

ODE Solver Multi-Language Wrapper Package Work-Precision Benchmarks (MATLAB, SciPy, Julia, deSolve (R))

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The following benchmarks demonstrate the performance differences due to using similar algorithms from wrapper packages in the main scripting languages across a range of stiff and non-stiff ODEs. It takes into account solver time and error in order to ensure correctness of interpretations. These were ran with Julia 1.3, MATLAB 2019B, deSolve 1.2.5, and SciPy 1.3.1.

These benchmarks are generated using the following bindings:

- [MATLABDiffEq.jl](#) (MATLAB)
- [SciPyDiffEq.jl](#) (SciPy)
- [deSolveDiffEq.jl](#) (deSolve)
- [OrdinaryDiffEq.jl](#) (OrdinaryDiffEq.jl)
- [Sundials.jl](#) (Sundials)
- [ODEInterfaceDiffEq.jl](#) (Hairer and Netlib)

The respective repos verify negligible overhead on interop (MATLAB, ODEInterface, and Sundials overhead are negligible, SciPy is accelerated 3x over SciPy+Numba setups due to the Julia JIT on the ODE function, deSolve sees a 3x overhead over the pure-R version). Error and timing is compared together to ensure the methods are solving to the same accuracy when compared.

More wrappers will continue to be added as necessary.

0.1 Setup

```
using ParameterizedFunctions, MATLABDiffEq, OrdinaryDiffEq, ODEInterface,  
    ODEInterfaceDiffEq, Plots, Sundials, SciPyDiffEq, deSolveDiffEq  
using DiffEqDevTools  
using LinearAlgebra
```

```

f = @code_def_bare LotkaVolterra begin
    dx = a*x - b*x*y
    dy = -c*y + d*x*y
end a b c d
p = [1.5,1,3,1]
tspan = (0.0,10.0)
u0 = [1.0,1.0]
prob = ODEProblem(f,u0,tspan,p)
sol = solve(prob,Vern7(), abstol=1/10^14, reltol=1/10^14)
test_sol = TestSolution(sol)

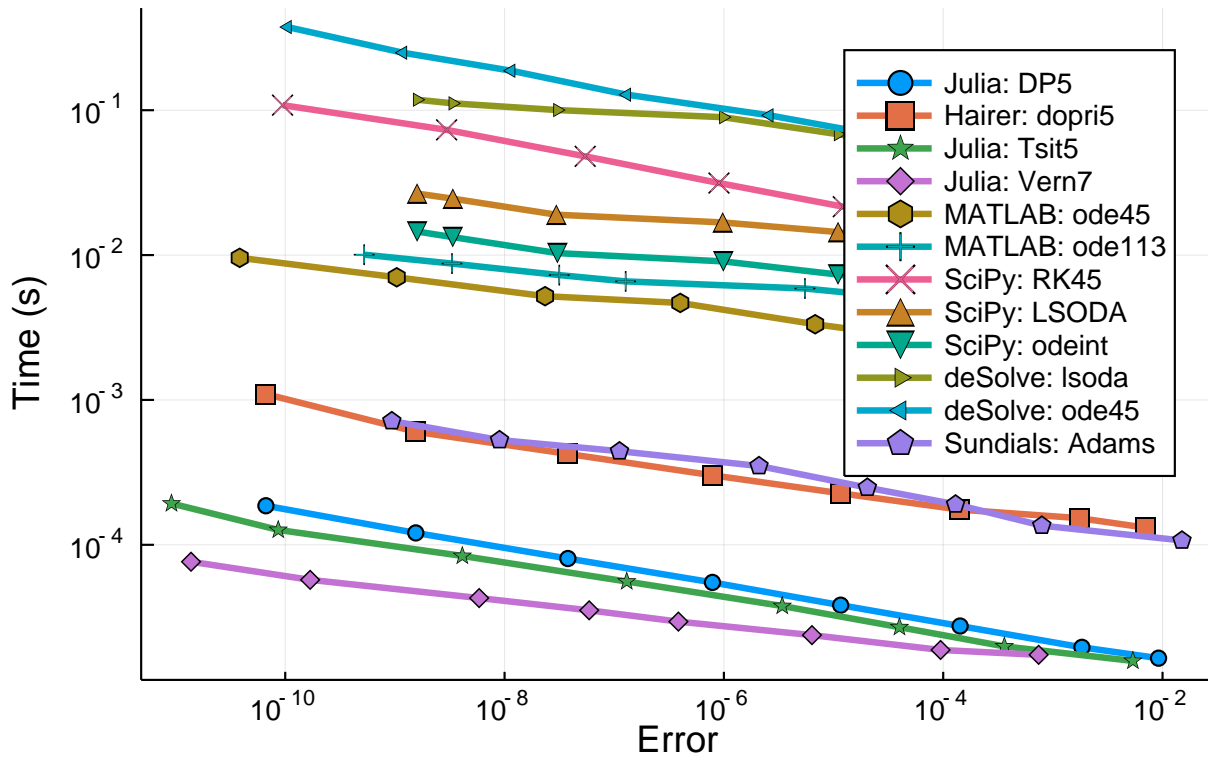
setups = [Dict(:alg=>DP5())
           Dict(:alg=>dopri5())
           Dict(:alg=>Tsit5())
           Dict(:alg=>Vern7())
           Dict(:alg=>MATLABDiffEq.ode45())
           Dict(:alg=>MATLABDiffEq.ode113())
           Dict(:alg=>SciPyDiffEq.RK45())
           Dict(:alg=>SciPyDiffEq.LSODA())
           Dict(:alg=>SciPyDiffEq.odeint())
           Dict(:alg=>deSolveDiffEq.lsoda())
           Dict(:alg=>deSolveDiffEq.ode45())
           Dict(:alg=>CVODE_Adams())
        ]

names = [
    "Julia: DP5"
    "Hairer: dopri5"
    "Julia: Tsit5"
    "Julia: Vern7"
    "MATLAB: ode45"
    "MATLAB: ode113"
    "SciPy: RK45"
    "SciPy: LSODA"
    "SciPy: odeint"
    "deSolve: lsoda"
    "deSolve: ode45"
    "Sundials: Adams"
]

abstols = 1.0 ./ 10.0 .^ (6:13)
reltols = 1.0 ./ 10.0 .^ (3:10)
wp = WorkPrecisionSet(prob,abstols,reltols,setups;
    names = names,
    appxsol=test_sol,dense=false,
    save_everystep=false,numruns=100,maxiters=10000000,
    timeseries_errors=false,verbose=false)
plot(wp,title="Non-stiff 1: Lotka-Volterra")

```

Non- stiff 1: Lotka- Volterra



```
f = @ode_def_bare RigidBodyBench begin
    dy1 = -2*y2*y3
    dy2 = 1.25*y1*y3
    dy3 = -0.5*y1*y2 + 0.25*sin(t)^2
end
prob = ODEProblem(f, [1.0; 0.0; 0.9], (0.0, 100.0))
sol = solve(prob, Vern7(), abstol=1/10^14, reltol=1/10^14)
test_sol = TestSolution(sol)

setups = [Dict(:alg=>DP5())
           Dict(:alg=>dopri5())
           Dict(:alg=>Tsit5())
           Dict(:alg=>Vern7())
           Dict(:alg=>MATLABDiffEq.ode45())
           Dict(:alg=>MATLABDiffEq.ode113())
           Dict(:alg=>SciPyDiffEq.RK45())
           Dict(:alg=>SciPyDiffEq.LSODA())
           Dict(:alg=>SciPyDiffEq.odeint())
           Dict(:alg=>deSolveDiffEq.lsoda())
           Dict(:alg=>deSolveDiffEq.ode45())
           Dict(:alg=>CVODE_Adams())
        ]

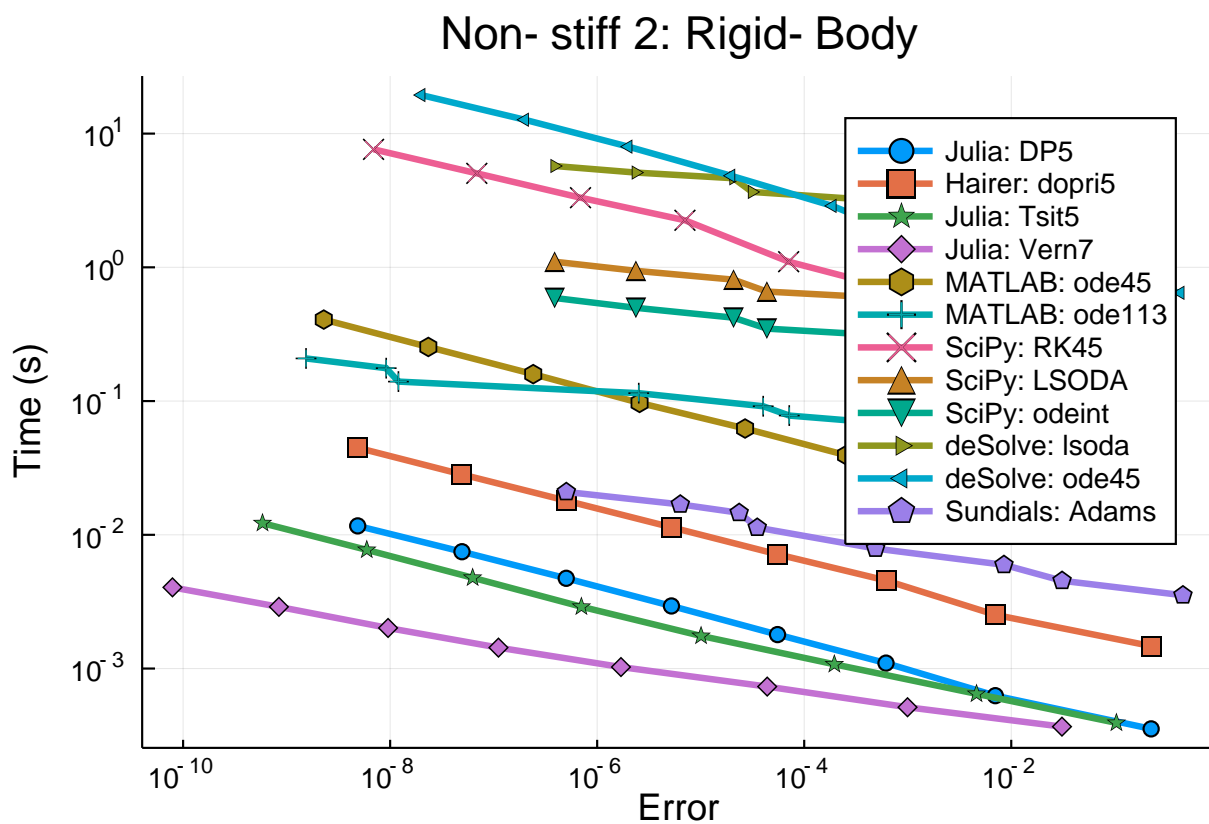
names = [
    "Julia: DP5"
    "Hairer: dopri5"
    "Julia: Tsit5"
    "Julia: Vern7"
    "MATLAB: ode45"
    "MATLAB: ode113"
```

```

"SciPy: RK45"
"SciPy: LSODA"
"SciPy: odeint"
"deSolve: lsoda"
"deSolve: ode45"
"Sundials: Adams"
]

abstols = 1.0 ./ 10.0 .^ (6:13)
reltols = 1.0 ./ 10.0 .^ (3:10)
wp = WorkPrecisionSet(prob,abstols,reltols,setup;
    names = names,
    appxsol=test_sol,dense=false,
    save_everystep=false,numruns=100,maxiters=10000000,
    timeseries_errors=false,verbose=false)
plot(wp,title="Non-stiff 2: Rigid-Body")

```



```

rober = @ode_def begin
    dy_1 = -k_1*y_1+k_3*y_2*y_3
    dy_2 = k_1*y_1-k_2*y_2^2-k_3*y_2*y_3
    dy_3 = k_2*y_2^2
end k_1 k_2 k_3
prob = ODEProblem(rober,[1.0,0.0,0.0],(0.0,1e5),[0.04,3e7,1e4])
sol = solve(prob,CVODE_BDF(),abstol=1/10^14,reltol=1/10^14)
test_sol = TestSolution(sol)

abstols = 1.0 ./ 10.0 .^ (7:8)
reltols = 1.0 ./ 10.0 .^ (3:4);

```

```

setups = [Dict(:alg=>Rosenbrock23())
           Dict(:alg=>TRBDF2())
           Dict(:alg=>RadauIIA5())
           Dict(:alg=>rodas())
           Dict(:alg=>radau())
           Dict(:alg=>MATLABDiffEq.ode23s())
           Dict(:alg=>MATLABDiffEq.ode15s())
           Dict(:alg=>SciPyDiffEq.LSODA())
           Dict(:alg=>SciPyDiffEq.BDF())
           Dict(:alg=>SciPyDiffEq.odeint())
           Dict(:alg=>deSolveDiffEq.lsoda())
           Dict(:alg=>CVODE_BDF())
        ]

names = [
    "Julia: Rosenbrock23"
    "Julia: TRBDF2"
    "Julia: radau"
    "Hairer: rodas"
    "Hairer: radau"
    "MATLAB: ode23s"
    "MATLAB: ode15s"
    "SciPy: LSODA"
    "SciPy: BDF"
    "SciPy: odeint"
    "deSolve: lsoda"
    "Sundials: CVODE"
]

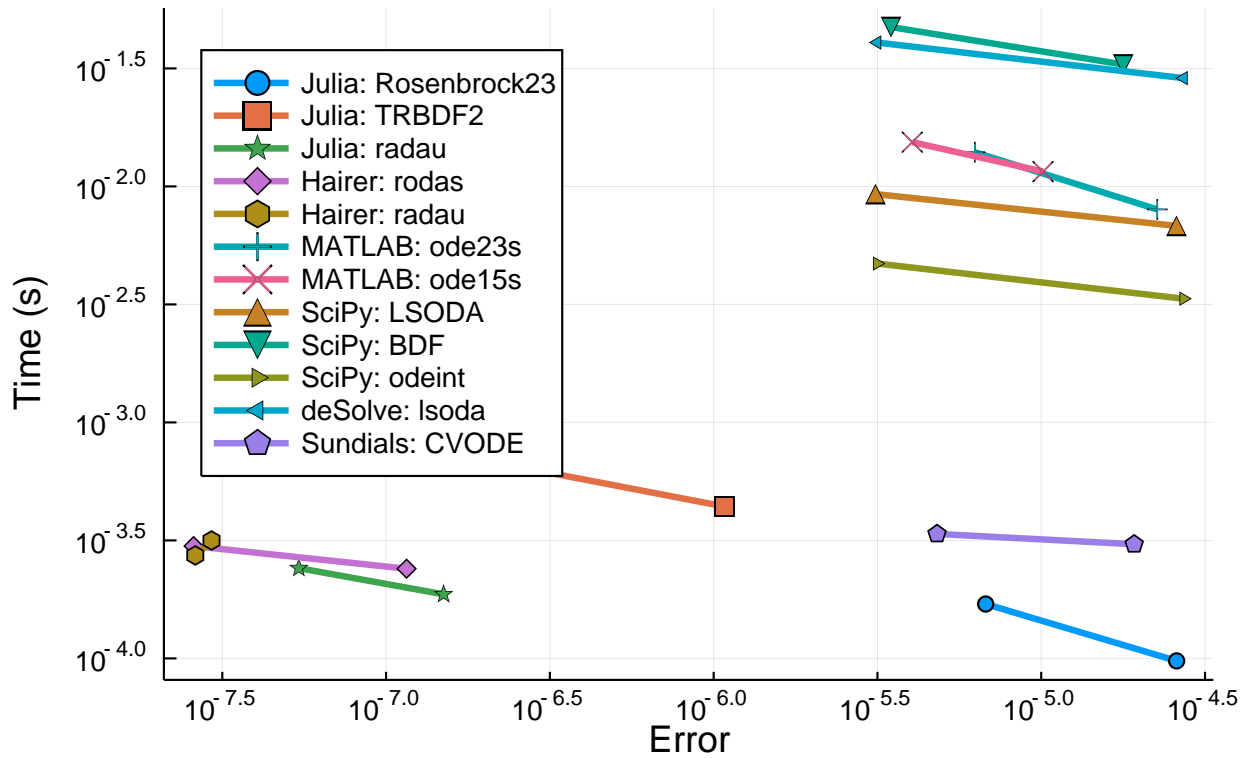
wp = WorkPrecisionSet(prob, abstols, reltols, setups;
                      names = names, print_names = true,
                      dense=false, verbose = false,
                      save_everystep=false, appxsol=test_sol,
                      maxiters=Int(1e5))

Julia: Rosenbrock23
Julia: TRBDF2
Julia: radau
Hairer: rodas
Hairer: radau
MATLAB: ode23s
MATLAB: ode15s
SciPy: LSODA
SciPy: BDF
SciPy: odeint
deSolve: lsoda
Sundials: CVODE

plot(wp, title="Stiff 1: ROBER", legend=:topleft)

```

Stiff 1: ROBER



```
f = @ode_def Hires begin
  dy1 = -1.71*y1 + 0.43*y2 + 8.32*y3 + 0.0007
  dy2 = 1.71*y1 - 8.75*y2
  dy3 = -10.03*y3 + 0.43*y4 + 0.035*y5
  dy4 = 8.32*y2 + 1.71*y3 - 1.12*y4
  dy5 = -1.745*y5 + 0.43*y6 + 0.43*y7
  dy6 = -280.0*y6*y8 + 0.69*y4 + 1.71*y5 -
        0.43*y6 + 0.69*y7
  dy7 = 280.0*y6*y8 - 1.81*y7
  dy8 = -280.0*y6*y8 + 1.81*y7
end

u0 = zeros(8)
u0[1] = 1
u0[8] = 0.0057
prob = ODEProblem(f,u0,(0.0,321.8122))

sol = solve(prob,Rodas5(), abstol=1/10^14, reltol=1/10^14)
test_sol = TestSolution(sol)

abstols = 1.0 ./ 10.0 .^ (5:8)
reltols = 1.0 ./ 10.0 .^ (1:4);

setups = [Dict(:alg=>Rosenbrock23())
           Dict(:alg=>TRBDF2())
           Dict(:alg=>RadauIIA5())
           Dict(:alg=>rodas())
           Dict(:alg=>radau())
           Dict(:alg=>MATLABDiffEq.ode23s())
           Dict(:alg=>MATLABDiffEq.ode15s())
```

```

Dict(:alg=>SciPyDiffEq.LSODA())
Dict(:alg=>SciPyDiffEq.BDF())
Dict(:alg=>SciPyDiffEq.odeint())
Dict(:alg=>deSolveDiffEq.lsoda())
Dict(:alg=>CVODE_BDF())
]

names = [
  "Julia: Rosenbrock23"
  "Julia: TRBDF2"
  "Julia: radau"
  "Hairer: rodas"
  "Hairer: radau"
  "MATLAB: ode23s"
  "MATLAB: ode15s"
  "SciPy: LSODA"
  "SciPy: BDF"
  "SciPy: odeint"
  "deSolve: lsoda"
  "Sundials: CVODE"
]

wp = WorkPrecisionSet(prob, abstols, reltols, setups;
  names = names, print_names = true,
  save_everystep=false, appxsol=test_sol,
  maxiters=Int(1e5), numruns=100)

Julia: Rosenbrock23
Julia: TRBDF2
Julia: radau
Hairer: rodas
Hairer: radau
MATLAB: ode23s
MATLAB: ode15s
SciPy: LSODA
SciPy: BDF
SciPy: odeint
deSolve: lsoda
Sundials: CVODE

plot(wp, title="Stiff 2: Hires", legend=:topleft)

```

Stiff 2: Hires

