

Elliptic

April 9, 2015

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In [1]: # Solving Poisson's equation
        #  $u_{xx} + u_{yy} = 0$ 
        # For the boundary conditions
        #  $u = 0$ ; for  $x = 0$ ;  $y = 0$ 
        #  $u = x^2$  along  $y = 4$ ;  $0 < x < 4$ 
        #  $u = 16y$  along  $x = 4$ ;  $0 < y < 4$ 

import numpy as np

dx = 0.05
dy = 0.05

# Max values of X and Y are 4
n = int(4/dx)
m = int(4/dy)
X = np.linspace(0, 4, n)
Y = np.linspace(0, 4, m)

U = np.zeros((n, m), dtype=np.float32) # U at nth iteration
# U at (n + 1)th iteration, yet to be calculated

# Initializing U
U[n-1, :] = X**2
U[:, m-1] = 16*Y

U_ = np.zeros((n, m), dtype=np.float32)
for k in range(40): # number of iterations
    U_ = np.zeros((n, m), dtype=np.float32)
    U_[n-1, :] = X**2
    U_[:, m-1] = 16*Y
    for i in range(1, n - 1):
        for j in range(1, m - 1):
            U_[i, j] = (1/(2*(dx**2 + dy**2)))*((dy**2)*(U_[i-1, j] + U_[i+1, j]) + (dx**2)*(U_[i, j-1] + U_[i, j+1]))
    U = U_.copy()

In [6]: %matplotlib inline
import matplotlib.pyplot as plt

plt.plot(X, U[:, 60]); plt.plot(X, U[:, 70]); plt.plot(X, U[:, 75])
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Out[6]: [<matplotlib.lines.Line2D at 0x7f2e4c01b250>]
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