## Find All subsets of an array (Power Set) <a href="LeetCode"><u>LeetCode</u></a>

You are tasked with developing a program that generates all possible subsets of a given set of distinct integers. A subset of a set is defined as a group of elements that can be selected from the original set, maintaining their relative order.

## Approach 1: Function to find all subsets using backtracking

- 1. The **solve** function is the core of this approach, implementing backtracking.
- 2. The function takes four parameters:
  - nums: The input set of distinct integers.
  - output: The current subset being formed.
  - index: The current index in the input set.
  - ans: The vector to store the generated subsets.
- 3. The base case checks if the current **index** is greater than or equal to the size of the input set. If true, it means all elements have been considered, so the current **output** is added to **ans**.
- 4. The function first explores the scenario where the current element is excluded from the subset by calling **solve** with the same **index** but incremented by 1.
- 5. Then, it includes the current element in the subset, adds it to **output**, and again calls **solve** with an incremented **index**.
- 6. This approach systematically explores all possible combinations of including or excluding each element in the subset.
- 7. Time Complexity: Exponential O(2^n), where n is the number of elements in the input set.
- 8. Space Complexity: Linear O(n), due to recursion stack and output vector.

## Approach 2: Function to find all subsets using backtracking (Alternative implementation)

- 1. The **findSubset** function is the key recursive function for this approach.
- 2. Similar to Approach 1, it takes four parameters: nums, output, index, and ans.
- 3. After adding the current **output** to **ans**, the function iterates through the remaining elements, starting from the given **index**.
- 4. For each element, it includes the element in the **output**, recursively calls **findSubset** with an incremented index, and then removes the last added element from the **output** (backtrack).

- 5. This approach is also a backtracking approach, but the logic is organized slightly differently compared to Approach 1.
- 6. Time Complexity: Exponential O(2^n), akin to the first approach.
- 7. Space Complexity: Linear O(n), similar to the first approach.

## Approach 3: Function to find the power set using the Bitwise approach

- 1. This approach uses bitwise manipulation to generate subsets directly.
- 2. It calculates the total number of subsets as 2<sup>n</sup>, where n is the number of elements in the input set.
- 3. The outer loop iterates through integers from 0 to 2<sup>n</sup> 1.
- 4. For each integer, the inner loop iterates through each bit position (element index) in the input set.
- 5. If the j-th bit of the current integer is set (using bitwise AND with (1 << j)), the corresponding element is included in the current subset.
- 6. The subsets are constructed and added to the final ans.
- 7. Time Complexity: Exponential O(n \* 2^n), as each subset involves iterating over all elements.
- 8. Space Complexity: Exponential O(n \* 2^n), due to storing all generated subsets.