

① let  $S = \{1, 2, 3, \dots, n\}$

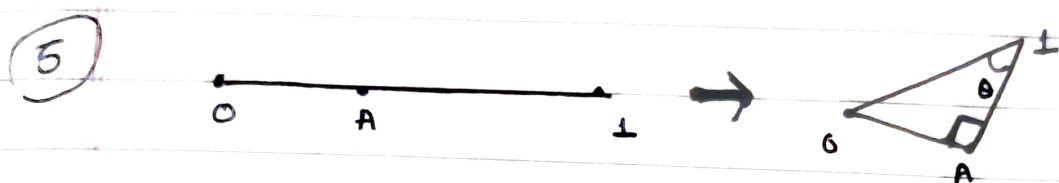
$f$  be a bijective function from  $S$  to  $S$   
if  $f(i) = i$  we call it a fixed point.

if we select a random  $f$  from the set of all bijective functions from  $S$  to  $S$  what is the expected no. of fixed points and variance for the same.

② Let two random variables  $X$  and  $Y$  and CDF  $F_X$  and  $F_Y$ ; find CDF of  $Z = \min(X, Y)$

③ You are given an urn with 100 balls (50 black, 50 white), You start picking balls one by one, until all the balls are all out. What is the expected no. of colour switches you will encounter while randomly picking the balls.

- ④ You are given a Box with 6 coupons, ~~and~~ labelled 1, 2, 3, 6. You are picking one by one with replacement. What is the expected no. of ~~tries~~ ~~times~~ you will need to get all the different coupons. Try to solve for general  $n$  coupons.



A point A is chosen at random on a rod of length 1. The rod is bent at A to form a right angle triangle. If  $\theta$  is the smallest angle of the triangle, what is the expected value of  $\tan \theta$ .

- ⑥ Two people visit a park between 5-6 pm. Each arrives at a random time ~~between~~ between 5-6 pm. ~~Intervat~~ and stays ~~of~~ for 30 min. in the park. What is the probability that they will meet each other.

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let  $X \sim N(0,1)$  [Normal (1,0)]~~then~~ then prove that  $X^2 \sim \text{gamma}(\frac{1}{2}, \frac{1}{2})$ 

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 $X \sim N(\mu, \sigma^2)$ find  $E(e^{xt})$