

Merge K Sorted Arrays [CodeStudio](#)

You are given K arrays which are individually sorted in ascending order. You need to merge all the given arrays such that the output array should be sorted in ascending order.

Example: [1, 5, 9], [45, 90], [2, 6, 78, 100, 234]

Output: [1, 2, 5, 6, 9, 45, 78, 90, 100, 234]

Approach 1: Function to merge k sorted arrays using a brute force approach

- **Functionality:**
 - Merges k sorted arrays using a brute force approach.
- **Explanation:**
 - Iterates through each array and element to collect all values.
 - Sorts the collected values to obtain the final merged array.
- **Time Complexity:**
 - **mergeKSortedArraysBruteForce:**
 - Time complexity for iterating through each array and element: $O(N)$, where N is the total number of elements in all arrays.
 - Sorting the collected values: $O(N \log N)$.
 - Overall Time Complexity: $O(N \log N)$.
- **Space Complexity:**
 - $O(N)$, where N is the total number of elements in all arrays.

Approach 2: Function to merge k sorted arrays using a min-heap

- **Functionality:**
 - Merges k sorted arrays using a min-heap.
- **Explanation:**
 - Creates a min-heap using **Element** objects representing values, row index, and column index.
 - Initializes the min-heap with the first element from each array.
 - Continues merging elements until the min-heap is empty.
- **Time Complexity:**
 - **mergeKSortedArraysUsingHeap:**

- Time complexity for initializing the min-heap: $O(K \log K)$, where K is the number of arrays.
- Each insertion and extraction from the heap: $O(N \log K)$, where N is the total number of elements in all arrays.
- Overall Time Complexity: $O(N \log K)$.
- Space Complexity:
 - $O(K)$, where K is the number of arrays.

Approach 3: Merge k sorted arrays using a divide and conquer approach

- **Functionality:**
 - Merges two sorted arrays, recursively merges halves of k arrays, and merges k sorted arrays using divide and conquer.
- **Explanation:**
 - Utilizes **mergeTwoSortedArray** to merge two sorted arrays.
 - Recursively merges left and right halves using **mergeKSortedArrayHelper**.
 - Merges the two sorted halves using **mergeTwoSortedArray**.
- **Time Complexity:**
 - **mergeTwoSortedArray**: $O(M + N)$, where M and N are the sizes of the two arrays being merged.
 - **mergeKSortedArrayHelper**:
 - Time complexity for each level of recursion: $O(N)$.
 - Number of levels in the recursion: $O(\log K)$.
 - Overall Time Complexity: $O(N \log K)$, where N is the total number of elements in all arrays, and K is the number of arrays.
 - **mergeKSortedArraysDivideAndConquer**: $O(N \log K)$.
- **Space Complexity:**
 - $O(N)$, where N is the total number of elements in all arrays.

Conclusion

- **Brute Force**: Simple, but less efficient due to sorting.
- **Min Heap**: Efficient for large datasets, particularly when K is significantly smaller than the total number of elements.

- **Divide and Conquer:** Balances efficiency and simplicity, suitable for various scenarios.