Mendes Multistate Model

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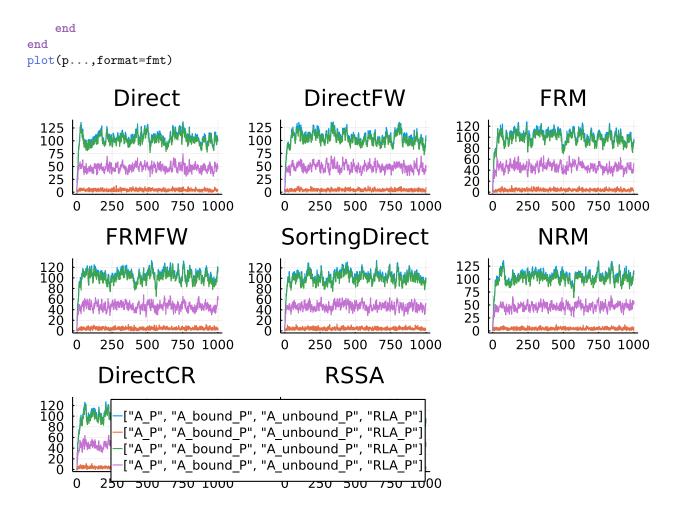
June 14, 2021

Taken from Gupta and Mendes, An Overview of Network-Based and -Free Approaches for Stochastic Simulation of Biochemical Systems, Computation, 6 (9), 2018.

```
using DiffEqBase, Catalyst, DiffEqJump, DiffEqProblemLibrary.JumpProblemLibrary, Plots,
Statistics
gr()
fmt = :png
JumpProblemLibrary.importjumpproblems()
```

1 Plot solutions by each method

```
methods = (Direct(),DirectFW(),FRM(),FRMFW(),SortingDirect(),NRM(),DirectCR(),RSSA())
shortlabels = [string(leg)[12:end-2] for leg in methods]
jprob = prob_jump_multistate
       = 10.0*jprob.tstop
prob
        = DiscreteProblem(jprob.u0, (0.0,tf), jprob.rates)
       = jprob.network
varlegs = ["A_P", "A_bound_P", "A_unbound_P", "RLA_P"]
Ovariables t S7(t) S8(t) S9(t)
varsyms = [
    [S7,S8,S9],
    [S9],
    [S7,S8],
    [S7]
varidxs = []
for vars in varsyms
   push!(varidxs, [findfirst(isequal(sym),rn.states) for sym in vars])
end
p = []
for (i,method) in enumerate(methods)
    jump_prob = JumpProblem(rn, prob, method, save_positions=(false, false))
    sol = solve(jump_prob, SSAStepper(), saveat=tf/1000.)
    solv = zeros(1001,4)
    for (i,varidx) in enumerate(varidxs)
        solv[:,i] = sum(sol[varidx,:], dims=1)
    if i < length(methods)</pre>
        push!(p, plot(sol.t,solv,title=shortlabels[i],legend=false,format=fmt))
    else
        push!(p,
plot(sol.t,solv,title=shortlabels[i],legend=true,labels=varlegs,format=fmt))
```



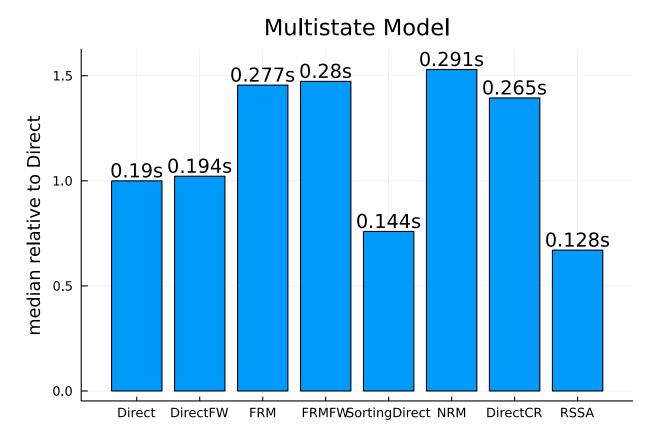
2 Benchmarking performance of the methods

```
function run_benchmark!(t, jump_prob, stepper)
    sol = solve(jump_prob, stepper)
    @inbounds for i in 1:length(t)
        t[i] = @elapsed (sol = solve(jump_prob, stepper))
    end
end
run_benchmark! (generic function with 1 method)
nsims = 100
benchmarks = Vector{Vector{Float64}}()
for method in methods
    jump_prob = JumpProblem(rn, prob, method, save_positions=(false, false))
    stepper = SSAStepper()
    time = Vector{Float64}(undef, nsims)
    run_benchmark!(time, jump_prob, stepper)
    push!(benchmarks, time)
end
medtimes = Vector{Float64}(undef,length(methods))
stdtimes = Vector{Float64}(undef,length(methods))
avgtimes = Vector{Float64}(undef,length(methods))
for i in 1:length(methods)
    medtimes[i] = median(benchmarks[i])
    avgtimes[i] = mean(benchmarks[i])
```

```
stdtimes[i] = std(benchmarks[i])
end
using DataFrames

df =
DataFrame(names=shortlabels,medtimes=medtimes,relmedtimes=(medtimes/medtimes[1]),avgtimes=avgtimes,
std=stdtimes, cv=stdtimes./avgtimes)

sa = [text(string(round(mt,digits=3),"s"),:center,12) for mt in df.medtimes]
bar(df.names,df.relmedtimes,legend=:false, fmt=fmt)
scatter!(df.names, .05 .+ df.relmedtimes, markeralpha=0, series_annotations=sa, fmt=fmt)
ylabel!("median relative to Direct")
title!("Multistate Model")
```



2.1 Appendix

These benchmarks are a part of the SciMLBenchmarks.jl repository, found at: https://github.com/SciML, For more information on high-performance scientific machine learning, check out the SciML Open Source Software Organization https://sciml.ai.

To locally run this benchmark, do the following commands:

```
using SciMLBenchmarks
SciMLBenchmarks.weave_file("benchmarks/Jumps","Mendes_multistate_example.jmd")
```

Computer Information:

```
Julia Version 1.6.1
Commit 6aaedecc44 (2021-04-23 05:59 UTC)
```

```
Platform Info:
  OS: Linux (x86_64-pc-linux-gnu)
  CPU: AMD EPYC 7502 32-Core Processor
  WORD SIZE: 64
  LIBM: libopenlibm
  LLVM: libLLVM-11.0.1 (ORCJIT, znver2)
Environment:
  JULIA DEPOT PATH = /root/.cache/julia-buildkite-plugin/depots/5b300254-1738-4989-ae0a
Package Information:
      Status `/var/lib/buildkite-agent/builds/amdci3-julia-csail-mit-edu/julialang/sci
  [479239e8] Catalyst v6.13.0
  [a93c6f00] DataFrames v1.1.1
  [2b5f629d] DiffEqBase v6.62.2
  [c894b116] DiffEqJump v6.14.2
  [a077e3f3] DiffEqProblemLibrary v4.13.0
  [961ee093] ModelingToolkit v5.19.1
  [1dea7af3] OrdinaryDiffEq v5.57.0
  [91a5bcdd] Plots v1.16.5
  [31c91b34] SciMLBenchmarks v0.1.0
  [10745b16] Statistics
And the full manifest:
      Status \( \tau \)/var/lib/buildkite-agent/builds/amdci3-julia-csail-mit-edu/julialang/sci
  [c3fe647b] AbstractAlgebra v0.17.1
  [1520ce14] AbstractTrees v0.3.4
  [79e6a3ab] Adapt v3.3.1
  [ec485272] ArnoldiMethod v0.1.0
  [4fba245c] ArrayInterface v3.1.17
  [4c555306] ArrayLayouts v0.7.0
  [aae01518] BandedMatrices v0.16.9
  [8e7c35d0] BlockArrays v0.15.3
  [ffab5731] BlockBandedMatrices v0.10.6
  [00ebfdb7] CSTParser v2.5.0
```

[b152e2b5] CompositeTypes v0.1.2

[bbf7d656] CommonSubexpressions v0.3.0

[479239e8] Catalyst v6.13.0

[d360d2e6] ChainRulesCore v0.9.45 [35d6a980] ColorSchemes v3.12.1 [3da002f7] ColorTypes v0.11.0 [5ae59095] Colors v0.12.8

[861a8166] Combinatorics v1.0.2 [a80b9123] CommonMark v0.8.1 [38540f10] CommonSolve v0.2.0

[34da2185] Compat v3.30.0

```
[8f4d0f93] Conda v1.5.2
```

[187b0558] ConstructionBase v1.2.1

[d38c429a] Contour v0.5.7

[a8cc5b0e] Crayons v4.0.4

[9a962f9c] DataAPI v1.6.0

[a93c6f00] DataFrames v1.1.1

[864edb3b] DataStructures v0.18.9

[e2d170a0] DataValueInterfaces v1.0.0

[2b5f629d] DiffEqBase v6.62.2

[c894b116] DiffEqJump v6.14.2

[9fdde737] DiffEqOperators v4.28.0

[a077e3f3] DiffEqProblemLibrary v4.13.0

[163ba53b] DiffResults v1.0.3

[b552c78f] DiffRules v1.0.2

[b4f34e82] Distances v0.10.3

[31c24e10] Distributions v0.24.18

[ffbed154] DocStringExtensions v0.8.5

[e30172f5] Documenter v0.26.3

[5b8099bc] DomainSets v0.5.2

[da5c29d0] EllipsisNotation v1.1.0

[d4d017d3] ExponentialUtilities v1.8.4

[e2ba6199] ExprTools v0.1.3

[c87230d0] FFMPEG v0.4.1

[7034ab61] FastBroadcast v0.1.8

[9aa1b823] FastClosures v0.3.2

[1a297f60] FillArrays v0.11.7

[6a86dc24] FiniteDiff v2.8.0

[53c48c17] FixedPointNumbers v0.8.4

[59287772] Formatting v0.4.2

[f6369f11] ForwardDiff v0.10.18

[069b7b12] FunctionWrappers v1.1.2

[28b8d3ca] GR v0.57.5

[5c1252a2] GeometryBasics v0.3.12

[d7ba0133] Git v1.2.1

[42e2da0e] Grisu v1.0.2

[cd3eb016] HTTP v0.9.10

[eafb193a] Highlights v0.4.5

[0e44f5e4] Hwloc v2.0.0

[7073ff75] IJulia v1.23.2

[b5f81e59] IOCapture v0.1.1

[615f187c] IfElse v0.1.0

[d25df0c9] Inflate v0.1.2

[83e8ac13] IniFile v0.5.0

[8197267c] IntervalSets v0.5.3

[41ab1584] InvertedIndices v1.0.0

[c8e1da08] IterTools v1.3.0

[42fd0dbc] IterativeSolvers v0.9.1

[82899510] IteratorInterfaceExtensions v1.0.0

[692b3bcd] JLLWrappers v1.3.0

```
[682c06a0] JSON v0.21.1
```

[98e50ef6] JuliaFormatter v0.13.7

[b964fa9f] LaTeXStrings v1.2.1

[2ee39098] LabelledArrays v1.6.1

[23fbe1c1] Latexify v0.15.6

[5078a376] LazyArrays v0.21.6

[d7e5e226] LazyBandedMatrices v0.5.8

[093fc24a] LightGraphs v1.3.5

[d3d80556] LineSearches v7.1.1

[2ab3a3ac] LogExpFunctions v0.2.4

[bdcacae8] LoopVectorization v0.12.37

[1914dd2f] MacroTools v0.5.6

[a3b82374] MatrixFactorizations v0.8.3

[739be429] MbedTLS v1.0.3

[442fdcdd] Measures v0.3.1

[e1d29d7a] Missings v1.0.0

[961ee093] ModelingToolkit v5.19.1

[46d2c3a1] MuladdMacro v0.2.2

[ffc61752] Mustache v1.0.10

[d41bc354] NLSolversBase v7.8.0

[2774e3e8] NLsolve v4.5.1

[872c559c] NNlib v0.7.21

[77ba4419] NaNMath v0.3.5

[8913a72c] NonlinearSolve v0.3.8

[6fe1bfb0] OffsetArrays v1.9.2

[bac558e1] OrderedCollections v1.4.1

[1dea7af3] OrdinaryDiffEq v5.57.0

[90014a1f] PDMats v0.11.1

[d96e819e] Parameters v0.12.2

[69de0a69] Parsers v1.1.0

[ccf2f8ad] PlotThemes v2.0.1

[995b91a9] PlotUtils v1.0.10

[91a5bcdd] Plots v1.16.5

[e409e4f3] PoissonRandom v0.4.0

[f517fe37] Polyester v0.3.1

[2dfb63ee] PooledArrays v1.2.1

[21216c6a] Preferences v1.2.2

[08abe8d2] PrettyTables v1.1.0

[1fd47b50] QuadGK v2.4.1

[fb686558] RandomExtensions v0.4.3

[e6cf234a] RandomNumbers v1.4.0

[3cdcf5f2] RecipesBase v1.1.1

[01d81517] RecipesPipeline v0.3.2

[731186ca] RecursiveArrayTools v2.11.4

[f2c3362d] RecursiveFactorization v0.1.12

[189a3867] Reexport v1.1.0

[ae029012] Requires v1.1.3

[79098fc4] Rmath v0.7.0

[7e49a35a] RuntimeGeneratedFunctions v0.5.2

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[476501e8] SLEEFPirates v0.6.21
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[1bc83da4] SafeTestsets v0.0.1

[Obca4576] SciMLBase v1.13.5

[31c91b34] SciMLBenchmarks v0.1.0

[6c6a2e73] Scratch v1.1.0

[efcf1570] Setfield v0.7.0

[992d4aef] Showoff v1.0.3

[699a6c99] SimpleTraits v0.9.3

[b85f4697] SoftGlobalScope v1.1.0

[a2af1166] SortingAlgorithms v1.0.0

[47a9eef4] SparseDiffTools v1.13.2

[276daf66] SpecialFunctions v1.5.1

[aedffcd0] Static v0.2.5

[90137ffa] StaticArrays v1.2.2

[82ae8749] StatsAPI v1.0.0

[2913bbd2] StatsBase v0.33.8

[4c63d2b9] StatsFuns v0.9.8

[7792a7ef] StrideArraysCore v0.1.13

[69024149] StringEncodings v0.3.4

[09ab397b] StructArrays v0.5.1

[d1185830] SymbolicUtils v0.11.3

[0c5d862f] Symbolics v0.1.32

[3783bdb8] TableTraits v1.0.1

[bd369af6] Tables v1.4.3

[8290d209] ThreadingUtilities v0.4.4

[a759f4b9] TimerOutputs v0.5.9

[0796e94c] Tokenize v0.5.16

[a2a6695c] TreeViews v0.3.0

[5c2747f8] URIs v1.3.0

[3a884ed6] UnPack v1.0.2

[1986cc42] Unitful v1.8.0

[3d5dd08c] VectorizationBase v0.20.16

[81def892] VersionParsing v1.2.0

[19fa3120] VertexSafeGraphs v0.1.2

[44d3d7a6] Weave v0.10.9

[ddb6d928] YAML v0.4.7

[c2297ded] ZMQ v1.2.1

[700de1a5] ZygoteRules v0.2.1

[6e34b625] Bzip2 jll v1.0.6+5

[83423d85] Cairo_jll v1.16.0+6

[5ae413db] EarCut jll v2.1.5+1

[2e619515] Expat_jll v2.2.10+0

[b22a6f82] FFMPEG_jll v4.3.1+4

[a3f928ae] Fontconfig_jll v2.13.1+14

[d7e528f0] FreeType2 jll v2.10.1+5

[559328eb] FriBidi jll v1.0.10+0

[0656b61e] GLFW_jll v3.3.5+0

[d2c73de3] GR jll v0.57.3+0

[78b55507] Gettext jll v0.20.1+7

```
[f8c6e375] Git jll v2.31.0+0
[7746bdde] Glib jll v2.59.0+4
[e33a78d0] Hwloc_jll v2.4.1+0
[aacddb02] JpegTurbo jll v2.1.0+0
[c1c5ebd0] LAME jll v3.100.1+0
[dd4b983a] LZO jll v2.10.1+0
[dd192d2f] LibVPX jll v1.10.0+0
[e9f186c6] Libffi_jll v3.2.2+0
[d4300ac3] Libgcrypt jll v1.8.7+0
[7e76a0d4] Libglvnd_jll v1.3.0+3
[7add5ba3] Libgpg_error_jll v1.42.0+0
[94ce4f54] Libiconv jll v1.16.1+0
[4b2f31a3] Libmount_jll v2.35.0+0
[89763e89] Libtiff jll v4.3.0+0
[38a345b3] Libuuid jll v2.36.0+0
[e7412a2a] Ogg jll v1.3.5+0
[458c3c95] OpenSSL jll v1.1.10+0
[efe28fd5] OpenSpecFun_jll v0.5.5+0
[91d4177d] Opus_jll v1.3.2+0
[2f80f16e] PCRE jll v8.44.0+0
[30392449] Pixman jll v0.40.1+0
[ea2cea3b] Qt5Base_jll v5.15.2+0
[f50d1b31] Rmath jll v0.3.0+0
[a2964d1f] Wayland jll v1.17.0+4
[2381bf8a] Wayland_protocols_jll v1.18.0+4
[02c8fc9c] XML2_jll v2.9.12+0
[aed1982a] XSLT jll v1.1.34+0
[4f6342f7] Xorg libX11 jll v1.6.9+4
[OcOb7dd1] Xorg libXau jll v1.0.9+4
[935fb764] Xorg libXcursor jll v1.2.0+4
[a3789734] Xorg_libXdmcp_jll v1.1.3+4
[1082639a] Xorg libXext jll v1.3.4+4
[d091e8ba] Xorg_libXfixes_jll v5.0.3+4
[a51aa0fd] Xorg libXi jll v1.7.10+4
[d1454406] Xorg libXinerama jll v1.1.4+4
[ec84b674] Xorg libXrandr jll v1.5.2+4
[ea2f1a96] Xorg_libXrender_jll v0.9.10+4
[14d82f49] Xorg libpthread stubs jll v0.1.0+3
[c7cfdc94] Xorg libxcb jll v1.13.0+3
[cc61e674] Xorg_libxkbfile_jll v1.1.0+4
[12413925] Xorg xcb util image jll v0.4.0+1
[2def613f] Xorg xcb util jll v0.4.0+1
[975044d2] Xorg_xcb_util_keysyms_jll v0.4.0+1
[Od47668e] Xorg_xcb_util_renderutil_jll v0.3.9+1
[c22f9ab0] Xorg xcb util wm jll v0.4.1+1
[35661453] Xorg_xkbcomp_jll v1.4.2+4
[33bec58e] Xorg_xkeyboard_config_jll v2.27.0+4
[c5fb5394] Xorg xtrans jll v1.4.0+3
[8f1865be] ZeroMQ_jll v4.3.2+6
```

```
[3161d3a3] Zstd jll v1.5.0+0
```

[0ac62f75] libass jll v0.14.0+4

[f638f0a6] libfdk_aac_jll v0.1.6+4

[b53b4c65] libpng jll v1.6.38+0

[a9144af2] libsodium jll v1.0.20+0

[f27f6e37] libvorbis_jll v1.3.7+0

[1270edf5] x264 jll v2020.7.14+2

[dfaa095f] x265 jll v3.0.0+3

[d8fb68d0] xkbcommon jll v0.9.1+5

[Odad84c5] ArgTools

[56f22d72] Artifacts

[2a0f44e3] Base64

[ade2ca70] Dates

[8bb1440f] DelimitedFiles

[8ba89e20] Distributed

[f43a241f] Downloads

[7b1f6079] FileWatching

[9fa8497b] Future

[b77e0a4c] InteractiveUtils

[b27032c2] LibCURL

[76f85450] LibGit2

[8f399da3] Libdl

[37e2e46d] LinearAlgebra

[56ddb016] Logging

[d6f4376e] Markdown

[a63ad114] Mmap

[ca575930] NetworkOptions

[44cfe95a] Pkg

[de0858da] Printf

[3fa0cd96] REPL

[9a3f8284] Random

[ea8e919c] SHA

[9e88b42a] Serialization

[1a1011a3] SharedArrays

[6462fe0b] Sockets

[2f01184e] SparseArrays

[10745b16] Statistics

[4607b0f0] SuiteSparse

[fa267f1f] TOML

[a4e569a6] Tar

[8dfed614] Test

[cf7118a7] UUIDs

[4ec0a83e] Unicode

[e66e0078] CompilerSupportLibraries_jll

[deac9b47] LibCURL jll

[29816b5a] LibSSH2 jll

[c8ffd9c3] MbedTLS_jll

[14a3606d] MozillaCACerts jll

[efcefdf7] PCRE2 jll

[83775a58] Zlib_jll [8e850ede] nghttp2_jll [3f19e933] p7zip_jll