

Lecture - 11

$$\rightarrow n, l, m \quad , \quad s = \pm \frac{1}{2}$$

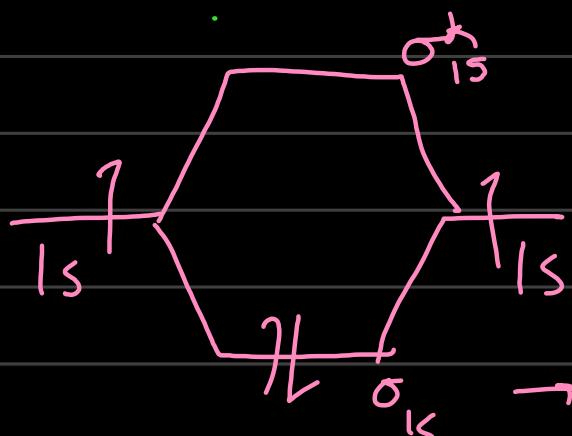
$$E = f(n) \quad L = f(l) = \pm \sqrt{l(l+1)}$$

$$L_z = f(m)$$

$$S = \pm \frac{1}{2} = \pm \frac{1}{2} \quad \Rightarrow \underline{2s+1 \text{ levels}}$$

LCAO:

Hydrogen:



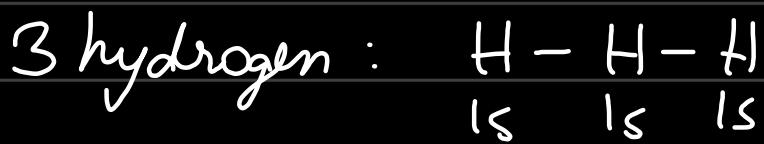
H_2 is formed.

→ Net lower energy than individual atoms.

Helium:



He_2 is not formed. → Net energy higher than sum of individual atoms.



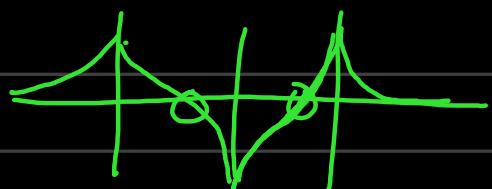
$$\Psi_1 = \Psi_{1s}(A) + \Psi_{1s}(B) + \Psi_{1s}(C)$$



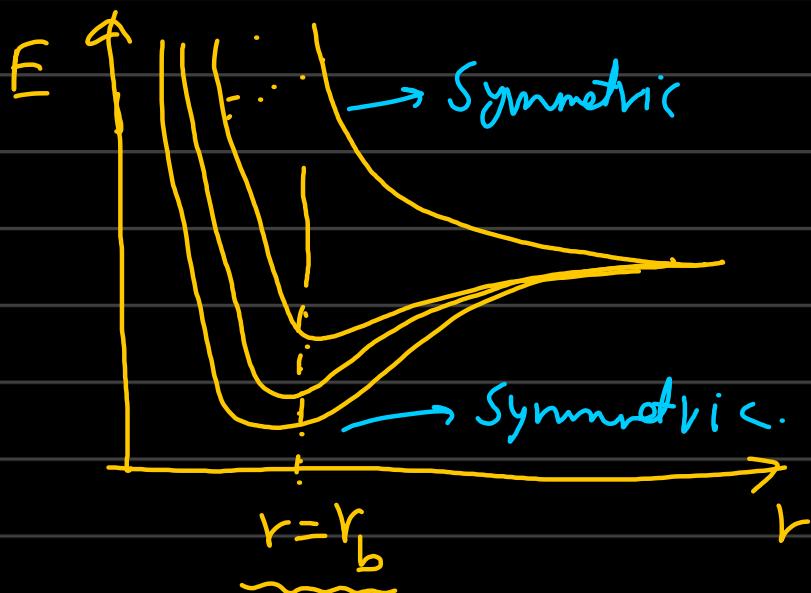
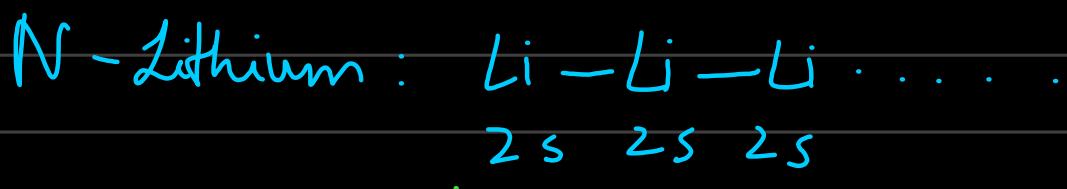
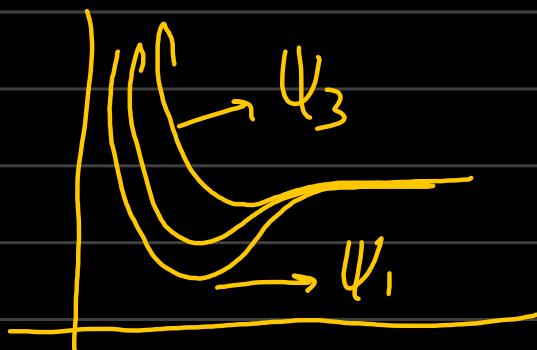
$$\Psi_2 = \Psi_{1s}(A) + \Psi_{1s}(B) - \Psi_{1s}(C)$$



$$\Psi_3 = \Psi_{1s}(A) - \Psi_{1s}(B) + \Psi_{1s}(C)$$



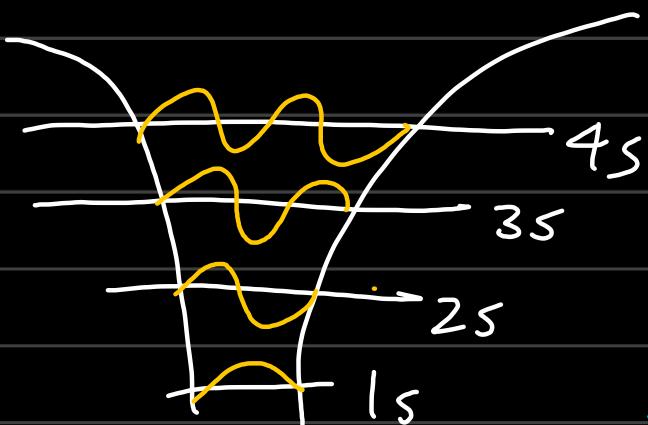
$$E_3 > E_2 > E_1$$



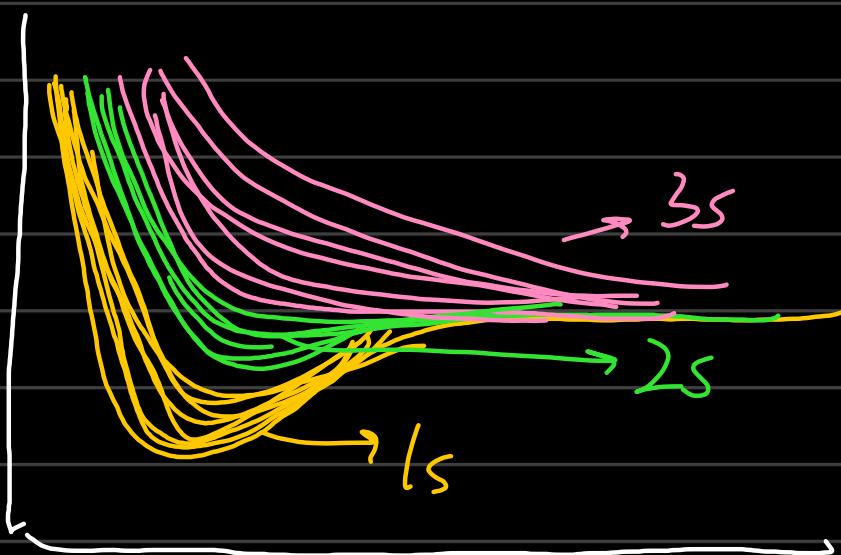
→ At $r=r_b$: collection infinite energy states creates energy bands.

- large no. of discrete energy levels, results in formation of bands.
- seems continuous energy spectrum.

⇒ No. of occupied states: $N/2$



→ As n increases, length/size of wave functions increases.
→ higher energy.



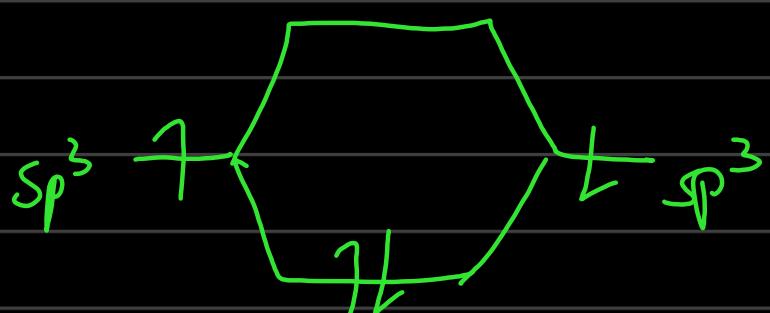
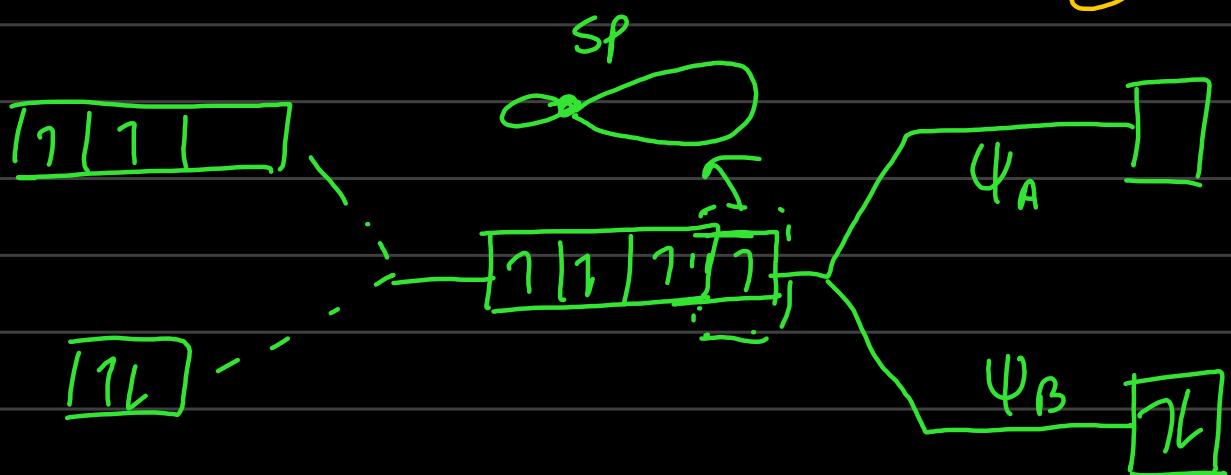
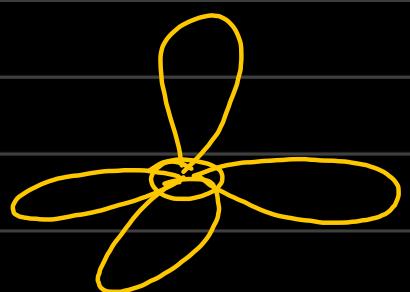
Why $E_{2p} \neq E_{2s}$?

Semiconductor:

→ Hybridisation:

$$3s + 3p_x + 3p_y + 3p_z = 4 \text{ } sp^3 \text{ orbitals}$$

$$0 + 8 + \infty + 8 \Rightarrow$$

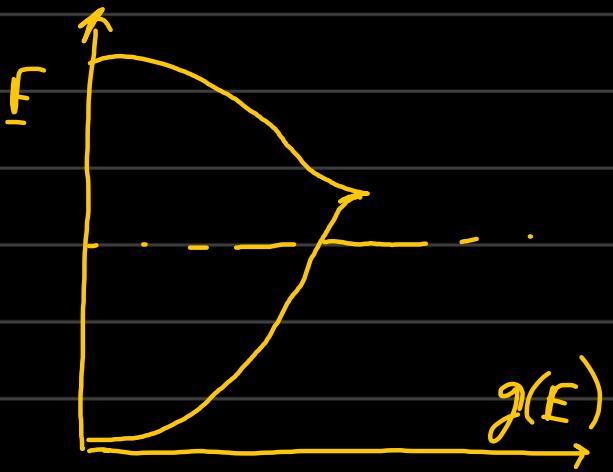


Linear combination of 2 sp^3 orbitals when bonded.

Density of States:

D = density of states

↳ total no. of states per unit volume per unit energy.

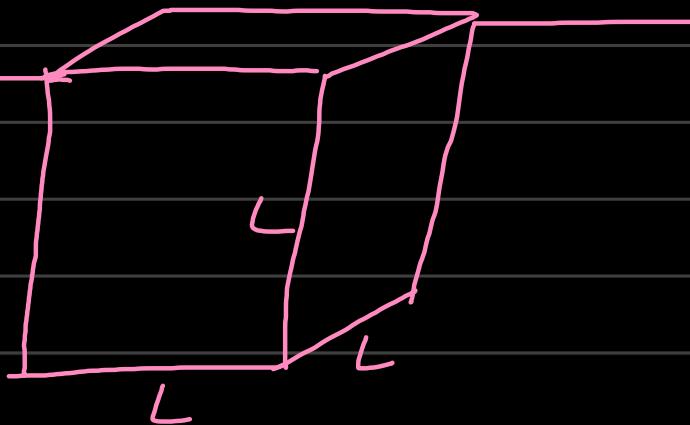


$$D(E) = \frac{1}{V} \frac{dN}{dE}$$

fnc of Energy

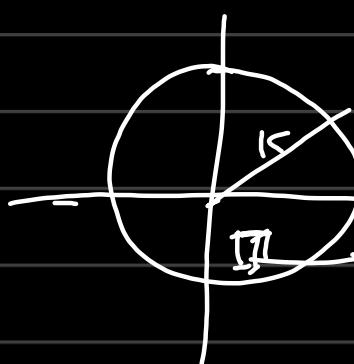
$$V = L^3$$

$$\Psi = A e^{i(k_x x + k_y y + k_z z)} \rightarrow \text{plane wave}$$



$$E = \frac{\hbar^2}{2m} (k_x^2 + k_y^2 + k_z^2)$$

$$dE = \frac{\hbar^2 k}{m} dk$$



$$k \text{ is discrete: } k_x = \frac{2\pi n}{L}; k_y = \frac{2\pi n}{L}; k_z = \frac{2\pi n}{L}$$

$$\text{smallest } k \text{ volume} \Rightarrow k_x k_y k_z = \left(\frac{2\pi n}{L}\right)^3$$

* No. of k points: $\frac{\frac{4\pi}{3}k^3}{(2\pi)^3}$