

Lecture-11

$$\rightarrow n, l, m, s = \pm \frac{1}{2}$$

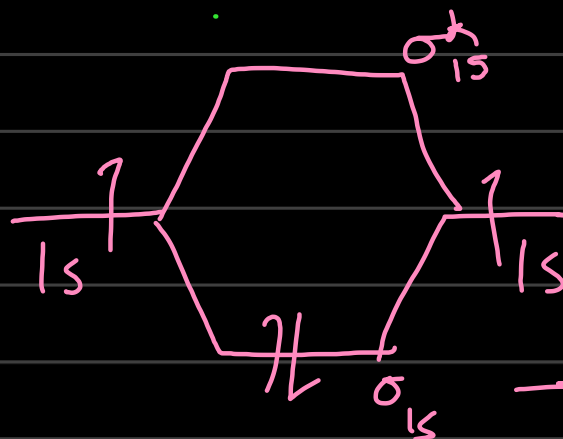
$$E = f(n) \quad L = f(l) = \hbar \sqrt{l(l+1)}$$

$$L_z = f(m)$$

$$S = \hbar s = \pm \frac{\hbar}{2} \Rightarrow \underline{\underline{2s+1 \text{ levels}}}$$

LCAO:

Hydrogen:



H_2 is formed.

→ Net lower energy than individual atoms.

Helium:



He_2 is not formed.

→ Net energy higher

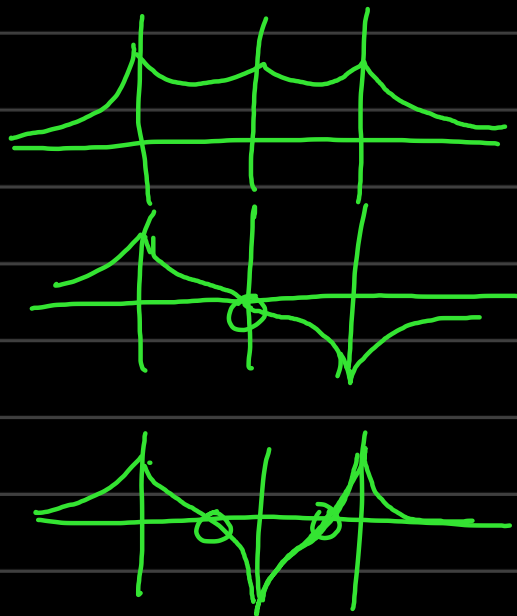
than sum of individual atoms.

3 hydrogen : $\underset{1s}{H} - \underset{1s}{H} - \underset{1s}{H}$

$$\psi_1 = \psi_{1s}(A) + \psi_{1s}(B) + \psi_{1s}(C)$$

$$\psi_2 = \psi_{1s}(A) + \psi_{1s}(B) - \psi_{1s}(C)$$

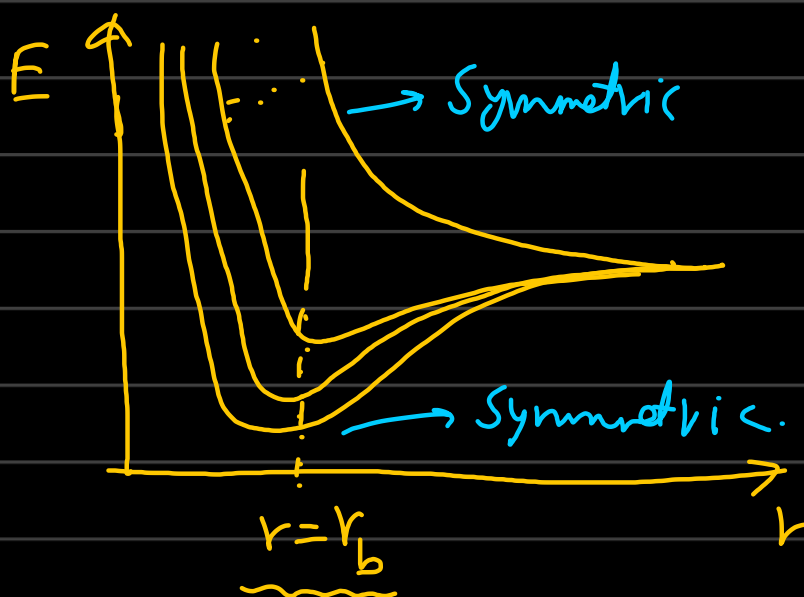
$$\psi_3 = \psi_{1s}(A) - \psi_{1s}(B) + \psi_{1s}(C)$$



$$E_3 > E_2 > E_1$$



N-Lithium : $\underset{2s}{Li} - \underset{2s}{Li} - \underset{2s}{Li} \dots \dots$

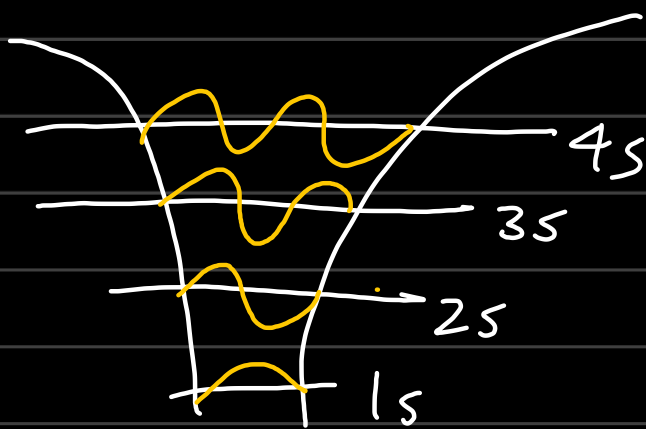


→ At $r = r_b$: collection infinite energy states creates energy bands.

→ large no. of discrete energy levels,
results in formation of bands.

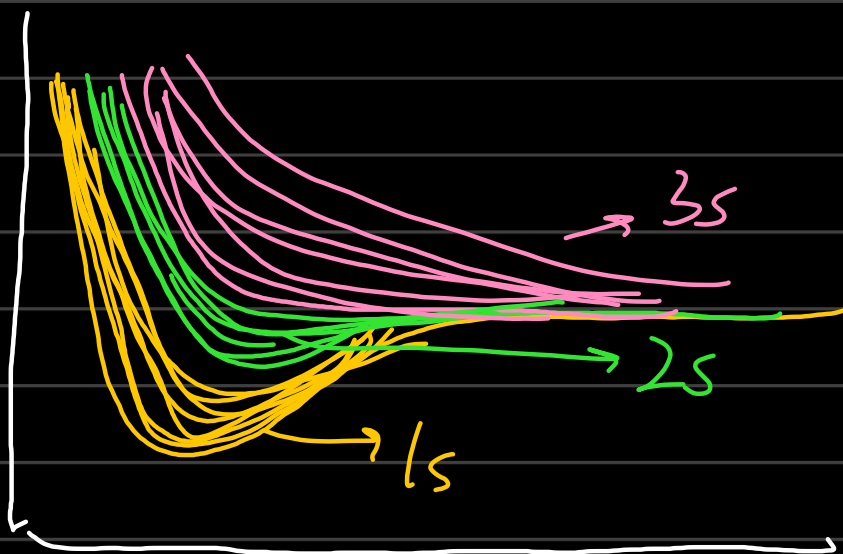
→ seems continuous energy spectrum.

* No. of occupied states: $N/2$



→ As n ↑, length/size
of wave functions ↑.

→ higher energy.



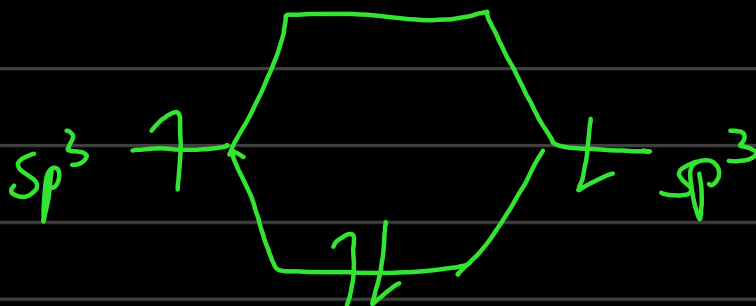
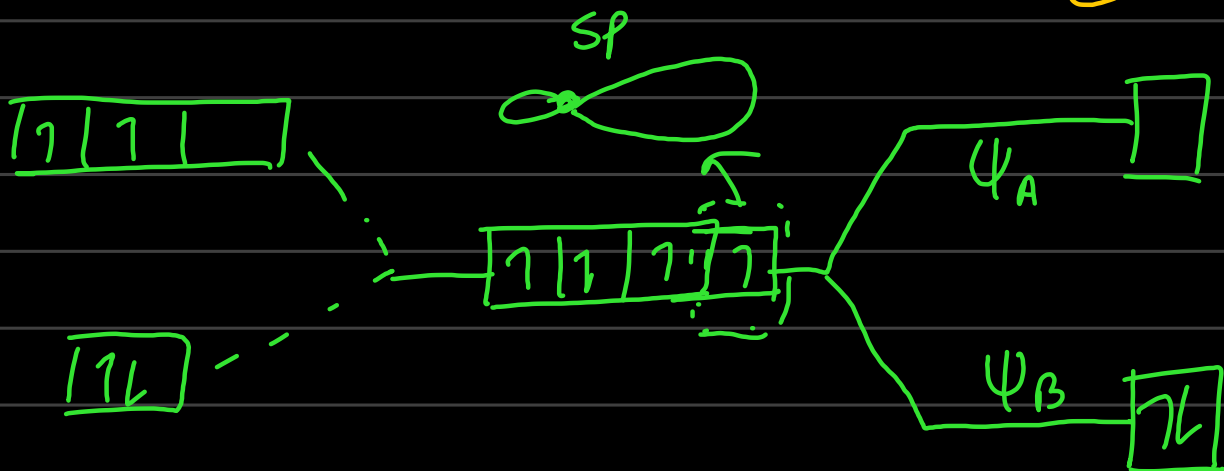
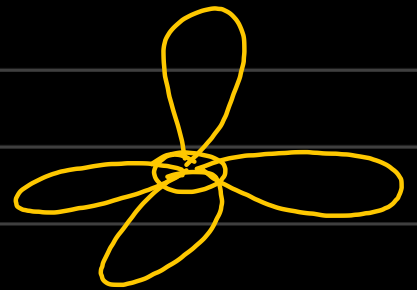
why $E_{2p} \neq E_{2s}$?

Semiconductor:

→ Hybridisation:

$$3s + 3p_x + 3p_y + 3p_z = 4 sp^3 \text{ orbitals}$$

$$0 + 8 + 8 + 8 \Rightarrow$$

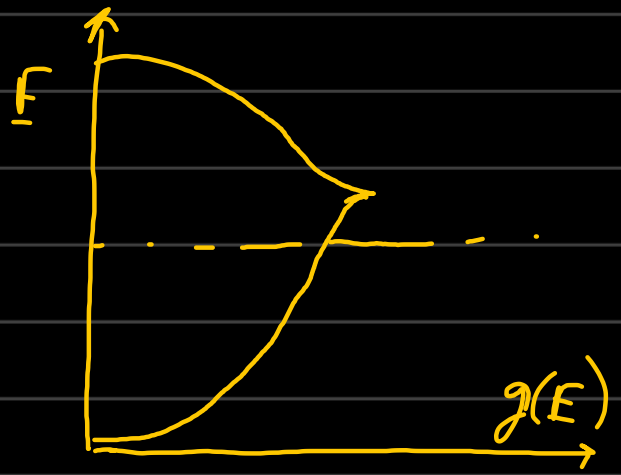


Linear combination of $2 sp^3$ orbitals when bonded.

Density of States:

D = density of states

↳ total no. of states per unit volume per unit energy.



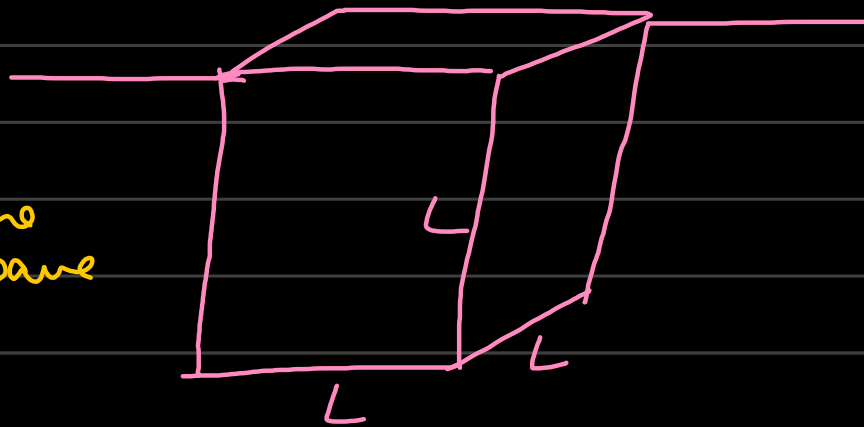
$$D(E) = \frac{1}{V} \frac{dN}{dE}$$

↓
fnc of energy

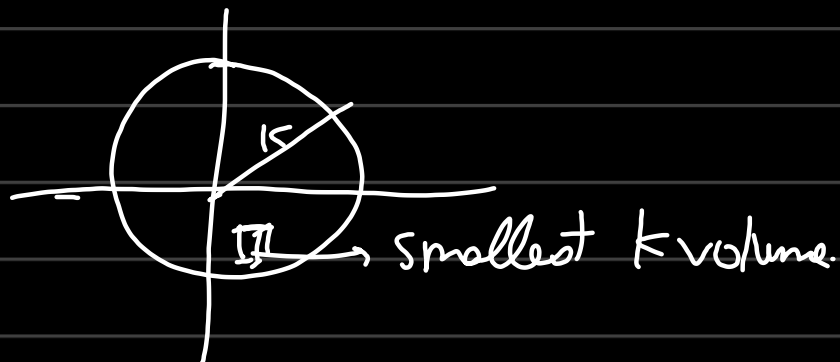
↗ vol
 $V = L^3$

↗ plane wave
 $\psi = Ae^{i(k_x x + k_y y + k_z z)}$

$$E = \frac{\hbar^2}{2m} (k_x^2 + k_y^2 + k_z^2)$$



$$dE = \frac{\hbar^2 k}{m} dk$$



k is discrete: $k_x = \frac{2\pi n}{L}$; $k_y = \frac{2\pi n}{L}$; $k_z = \frac{2\pi n}{L}$

smallest k volume $\Rightarrow k_x k_y k_z = \left(\frac{2\pi}{L}\right)^3$

* No. of k points: $\frac{\frac{4\pi}{3} k^3}{\left(\frac{2\pi}{L}\right)^3}$