

## Algorithm for Midpoint Circle Drawing and Rotation

### **Step 1:**

Input the radius and the center coordinates of the circle:

- Radius ( $r$ )
- Center ( $x_c, y_c$ )

### **Step 2:**

Initialize variables:

- $x = 0$
- $y = r$
- $p = 1 - r$  (decision parameter)
- $xes = []$  (list to store x-coordinates of points)
- $yes = []$  (list to store y-coordinates of points)

### **Step 3:**

Calculate the initial symmetric points of the circle using the function `points_plot`:

- This function adds all symmetric points of the circle to  $xes$  and  $yes$ .

### **Step 4:**

Iteratively calculate points for the circle using the midpoint algorithm:

- Increment  $x$  in each iteration.
- If  $p < 0$ , update  $p = p + 2 * x + 1$ .
- Otherwise, decrement  $y$  and update  $p = p + 2 * (x - y) + 1$ .
- Calculate the symmetric points for each  $(x, y)$ .

### **Step 5:**

Define the rotation matrix to rotate the circle:

- Rotation angle: 90 degrees ( $\pi/2$  radians).
- Rotation matrix:  
$$\begin{bmatrix} \cos(\theta) & -\sin(\theta) & 0 \\ \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

### **Step 6:**

Define translation matrices to rotate the circle around its center:

- Translation to the origin using `reverse_translation_matrix`.

- Translate back to the center using `translation_matrix`.

### **Step 7:**

Compute the composite transformation matrix:

- $\text{Composite} = \text{Translation Back} * \text{Rotation} * \text{Translation to Origin}$ .

Apply this transformation to the circle points.

### **Step 8:**

Plot the original and rotated circles on the same graph:

- Use matplotlib to display the circles with different styles and colors.
- Ensure equal scaling with `plt.axis("equal")`.