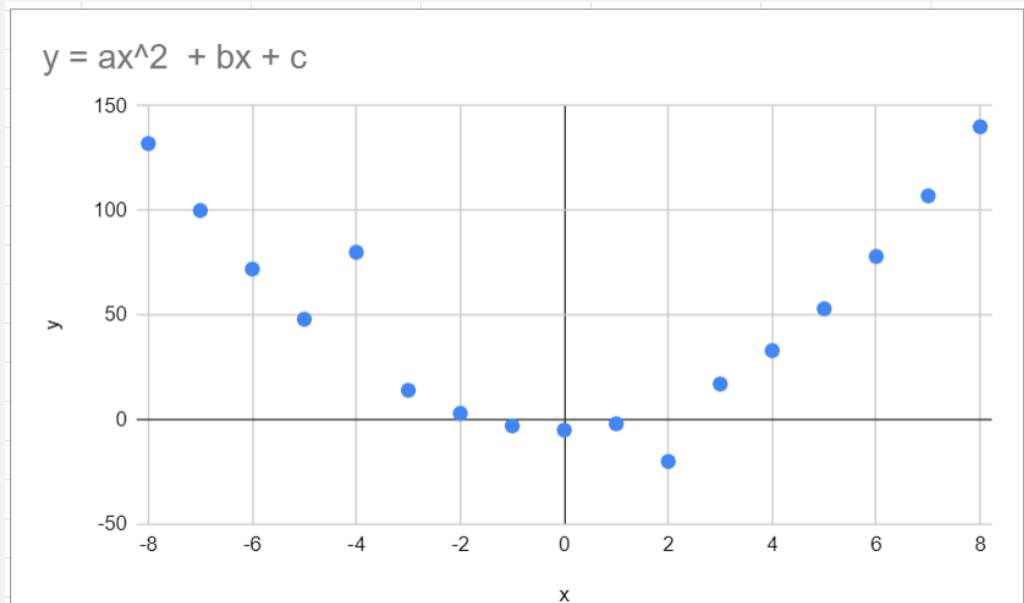




1. **20 points. 1 hour. RANSAC Regression.** Use RANSAC to find a , b , c for the following dataset where points (x_i, y_i) are discrete samples from a function $f(x) = ax^2 + bx + c$ with 2 outliers. *Hint:* You should get a , b , and c close to 2.2, 0.5, -4.5, respectively.

x_i	y_i
-8	132
-7	100
-6	72
-5	48
-4	80
-3	14
-2	3
-1	-3
0	-5
1	-2
2	-20
3	17
4	33
5	53
6	78
7	107
8	140



2. **Use K Means clustering on the IRIS dataset.**

- 2.1 **10 points. 0.5 hour.** Using $K = 3$, cluster the entire dataset into 3 labels using only features 1 & 3; namely, sepal length and petal length (Note: the example in class used all 4 features for clustering). Show a scatter plot based on these 2 features using known training 3 classes using markers "<" for class 1 (Setosa), ">" for class 2 (Versicolor), and "^" for class 3 (Virginica) while also using colors based on the 3 computed clusters using colors of "pink" for cluster 1, "yellow" for cluster 2, and "cyan" for cluster 3.
- 2.2 **5 points.** Report based on known labels what percent is misclassified when using 2 features.
- 2.3 **10 points. 0.5 hour.** Plot the result of K Means clustering using all 4 features with $K = 4$.
- 2.4 **15 points. 1 hour.** Reduce the 4 features (sepal length, sepal width, petal length, petal width) into 2 PCA features (an example is also provided in class). Use $K = 3$ to cluster the entire dataset using these 2 PCA features. Show a scatter plot like in problem 2.1 along with percent misclassified as in problem 2.2.
- 2.5 **20 points.** Redo the example in class with all 4 features and $K = 3$, but using your own class or function **my_k_means** in Python that has initialization parameters: K , X , max_iterations , $\text{centroid_move_epsilon}$ and returns y as a 1-D array of integer labels of 1, 2, ..., K . Each input N -dimensional data $X[i]$ will have a 1-dimensional output label $y[i]$ for $i = 1..M$ where M is the number of data points. The algorithm should start by assigning K cluster centers based on random values from the (min, max) range of each dimension in the N -dimensional data X . It should stop when all centers have moved by less than the $\text{centroid_move_epsilon}$ or when the max_iterations is reached. Make sure your results are similar to the K Means library class.

Algorithm 1 k -means algorithm

- 1: Specify the number k of clusters to assign.
 - 2: Randomly initialize k centroids.
 - 3: **repeat**
 - 4: **expectation:** Assign each point to its closest centroid.
 - 5: **maximization:** Compute the new centroid (mean) of each cluster.
 - 6: **until** The centroid positions do not change.
-

3. 15 points. 1 hour. Decision Trees. Change the “IRIS Decision Tree.ipynb” shown in class, to use SKlearn’s Wine Recognition Dataset instead. Report the classification accuracy % for a single tree using 70% training samples and for a random forest with 100 estimators.