha + \sin^{-1} \delta) = 0.41 + \log_{10} (\text{Re}_s \cdot C_f) - (n + 0.5) \log_{10} \left( \frac{T_w}{T_e} \right)$$

where  $\alpha = \frac{2A^2 - B}{(B^2 + 4A^2)^{1/2}}$  and  $\delta = \frac{B}{(B^2 + 4A^2)^{1/2}}$

Re is the local Reynolds number and  $C_f$  is the local skin friction coefficient.

$$A^2 = \frac{(\gamma - 1) M_e^2}{2 \left( \frac{T_w}{T_e} \right)}; \quad B = \frac{1 + \frac{\gamma - 1}{2} M_e^2}{\left( \frac{T_w}{T_e} \right)} - 1$$

Stanton Number  $C_h = \frac{C_f}{2} \cdot \gamma_{af}$  where  $\gamma_{af}$  is the Reynolds analogy factor.

Heat flux,  $q = C_h \rho_e u_e (H_{rec} - H_w)$

$$H_{rec} = h_e + rec \left( \frac{u_e^2}{2} \right) \text{ where } rec \text{ is the recovery factor.}$$

$$\gamma_{af} = \text{Pr}_t \left[ 1 + 5 \sqrt{\frac{C_f}{2}} \left\{ \frac{(1 - \text{Pr}_t)}{5K} \left( \frac{\pi^2}{6} + \frac{3}{2} - \frac{3}{2} \text{Pr}_t \right) + \left( \frac{\text{Pr}}{\text{Pr}_t} - 1 \right) + \ln \left( \frac{1}{6} + \frac{5}{6} \frac{\text{Pr}}{\text{Pr}_t} \right) \right\} \right]$$

$$rec = \text{Pr}_t \left[ 1 + \frac{2}{k} \sqrt{\frac{C_f}{2}} (1 - \text{Pr}_t) \left\{ \frac{\pi^2}{6} + 1.5(1 - \text{Pr}_t) \right\} + 12.5 C_f \left\{ \frac{\text{Pr}}{\text{Pr}_t} - 1 + 2 \ln \left( \frac{1}{6} + \frac{5}{6} \frac{\text{Pr}}{\text{Pr}_t} \right) + \ln(6) \ln \left( \frac{1}{8} + \frac{7}{8} \frac{\text{Pr}}{\text{Pr}_t} \right) - \ln(6) \ln \left( \frac{3}{4} + \frac{1}{4} \frac{\text{Pr}}{\text{Pr}_t} \right) \right\} \right]$$

where k is the Karman mixing length constant (k = 0.4)

n is the exponent in viscosity law (n = 0.707)

$\text{Pr}_t$  is the turbulent Prandtl number ( $\text{Pr}_t = 0.86$ )

## **Van Driest Formula for Laminar Flow over Flat Plate**

$$C_f = \frac{F_1 + F_2 \left( \frac{T_w}{T_e} \right)}{\sqrt{\text{Re}_s}}$$

where  $F_1 = 0.416594 + (0.246733\text{E-}2)\text{M}_e - (0.817489\text{E-}3)\text{M}_e^2 + (0.2734033\text{E-}4)\text{M}_e^3$

$F_2 = -(0.134671\text{E-}1) + (0.2635807\text{E-}3)\text{M}_e + (0.581944\text{E-}4)\text{M}_e^2 - (0.2173257\text{E-}5)\text{M}_e^3$

Reynolds Analogy Factor,  $\gamma_{af} = \text{Pr}^{2/3}$

Recovery Factor,  $r_e = \text{Pr}^{1/2}$

## APPENDIX – A7

### Eckert Formula for Flat plate Flow

$h_e$  - Static enthalpy

$T_e$  - Total enthalpy

$$\text{Recovery factor, } rec = \begin{cases} Pr^{\frac{1}{2}}, & \text{lam in a r f l o w} \\ Pr^{\frac{1}{3}}, & \text{t u r b u l e n t f l o w} \end{cases}$$

$$H_{rec} = h_e + rec \cdot \frac{u_e^2}{2}$$

From  $H_{rec}$ ,  $T_{rec}$  is calculated using Newton-Raphson iteration and Hansen's tables.

$$T_{rec}^n = T_{rec}^{n-1} + \frac{(H_{rec} - H_r)^{n-1}}{Cp^{n-1}}$$

$$\text{Starting from an initial value of } T_{rec} = T_e + \left(1 + \frac{\gamma-1}{2} M_e^2 \cdot rec\right)$$

The reference temperature  $T^*$  is calculated iteratively by matching reference enthalpy  $H^*$ , using Hansen's tables. The reference enthalpy  $H^*$  is calculated as

$$H^* = 0.5(H_w - H_e) + 0.22(H_{rec} - H_e)$$

The local Reynold's number is calculated using the reference temperature  $T^*$ , for evaluating

$$\rho^* \text{ and } \mu^*. \quad Re^* = \frac{\rho^* u_e r}{\mu^*}$$

The local skin friction coefficient  $C_f$  is computed using  $Re^*$ .

$$C_f = \begin{cases} \frac{0.664}{(Re^*)^{\frac{1}{2}}}, & \text{lam in a r f l o w} \\ \frac{0.37}{(\log_{10} Re^*)^{2.584}}, & \text{t u r b u l e n t f l o w} \end{cases}$$

Stanton number is now computed using Reynold's analogy factor as follows

$$C_h = \begin{cases} \frac{C_f}{2} Pr^{\frac{1}{2}}, & \text{lam in a r f l o w} \\ \frac{C_f}{2} Pr^{\frac{2}{3}}, & \text{t u r b u l e n t f l o w} \end{cases}$$

$$\text{Heat flux is estimated as } \dot{q} = \rho_e u_e (H_{rec} - H_w) = \rho_e u_e c_h (T_{rec} - T_w)$$

$$\text{Heat transfer coefficient} = \rho_e u_e c_h$$

## APPENDIX – A8

### Chen and Thyson Formula for Boundary Layer Transition

Intermittency factor is given by

$$\gamma_{tr} = 1 - \exp \left[ -G r_o(x_{tr}) \int_{x_{tr}}^x \frac{dx}{r_o} \int_{x_{tr}}^x \frac{dx}{u_e} \right] \quad (1)$$

where  $r_o$  is the local body radius,  $x_{tr}$  is the location of the onset of transition

G is a spot formation rate parameter defined by  $G = \frac{3}{C^2} \left( \frac{Ue^2}{\nu e^2} \right) \text{Re}_{tr}^{-1.34}$

where  $C = 4.86 M_e^{1.92} + 60$

$\text{Re}_{tr}$  is the transition Reynolds number,  $\nu_e = \frac{\mu_e}{\rho_e}$

In the case of cylindrical and flat plate flow,  $r_o$  and  $u_e$  are constants.

Equation (1) becomes  $\gamma_{tr} = 1 - \exp \left[ \frac{-3}{C^2} (\text{Re}_x - \text{Re}_{tr})^2 \text{Re}_{tr}^{-1.34} \right]$

In the case of conical and wedge flow,  $r_o = x \tan \alpha$  and  $u_e$  is constant.

Equation (1) becomes  $\gamma_{tr} = 1 - \exp \left[ \frac{-3}{C^2} (\text{Re}_x - \text{Re}_{tr}) \ln \frac{\text{Re}_x}{\text{Re}_{tr}} \text{Re}_{tr}^{-0.34} \right]$

$$C_f = \gamma_{tr} C_{f_{turb}} + (1 - \gamma_{tr}) C_{f_{lamin}}$$

## APPENDIX – A9

### Heat Transfer along the Windward Generator of a Swept Infinite Cylinder: (Beckwith & Gallagher)

#### Turbulent Flow

$$\frac{hD}{k} = \left[ \frac{u_{\infty} D}{\gamma_{\infty}} \right]^{0.8} Pr^{1/3} \left[ 0.0228 \frac{\mu_w}{\mu_o} \frac{T_{\infty}}{T_w} \frac{P_s}{P_{\infty}} \right]^{0.8} \sin^{0.6} \lambda \left\{ 0.13032 \frac{\mu_o}{\mu_{\infty}} \cos \lambda \frac{D}{V_N} \cdot \left( \frac{dV_N}{dx} \right)_s \right\}^{0.2}$$

Where D is the diameter of the cylinder

$\lambda$  is the sweep back angle

$u_{\infty}$  is the free stream velocity

$$V_N = u \sin \lambda$$

k is conductivity of air

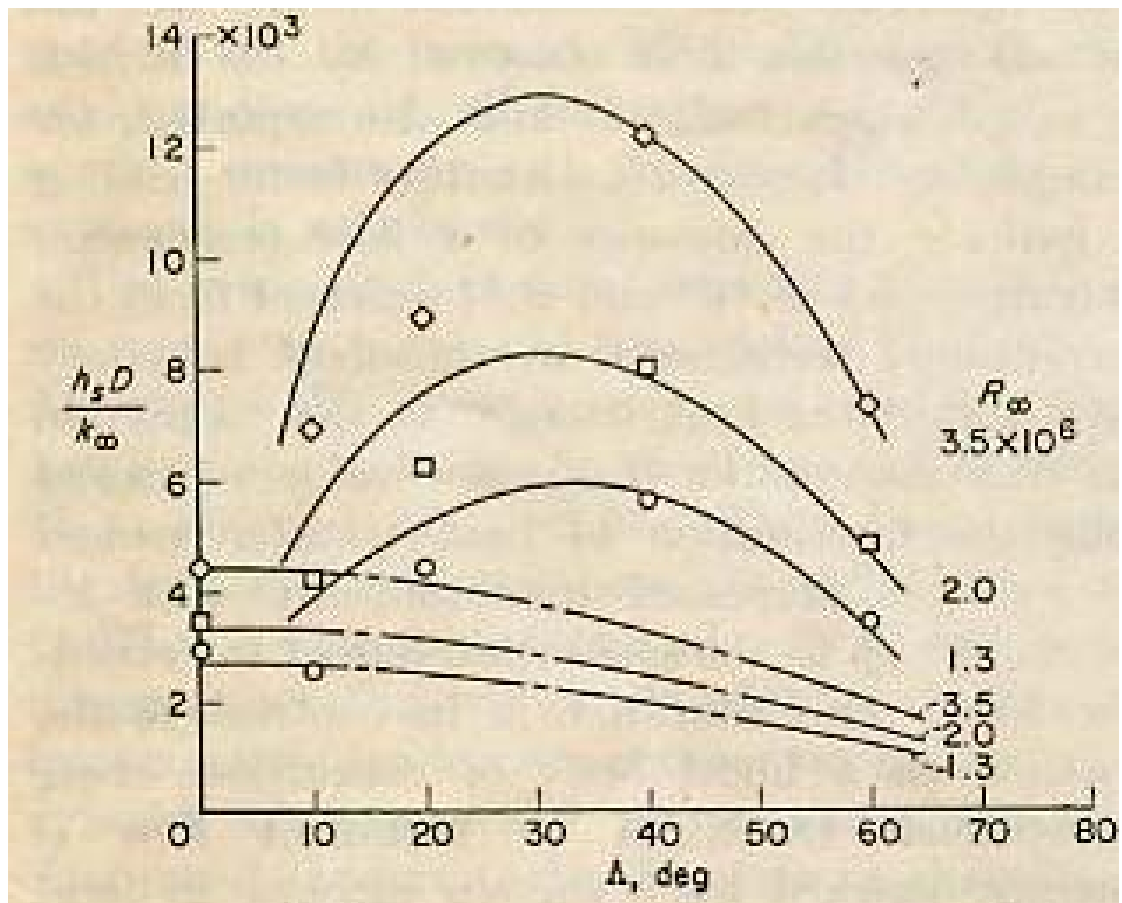
$\frac{dV_N}{dx}$  is the velocity gradient at stagnation point

$$\dot{q} = h(T_{rec} - T_w)$$

#### Laminar Flow (Modified Fay and Riddell formula)

$$\frac{R_D}{k} = 0.5 \left( 2 \frac{Re_{\infty}}{M_{\infty}} \frac{\mu_s}{\mu_{\infty}} \right)^{\frac{1}{2}} \left[ \frac{2}{\gamma} \frac{T_{\infty}}{T_s} \frac{p_s}{p_{\infty}} \left( \frac{p_s}{p_{\infty}} - 1 \right) \right]^{\frac{1}{4}} (\cos \lambda)^{1.1}$$

$$\dot{q} = 0.57 Pr^{-0.6} (\rho_w \mu_w)^{0.1} (\rho_o \mu_o)^{0.4} (H_o - H_w) \sqrt{\left( \frac{dV_N}{dx} \right)_s} * 0.7071 (\cos \lambda)^{1.15}$$





## APPENDIX – A10

### Free Molecular and Transitional Flows

Flow regimes are characterized based on Knudsen number (Kn), which is defined as

$$K_n = \frac{\lambda}{c}$$

Where  $\lambda$  is the mean free path and  $c$  is a characteristic length (usually the body dimension or boundary layer thickness  $\delta$ ).

$$\lambda = \frac{\mu}{\rho} \sqrt{\frac{\pi}{2RT}}$$

Based on boundary layer thickness,  $K_n = \sqrt{\frac{\pi r}{2}} \frac{M}{\sqrt{Re}}$ , for  $Re \gg 1$ .

Based on body length,  $K_n = \sqrt{\frac{\pi r}{2}} \frac{M}{Re}$ , for  $Re < 1$ .

| Knudsen Number  | Flow Type      |
|-----------------|----------------|
| $Kn < 0.01$     | Continuum      |
| $0.01 < Kn < 1$ | Slip           |
| $1 < Kn < 10$   | Transition     |
| $Kn > 10$       | Free molecular |

Heat transfer in the intermediate regime is given as

$$q_{tran} = p q_{free} + (1 - p) q_{continuum}$$

$$\text{where } p = \frac{Kn}{1 + Kn}$$

Free molecular heat transfer is given by

$$q_{tran} = \alpha \rho R T_\infty \sqrt{\frac{RT_\infty}{2\pi}} \left\{ \left( s^2 + \frac{r}{r-1} - \frac{r+1}{2(r-1)} \frac{T_w}{T_\infty} \right) + \left( e^{-(s \sin \theta)^2} + \sqrt{\pi} s \sin \theta (1 + e r f s \sin \theta) \right) - \frac{1}{2} e^{-(s \sin \theta)^2} \right\}$$

Where  $\alpha$  is the accommodation coefficient

$$s \text{ is the speed ratio, } s = \frac{\mu_\infty}{\sqrt{2RT_\infty}}$$

$\theta$  is the flow angle of incidence

## APPENDIX – A11

### Free Convection and Radiation inside the air gap of a Multilayer Insulation system

In the air layer, all the three modes of heat transfer take place and for solving the multilayer conduction equation an equivalent conductivity can be estimated.

#### Two dimensional free convection between Parallel Plates (with length L and gap h)

Rayleigh number,

$$Ra = \frac{g\beta(T_{outer} - T_{inner})}{\nu \left( \frac{k}{\rho \alpha_p} \right)}$$

$$\nu = \frac{\mu}{\rho} \text{ and } \beta = \frac{2}{(T_{outer} + T_{inner})}$$

$$\overline{Ra} = Ra \cdot \frac{h}{L}$$

$$C_l = \frac{4}{3} * 0.48 \left( \frac{Pr}{Pr + 0.861} \right)^{\frac{1}{4}}$$

Define  $C_3 = 12 * 0.919 * C_l^{\frac{1}{4}}$

Then the heat transfer parameter (Nusselt number) is given by

$$Nu = C_l \left( \overline{Ra} \right)^{\frac{1}{4}} S$$

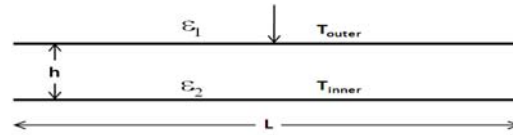
and heat transfer coefficient is given as

$$h_c = \frac{Nu \cdot k}{h}$$

where  $S = \sum_{n=1}^{\infty} C_3^{n-1} (-1)^{n-1} \frac{3}{(4n-1)(n-1)!}$

Free convection heat flux between the plates,

$$q_c = h_c (T_{outer} - T_{inner})$$



## Axissymmetric Free Convection in the Annular Region between Two Co-axial Infinite Cylinders (with gap h)

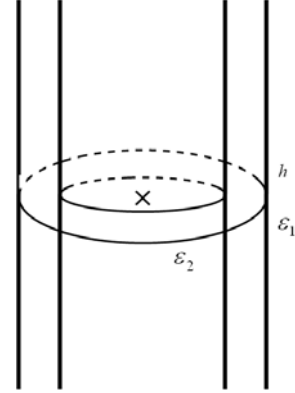
Rayleigh number,

$$Ra = \frac{g \beta (T_{outer} - T_{inner}) h^3}{\nu \left( \frac{k}{\rho c_p} \right)}$$

$$\overline{Ra} = \frac{Ra \ln \left( \frac{D_{outer}}{D_{inner}} \right)^4}{h^3 \nu (D_{outer}^{-0.6} + D_{inner}^{-0.6})^5}$$

$$K_{eff} = 0.386 \left( \frac{Pr}{Pr + 0.861} \right)^{\frac{1}{4}} (\overline{Ra})^{\frac{1}{4}}$$

$$h_c = \frac{2k k_{eff}}{\ln \left( \frac{D_{outer}}{D_{inner}} \right) D_{inner}} \quad Nu = \frac{2h h_c}{k}$$



Free convection heat flux between the cylinders is

$$q_c = h_c (T_{outer} - T_{inner})$$

### Radiative heat flux between the two surfaces

Define  $F = \sqrt{1 + \left( \frac{L}{R} \right)^2} - \frac{h}{L}$  (for 2D)

$$F = \frac{D_{inner}}{D_{outer}} \text{ (for axis-symmetric)}$$

Define  $\varepsilon_{equivalent} = \frac{1}{\frac{(1 - \varepsilon_1)}{\varepsilon_1} + \frac{(1 - \varepsilon_2)}{\varepsilon_2} + \frac{1}{F}}$

$$\text{Radiative flux } q_{rad} = \sigma \varepsilon_{eq} (T_{outer}^4 - T_{inner}^4)$$

## APPENDIX – A12

### Input Variables

1. **TITLE** : 80 CHARACTERS

2. **INPUT CARDS:**

| Card 1       | Card 2        | Card 3       | Card 4      | Card 5       | Card 6        | Card 7      | Card 8       | Card 9       | Card 10       |
|--------------|---------------|--------------|-------------|--------------|---------------|-------------|--------------|--------------|---------------|
| <b>ITIPR</b> | <b>ITERPR</b> | <b>IMACH</b> | <b>IKHS</b> | <b>NCOMP</b> | <b>IAXISM</b> | <b>IPAR</b> | <b>ICART</b> | <b>ITHIN</b> | <b>KELVIN</b> |

| Card 11       | Card 12     | Card 13    | Card 14    | Card 15   | Card 16      | Card 17      | Card 18     | Card 19     | Card 20     |
|---------------|-------------|------------|------------|-----------|--------------|--------------|-------------|-------------|-------------|
| <b>ITABLE</b> | <b>ISHK</b> | <b>INV</b> | <b>IGM</b> | <b>IT</b> | <b>ICOND</b> | <b>ITRAN</b> | <b>IAIR</b> | <b>IFRC</b> | <b>IRAD</b> |

|               |     |  |
|---------------|-----|--|
| <b>ITIPR</b>  | = 0 | No detailed print  |
|               | = 1 | Detailed print at each time step   |
|               | = N | Detailed print after n time step   |
| <b>ITERPR</b> | = 0 | No detailed print during iteration                                       |
|               | = 1 | Detailed print during iteration interval mentioned in the following line |
| <b>IMACH</b>  | = 0 | Mach no history is read in trajectory                                    |
|               | = 1 | Velocity history is read in trajectory                                   |
| <b>IKHS</b>   | = 0 | Aerodynamic heating is computed  |
|               | = 1 | Heat flux history is given as input                                      |
| <b>NCOMP</b>  |     | No of geometrical component on the body                                  |
| <b>IAXISM</b> | = 0 | The flow is two dimensional  |
|               | = 1 | The flow is axi-symmetric  |
| <b>IPAR</b>   | = 0 | No perturbation on nominal values of various parameters                  |
|               | = 1 | Perturbation ratios given in variable <b>PAR</b> read afterwards         |
| <b>ICART</b>  | = 0 | Cartesian coordinate for conduction analysis                             |
|               | = 1 | Cylindrical coordinate for conduction analysis                           |
|               | = 2 | Spherical coordinate for conduction analysis                             |
| <b>ITHIN</b>  | = 0 | Thin layer option not used in phase change studies                       |
|               | = 1 | Thin layer option used in phase change studies                           |
| <b>KELVIN</b> | = 0 | Temperature values in table in Kelvin                                    |
|               | = 1 | Temperature values in table in Celsius                                   |

|                           |     |   |
|---------------------------|-----|---|
| <b>ITABLE</b>             | = 0 | Tables of output parameters not required  |
|                           | = 1 | Tables with parameters after each time steps  |
|                           | = N | Tables with parameters after n time steps   |
| <b>ISHK</b>               | = 0 | No shock is considered ahead of body  |
|                           | = 1 | Ideal shock ahead of body   |
|                           | = 2 | Real shock ahead of body  |
| <b>INV</b>                |     | Parameters used for inviscid flow field selection   |
| <b>IGM</b>                |     | Parameter used for defining geometry for stagnation point computation                       |
| <b>(Case 1: IAXISM=0)</b> |     |   |
| <b>IGM</b>                | = 1 | Thick infinite flat plate (for IAXISM=0)  |
|                           | = 2 | Cylinder in cross flow with no sweep  |
|                           | = 3 | Cylinder in cross flow with sweep, laminar  |
|                           | = 4 | Cylinder in cross flow with sweep, turbulent  |
| <b>(Case 2: IAXISM=1)</b> |     |   |
| <b>IGM</b>                | = 1 | Flat heat cylinder  |
|                           | = 2 | Cone frustum  |
|                           | = 3 | Sphere  |
| <b>IT</b>                 | = 0 | Flow can be laminar transitional or turbulent   |
|                           | = 1 | Flow is considered turbulent for low value of Reynolds No: also                             |
| <b>ICOND</b>              | = 0 | Thermal response analysis required  |
|                           | = 1 | Coldwall heatflux   |
| <b>ITRAN</b>              | = 1 | Transition from laminar to turbulent flow is based on Reynolds No. using wetted length      |
|                           | = 2 | Transition from laminar to turbulent flow is based on Reynolds No. using momentum thickness |
| <b>IAIR</b>               | = 0 | If no air layer is considered   |
|                           | = N | If the nth layer is air layer considered  |
| <b>IFRC</b>               | = 1 | Free convection to be considered at inner surface   |
|                           | = 0 | Free convection not to be considered at inner surface                                       |
| <b>IRAD</b>               | = 1 | Radiation to be considered at the inner surface   |
|                           | = 0 | Radiation from the inner surface not to be considered                                       |

### 3. PRINT COMMANDS: TITER1,TITER2(READ IF ITERPR=1)

|               |                                   |
|---------------|-----------------------------------|
| <b>TITER1</b> | Time for starting iteration print |
| <b>TITER2</b> | Time for stopping iteration print |

**4. INPUT FOR CYLINDRICAL & SPHERICAL COORDINATE SYSTEM: RRT (READ IF ICART  $\neq$  0)**

**RRT**                      Outer radius for cylindrical and spherical co-ordinate systems

**5. LIMITING LENGTHS FOR THIN LAYER OPTIONS: X1THIN,X2THIN(READ IF ITHIN#0)**

**X1THIN**                      Thickness of first layer less than which thin layer options are exercised

**X2THIN**                      Thickness of second layer less than which thin layer options are exercised

**6. INPUTS FOR AIR COLUMNS / GAPS: EL,EH,E1,E2(READ IF IAIR#0)**

**EL**                              Length of air column if ICART = 0  
Outer radius of air column if ICART  $\neq$  0

**EH**                              Gap of air column if ICART = 0  
Inner radius of air column if ICART  $\neq$  0

**E1**                              Emissivity of outer surface close to air column

**E2**                              Emissivity of inner surface close to air column

**7. FREE CONVECTION PARAMETERS: AL,TAMB( READ IF IFRC # 0)**

**AL**                              Length of body participating in free convection heat transfer

**TAMB**                              Ambient temperature

**8. AMBIENT TEMPERATURE: TAMB(READ IF IRAD #0)**

**TAMB**                              AMBIENT TEMPERATURE

**9. GEOMETRY DESCRIPTION VARIABLES: (RR(I), EPS(I), RL(I), I=1, NCOMP)**

**RR(I)**                              Rounding radius of each geometrical component in the vehicle configuration

**EPS(I)**                              Body angle of each geometrical

**RL(I)**                              Length of each geometrical component in the vehicle configuration

**10. FLOW PARAMETERS: RETR,RETS,ALAMDA,ALFA,QRAD,QINS,RC,GIN**

**RETR**                              Transition Reynolds No:

**RETS**                              Reynolds no at the station where transition is initiated

**ALAMDA**                              Sweep angle

**ALFA**                              Total angle of attack

**QRAD**                              Radiative heat input

**QINS**                              Heat generated inside

|            |  |
|------------|--|
| <b>RC</b>  | Typical body dimension for computation of Knudsen number           |
| <b>GIN</b> | Initial value of gas constant (GIN = 1.2 for reentry trajectories) |

**11. NUMBER OF TRAJECTORY POINTS: NT**

|           |                                   |
|-----------|-----------------------------------|
| <b>NT</b> | Total number of trajectory points |
|-----------|-----------------------------------|

**12. TRAJECTORY DATA: TIMM(I),ALT(I),AMACH(I),ALPHA(I),I=1,NT)**

|                 |  |
|-----------------|--|
| <b>TIMM(I)</b>  | Time values in trajectory input            |
| <b>ALT(I)</b>   | Altitude values in trajectory input        |
| <b>AMACH(I)</b> | Mach no values in trajectory input         |
| <b>ALPHA(I)</b> | Angle of attack values in trajectory input |

**13. INITIAL CONDITION & CONVERGENCE CRITERIA: TW1,MPD,MCD,TOL1,TOL2**

|             |   |
|-------------|---|
| <b>TW1</b>  | Initial temperature                                       |
| <b>MPD</b>  | Initial rate at which charring is taking place            |
| <b>MCD</b>  | Initial rate at which ablation is taking place            |
| <b>TOL1</b> | Upper limit error for convergence in temperature          |
| <b>TOL2</b> | Upper limit for convergence in charring or ablation rates |

**14. TIME OF START & STOP: TIN, TFINAL**

|             |                                       |
|-------------|---------------------------------------|
| <b>TIN</b>  | Initial time for starting computation |
| <b>TFIN</b> | Final time for stopping computation   |

**15. NUMBER OF STEPS IN COMPUTATION INTERVAL: NDT**

|            |  |
|------------|--|
| <b>NDT</b> | No of steps in changing computation interval |
|------------|--|

**16. TIME ARRAY FOR COMPUTATION INTERVAL CHANGE: TIA(I),DTA(I),I=1,NDT**

|                |   |
|----------------|---|
| <b>TIA (I)</b> | Time array for computation interval change      |
| <b>DTA (I)</b> | Time step array for computation interval change |

**17. DEFINE MATERIAL, THICKNESS & OPTIMIZATION CONTROL PARAMETERS:**

**NLAYER,(L(I),I=1,NLAYER),LAYOPT,MOPT(M(I)=1,NLAYER),X,(X3(I),I=1,NLAYER),  
OPTW,TOLOPT,DXOPT,ISUBLM**

|               |  |
|---------------|--|
| <b>NLAYER</b> | No of material layer analysis  |
| <b>L(I)</b>   | No of computational steps in in each layer                                   |
| <b>LAYOPT</b> | Index of the interface node where temperature constraint is to be maintained |
| <b>MOPT</b>   | Index of the material layer whose thickness is to be optimized               |

|               |     |   |
|---------------|-----|---|
|               |     | for meeting the temperature constraint                            |
| <b>M(I)</b>   |     | Material index of each layer as given in material file            |
| <b>X</b>      |     | Axial distance from nose tip                                      |
| <b>X3(I)</b>  |     | Material thickness for each layer                                 |
| <b>OPTW</b>   |     | Temperature constraint  |
| <b>TOLOPT</b> |     | Tolerance for convergence on temperature constraint               |
| <b>DXOPT</b>  |     | Initial trial variation in the thickness of layer to be optimized |
| <b>ISUBLM</b> | = 0 | First layer is not subliming type                                 |
|               | = 1 | First layer is subliming type                                     |

**18. AUGMENTATION / PERTURBATION PARAMETERS: PAR(I),I=1,16 (READ IF IPAR=1)**

|                 |  |
|-----------------|--|
| <b>PAR (I)</b>  | Perturbation values for various parameters |
| <b>PAR (1)</b>  | Heat transfer co-efficient                 |
| <b>PAR (2)</b>  | Emissivity                                 |
| <b>PAR (3)</b>  | Char layer density                         |
| <b>PAR (4)</b>  | Char layer specific heat                   |
| <b>PAR (5)</b>  | Char layer conductivity                    |
| <b>PAR (6)</b>  | Virgin layer density                       |
| <b>PAR (7)</b>  | Virgin layer specific heat                 |
| <b>PAR (8)</b>  | Virgin layer conductivity                  |
| <b>PAR (9)</b>  | Third layer density                        |
| <b>PAR (10)</b> | Third layer specific heat                  |
| <b>PAR (11)</b> | Third layer conductivity                   |
| <b>PAR (12)</b> | Specific heat of pyrolysis gas             |
| <b>PAR (13)</b> | Ablation temperature                       |
| <b>PAR (14)</b> | Heat of ablation                           |
| <b>PAR (15)</b> | Pyrolysis temperature                      |
| <b>PAR (16)</b> | Heat of pyrolysis                          |



## **APPENDIX – A13**

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### **List of Subroutines**

#### **Main Program**

The main program reads various inputs (like the body geometry, trajectory, inviscid data and material properties) and various options. Various control parameters for output are also read along with other inputs. The input variables are printed after reading for verification. The variable types and dimensions are defined in the main program. For a specified location on body, the main program calls other subroutines in a sequence and stores the results like heat flux and temperature distribution. Based on these inputs, writing of the various parameters is also carried out in this module. Storing of all relevant variables for further processing as well as writing in tables is carried out in this module. The flow chart of the software code is given in [Fig. 18](#). Following are the subroutines used in the software package.

#### **BODY**

This subroutine computes the local radius, surface distance and body angle for the given axial location by using the vehicle geometry

#### **ATMOS**

For the altitude under consideration, this subroutine computes the free stream properties of temperature, pressure, density and sonic speed.

#### **MATPRO**

From a material library, this subroutine reads the temperature dependent properties of thermal conductivity, specific heat, density (with phase change) and emissivity and later during the computation computes the properties at all nodal points. It also reads the char-ablation properties for applicable cases.

#### **SHOCK**

This subroutine computes the flow properties after a normal shock by solving one-dimensional conservation of mass, momentum and energy, numerically using Hansen's tables.

#### **SHWAVE**

For a given free stream Mach number and flow deflection angle, this subroutine computes the flow properties after an oblique shock.

#### **INVSCD**

This subroutine computes the local flow properties (pressure, temperature and Mach number) at the boundary layer edge, from the post shock conditions using isentropic relations based on the local pressure or Mach number (either read as input or using build in routines).

#### **GASPRO**

The air properties for ideal gas and real gas options are evaluated in this subroutine. For computation of equilibrium air properties, the subroutine calls Subroutine HANSEN

#### **HANSEN**

Subroutine HANSEN evaluates thermo-dynamic and transport properties of air at given temperature and pressure. There are two options built in the program. The properties are interpolated from a given table.

#### **STAGPT**

This subroutine computes the stagnation point heat flux using the method of Fay and Riddell and the stagnation line heat flux using Beckwith and Gallagher formula.

#### **HEATSR**

The heat flux in the stagnation region is computed in this subroutine using the method of Lees where the stagnation point heat flux is also used.

#### **AEROHT**

This subroutine computes the heat flux at a location on the aft-body. For laminar as well as transitional turbulent flows, using Van Driest or Eckert Formulas [5].

#### **FREEMOL**

The heat flux in the free-molecular regime is computed in this subroutine using standard correlations available.

#### **TRANMOL**

The heat in the transition regime (transition from free-molecular to continuum) is computed here using both free-molecular and continuum heat flux values.

#### **TEMP1D**

This subroutine computes the tri-diagonal matrix of finite difference equations generated using fully implicit scheme.

#### **SURM1D**

This subroutine computes the mass loss and the surface movement in case of ablation or melting and charring rate and interface movement in case of pyrolysis.

#### **SOURCE**

Any heat generation or dissipation is introduced in the finite difference equation here.

#### **BOUNDS**

The finite difference equations are modified in this subroutine to take care of surface boundary conditions.

**BOUNDI**

The finite difference equations are modified in this subroutine to take care of inside boundary conditions.

**GAUSS**

This subroutine computes the nodal temperatures from the finite difference equations using the tri-diagonal matrix solution procedure.

**LINEA**

This is a subroutine for linear interpolation from a given table.

## APPENDIX – A14

### Output Variables

1. TI,ALTI,EMINF,ALFA,TINF,ROINF,PINF,EME,TE,ROE,UE,PE,REY,CF,CH,TAW,EKS,P,QFM,QCONT,IFL,ITRN,RATIO,TO,GO,DYNP,CFL,CFT,HOI

|              |  |
|--------------|--|
| <b>TI</b>    | Current time   |
| <b>ALTI</b>  | Altitude at time T1  |
| <b>EMINF</b> | Mach Number at time T1   |
| <b>ALFA</b>  | Angle of attack  |
| <b>TINF</b>  | Free stream temperature  |
| <b>ROINF</b> | Free stream density  |
| <b>PINF</b>  | Free stream pressure   |
| <b>EME</b>   | Mach No. at boundary layer edge  |
| <b>TE</b>    | Temperature at boundary layer edge   |
| <b>ROE</b>   | Density at boundary layer edge   |
| <b>UE</b>    | Velocity at boundary layer edge  |
| <b>PE</b>    | Pressure at boundary layer edge  |
| <b>Rey</b>   | Reynolds No: at boundary layer edge  |
| <b>CF</b>    | Skin friction coefficient  |
| <b>CH</b>    | Stanton number   |
| <b>TAW</b>   | Adiabatic wall temperature   |
| <b>EKS</b>   | Knudsen number   |
| <b>P</b>     | Intermittency factor between free molecular and continuum heat flux                |
| <b>QFM</b>   | Free molecular heat flux   |
| <b>QCONT</b> | Continuum heat flux  |
| <b>IFL</b>   | Parameter showing condition of flow  |
| <b>IFL</b>   | = 0 Continuum flow   |
|              | = 1 Transition flow  |
|              | = 2 Free molecular flow  |
| <b>ITRN</b>  | Parameter showing number of iterations   |
| <b>RATIO</b> | Ratio of heat flux on specific location on sphere to heat flux at stagnation point |
| <b>TO</b>    | Total temperature  |
| <b>GO</b>    | Ratio of specific heats of gases at temperature TO                                 |
| <b>DYNP</b>  | Dynamic pressure   |
| <b>CFL</b>   | Laminar skin friction coefficient  |
| <b>CFT</b>   | Turbulent skin friction coefficient  |
| <b>HOI</b>   | Total enthalpy   |

**2. H,TW,QAAERO,QNET,QQW,MPD,MCD,X1,X2**

|              |                                      |
|--------------|--------------------------------------|
| <b>H</b>     | Heat transfer coefficient            |
| <b>TW</b>    | Wall temperature                     |
| <b>QAERO</b> | Heat flux due to aerodynamic heating |
| <b>QNET</b>  | Net heat flux                        |
| <b>QQW</b>   | Instrument heating                   |
| <b>MPD</b>   | Rate of char formation               |
| <b>MCD</b>   | Rate of char ablation                |
| <b>X1</b>    | Current thickness of first layer     |
| <b>X2</b>    | Current thickness of second layer    |

**3. (T(I), I = IFIRST, ILAST)**

|             |                                       |
|-------------|---------------------------------------|
| <b>T(I)</b> | Temperature at different nodal points |
|-------------|---------------------------------------|

## APPENDIX – A15

### Sample of Input File

**RLV AERODYNAMIC HEATING FOR HEX MISSION NOSECAP (RLV PROJECT) upper bound**

**ITI, ITER, IMA, IKHS, NCO, IAX, IPA, ICAR, ITHN, KEL, ITAB, ISHK, INV, IGM, IT, CON, ITR, IAI, IFR, IRA, IAL**

100 0 1 0 2 1 1 0 0 0 10 2 4 3 0 1 1 0 0 0 1

0.125 14.0 0.418 0.0 0.0 6.5

0.50E+06 0.0 0.0 0.0 0.0 0.0 0.125 1.4

1037

|    |          |         |        |         |         |
|----|----------|---------|--------|---------|---------|
| 0  | 15.188   | 0       | 0      | 0       | 0       |
| 10 | 488.249  | 108.401 | 0.3134 | -1.5737 | 6.5671  |
| 20 | 2227.821 | 249.331 | 0.7338 | -0.4844 | 29.3963 |
| 30 | 4944.63  | 327.958 | 0.9898 | -0.4524 | 38.4456 |

-----

-----

|      |         |         |        |        |        |
|------|---------|---------|--------|--------|--------|
| 1000 | 875.735 | 126.367 | 0.3668 | 6.6442 | 8.5994 |
| 1010 | 632.031 | 125.071 | 0.3621 | 6.6374 | 8.6242 |
| 1020 | 391.307 | 123.742 | 0.3574 | 6.6305 | 8.6353 |
| 1036 | 10.515  | 121.725 | 0.3502 | 6.6217 | 8.6524 |

313.0 2\*0.0 1.0 0.0

0.0 1.0 1036.0 13\*0.0 1036.0

1 50 0 0 41 0.0 0.003 1033.0 1.0 0.0001 0

0.0 15\*0.0

## Sample of Output File

### RLV AERODYNAMIC HEATING FOR HEX MISSION NOSECAP (RLV PROJECT) upper bound

ITIPR=10 ITERPR= 0 IMACH= 1 IKHS= 0 NCOMP= 2 IAXISM= 1 IPAR= 1 ICART= 0 ITHIN= 0 KELVIN= 0 ITABLE=10

ISHK= 2 INV= 4 IGM= 3 IT= 0 ICOND= 1 ITRAN= 1 IAIR= 0 IFRC= 0 IRAD= 0 IALFA= 1

RADIUS,ANGLE + LENGTH FOR EACH PART IS

0.125000 14.000000 0.418000

0.000000 0.000000 6.500000

RETR= 0.50000E+06 RETS= 0.00000E+00 ALAMDA= 0.00 ALFA= 0.00 QAB= 0.000 QINS= 0.000 RC= 0.125

### TRAJECTORY DATA

#### TIME

0.00E+00 1.00E+00 2.00E+00 3.00E+00 4.00E+00 5.00E+00 6.00E+00 7.00E+00 8.00E+00 9.00E+00

-----  
-----

1.03E+03 1.03E+03 1.03E+03 1.03E+03 1.03E+03 1.04E+03 1.04E+03

#### ALT

1.52E-02 1.65E-02 2.61E-02 4.54E-02 7.46E-02 1.14E-01 1.65E-01 2.28E-01 3.02E-01 3.89E-01

-----

---

1.53E-01 1.29E-01 1.05E-01 8.17E-02 5.80E-02 3.42E-02 1.05E-02

**MACH.NO**

0.00E+00 5.46E+00 1.48E+01 2.47E+01 3.50E+01 4.59E+01 5.72E+01 6.91E+01 8.16E+01 9.47E+01

---



---

1.22E+02 1.22E+02 1.22E+02 1.22E+02 1.22E+02 1.22E+02 1.22E+02

**ANGLE OF ATTACK**

0.00E+00 -4.20E-03 -1.09E-02 -2.01E-02 -7.40E-01 -2.46E+00 -3.46E+00 -3.65E+00 -3.00E+00 -2.24E+00

---



---

6.62E+00 6.62E+00 6.62E+00 6.62E+00 6.62E+00 6.62E+00 6.62E+00

0 1 1036 0 0 0 0 0 0 0 0 0 0

0 0 0 1036

PAR- 0 0 0 0 0 0 0 0 0 0

0 0 0 0 0 0 0



**LOCATION= 0.000000**

THICKNESS 0.003000

NLAYER= 1 L= 50

TWI= 313.00 MPD= 0.00000 MCD= 0.00000 TOL1= 1.00000

TOL2= 0.00000

**LAYER NO. 1 INCONEL 71**

| TEMP           | CONDUCTIVITY | TEMP         | SP.HEAT      | TEMP         | DENSITY      | TEMP       | EMISSIVITY |
|----------------|--------------|--------------|--------------|--------------|--------------|------------|------------|
| + 0.300000E+03 | 0.262700E-02 |              |              |              |              |            |            |
| +              |              | 0.300000E+03 | 0.920000E-01 |              |              |            |            |
| +              |              |              |              | 0.293000E+03 | 0.822000E+04 |            |            |
| +              |              |              |              |              |              | 273.000000 | 0.500000   |
| + 0.373000E+03 | 0.284300E-02 |              |              |              |              |            |            |
| +              |              | 0.513000E+03 | 0.979000E-01 |              |              |            |            |
| +              |              |              |              | 0.973000E+03 | 0.822000E+04 |            |            |
| +              |              |              |              |              |              | 973.000000 | 0.500000   |
| + 0.473000E+03 | 0.324900E-02 |              |              |              |              |            |            |
| +              |              | 0.605000E+03 | 0.109400E+00 |              |              |            |            |
| + 0.573000E+03 | 0.363100E-02 |              |              |              |              |            |            |
| +              |              | 0.715000E+03 | 0.123300E+00 |              |              |            |            |

+ 0.973000E+03 0.520800E-02

+ 0.833000E+03 0.138100E+00

+ 0.107300E+04 0.561400E-02

+ 0.901000E+03 0.146400E+00

+ 0.157300E+04 0.752500E-02

+ 0.103500E+04 0.163200E+00

+ 0.113800E+04 0.175000E+00

TA= 5000.00 TP= 5000.00 HA= 1.00 HP= 2.00 RAW110= 3.00 RAW10= 4.00 RAW20= 5.00

### ***INITIAL TEMP DISTRIBUTION***

313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0

313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0

313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0

313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0 313.0

313.0 313.0 313.0 313.0 313.0 313.0 313.0

---

X= 0.00000E+00 Y= 0.00000E+00 S= 0.00000E+00 THET= 0.90000E+02 IC= 0

\*\*\*\*\* ITERATION CONVERGED \*\*\*\*\*

TIME=0.1000E+01 ALT= 0.017 M8= 0.016 U8= 5.5 T8=300.6 R8=0.1167E+01 P8=0.1027E+05 REN=0.3449E+06 TAUW=0.1738E+02 HO= 72.15  
EME= 0.00 TE= 300.61 UE=0.00000E+00 PE=0.10273E+05 ROE=0.11676E+01 REY=0.00000E+00 CFL=0.00000E+00 CFT=0.00000E+00 CF=0.00000E+00  
EKS=0.53995E-06 P= 0.000 QFM=0.00000E+00 QCONT=-.83906E-01 IFL= 0 ITR= 0 0 0 0 0 0 0 0 0 0 RATIO= 0.000  
GE= 0.000 CH=0.00000E+00 TAW= 0.0 TRCR=0.00000E+00 REZ=0.00000E+00 FACT=0.000 IBL= 0 ELN=0.00000E+00 HD=0.00000E+00 FRF=0.99933E+00

TIME=0.1036E+04 ALT= 0.011 M8= 0.350 U8= 121.7 T8=300.6 R8=0.1168E+01 P8=0.1028E+05 REN=0.7699E+07 TAUW=0.8654E+04 HO= 73.92  
EME= 0.00 TE= 308.01 UE=0.00000E+00 PE=0.11188E+05 ROE=0.12410E+01 REY=0.00000E+00 CFL=0.00000E+00 CFT=0.00000E+00 CF=0.00000E+00  
EKS=0.53968E-06 P= 0.000 QFM=0.00000E+00 QCONT=-.16462E+00 IFL= 0 ITR= 1 50 50 50 50 50 50 50 50 1 RATIO= 0.000  
GE= 0.000 CH=0.14013E-44 TAW= 0.0 TRCR=0.00000E+00 REZ=0.00000E+00 FACT=0.000 IBL= 0 ELN=0.00000E+00 HD=0.00000E+00 FRF=0.99673E+00

TIME=0.1400E+01 ALT= 0.000 M8=\*\*\*\*\* U8= 0.0 T8= 0.0 R8=0.0000E+00 P8=0.0000E+00 REN=0.1400E+01 TAUW=0.1228E-35 HO= 1.00

EME=

PO=0.1119E+05 TO= 308.0 CPP= 0.000000

H= 0.32989E-01 TW= 313.0 QAERO= -0.165 QNETT= -0.230 QQW= 0.00000 MPD= 0.00000 MCD= 0.00000 X1=0.300000E-02 X2=0.000000E+00

**RLV AERODYNAMIC HEATING FOR HEX MISSION NOSECAP (RLV PROJECT) upper bound**

**0.3000E-02**

**LOCATION= 0.000000**

**THICKNESS 0.003000**

| TIME | ALT   | M8   | ME | REY.NO   | TAUW     | H        | TAW    | QAERO  | QNET   | TEMP.DISTRIBUTION |     |     |
|------|-------|------|----|----------|----------|----------|--------|--------|--------|-------------------|-----|-----|
| 10   | 0.49  | 0.31 | 0  | 6.61E+06 | 6.57E+03 | 1.22E-02 | 303.6  | -0.119 | -0.147 | 3                 | 313 | 313 |
| 80   | 28.55 | 5.61 | 0  | 2.62E+06 | 3.32E+04 | 2.50E-02 | 1535.5 | 30.479 | 30.452 | 3                 | 313 | 313 |
| 83   | 31.16 | 6.22 | 0  | 1.93E+06 | 2.79E+04 | 2.39E-02 | 1847.7 | 36.22  | 36.192 | 3                 | 313 | 313 |
| 100  | 45.54 | 5.86 | 0  | 2.26E+05 | 3.60E+03 | 8.81E-03 | 1864.5 | 13.325 | 13.298 | 3                 | 313 | 313 |
| 180  | 77.31 | 6.26 | 0  | 3.60E+03 | 3.98E+01 | 8.72E-04 | 1547   | 1.074  | 1.046  | 0                 | 313 | 313 |
| 200  | 76.38 | 6.24 | 0  | 4.18E+03 | 4.66E+01 | 7.04E-04 | 1551.8 | 0.877  | 0.85   | 35                | 313 | 313 |
| 280  | 42.06 | 5.28 | 0  | 3.23E+05 | 4.56E+03 | 6.91E-03 | 1571.5 | 8.812  | 8.784  | 35                | 313 | 313 |
| 288  | 38.4  | 5    | 0  | 5.16E+05 | 6.62E+03 | 8.51E-03 | 1408.6 | 9.418  | 9.39   | 32.7              | 313 | 313 |
| 300  | 35.37 | 4.45 | 0  | 7.23E+05 | 7.90E+03 | 9.80E-03 | 1150.1 | 8.217  | 8.19   | 27.3              | 313 | 313 |
| 400  | 32.89 | 2.66 | 0  | 6.31E+05 | 3.98E+03 | 6.97E-03 | 569    | 1.788  | 1.761  | 16.2              | 313 | 313 |
| 500  | 20.53 | 1.88 | 0  | 3.46E+06 | 1.29E+04 | 1.22E-02 | 355.5  | 0.519  | 0.491  | 5                 | 313 | 313 |
| 600  | 13.57 | 0.81 | 0  | 4.71E+06 | 7.70E+03 | 9.23E-03 | 238.8  | -0.686 | -0.713 | 6.9               | 313 | 313 |
| 700  | 9.25  | 0.63 | 0  | 5.69E+06 | 8.88E+03 | 1.08E-02 | 265.6  | -0.514 | -0.542 | 6.2               | 313 | 313 |
| 800  | 6.23  | 0.49 | 0  | 5.99E+06 | 8.07E+03 | 1.14E-02 | 278.7  | -0.39  | -0.418 | 6.7               | 313 | 313 |
| 900  | 3.43  | 0.42 | 0  | 6.76E+06 | 8.41E+03 | 1.25E-02 | 291.4  | -0.269 | -0.297 | 6.7               | 313 | 313 |
| 1000 | 0.88  | 0.37 | 0  | 7.47E+06 | 8.60E+03 | 1.35E-02 | 303.3  | -0.13  | -0.158 | 6.6               | 313 | 313 |
| 1036 | 0.01  | 0.35 | 0  | 7.70E+06 | 8.65E+03 | 1.38E-02 | 308    | -0.069 | -0.096 | 6.6               | 313 | 313 |

**QTOTAL= 185.38 J/CM\*CM**

## **ANNEXURE – B 1**

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### **EXTERNAL TPS DESIGN PHILOSOPHY**

#### **Thermal Environments**

- ✓ Aerodynamic heating rates and total heat loads are computed for worst case trajectory considering 3-sigma dispersions in vehicle performance and atmospheric parameters.
- ✓ Heat load due to solar radiation and earth albedo is to be added to convective heating rates.
- ✓ Localized increase in heating rate in the vicinity of and on protuberance is to be considered.
- ✓ In the base region of the vehicle (of multi-strapon configuration) convective heating due to recirculating flow, radiation heating from solid particles in jet exhaust and radiation heating from hot nozzle divergent of liquid engines should be taken into account
- ✓ Effect of reflected radiation and recirculating flow after jet impingement on flame deflector at the time of lift-off.

#### **Design practices being followed / recommended for external TPS design**

For identification of thermal environments till PSLV program, worst case trajectory was being selected from among a set of actual control trajectories simulating winds, wind shear and gust at different key level altitudes along with 3-sigma dispersions in performance of various stage motors. For GSLV, ideal control trajectory along with 3-sigma dispersions in propulsion parameters and constant angle of attack of 4 deg throughout the ascent phase of flight was used. Considering the uncertainties in modeling of boundary layer transition, aerodynamic heating rates are computed assuming fully turbulent flow for ascent vehicles. Augmentation in heating rates in the vicinity of protuberances is based on [23].

- (a) Experimental data for similar protuberances available in literature
- (b) Augmentation in heat transfer coefficient based on correlation formulae proposed by F. T. Hung involving pressure ratio before and after the shock formed ahead of protuberance

The dispersions in the atmospheric data (pressure, temperature and density are considered separately. The pressure distribution over the vehicle supplied is considered for heat load calculations. No perturbation over this is considered.

The computations of heat flux on spacecraft front surface after heat shield jettisoning is based on stagnation point heating computed for continuum flow and fully free molecular flow and use of bridging relation based on Knudsen number for transitional flow regime. A 15% margin on TPS thickness is considered to account for uncertainties in thermo-physical and optical properties of insulation material at elevated temperatures; perturbations in atmospheric density and temperature; inviscid flow field data variations. Details were accepted in GDRT (V & M) [24, 25].

## ANNEXURE – B 2



Aeronautics Entity  
VIKRAM SARABHAI SPACE CENTRE  
THIRUVANANTHAPURAM - 695022

**S.V.Sharma**  
**Deputy Director**

VSSC: AERO: A-1.1:10

06-01-2010

### OFFICE ORDER NO 01/2010

ISRO is developing new vehicles like RLV & Human Rated Launch Vehicle and Modules like Crew Module and also modifying of existing launch vehicles and re-entry modules. These vehicles and modules require generation of data on aerodynamics venting, base heating and thermal design.

To cater to these requirements existing software codes like Boundary Layer Code "KELBLR", BASE2D, VENT and One Dimensional Thermal Analysis Package "OTAP" are being used.

To meet the center level requirements on software configuration control and to ensure continuity in the usage of these softwares, following team is constituted to bring out a formulation document and user's manual for all the above mentioned softwares:

1. Shri. R.Swaminathan, Chairman/Head, ARD
2. Shri. V.Ashok, Vice Chairman/Dy. Head, ARD
3. Shri. Venkat Sivaram Jadhav ARD
4. Shri Haroon Rasheed, ARD
5. Shri. C. Babu, ARD
6. Dr. T.V.Radhakrishnan, AHTD
7. Shri. P.Anoop, AHTD
8. Shri. Rony C. Varghese, AHTD
9. Shri. Ram Prabhu, AHTD
10. Shri. Sundar.B, AHTD, Convenor

The team may complete the above tasks by Feb 2010.

*S.V.Sharma*  
**(S.V.SHARMA)**

To

All the members of the team  
GD,ADTG  
Head, AHTD  
Head, ARD  
Head, PPEC