

## Midpoint Ellipse Algorithm

1. **Input:** Provide the radii  $r_x, r_y$ , and the ellipse center  $(x_c, y_c)$ . Initialize the first point on the ellipse centered on the origin as:

$$(x_0, y_0) = (0, r_y)$$

2. **Region 1 Decision Parameter:** Calculate the initial decision parameter for Region 1 as:

$$P_1 = r_y^2 - r_x^2 r_y + \frac{1}{4} r_x^2$$

3. **Iteration in Region 1:** For each  $x$ -position in Region 1 (starting at  $k = 0$ ), perform the following:

- If  $P_1 < 0$ , the next point is  $(x_k + 1, y_k)$  and update:

$$P_1 = P_1 + 2r_y^2 x_k + r_y^2$$

- Otherwise, the next point is  $(x_k + 1, y_k - 1)$  and update:

$$P_1 = P_1 + 2r_y^2 x_k - 2r_x^2 y_k + r_y^2$$

- Continue until  $2r_y^2 x = 2r_x^2 y$ .

4. **Region 2 Decision Parameter:** Using the last point  $(x_p, y_p)$  from Region 1, calculate the initial decision parameter for Region 2:

$$P_2 = r_y^2 \left(x_p + \frac{1}{2}\right)^2 + r_x^2 (y_p - 1)^2 - r_x^2 r_y^2$$

5. **Iteration in Region 2:** For each  $y$ -position in Region 2 (starting at  $k = 0$ ), perform the following:

- If  $P_2 > 0$ , the next point is  $(x_k, y_k - 1)$  and update:

$$P_2 = P_2 - 2r_x^2 y_k + r_x^2$$

- Otherwise, the next point is  $(x_k + 1, y_k - 1)$  and update:

$$P_2 = P_2 + 2r_y^2 x_k - 2r_x^2 y_k + r_x^2$$

6. **Symmetry Points:** For each calculated pixel position  $(x, y)$ , determine the symmetric points in the other three quadrants.

7. **Translation:** Translate each pixel position to the ellipse centered at  $(x_c, y_c)$ :

$$(x', y') = (x + x_c, y + y_c)$$

8. **Plot:** Plot the points for both regions until the stopping condition  $2r_y^2 x = 2r_x^2 y$  is satisfied.