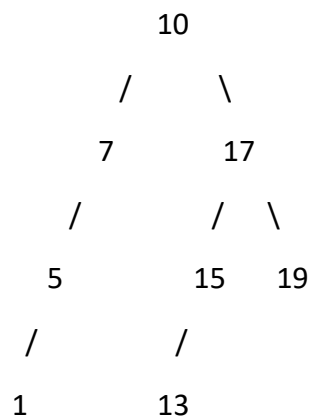


Merge Two Binary Search Trees into one Balanced Binary Tree [CodeStudio](#)

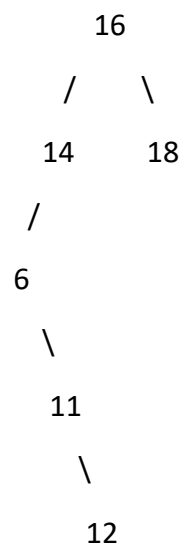
You are given Two Binary Search Tree of integers having M and N nodes merge the two trees and return the root of the newly created balanced binary tree.

Example:

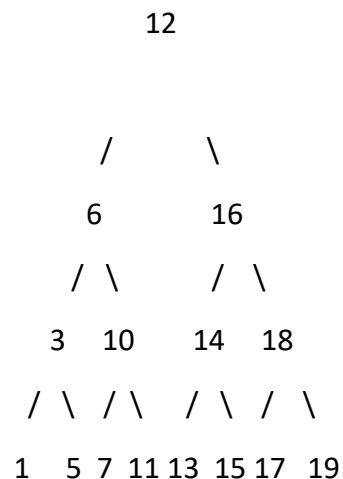
Tree 1:



Tree 2:



Output:



Inorder Traversal: 1 3 5 6 7 10 11 12 13 14 15 16 17 18 19

Approach 1: Merge two Binary Search Trees into a single Binary Search Tree using Inorder Traversal

- **Function Purpose:**
 - Merges two Binary Search Trees (BSTs) into a single balanced BST.
- **Explanation:**
 - Perform in-order traversal on both input BSTs and store the nodes in two separate arrays.
 - Merge the two sorted arrays into one.
 - Create a balanced Binary Search Tree from the merged array.
- **Time Complexity:**
 - In-order traversal of each BST: $O(N1)$ and $O(N2)$, where $N1$ and $N2$ are the number of nodes in the respective BSTs.
 - Merging two sorted arrays: $O(N1 + N2)$.
 - Creating a balanced BST: $O(N1 + N2)$.
 - Total time complexity: $O(N1 + N2)$.
- **Space Complexity:**
 - Space for storing in-order traversal arrays: $O(N1 + N2)$.
 - Additional space for recursion and variables: $O(H1 + H2)$, where $H1$ and $H2$ are the heights of the two BSTs.
 - Total space complexity: $O(N1 + N2 + H1 + H2)$.

Approach 2: Merge two BSTs into one optimized BST using Doubly Linked List

- **Function Purpose:**
 - Merges two Binary Search Trees (BSTs) into a single optimized balanced BST using doubly linked lists.
- **Explanation:**
 - Convert both input BSTs to sorted doubly linked lists.
 - Merge the two sorted doubly linked lists into one.
 - Create a balanced Binary Search Tree from the merged doubly linked list.
- **Time Complexity:**
 - Converting BSTs to doubly linked lists: $O(N1 + N2)$.
 - Merging sorted doubly linked lists: $O(N1 + N2)$.
 - Creating a balanced BST from the merged doubly linked list: $O(N1 + N2)$.
- **Space Complexity:**
 - Space for storing doubly linked lists: $O(N1 + N2)$.
 - Additional space for recursion and variables: $O(H1 + H2)$.
 - Total space complexity: $O(N1 + N2 + H1 + H2)$.

Conclusion:

- Both approaches have the same time and space complexities.
- The choice between Approach 1 and Approach 2 depends on the specific use case and preference.
- Approach 1 directly uses arrays, while Approach 2 uses doubly linked lists, which may be more memory-efficient in certain scenarios.
- **Approach 2 can be advantageous when memory efficiency is a concern, while Approach 1 may be preferable for simplicity.**