# 09.4 - Deep Learning - Convolutional Neural Networks

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# 1 Programming for Data Science and Artificial Intelligence

# 1.1 9.4 Deep Learning - Convolutional Neural Networks

# 1.1.1 Readings

- [WEIDMAN] Ch5
- [CHARU] Ch8

```
[1]: #import from last time work so we can extend further
from neuralnet.second_version import *
import numpy as np
from numpy import ndarray
```

So far we have focus on **Dense** layers (or also known as fully-connected layer) which are nice in understanding relationships. Adding **activation function** like Sigmoid or Tanh allows us to understand the non-linear relationship between features and output, with Tanh having a steeper gradient, allowing the network to learn faster. Adding **SoftMaxCrossEntropy** also enhance the gradient produced but remember that it only works with classification problems. Adding **Dropout** helps in overfitting; **glorot initialization** to make sure the weight is normally distributed, **learning decay** to make sure we eventually reach the minimum instead of hopping all over the places, and last, the **momentum** to make sure we do not stuck in local minimum. Such architecture is usally quite okay for **normal classification** problem.

However, when we talk about specific classification problem such as image or text or signal, they all have specific nature that would benefit from different architectures.

Today, we gonna work on image (this field is called computer vision) and discuss why Dense layer may not be the best, and propose CNN (Convolutional Neural Network) as a better way for dealing with image classification.

There are mainly three layers that can help dealing with images:

- 1. Convolutional layer
- 2. Max/Average pooling layer
- 3. Flatten layer

#### 1.1.2 1. Convolutional Layer

Let's say given a image of  $24 \times 24$  pixels = 576 features like this. Each data point is an array of numbers describing how dark each pixel is, where value range from 0 to 255. These values can be normalized ranging from 0 to 1. For example, for the following digit (the digit 1), we could have:

We might input these features into Dense layers and try to ask the Dense layers to understand the relationships.

However, this is not so optimal since we do not actually understand the nature of image. The key is that each single pixel actually holds very little information, right? However, pattern of image can be better recognized by patches of pixels, rather than single pixel. Imagine I give you a picture of cat, and I give you only a one-fourth of the picture, can you recognize that it's a cat? Probably yes. But what if I give you a single pixel....you will have zero idea.

Why pattern of images are better recognized by patches?...because humans recognize some visual patterns like corners, edges, sharpness. Combining all these visual patterns form the image. This is how humans visualize, and in fact, we should also apply these principles to neural networks

So how do we generate each patch of feature?...actually, it is very easy. We simply perform a convolution operation like this:

Mathematically, it looks like this:

Let's say we have a 5 x 5 input image I:

$$I = \begin{bmatrix} i_{11} & i_{12} & i_{13} & i_{14} & i_{15} \\ i_{21} & i_{22} & i_{23} & i_{24} & i_{25} \\ i_{31} & i_{32} & i_{33} & i_{34} & i_{35} \\ i_{41} & i_{42} & i_{43} & i_{44} & i_{45} \\ i_{51} & i_{52} & i_{53} & i_{54} & i_{55} \end{bmatrix}$$

Each of this pixel may represent the brightness ranging from 0 to 255.

If we define a 3 x 3 patch which we commonly called **weights** (**W**) or in computer vision, we called **filters/kernels** like this:

$$w = \begin{bmatrix} w_{11} & w_{12} & w_{13} \\ w_{21} & w_{22} & w_{23} \\ w_{31} & w_{32} & w_{33} \end{bmatrix}$$

Let's say we are scanning the middle of the image, then the output feature would be (we'll denote this as  $o_{33}$ ):

$$o_{33} = w_{11} * i_{22} + w_{12} * i_{23} + w_{13} * i_{24} + w_{21} * i_{32} + w_{22} * i_{32} + w_{23} * i_{34} + w_{32} * i_{43} + w_{33} * i_{44}$$

This will result in one output feature. Of course, we may add bias to it and then will be fed through an activation function.

When we do this operation across the whole image, this is called **convolution** which will result in the output features

There are actually a few questions remain to be answer namely:

- 1. How should the weights/filters/kernels look like? How many filters we should apply?
- 2. How should we convolve?

- 3. How about the step of convolution?
- 4. What should be the shape of the weight matrix or the convolutional filters and the output matrix?

#### A. Kernels

1. How should the weights/filters/kernels look like? It turns out that each filter actually detect the presence of certain visual pattern. For example, this filter below detects whether there is an edge at that location of the image. There are also other similar filters detecting corners, lines, etc. Check out https://setosa.io/ev/image-kernels/ and try changing the values

$$w = \begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

Real kernels can look like this. They may look somewhat random at first glance, but we can see that clear structure being learned in most kernels. For example, kernels 3 and 4 seem to be learning diagonal edges in opposite directions, and other capture round edges or enclosed spaces:

Then how many filters we should apply. For each image, we can apply multiple filters. If we apply 2 filters, the output features will become 3D like this:

.

We commonly called number of filters as **channels** (or **feature maps**) and then can also easily generalize to

Actual feature map look like this. Each feature map is a output of a single training example and convolve each kernel over the sample. In simple words, if we have n filters, then we have n feature maps. They represent the activation part corresponding to the kernels.

#### B. Padding

2. How should we convolve?. Should we do the entire image? Should we maintain the output features to be the same size as input features? Recall this image:

It has  $4 \times 4$  pixels = 16 features. But after convolution, we only got  $2 \times 2$  pixels = 4 features left. Is that good? There is no correct answers here but we are quite sure that we lose some information. In fact, it is always nice to **maintain the output features to be the same size as input features**, but how? There is no space to convolve since the filter is  $2 \times 2$  and it can only shift right one time.

The answer is **padding**, where we can enlarge the input image by padding the surroundings with zeros. How much? Padding until we get the original size or larger size, for example, like this. The below put **half padding** which result the output features to be the same size as input features.

The below put **full padding** which pad to make sure each single pixel is convoluted, which result the output features to be even large

Mathematically, it is easiest to understand padding from the 1D input like this:

$$input = [1, 2, 3, 4, 5]$$

to

$$input_{padded} = [0, 1, 2, 3, 4, 5, 0]$$

Normally, large size may benefit from more features, but also suffer from lengthy training time. It is probably best to only perform enough padding to get the same size as input features.

#### C. Strides

3. How about the step of convolution Should we shift 1 step per convolution, or 2 steps, or how many steps. In fact, it really depends on how detail you want it to be. But defining bigger steps reduce the feature size and thus reduce the computation time. Bigger step is like human scanning picture more roughly but can reduce the computation time....whether to use it is something to be experimented though.

In computer vision, we called this step as **stride**. Example is like this:

No padding with stride of 1

Padding with stride of 1

Padding with stride (odd)

Actual image convolution can look like this:

And the convoluted image look like this:

The formula to be used to measure the padding value to get the spatial size of the input and output volume to be the same with stride 1 is

$$\frac{K-1}{2}$$

where K is the filter size.

Here, our K has size 3 so the padding should be (3-1)/2=1

This means that if our image is size 24\*24, and the filter size is 3x3, then we need to add **a border** of one pixel valued 0 around the outside of the image, which would result in the input image of size 26\*26

In some python library such as Keras, we can set the padding=same to get this effect

# D. Shape of the weight matrix and output

4. What should be the shape of the weight matrix or the convolutional filters and the output matrix? Recall that in Dense layer, the shape of weight matrix is defined as

$$neuron_{in} * neuron_{out}$$

For example, given a image of  $24 \times 24$  pixels = 576 features. Let's say we got around 1000 images, thus our input has a shape of (1000, 576). Thus the input layer should have 576 neurons. Let's say our next hidden layer has 10 neurons, what should be the shape of the weight matrix? The answer is easy, we need to simply find the? here:

$$(1000, 576)$$
@? =  $(1000, 10)$ 

Obviously, the weight matrix would be

where you can clearly see 576 is the number of input neurons and 10 is the number of output neurons.

Now our question is **how about convolutional layers**. In convolutional layer, the shape of input has shape of (num of samples \* image height \* image width \* num of channels). For example, let's say after our first CNN layer, we have 1000 samples, 4 channels - edges, corners and horizontal and vertical lines, and image height and width to be 24, thus the shape of input is (1000, 24, 24, 4). Now let's say we want to go to the next CNN layer and apply 2 filters? What should be the shape of the weight matrix? Also, what would be the shape of the output? The answer is a little tough, but we know one thing is that the number of samples will remain the same, and the channel will be same as number of filters we apply, thus we get:

$$(1000, 24, 24, 4) \otimes ? = (1000, ?, ?, 2)$$

The size actually depends on the stride (S), padding (P), and input size (W) with the formula as follows:

$$O = \frac{W - F + 2P}{S} + 1$$

Here, O is the output height/length, W is the input height/length, F is the filter size, P is the padding, and S is the stride.

Suppose we have an input image of size 24 \* 24 \* 4, we apply 2 filters of size 3 \* 3, with single stride and no zero padding.

Here W=24, F=3, P=0 and S=1.

The size of the output volume will be ([24-3+0]/1)+1=22. Therefore the output volume will be 22\*22\*2. Thus

$$(1000, 24, 24, 4) \otimes (4, 2, 3, 3)_{p=0, s=1} = (1000, 22, 22, 2)$$

In conclusion,

- The input will have a 4D shape of (size, image height, image width, input channels)
- The output will have a 4D shape of (size, changed image height, changed image width, ouput channels)
- The convolutional filters will have 4D shape of (input channels, filter height, filter width, output channels)

Note: The order does not matter and it depends on the python library you use but these four dimensions always exist in CNN.

\*\*The general rule of selecting padding, stride and filter size are of course of trial-and-error. But it's important to remember that they should result in output image size of integers not decimals"

**Demo** https://www.cs.ryerson.ca/~aharley/vis/conv/

# 1.1.3 2. Max/Average Pooling Layer

Talking about **reducing computation time**, another way is to perform a **pooling layer** which simply downsample the image by average a set of pixels, or by taking the maximum value. If we define a pooling size of 2, this involves mapping each 2 x 2 pixels to one output, like this:

Nevertheless, pooling has a really big downsides, i.e., it basically lose a lot of information. Compared to strides, strides simply scan less but maintain the same resolution but pooling simply reduce the resolution of the images....As Geoffrey Hinton said on Reddit AMA in 2014 - **The pooling operation used in CNN is a big mistake and the fact that it works so well is a disaster**. In fact, in most recent CNN architectures like ResNets, it uses pooling very minimially or not at all. In this lecture, we are not going to implement pooling, but we just talk about it for the sake of completeness since very early architectures like AlexNet uses pooling

# 1.1.4 3. Flatten Layer

It must be said that in CNN, probably there are many convolutional layers. However, in the last layer, typically, if we want to predict a certain class, it make sense to use Dense layer as the output layer. However, the question is how do we send input of shape (size, image height, image width, input channels) into Dense layer?

This is actually quite easy. What we can do is simply squash all these 4D vectors into 2D vectors. For example, given (1000, 22, 22, 2), through a *flatten* operation, the vector becomes (1000, 968), which we can then multiply with weight just like in Dense layer, make predictions, and calculate loss just like we did in previous class.

Why we can perform *flatten* operation? Does it not lost any information? This is because through flattening, the information is not lost...in fact, it is just another representations, thus flattening does not result in any loss of information. It also allow the Dense layer to understand the relationships of visual patterns from prior convolutional layers to the output.

Flattening is as simple as this:

# 1.1.5 Let's start coding!!

### 1.1.6 1D input

First off, to make us easily understand CNN coding, let's start simple, working with 1D input. Also let's write some helpers to make our life easier, namely assert—same—shape, and assert—dim

```
[2]: def assert_same_shape(A: ndarray, B: ndarray):
    assert A.shape == B.shape

def assert_dim(X: ndarray, dim: ndarray):
    assert len(X.shape) == dim
```

Padding Padding can be easily coded. Let's start simple with 1D input like this:

```
[3]: input_1d = np.array([1,2,3,4,5])
param_1d = np.array([1,1,1])
```

```
[5]: _pad_1d(input_1d, 1)
```

[5]: array([0, 1, 2, 3, 4, 5, 0])

Forward pass - convolution Convolution in 1D is simple.

We are actually doing something like this: [0, 1, 2, 3, 4, 5, 0] [1, 1, 1] = 0\*1 + 1\*1 + 2\*1 = 3 [1, 1, 1] = 1\*1 + 2\*1 + 3\*1 = 6 [1, 1, 1] = 9 [1, 1, 1] = 12 [1, 1, 1] = 9

```
output = np.zeros(input_.shape) # [0, 0, 0, 0, 0]

# perform the 1d convolution
# 2. Use the padded input and params to compute output
for o in range(output.shape[0]): #0 to 4
    for w in range(param_len): #0 to 2
        output[o] += param[w] * input_pad[o+w] #0 move along with w thus o+w

# ensure input has same shape as output
# this is actually optional
assert_same_shape(input_, output)

return output
```

Next, we code the sum, which is basically sum everything return by the convolution.

```
[8]: conv_1d_sum(input_1d, param_1d)
```

[8]: 39.0

**Gradients** How to compute the gradients of convolution?

Let's first try some set of numbers and manually get the gradients:

```
[9]: #randomly choose to increase 5th element by 1
#so we can know the gradient of 5th element in respect to the convolution sum
input_1d_2 = np.array([1,2,3,4,6])
param_1d = np.array([1,1,1])

conv_1d_sum(input_1d_2, param_1d)
```

[9]: 41.0

What does this mean? Since we change the 5th element by 1, which increase the convolution sum by 2, thus the gradient of the 5th element is 2.

Let's see how we actually get the 2.

Given

$$t = [0, 1, 2, 3, 4, 5, 0]$$

and

$$w = [1, 1, 1]$$

and let o be the output of convolution:  $o_0....o_4$ 

First, let's look at the convolution equation like this:

$$o_0 = t_0 * w_0 + t_1 * w_1 + t_2 * w_2$$

$$o_1 = t_1 * w_0 + t_2 * w_1 + t_3 * w_2$$

$$o_2 = t_2 * w_0 + t_3 * w_1 + t_4 * w_2$$

$$o_3 = t_3 * w_0 + t_4 * w_1 + t_5 * w_2$$

$$o_4 = t_4 * w_0 + t_5 * w_1 + t_6 * w_2$$

Look at  $t_5$  which is our 5th element, where  $t_5$  is a function of  $w_2$  in respect to  $O_3$ ,  $w_1$  in respect to  $O_4$ , and  $w_0$  in respect to  $O_5$  (which we don't have)

This gradient can be written as:

$$\frac{\partial L}{\partial t_5} = \frac{\partial L}{\partial o_3} * w_2 + \frac{\partial L}{\partial o_4} * w_1 + \frac{\partial L}{\partial o_5} * w_0$$

Since  $o_i$  is contributing to the sum of the convolution sum, its derivative is simply

$$\frac{\partial L}{\partial o_i} = 1$$

Thus,

$$\frac{\partial L}{\partial t_5} = \frac{\partial L}{\partial o_3}*w_2 + \frac{\partial L}{\partial o_4}*w_1 + \frac{\partial L}{\partial o_5}*w_0 = 1*w_2 + 1*w_1 + 0*w_0 = 2$$

since  $o_5$  does not exist

Since we need to code this, we need to see whether there is any general pattern. Let's look at other elements as well:

$$\frac{\partial L}{\partial t_5} = \frac{\partial L}{\partial o_3} * w_2 + \frac{\partial L}{\partial o_4} * w_1 + \frac{\partial L}{\partial o_5} * w_0$$

$$\frac{\partial L}{\partial t_4} = \frac{\partial L}{\partial o_2} * w_2 + \frac{\partial L}{\partial o_3} * w_1 + \frac{\partial L}{\partial o_4} * w_0$$

$$\frac{\partial L}{\partial t_3} = \frac{\partial L}{\partial o_1} * w_2 + \frac{\partial L}{\partial o_2} * w_1 + \frac{\partial L}{\partial o_3} * w_0$$

$$\frac{\partial L}{\partial t_2} = \frac{\partial L}{\partial o_0} * w_2 + \frac{\partial L}{\partial o_1} * w_1 + \frac{\partial L}{\partial o_2} * w_0$$

$$\frac{\partial L}{\partial t_1} = \frac{\partial L}{\partial o_{-1}} * w_2 + \frac{\partial L}{\partial o_0} * w_1 + \frac{\partial L}{\partial o_1} * w_0$$

How should we code this? In terms of code, it is easy to represent

$$w_0, w_1, w_2$$

simply by iterating.

But we need to find a way to represent the output gradients of:

$$\frac{\partial L}{\partial o_{-1}}$$
 to  $\frac{\partial L}{\partial o_5}$ 

In fact, we know

$$\frac{\partial L}{\partial o_{-1}} = 0$$

as well as

$$\frac{\partial L}{\partial o_5} = 0$$

while other gradients are simply one. Thus, we can represent as a list of

Let's called this gradients (grad). It can be a bit confusing now that we got this new grad indices. Also, we shall call the result input\_grad which range from 0 to 4 for each of five elements. Let's rewrite the equation using these indices:

$$inputgrad_4 = grad_4 * w_2 + grad_5 * w_1 + grad_6 * w_0$$
  
 $inputgrad_3 = grad_3 * w_2 + grad_4 * w_1 + grad_5 * w_0$   
 $inputgrad_2 = grad_2 * w_2 + grad_3 * w_1 + grad_4 * w_0$   
 $inputgrad_1 = grad_1 * w_2 + grad_2 * w_1 + grad_3 * w_0$   
 $inputgrad_0 = grad_0 * w_2 + grad_1 * w_1 + grad_2 * w_0$ 

Now we have to map the indices in coding. This is simple.

For each input rad, we need to repeatingly run,  $w_0$  to  $w_2$ , we simply iterate using something like for each input rad for each w

Then for the first input  $input grad_0$ , we need to make sure to run the grad indicies to be 2, 1, 0 in this order. grad indices depend on two things: a) As w up by 1, grad index lower by 1; this can be easily coded simply by subtracting w, thus when w increases, the grad decreases; b) grad index starts at index of input grad + 2, where 2 is actually length of w - 1.

Thus, this can be summarized using this following pseudocode:

for i in range(5) #this will represent index of input grad for w in range(3) # this will represent index of w input grad\_i += grad[i + (len(w) - 1) - w] \* param[w]

This can be written as function like this:

```
[10]: def _input_grad_1d(input_: ndarray,
                          param: ndarray,
                          grad: ndarray = None) -> ndarray:
          param_len = param.shape[0]
          param_mid = param_len // 2
          if grad is None:
              grad = np.ones_like(input_) #choose one so grad can be multiplied and_
       \rightarrownot become zero
          else:
              assert_same_shape(input_, grad)
          #1. pad the output gradients
          grad = _pad_1d(grad, param_mid) #[0, 1, 1, 1, 1, 1]
          #prepare input grad which has grad of the five elements
          #thus the initial look can be [0, 0, 0, 0, 0]
          input_grad = np.zeros_like(input_)
          #2. Use the padded output gradients, along with param, to compute the input \Box
       \rightarrow gradient
          for i in range(input_.shape[0]): #for each input grad which follows the_
       \rightarrow same shape as input
              for p in range(param.shape[0]): #for each param
                   input_grad[i] += grad[i + param_len - 1 - p] * param[p]
          assert_same_shape(input_grad, input_)
          return input_grad
```

[11]: \_input\_grad\_1d(input\_1d, param\_1d)

[11]: array([2, 3, 3, 3, 2])

We just find the gradients of the input. How about the gradients of the w?

Let's try change element 1 by 1

```
[12]: input_1d = np.array([1,2,3,4,5])
param_1d_2 = np.array([2,1,1]) #increase first element by 1
print(conv_1d_sum(input_1d, param_1d_2) - conv_1d_sum(input_1d, param_1d))
```

10.0

So we find that

$$\frac{\partial L}{\partial w_0} = 10$$

Recall this:

$$t = [0, 1, 2, 3, 4, 5, 0]$$

$$w = [1, 1, 1]$$

$$o_0 = t_0 * w_0 + t_1 * w_1 + t_2 * w_2$$

$$o_1 = t_1 * w_0 + t_2 * w_1 + t_3 * w_2$$

$$o_2 = t_2 * w_0 + t_3 * w_1 + t_4 * w_2$$

$$o_3 = t_3 * w_0 + t_4 * w_1 + t_5 * w_2$$

$$o_4 = t_4 * w_0 + t_5 * w_1 + t_6 * w_2$$

We can clearly see that  $w_o$  is changing in respect from  $t_0$  to  $t_4$ . Since  $t_0$  is a 0, and we know that  $\frac{\partial L}{\partial o_i} = 1$ , thus the gradient of the first element is:

$$w_0^{grad} = t_1 + t_2 + t_3 + t_4 = 10$$

The general pattern is:

$$w_0^{grad} = t_0 + t_1 + t_2 + t_3 + t_4$$

$$w_1^{grad} = t_1 + t_2 + t_3 + t_4 + t_5$$

$$w_2^{grad} = t_2 + t_3 + t_4 + t_5 + t_6$$

#### How to code this?

Luckily, you can clearly see that the indices are moving the same direction, thus it is easy to code like this. We simply define grad to be [1, 1, 1, 1, 1] and simply let it multiply with the input\_pad of [0, 1, 2, 3, 4, 5, 0] like this:

[0, 1, 2, 3, 4, 5, 0] [1, 1, 1, 1, 1] = gradient of w0 [1, 1, 1, 1, 1] = gradient of w1 [1, 1, 1, 1, 1] = gradient of w2

```
else:
    assert_same_shape(input_, grad)

#prepare param_grad which has grad of the three w
#thus the initial look can be [0, 0, 0]

param_grad = np.zeros_like(param) #[0, 0, 0]

#2. Use the padded output gradients, along with padded input, to compute_
the param gradient

for i in range(input_.shape[0]):
    for p in range(param.shape[0]):
        #as w increase, shift input_pad right by w amount
        param_grad[p] += input_pad[i+p] * grad[i]

assert_same_shape(param_grad, param)

return param_grad
```

```
[14]: _param_grad_1d(input_1d, param_1d)
```

[14]: array([10, 15, 14])

# 1.1.7 1D input with batch (sample > 1)

How about if we have more samples of the 1D input like this?

# **Padding**

In fact, this is simple, we simply run cov\_1d on the first sample, and iterate and stack the results on top.

```
[17]: _pad_1d_batch(input_1d_batch, 1)
```

```
[17]: array([[0, 0, 1, 2, 3, 4, 5, 6, 0], [0, 1, 2, 3, 4, 5, 6, 7, 0]])
```

#### Forward pass

Same concept. For forward pass, we simply iterate our previous method

```
[19]: conv_1d_batch(input_1d_batch, param_1d)
```

```
[19]: array([[ 1., 3., 6., 9., 12., 15., 11.], [ 3., 6., 9., 12., 15., 18., 13.]])
```

# Backward pass: gradients

For input\_grad, it's the same concept. We simply do a for loop on the previous function we have already defined

```
[21]: input_grad_1d_batch(input_1d_batch, param_1d)
```

However, for param\_grad, since param\_grad is a filter that dependent across samples, thus we need to change our previous code. So, to compute the parameter gradient, we have to loop through all of the observations and increment the appropriate values of the parameter gradient as we do so. Still, this just involves adding an outer for loop to the code to compute the parameter gradient that we saw earlier.

```
input_pad = _pad_1d_batch(input_, 1)

param_grad = np.zeros_like(param)

for s in range(input_.shape[0]):
    for i in range(input_.shape[1]):
        for w in range(param.shape[0]):
            param_grad[w] += input_pad[s][i+w] * grad[s][i]

return param_grad
```

```
[23]: param_grad_1d_batch(input_1d_batch, param_1d)
```

[23]: array([36, 49, 48])

#### 1.1.8 2D convolutions

The 2D convolution is a straightforward extension of the 1D case because, fundamentally, the way the input is connected to the output via the filters in each dimension of the 2D case is identical to the 1D case. Consider this data:

```
[24]: imgs_2d_batch = np.random.randn(3, 5, 5)
param_2d = np.random.randn(3, 3)
```

**Forward pass** Recall that for 1D convolutions the code for computing the output given the input and the parameters on the forard pass looked as follows:

```
\label{lem:def:conv_1d(input_: ndarray, param: ndarray) -> ndarray: param_len = param.shape[0] \\ param_mid = param_len // 2 \\ input_pad = _pad_1d(input_, param_mid) \\ output = np.zeros(input_.shape) for o in range(output.shape[0]): for w in range(param_len): \\ output[o] += param[w] * input_pad[o+w] return output
```

For 2D convolutions, instead of 1D output, we simply make it loop twice for height and width. In addition, instead of 1D param (filter), we break it into two loops, one for filter width, and another for filter height. The code will be simple as this:

**Padding** Of course, this function would requires us to implement \_pad\_2d\_samples which is actually very straightforward. Recall that the code is like this:

def pad\_1d(input: ndarray, padding: int) -> ndarray: zero = np.array([0]) zero = np.repeat(zero, padding) #number of zeros \* num return np.concatenate([zero, input\_, zero])

Let's first check whether the padding works fine:

```
[27]: print("Original shape: ", imgs_2d_batch.shape)
print("Padded shape (must plus 2): ", _pad_2d(imgs_2d_batch, 1).shape)
```

Original shape: (3, 5, 5)

```
Padded shape (must plus 2): (3, 7, 7)
```

Let's try our forward pass for 2D data with samples

```
[28]: print("Original shape: ", imgs_2d_batch.shape)
print("Convoluted shape(must be same): ", _conv_2d(imgs_2d_batch, param_2d).

→shape)
```

```
Original shape: (3, 5, 5)
Convoluted shape(must be same): (3, 5, 5)
```

# Backward pass Input gradients

Recall that for input\_grad, our code is like this:

def \_\_input\_grad\_1d(input\_: ndarray, param: ndarray, grad: ndarray = None) -> ndarray: param\_len = param.shape[0] param\_mid = param\_len // 2 if grad is None: grad = np.ones\_like(input\_) else: assert\_same\_shape(input\_, grad) grad = \_pad\_1d(grad, param\_mid) #[0, 1, 1, 1, 1, 0] input\_grad = np.zeros\_like(input\_) for i in range(input\_.shape[0]): for w in range(param.shape[0]): input\_grad[i] += grad[i + param\_len - 1 - w] \* param[w] return input\_grad

In the 2D case, we simply break our input to 2 loops since we have image width and height, and we also break the param into 2 loops since we have width and height of the filters. Yes, that's it!

```
[29]: def _input_grad_sample_2d(sample: ndarray,
                                param: ndarray,
                                grad: ndarray) -> ndarray:
          param_size = param.shape[0]
          grad = _pad_2d_sample(grad, param_size // 2) #sample refers to each sample
          input_grad = np.zeros_like(sample)
          for i w in range(sample.shape[0]): #imq width
              for i_h in range(sample.shape[1]): #img height
                  for p w in range(param size):
                                                      #filter width
                      for p_h in range(param_size):
                                                        #filter height
                          input_grad[i_w][i_h] += grad[i_w + param_size - 1 -_
       \rightarrowp_w][i_h + param_size - 1 - p_h] \
                          * param[p_w][p_h]
          return input grad
      def _input_grad_2d(samples: ndarray,
                         param: ndarray,
                         grad: ndarray) -> ndarray:
          grads = [_input_grad_sample_2d(samples[i], param, grad[i]) for i in_
       →range(grad.shape[0])]
          return np.stack(grads)
```

[30]: (3, 5, 5)

Param gradients

For the parameter gradient, we have to loop through all the images in the batch and add components from each one to the appropriate places in the parameter gradient. The reason is because the filter gradients overlap over multiple samples.

This is the code we have used earlier for 1D batch

```
\label{lem:def_param_grad_1d_batch(input_: ndarray, param: ndarray) -> ndarray: grad = np.ones_like(input_) input_pad = _pad_1d_batch(input_, 1) param_grad = np.zeros_like(param) for s in range(input_.shape[0]): for i in range(input_.shape[1]): for w in range(param.shape[0]): param_grad[w] += input_pad[s][i+w] * grad[s][i] return param_grad
```

What we have to do is that we have to replace i with two loops representing img width and height, and replace w with two loops, representing filter width and height. Let's do it.

```
Param shape: (3, 3)
Param_grad shape (must equal param2d): (3, 3)
```

**Testing gradients** Let's test whether our code really works. Let's make a code to perform convolution sum for 2d batch, and then we can manually subtract to find the gradients

```
#Testing input gradient

#let's randomly change one pixel of a sample by 1
imgs_2d_batch_2 = imgs_2d_batch.copy()
imgs_2d_batch_2[0][2][2] += 1

manual = conv_2d_sum(imgs_2d_batch_2, param_2d) - conv_2d_sum(imgs_2d_batch, □
→param_2d)
print("Manual: ", manual)
print("Our code: ", img_grads[0][2][2]) #this is already computed above
```

Manual: -0.5138257424616004 Our code: -0.5138257424615983

Manual: -2.658933224682264 Our code: -2.6589332246822615

#### 1.1.9 Channels

Ok....so we have 2D input with batch size. But we still have one more dimension, and that is number of channels. Currently, we assume only one filter so far, what if we have more filters?

The answer, as it was when we added batches earlier, is simple: we add two outer for loops to the code we've already seen—one loop for the input channels and another for the output channels. By looping through all combinations of the input channel and the output channel, we make each output feature map a combination of all of the input feature maps, as desired.

Forward pass Let's code the forward pass for each sample which have channels. This is actually easy, we simply copy our previous code \_conv\_sample\_2d and add two more outer loops, make sure we loop through.

For your reference, this is the previous code we use:

def \_conv\_sample\_2d(sample: ndarray, param: ndarray): param\_mid = param.shape[0] // 2 sample\_pad = \_pad\_2d\_sample(sample, param\_mid) out = np.zeros\_like(sample) for o\_w in range(out.shape[0]): #loop through the image height for o\_h in range(out.shape[1]): #loop through the image width for p\_w in range(param.shape[0]): #loop through the filter width for p\_h in range(param.shape[1]): #loop through the filter height out[o\_w][o\_h] += param[p\_w][p\_h] \* sample\_pad[o\_w+p\_w][o\_h+p\_h] return out

```
[36]: def _conv_sample_channels_2d(sample: ndarray,
                                   param: ndarray):
          ,,,
          sample: [channels, img_width, img_height]
          param: [in_channels, out_channels, fil_width, fil_height]
          I \ I \ I
          assert_dim(sample, 3)
          assert dim(param, 4)
          param_size = param.shape[2]
          param_mid = param_size // 2
          sample_pad = _pad_2d_sample_channel(sample, param_mid) #pad_the input
          #define for loops
          in_channels = param.shape[0]
          out_channels = param.shape[1]
          img_size = sample.shape[1]
          out = np.zeros((out_channels,) + sample.shape[1:])
          for c_in in range(in_channels):
              for c_out in range(out_channels):
                  for i w in range(img size):
                      for i_h in range(img_size):
                          for p w in range(param size):
                              for p_h in range(param_size):
                                   out[c_out][i_w][i_h] += \
                                  param[c_in][c_out][p_w][p_h] *_
       ⇒sample_pad[c_in][i_w+p_w][i_h+p_h]
          return out
      def _conv_channels_2d(input_: ndarray,
                          param: ndarray) -> ndarray:
          input_: [batch_size, channels, img_width, img_height]
```

```
param: [in_channels, out_channels, fil_width, fil_height]

outs = [_conv_sample_channels_2d(sample, param) for sample in input_]

return np.stack(outs)
```

Before we can test this code, let's make sure we implement the padding for channels as well:

Let's test our code whether it works. I will leave the gradient test to you.

```
[38]: img = np.random.randn(10, 3, 32, 32)
param = np.random.randn(3, 16, 5, 5)

print(_conv_channels_2d(img, param).shape) #must equal 10, 16, 32, 32
```

(10, 16, 32, 32)

#### Backward pass Input gradients

We simply add two outer loops for in and out channels.

Here is the previous code for input\_grad for your comparison references

def \_\_input\_grad\_sample\_2d(sample: ndarray, param: ndarray, grad: ndarray) -> ndarray: param\_size = param.shape[0] grad = \_\_pad\_2d\_sample(grad, param\_size // 2) #sample refers to each sample input\_grad = np.zeros\_like(sample) for i\_w in range(sample.shape[0]): #img width for i\_h in range(sample.shape[1]): #img height for p\_w in range(param\_size): #filter width for p\_h in range(param\_size): #filter height input\_grad[i\_w][i\_h] += grad[i\_w + param\_size - 1 - p\_w][i\_h + param\_size - 1 - p\_h] \* param[p\_w][p\_h] return input\_grad def \_\_input\_grad\_2d(samples: ndarray, param: ndarray, grad: ndarray) -> ndarray: grads = [\_input\_grad\_sample\_2d(samples[i], param, grad[i]) for i in range(grad.shape[0])] return np.stack(grads)

```
[39]: def _input_grad_sample_channel_2d(sample: ndarray,
                             grad: ndarray,
                             param: ndarray) -> ndarray:
          111
          sample: [in_channels, imq_width, imq_height]
          grad: [out_channels, img_width, img_height]
          param: [in_channels, out_channels, img_width, img_height]
          111
          #for looping
          param_size = param.shape[2]
          img size = sample.shape[1]
          in_channels = sample.shape[0]
          out_channels = param.shape[1]
          #for holding the result
          input_grad = np.zeros_like(sample)
          #for the output grad
          grad = _pad_2d_sample_channel(grad, param_size // 2)
          for c_in in range(in_channels):
              for c_out in range(out_channels):
                  for i_w in range(img_size):
                      for i h in range(img size):
                          for p_w in range(param_size):
                              for p_h in range(param_size):
                                  input_grad[c_in][i_w][i_h] += \
       →grad[c_out][i_w+param_size-p_w-1][i_h+param_size-p_h-1] \
                                  * param[c_in][c_out][p_w][p_h]
          return input_grad
      def _input_grad_channel_2d(samples: ndarray,
                      grad: ndarray,
                      param: ndarray) -> ndarray:
          grads = [_input_grad_sample_channel_2d(samples[i], grad[i], param) for i in_
       →range(grad.shape[0])]
          return np.stack(grads)
```

Param gradients

Recall that the previous code without channel looks like this:

```
def _param_grad_2d(input_: ndarray, grad: ndarray, param: ndarray) -> ndarray:= param_size = param.shape[0] #for filter width, height input_pad = _pad_2d(input_, param_size // 2) #input_pad param_grad = np.zeros_like(param) img_shape = input_.shape[1:] #get only 5,
```

5 for s in range(input\_.shape[0]): #loop samples for i\_w in range(img\_shape[0]): #loop img width for i\_h in range(img\_shape[1]): #loop img height for p\_w in range(param\_size): #loop param width for p\_h in range(param\_size): #loop param height param\_grad[p\_w][p\_h] += input\_pad[s][i\_w+p\_w][i\_h+p\_h] \* grad[s][i\_w][i\_h] return param\_grad

```
[40]: def param grad 2d channel(input : ndarray,
                      grad: ndarray,
                      param: ndarray) -> ndarray:
          , , ,
          input_: [in_channels, img_width, img_height]
          grad: [out_channels, imq_width, imq_height]
          param: [in_channels, out_channels, imq_width, imq_height]
          #for looping
          sample_size = input_.shape[0]
          param_size = param.shape[2]
          img_size = input_.shape[2]
          in_channels = input_.shape[1]
          out channels = grad.shape[1]
          img_shape = grad.shape[2:]
          #for holding the results
          param_grad = np.zeros_like(param)
          #use for calculating param grads
          input_pad = _pad_2d_channel(input_, param_size // 2)
          for i in range(sample_size):
              for c_in in range(in_channels):
                  for c_out in range(out_channels):
                      for i_w in range(img_shape[0]):
                          for i_h in range(img_shape[1]):
                              for p_w in range(param_size):
                                  for p h in range(param size):
                                       param_grad[c_in][c_out][p_w][p_h] += \
                                       input_pad[i][c_in][i_w+p_w][i_h+p_h] \
                                       * grad[i][c_out][i_w][i_h]
          return param_grad
```

Testing gradients To test, let's simply create a convolution sum based on channels

Manual: -5.345935650419051 Our code: -5.345935650418792

Manual: 55.34918873134302 Our code: 55.34918873134217

# 1.1.10 Putting everything together!!

We need to implement a few more pieces before we can have a working CNN model:

- 1. We have to implement the Flatten operation which is just simple reshape method
- 2. We have to incorporate this Operation as well as the Conv2DOpOperation into a Conv2D Layer
- 3. Finally, for it to be runnable, we have to write an optimized version. I have included this code in the

**Flattening** Flatten is fairly easy:

```
[44]: class Flatten(Operation):
    def __init__(self):
        super().__init__()

def _output(self, inference: bool = False) -> ndarray:
        #squeeze everything to the second dimension
        #(10, 3, 32, 32) --> (10, 3072)
        return self.input_.reshape(self.input_.shape[0], -1)

def _input_grad(self, output_grad: ndarray) -> ndarray:
        #simply transform back
        return output_grad.reshape(self.input_.shape)
```

Layer Setting up the Layer is also fairly easy. We just have to make sure it is possible to set the flag flatten depending on whether we want the output of this layer to be passed forward into another convolutional layer or passed into another fully connected layer for predictions. Flatten should be set True when the next layer is a Dense layer where it expects a flatten input of shape (num\_samples, num\_features)

```
[45]: class Conv2D(Layer):
          def __init__(self,
                       out_channels: int,
                       param_size: int,
                       dropout: int = 1.0,
                       weight_init: str = "glorot",
                       activation: Operation = Linear(),
                       flatten: bool = False) -> None:
              super().__init__(out_channels)
              self.param_size = param_size
              self.activation = activation
              self.flatten = flatten
              self.dropout = dropout
              self.weight_init = weight_init
              self.out_channels = out_channels
          def _setup_layer(self, input_: ndarray) -> ndarray:
              self.params = []
              in_channels = input_.shape[1]
              if self.weight_init == "glorot":
                  scale = 2/(in_channels + self.out_channels)
              else:
                  scale = 1.0
```

**Operation and code optimization** The Operation will need to be revised, to be a more optimized version. As those of you who are familiar with computational complexity will realize, this code is catastrophically slow: to calculate the parameter gradient, we needed to write seven nested for loops! There's nothing wrong with doing this, since the purpose of writing the convolution operation from scratch was to solidify our understanding of how CNNs work.

We'll show how to express the batch, multichannel convolution operation in terms of a batch matrix multiplication to implement it efficiently in NumPy. To understand how the convolution works, consider what happens in the forward pass of a fully connected neural network:

We receive an input of size [batch\_size, in\_features]. We multiply it by a parameter of size [in\_features, out\_features]. We get a resulting output of size [batch\_size, out\_features].

In a convolutional layer, by contrast:

We receive an input of size [batch\_size, in\_channels, img\_height, img\_width]. We convolve it with a parameter of size [in\_channels, out\_channels, param\_height, param\_width]. We get a resulting output of size [batch\_size, out\_channels, img\_height, img\_width].

So the question is how to make the multiplication possible, since we need to prepare it to be something in the form of (i, j) @ (j, k) = (i, k)

The key to making the convolution operation look more like a regular feed-forward operation is to first extract  $img\_height \times img\_width$  "image patches" from each channel of the input image. Once these patches are extracted, the input can be reshaped so that the convolution operation can be expressed as a batch matrix multiplication using NumPy's np.matmul function."

The steps are the followings:

- 1. Get image patches of size [img\_height x img\_width, batch\_size, in\_channels, filter\_size, filter\_size]
- 2. Reshape this to be [batch\_size, img\_height  $\times$  img\_width, in\_channels  $\times$  filter\_size  $\times$  filter\_size
- 3. Reshape parameter to be [in\_channels × filter\_size × filter\_size, out\_channels]
- 4. After we do a batch matrix multiplication, the result will be [batch\_size, img\_height × img\_width, out\_channels]
- 5. Reshape this to be [batch\_size, out\_channels, img\_height, img\_width]

# That's it. That's the forward pass!

For backward pass, it's the same concept. We are just finding the right squeeze-reorder-reshape method so that things can be multiplied into desired shape. Fall in love with vectors? Fantastic right?

```
[46]: class Conv2D_Op(ParamOperation):
          def __init__(self, W: ndarray):
              super().__init__(W)
              self.param_size = W.shape[2]
              self.param_pad = self.param_size // 2
          def _pad_1d(self, inp: ndarray) -> ndarray:
              z = np.array([0])
              z = np.repeat(z, self.param_pad)
              return np.concatenate([z, inp, z])
          def pad 1d batch(self,
                            inp: ndarray) -> ndarray:
              outs = [self._pad_1d(obs) for obs in inp]
              return np.stack(outs)
          def _pad_2d_obs(self,
                                  #obs stands for observation
                          inp: ndarray):
              inp_pad = self._pad_1d_batch(inp)
              other = np.zeros((self.param_pad, inp.shape[0] + self.param_pad * 2))
              return np.concatenate([other, inp_pad, other])
          def _pad_2d_channel(self,
                              inp: ndarray):
              inp has dimension [num_channels, image_width, image_height]
              return np.stack([self._pad_2d_obs(channel) for channel in inp])
```

```
def _get_image_patches(self,
                           input_: ndarray):
       imgs_batch: [batch_size, channels, img_width, img_height]
       #pad the images
       imgs_batch_pad = np.stack([self._pad_2d_channel(obs) for obs in input_])
       patches = []
       img_height = imgs_batch_pad.shape[2]
       #for each location in the images, cut the filter width x filter heighting
\rightarrow image
       #and stack them
       for h in range(img_height-self.param_size+1):
           for w in range(img height-self.param size+1):
               patch = imgs_batch_pad[:, :, h:h+self.param_size, w:w+self.
→param_size]
               patches.append(patch)
       #[img_height * img_width, batch_size, in_channels, param_width,_
\rightarrow param_height]
       return np.stack(patches)
   def output(self,
               inference: bool = False):
       conv_in: [batch_size, channels, img_width, img_height]
       param: [in_channels, out_channels, fil_width, fil_height]
   #
        assert_dim(obs, 4)
        assert_dim(param, 4)
       batch_size = self.input_.shape[0]
       img_height = self.input_.shape[2]
       img_size = self.input_.shape[2] * self.input_.shape[3]
       patch_size = self.param.shape[0] * self.param.shape[2] * self.param.
→shape[3]
       #shape: [img_height * img_width, batch_size, in_channels, param_width, ___
\rightarrow param_height]
       patches = self._get_image_patches(self.input_)
       #reshape to: [batch_size, img_height * img_width, in_channels,_
→ param_width, param_height]
       #then squeeze into [batch size, imq height * imq width, in channels *_1
→param_width * param_height]
```

```
patches_reshaped = (patches
                            .transpose(1, 0, 2, 3, 4)
                            .reshape(batch_size, img_size, -1))
       #shape of param: [in channels, out channels, param width, param height]
       #make it into: [in_channels, param_width, param_height, out_channels]
       #then squeeze into: [in_channel * param_width * param_height,_
\rightarrow out_channels]
       param_reshaped = (self.param
                          .transpose(0, 2, 3, 1)
                          .reshape(patch_size, -1))
       #now patch @ param =
       #[batch_size, imq_height * imq_width, in_channels * param_width *_{\sqcup}
→param_height] @
       #[in_channel * param_width * param_height, out_channels] =
       #[batch_size, img_height * img_width, out_channels]
       #then reshape into [batch_size, img_height, img_width, out_channels]
       #then reorder into [batch size, out channels, imq_height, imq_width]
       #yay!
       output_reshaped = (
           np.matmul(patches_reshaped, param_reshaped)
           .reshape(batch_size, img_height, img_height, -1)
           .transpose(0, 3, 1, 2))
       return output_reshaped
   def _input_grad(self, output_grad: np.ndarray) -> np.ndarray:
       #simple parameter
       batch size = self.input .shape[0]
       img_size = self.input_.shape[2] * self.input_.shape[3]
       img height = self.input .shape[2]
       #first the output grad has shape of [batch sizes, out_channel, __
\rightarrow param_width, param_height]
       #then, get image patches will give out a shape of
       #[img_height * img_width, batch_size, out_channels, param_width,_
\rightarrow param_height]
       #then we reorder to [batch_size, img_height * img_width, out_channels,__
→ param_width, param_height]
       #then squeeze into [batch_size * img_height * img_width, out_channels *_\_
→ param_width * param_height]
       output_patches = (self._get_image_patches(output_grad)
                          .transpose(1, 0, 2, 3, 4)
```

```
.reshape(batch_size * img_size, -1))
       #param shape is
       #[in_channels, out_channels, param_width, param_height]
       #reshape into [in_channels, out_channels * param_width * param_height]
       #transpose to get [out_channels * param_width * param_height,_
\rightarrow in_channels]
      param_reshaped = (self.param
                         .reshape(self.param.shape[0], -1)
                         .transpose(1, 0))
       #gradient of input is simply gradients @ W.T
       #output_patches have shape of
       #[batch_size * imq_height * imq_width, out_channels * param_width *_
\rightarrow param_height]
       #param shape of [out_channels * param_width * param_height, in_channels]
       #the dot product is [batch_size * img_height * img_width, in_channels]
       #then we reshape to [batch_size, img_height, img_width, in_channels]
       #then we reorder to [batch_size, in_channels, img_height, img_width]
       #input grad should be the same shape as input, which is correct
      return (
           np.matmul(output_patches, param_reshaped)
           .reshape(batch_size, img_height, img_height, self.param.shape[0])
           .transpose(0, 3, 1, 2)
       )
  def param grad(self, output grad: ndarray) -> ndarray:
      batch_size = self.input_.shape[0]
       img_size = self.input_.shape[2] * self.input_.shape[3]
       in_channels = self.param.shape[0]
      out_channels = self.param.shape[1]
       #input has a shape of
       #[batch_size, in_channels, img_width, img_height]
       # get image patches will get [img_width * img_height, batch_size, __
→ in_channels, param_height, param_width]
       #reshape to [batch_size * img_width * img_height, in_channels *_
→param_height * param_width]
       #then reorder to [in channels * param height * param width, batch size_
→* img_width * img_height]
       in_patches_reshape = (
           self._get_image_patches(self.input_)
           .reshape(batch_size * img_size, -1)
           .transpose(1, 0)
           )
```

```
#output grad has a shape of
       #[batch_sizes, out_channel, imq_width, imq_height]
       #reorder to [batch sizes, ima width, ima height, out channel]
       #reshape to [batch_sizes * imq_width * imq_height, out_channel]
       out_grad_reshape = (output_grad
                            .transpose(0, 2, 3, 1)
                            .reshape(batch_size * img_size, -1))
       #gradient of param is simply X.T @ gradients
       #in patch @ out grad
       \#[in\_channels * param\_height * param\_width, batch\_size * img\_width *_\perp
\rightarrow img_height] @
       #[batch_sizes * imq_width * imq_height, out_channel] =
       #[in_channels * param_height * param_width, out_channel]
       #then we reshape to [in_channels, param_width, param_height,__
\hookrightarrow out_channel]
       #reorder to [in_channels, out_channels, param_width, param_height]
       return (np.matmul(in_patches_reshape,
                          out_grad_reshape)
                .reshape(in_channels, self.param_size, self.param_size, __
→out_channels)
                .transpose(0, 3, 1, 2))
```

# Now we can actually try out code here

```
[47]: from sklearn.datasets import fetch_openml
      #1. Load data
      mnist = fetch_openml('mnist_784', version=1, cache=True)
      mnist.target = mnist.target.astype(int)
      #2. Test train split
      X train = mnist['data'][:60000]
      y_train = mnist['target'][:60000]
      X_test = mnist['data'][60000:]
      y_test = mnist['target'][60000:]
      #3. Standardize data
      from sklearn.preprocessing import StandardScaler
      scaler = StandardScaler()
      X_train = scaler.fit_transform(X_train)
      X_test = scaler.transform(X_test)
      #4. Reshape X so that it has channel data
      print("X train shape: ", X_train.shape)
```

```
X_train_conv, X_test_conv = X_train.reshape(-1, 1, 28, 28), X_test.reshape(-1, 1, 28, 28)
print("X conv shape: ", X_train_conv.shape)

#4. One hot encoding
from sklearn import preprocessing
onehot = preprocessing.OneHotEncoder()

#sklearn expects a 2D array thus we have to reshape to (-1, 1)
y_train_encode = onehot.fit_transform(y_train.reshape(-1, 1)).toarray()
y_test_encode = onehot.fit_transform(y_test.reshape(-1, 1)).toarray()
print(y_train_encode.shape, y_test_encode.shape)
```

```
X train shape: (60000, 784)
X conv shape: (60000, 1, 28, 28)
(60000, 10) (10000, 10)
```

Let's try a CNN model now! We gonna use only one CNN layer...since training CNN can take a lot of time.

```
[48]: model = NeuralNetwork(
          layers=[Conv2D(out_channels=32,
                         param_size=5,
                         dropout=0.8,
                         weight_init="glorot",
                         flatten=True,
                        activation=Tanh()),
                  Dense(neurons=10,
                        activation=Linear())],
                  loss = SoftmaxCrossEntropy(),
      seed=20200720)
      trainer = Trainer(model, SGDMomentum(lr = 0.01, momentum=0.9))
      trainer.fit(X_train_conv, y_train_encode, X_test_conv, y_test_encode,
                  epochs = 1,
                  eval_every = 1,
                  seed=20200720,
                  batch_size=60)
```

Validation loss after 1 epochs is 0.508

```
[49]: #5. define a simple accuracy function
from sklearn.metrics import accuracy_score

def calc_accuracy(model, X_test, y_test):
    #getting the accuracy score with testing data
    preds = model.forward(X_test, inference=True)
```

```
preds = np.argmax(preds, axis=1)
  print("Accuracy: ", accuracy_score(y_test, preds))

calc_accuracy(model, X_test_conv, y_test)
```

Accuracy: 0.9153

Yay, with only one layer of CNN, and one iteration, we can already achieved over 90% accuracy!

Phew! We are finally done. It's a bit tough but it's satisfying, right?

Next class, we shall explore other type of data, namely, sequential data (text, signal), in which the previous data affects how we interpret the current data. In this case, we have a specialized network called RNN (Recurrent Neural Netork).