

Least Recently Used (LRU) Cache [LeetCode](#)

Design a data structure that follows the constraints of a **Least Recently Used (LRU)** cache.

Least recently used (LRU)

Discards the least recently used items first. **This algorithm requires keeping track of what was used when, which is expensive if one wants to make sure the algorithm always discards the least recently used item.**

Implement the LRUCache class:

- LRUCache(int capacity) Initialize the LRU cache with **positive** size capacity.
- int get(int key) Return the value of the key if the key exists, otherwise return -1.
- void put(int key, int value) Update the value of the key if the key exists. Otherwise, add the key-value pair to the cache. If the number of keys exceeds the capacity from this operation, **evict** the least recently used key.

Approach 1: Implementation of LRUCache using Queue and Hashmap approach

In this approach, we use a combination of a queue (to maintain the order of recently used keys) and a hashmap (to store key-value pairs). The queue helps us keep track of the least recently used item, and the hashmap allows for quick retrieval of values associated with keys.

1. LRUCache(int capacity)

- Constructor for initializing the LRUCache with a specified capacity.
- Initializes the capacity, creates a dummy head and tail for the doubly linked list, and initializes an empty hashmap.

2. get(int key)

- Retrieves the value associated with the given key from the cache.
- If the key is found in the hashmap:
 - Reorganizes the queue to move the accessed key to the front (indicating it's the most recently used).
 - Returns the value associated with the key.
- If the key is not found, returns -1 to indicate a cache miss.

- **Time Complexity: $O(n)$**

In the worst case, where 'n' is the capacity of the cache, when the key is not found in the cache and you need to reorganize the queue, it takes $O(n)$ time to search for the key in the queue.

- **Space Complexity: $O(n)$**

The space complexity is $O(n)$ because you are using a hashmap to store key-value pairs, and a queue to maintain the order of keys.

3. **put(int key, int value)**

- Inserts or updates a key-value pair in the cache.
- If the key is found in the hashmap (indicating an update):
 - Reorganizes the queue to move the modified key to the front (indicating it's the most recently used).
- If the key is not found (indicating an insert):
 - Adds the new key to the front of the queue.
- If the cache exceeds its capacity:
 - Removes the least recently used key from the queue and the hashmap.
- Updates the value associated with the key in the hashmap.
- **Time Complexity: $O(n)$**

Similar to get, in the worst case, it takes $O(n)$ time to search for the key in the queue when you need to reorganize it.

- **Space Complexity: $O(n)$**

The space complexity is $O(n)$ because you are using a hashmap to store key-value pairs, and a queue to maintain the order of keys.

Approach 2: Implementation of LRU Cache using Doubly Linked List and Hashmap approach

In this approach, we use a doubly linked list to maintain the order of recently used items and a hashmap to store key-value pairs. The doubly linked list provides efficient removal and insertion of nodes for LRU management.

1. **LRUCache(int capacity)**

- Constructor for initializing the LRU Cache with a specified capacity.
- Initializes the capacity, creates a dummy head and tail for the doubly linked list, and initializes an empty hashmap.

2. **get(int key)**

- Retrieves the value associated with the given key from the cache.
- If the key is found in the hashmap:
 - Removes the corresponding node from its current position in the doubly linked list.

- Moves the node to the front of the linked list (indicating it's the most recently used).
- Returns the value associated with the key.
- If the key is not found, returns -1 to indicate a cache miss.

- **Time Complexity: $O(1)$**

Retrieving the value associated with a key from the hashmap is an $O(1)$ operation. Additionally, moving a node to the front of the doubly linked list is also an $O(1)$ operation.

- **Space Complexity: $O(n)$**

The space complexity is $O(n)$ because you are using a hashmap to store key-value pairs, and a doubly linked list to maintain the order of keys.

3. **put(int key, int value)**

- Inserts or updates a key-value pair in the cache.
- If the key is found in the hashmap (indicating an update):
 - Updates the value associated with the key.
 - Removes the corresponding node from its current position in the doubly linked list.
 - Moves the node to the front of the linked list (indicating it's the most recently used).
- If the key is not found (indicating an insert):
 - Creates a new node with the key and value.
 - Inserts the new node to the front of the doubly linked list.
 - Adds the new key-value pair to the hashmap.
- If the cache exceeds its capacity:
 - Removes the least recently used node from the tail of the linked list.
 - Removes the corresponding key from the hashmap.
- **Time Complexity: $O(1)$**

Inserting or updating a key-value pair in the hashmap is an $O(1)$ operation. Moving a node to the front of the doubly linked list is also an $O(1)$ operation.
- **Space Complexity: $O(n)$**

The space complexity is $O(n)$ because you are using a hashmap to store key-value pairs, and a doubly linked list to maintain the order of keys.