

06/01/21

# Compiler Design

- Lexical Analysis
- Parsing / Syntax Analysis
- Semantic Analysis
- ICG (Intermediate Code Generation)
- Code Optimization
- Code Generation

## Reference Book:

- Compiler Principles, techniques & tools - Ullman, Aho, Sethi

Compiler → Translates a program written in one language into an equivalent program in another language.

<sup>Source Program</sup>  
↓  
<sup>Target Program</sup>

## Errors:-

Lexical → Spelling

Syntax → Grammar

Semantics → Meaning

### Lexical Errors (Spelling)

- Invalid words

Eg: int a - @<sup>→ invalid constant</sup>;

int 1x2y;<sup>→ invalid identifier</sup>

String s = "Hello"

<sup>↑</sup>  
invalid string

### Syntax Errors (grammatical)

- Improper Structure

Eg: ;int a,b

int a, b

main()  
    <sup>↑</sup>  
    <sup>↑</sup>

### (meaning) Semantics Error

Eg: int a[-2];

int a, b; e=a+b;

sum(1,2,3); sum(a)

Ist Compiler → FORTRAN by Backus Nov

Notes:

1. The translation process carried out by a compiler is called compilation.
2. Compilation can be done in different modules & each module is known as phase of the compiler.

Phase Diagram of Compiler.

High Level Language



Lexical Analysis

↓ tokens (key, id, output, constants).

Syntactic Analysis

↓ Parse tree

Symbol Table

↓ Semantic Analysis

↓ Annotated Parse tree

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↓ 3-address code

Machine Independent Code Optimization

↓ optimized 3-AC

Code Generation

↓ Assembly Language code

Machine Dependent Code Optimization

↓ optimized Assembly code.



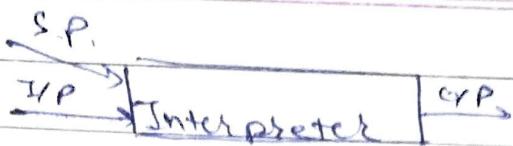
Middle End

Back End

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\* Interpreter → Instead of producing a target program as a result of translation, an interpreter directly executes the operation specified in the source program on its supplied by the user.



## \* Difference b/w High Level Language & low level language

HLL

- ⇒ Programmer friendly
- ⇒ Requires Compiler & interpreter
- ⇒ Easy to understand
- ⇒ Portable & M/C Independent
- ⇒ Simple

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- ⇒ M/c friendly
- ⇒ Executed directly
- ⇒ Hard to understand
- ⇒ Non-portable & M/c dependent
- ⇒ Complex

## \* Difference b/w Compiler & Interpreter

Compiler

- ⇒ Converts entire source code into executable m/c code.
- ⇒ More time to analyze sc.
- ⇒ Overall execution time is faster
- ⇒ Debugging is hard
- ⇒ Generate intermediate object code

Ex: C, C++, Java

Interpreter

- ⇒ Translate sc line by line.
- ⇒ Less time to analyze
- ⇒ Overall execution time is slow
- ⇒ easier.
- ⇒ No intermediate code

Ex Python, Perl

## \* Assembler → Translate assembly code into machine code

Compiler

## \* Difference b/w Compilers & Assembler

### Compiler

→ Src  $\leftrightarrow$  M/C

→ I/P is Src

→ whole program at once

→ O/P is binary

Ex - GNU

→ 2 phases

### Assembler

→ Assembly code  $\rightarrow$  M/C

→ I/P is assembly

→ Can't do it at once

→ O/P are target compiled, i.e., mnemonic (ADD, MUL)

Ex - C, C++, Java,

→ ~~6 phases~~ phases

## \* Language Processing System:

↓ Source Program (HLL)

Pre-processor : Does macro expansion

↓ modified S.P (ParoHLL)

### Compiler

↓ Assembly language

### Assembler

↓ M/C

### Linker / Loader

↓ Target M/C code

Linker: Link & combine the objects generated by compiler into single executable ~~program file~~. It is responsible to combine & link all the modules of the program if written separately.

Loader: Load the program from secondary memory to main memory.

E<sub>x</sub> !

$$a = r + c \neq d$$

L-9

1

~~id op rd GP id op id PM~~

1

## Syntax A:

1

E

$$icl = R$$

$$\begin{array}{c} B + B \\ \hline 1 & 1 \\ id & B \star \\ \hline & 1 \\ id & \end{array}$$

1

## Semantic A.

1

S. att de hute

111

$$fd = B_{\text{att}}$$

— 1 —

$E_{\text{ext}}$  +  $R_{\text{ext}}$

1

11 P u b E

10

id id

1

## Annotated / Decalated P.T

↓  
ILG  
↓

$$t_1 = c + d$$

$$t_2 = b + t_1$$

$$a = t_2$$

↓

Code Optimization

↓

$$t_1 = c + d$$

$$a = b + t_1$$

↓

Code Generation

↓

MOV C, R0

Assembly Code

MOV D, R0

ADD B, R0

MOV R0, A

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### \* Lexical Analysis:

→ Reads HLL program & breaks the program into tokens where tokens are the logical unit of programming lang.

→ It also identifies lexical errors present in the given program

Ex: if b int a, ✓      int @a ; X

### \* Syntax Analysis:

→ It groups all the tokens together & verifies their grammatical structure with the help of context-free grammar (CFG)

Ex: :b int a, X

→ If the tokens are syntactically correct then it produces valid O/P otherwise returns Syntax error

Ex. short c, d;

int c, d;

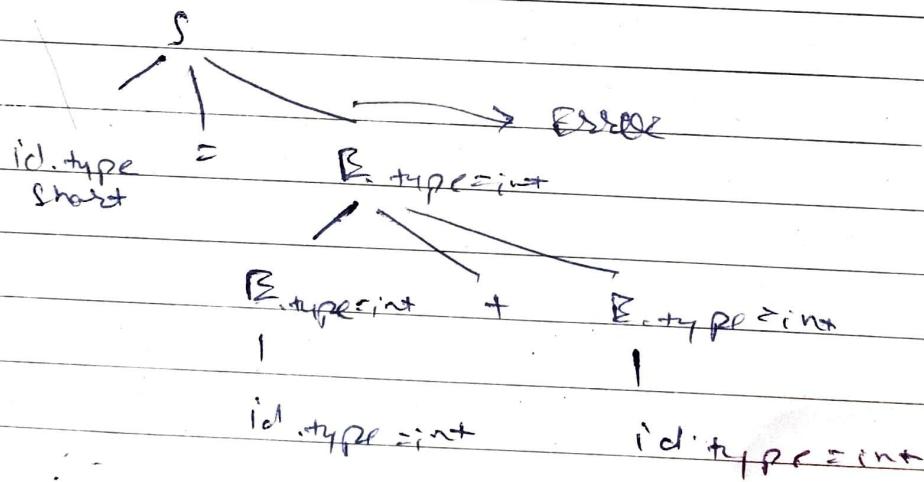
✓

a = c + d;

## \* Semantic Analysis :

- Takes parse tree as input & produces annotated parse tree as O/P.
- Type checking of the expression statements.
- Verifies any variable is used without declaration or not.
- Re-declaration of same variable multiple time in the same scope.
- Mismatch of formal & actual parameters.

Ex.



## \* Intermediate Code Generation :

- I.C. is a universal code from which generation of machine code for every machine becomes easy. This is known as retargeting.

→ No need to change complete compiler, only change the back end of the compiler.

→ Optimization on the intermediate code is also possible.

→ The main form of I.C. are

a) 3-Address Code

b) Syntax Tree

c) Postfix Code

### \* Code Optimization:

→ Improves the efficiency of target code by eliminating the unnecessary code.

### \* Code Generation:

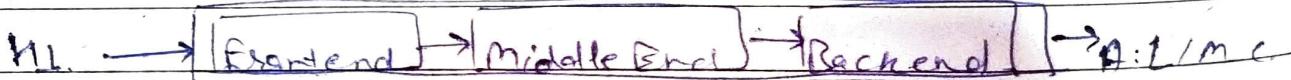
→ Generate target program code

### \* Single Pass & Multipass Compiler

Single Pass:



Multipass



Pass: (the complete seen of the source program is known)  
as the pass.

→ F.B.: HLL → Intermediate

M.B.: Optimize I.C

P.C.: I.C. → Target Program

\* Symbol Table: Data structure that maintains information about identifiers & constants present in the program.

| id | token | type | size | scope |
|----|-------|------|------|-------|
|----|-------|------|------|-------|

→ In the case of identifiers, ST stores information type of the identifier, memory, scope (global/local).

→ In case of functional identifiers: name of the function, return type, no. of arguments, type of arguments, way of passing.

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\* Compiler Construction Tools →

a) Scanner Generator: Lexical analyzer (using Regular expression) Ex: Lex

b) Parser: Syntax analyzer. Ex: YACC (Yet Another Compiler) (Compiler of Syntax)

c) Syntax directed generated translation engine: + generate assembly code + generate I.C.

d) Code generator: Generate Target code

e) Data flow analysis engine: Optimization

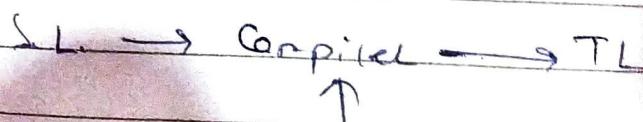
f) Compiler construction toolkit: Set of routines for constructing phases of compiler.

\* Bootstrapping: Used to construct a compiler

a) Source Lang

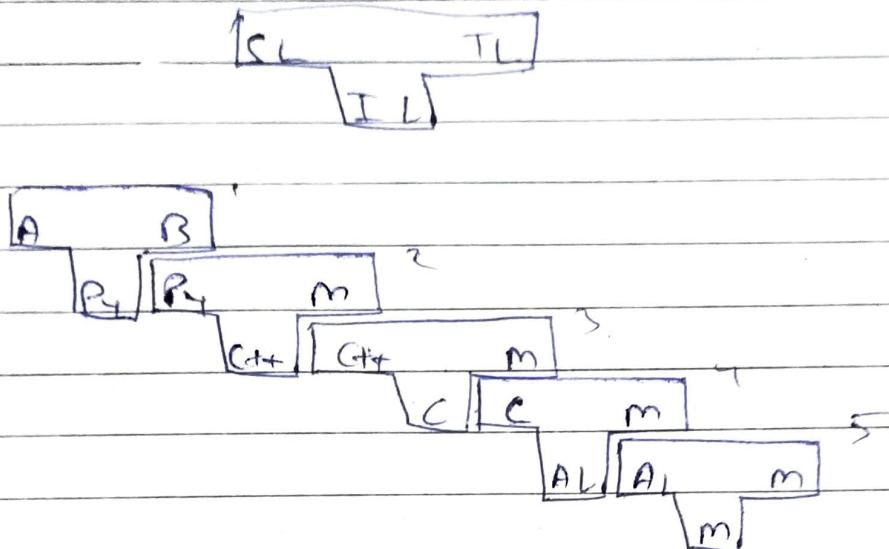
b) Target Lang

c) Implementation Lang



I C

T-Diagram - The compilation process of compiler can be represented using T-Diagram.



Bootstrapping is a process in which a simple language is used to translate more complicated program which in turn may handle more complex rated program. This complicated program can further handle even more complicated program to be run.

Cross compiler is a compiler which runs on one machine but produces target code of another machine.

#### \* Lexical Analysis Phase (Scanner):

- Reads S.P and character at a time from left to right.
- It breaks the program into tokens.
- It identifies lexical errors.
- It eliminates blank & comment lines in the program.
- It collects at the symbol table.
- It maintains line no.

Token: Tokens are the category of the T/P string.  
 (Keyword, identifier, operator, string, constants, punctuation mark).

Keywords: if, else, for, while

Identifiers: x, y, a, b, c, d, e, f, g, h, i, j, k, l, m, n, o, p, q, r, s, t, u, v, w, x, y, z

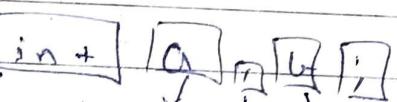
Operators: +, -, \*, /, =, <, >, >=, etc

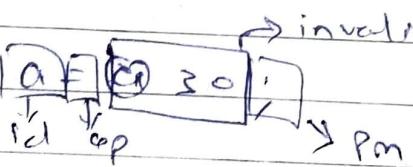
Constants: 100, 200, 3.5, 7.6, 9.1, 7

Punctuation marks: ;, :, {, }, [ ]

Patterns: Rules of the tokens

Lexeme: Sequence of characters in the source program that are matched with patterns of the tokens.

Ex(i)   
 Keyword id pm id SPM → Lexemes

(ii)   
 Keyword id op id SPM → Invalid Lexeme, lexical error

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Lexical Analyzer / Scanner

Manual Code

Tool Based - LEX / FLEX

## \* Rules of the Tokens:

### a) Regular Expression:

Ex.  $L = \{a, b\}$  R.E. =  $(a+b)^*$

$\rightarrow$  Kleen Closure

$+ \rightarrow$  Positive Closure

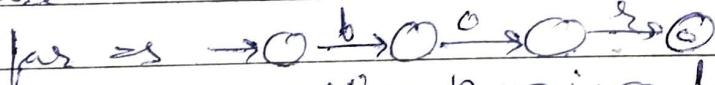
### b) Finite Automata

Deterministic Finite Automata: For each state & input, there will be exactly single transition

Keywords:

if  $\Rightarrow$  

else  $\Rightarrow$  

for  $\Rightarrow$  

while  $\Rightarrow$  

int  $\Rightarrow$  

Identifiers:

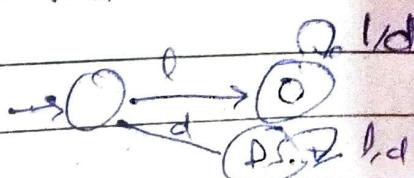
Symbols (i) letter  $l = \{a, \dots, z\}$

(ii) digits  $d = \{0, \dots, 9\}$

Rules of Identifiers :  $I(l+ld)^*$

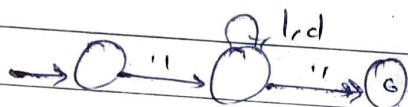
$\rightarrow$  Should start with a letter

$\rightarrow$  No limit on length.

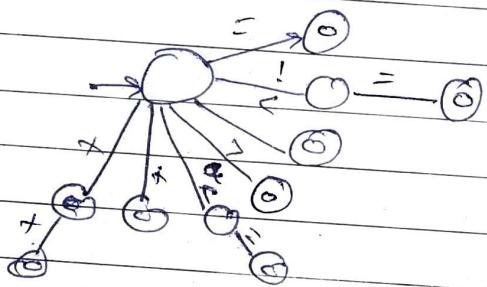


→ Length of the identifiers should be 32  
 $l(1+d+\epsilon)^{31} \rightarrow RB$ ,

String - "  $(1+d)^*$  "



Operators:

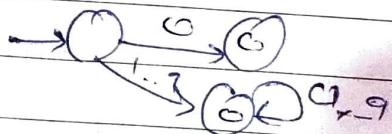


char:  $(1+d)$

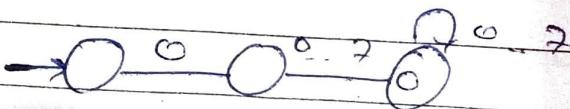


Constants:

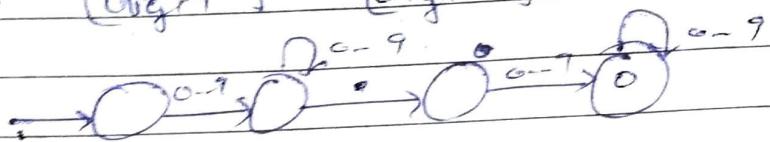
int →  $0 + [1+2+\dots+9][0+1+\dots+9]^*$



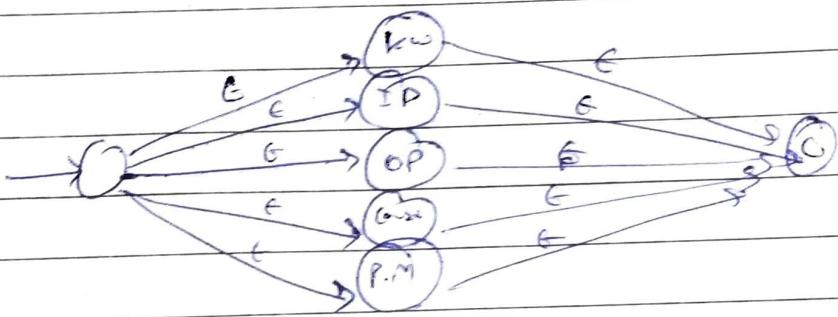
Octal →  $0 + [0+\dots+7] +$



Real  $\rightarrow$  [digit]<sup>+</sup> · [digit]<sup>+</sup>



### Ø Entree Rule (contd.)



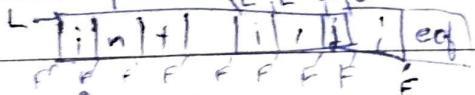
Input Buffering: Code stays in secondary memory & at execution entry the main memory

a) One Buffer Scheme

↳ Two " "

a) One Buffer Scheme

We use two pointers Lexeme Beginning & forward pointed



↳ Two Buffer Scheme

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Ex

### \* Problems Related to Lexical Analysis.

a) Identify whether the given program format gives the L.F. or not.

Eg. (i)  $f: (a>b)$

$a = (a;c)$  No error in L.A.

(ii) int a = @; g; Here L.F. is present

i.) No. of tokens in given program format

(ii) `for (if (of, i <= 10, / i++))` # of tokens = 13

(iii) `printf ("Welcome");` # of tokens = 5

(iv) `if (b > w)`  
 $a = a + b;$  /\* addition cannot  
 29

Non tokens: comments, preprocessor directive, blank, tab,  
 new line, macros, etc

(v) `int a, b, c;` Not known to LA  
 label tokenid type mem scope  
 a id  
 b id  
 c id

Q.1 Find C.B.

(a) `int, a b,`

(b) `int a = $ 10;`

(c) `String s = "Hello"`

(d) `Float a = 2.3;`

(e) `Float b = 3.4;`

Q.2. # of tokens

(a) `int a = 1, b = 2;`

(b) `a = (c d); +`

(c) `printf ("x.d y.d", x, y);`

(d) `while (i <= 10) {`

$a = a + i;$

$b = c + d;$  /\* addition of two no.

Dt. \_\_\_\_\_  
Pg. \_\_\_\_\_

### Q3. int main()

{

int i, n;

for (i=0; i<n; i++)

}

no. problem in L.A.

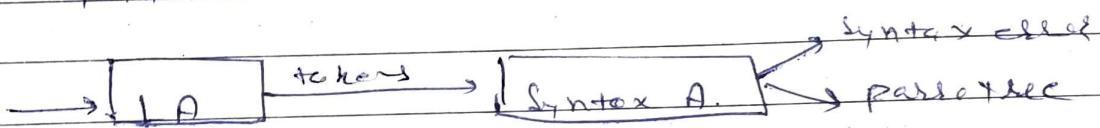
Syntax error

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### \* Syntax Error / Parser:



### Syntax Error

1. Lack of tokens to form the statement

Ex int a,b

2. More no. of tokens

Ex int a,,b;

3. Tokens not arranged properly

Ex ; int , a,b

\* (i) main () .

int a, b

if

; p} ("Hello")

}}

\* Rules of the Statement: Written using Context Free Grammars.  
 Regular grammars have less power than CFG & they  
 cannot handle comparison syntax.

Grammer:  $G = (V, T, P, S)$ .

$V$  = Set of variables (Non-Terminals) ( $A, B, C, D, E$ ) capital

$T$  = " Terminal - ( $a, b, c, d, \dots$ )

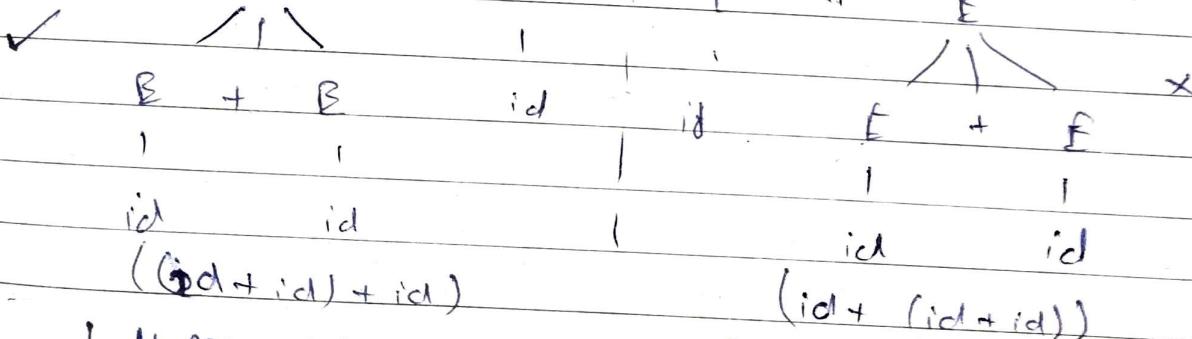
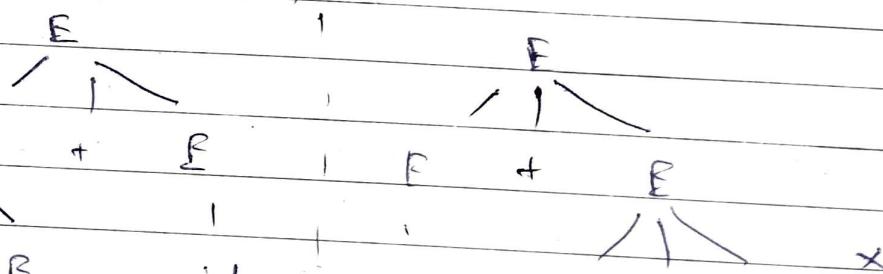
$P$  = No. of products

$S$  = Starting symbol

Ex.  $S \rightarrow id = R$

$E \rightarrow E + E / E * E / id$

Ex. :  
 $id + id + id$



$(id + id) + id$

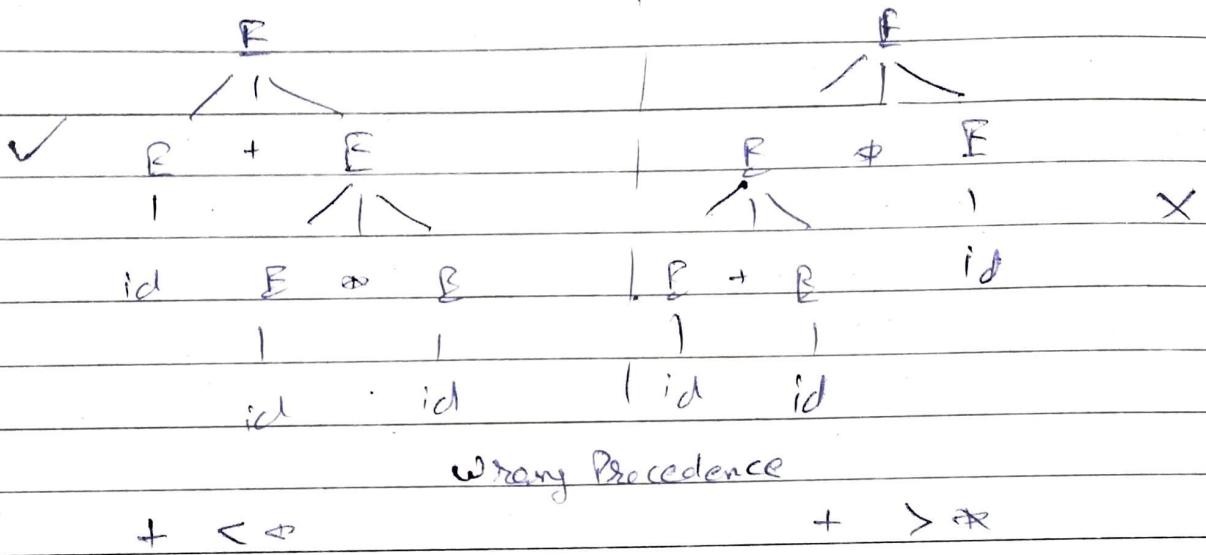
$(id + (id + id))$

Left Associativity

Right Associativity

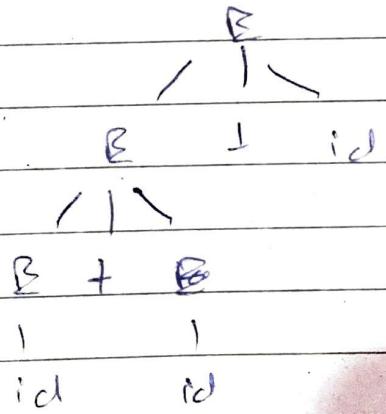
Wrong Ambiguous Grammer

Ex(id) id + id \* id



### \* Remove Ambiguity:

$E \rightarrow E + \text{id}/\text{id}$  (Left Recursion)



### \* Solve Precedence

$E \rightarrow E -> E + T/T$

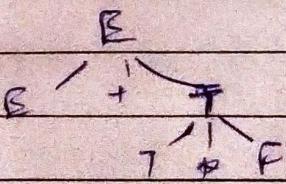
$T \rightarrow T * F/F$

$F \rightarrow \text{id}$

$+ > +$

$* > *$

$+ < *$



B7.  $P = \uparrow \rightarrow (\uparrow \rightarrow (\uparrow \rightarrow (\uparrow \rightarrow \downarrow)))$   $R \rightarrow L$

$E \rightarrow E + T / T$

$T \rightarrow T * F / F$

$F \rightarrow g \uparrow F / g$

$g \rightarrow id$

Associativity

$+ > *$

$* > *$

$\uparrow < \downarrow$

Precedence

$+ < * < \uparrow$

B8. Boolean Expression:

$E \rightarrow B \times P \text{ or } B \div P$

$/ B \times P \text{ & } B \div P$

$/ \text{ NOT } B \times P$

$/ \text{ True}$

$/ \text{ False}$

$E \rightarrow E \text{ or } F / F$

$F \rightarrow F \text{ & } g / g$

$g \rightarrow \text{Not } g / \text{True} / \text{False}$

Precedence

$OR < And < \text{Not}$

Associativity

$OR > OR$

$And > AND$

B9.

$A \rightarrow A \# B / B$

or Ambiguity

$B \rightarrow B \# C / C$

↳ Associativity of O/P

$C \rightarrow C @ D / D$

(ii) Precedence

$D \rightarrow d$

B10.  $E \rightarrow E \# F$

$F \rightarrow F - F$

$/ F + E$

$/ id$

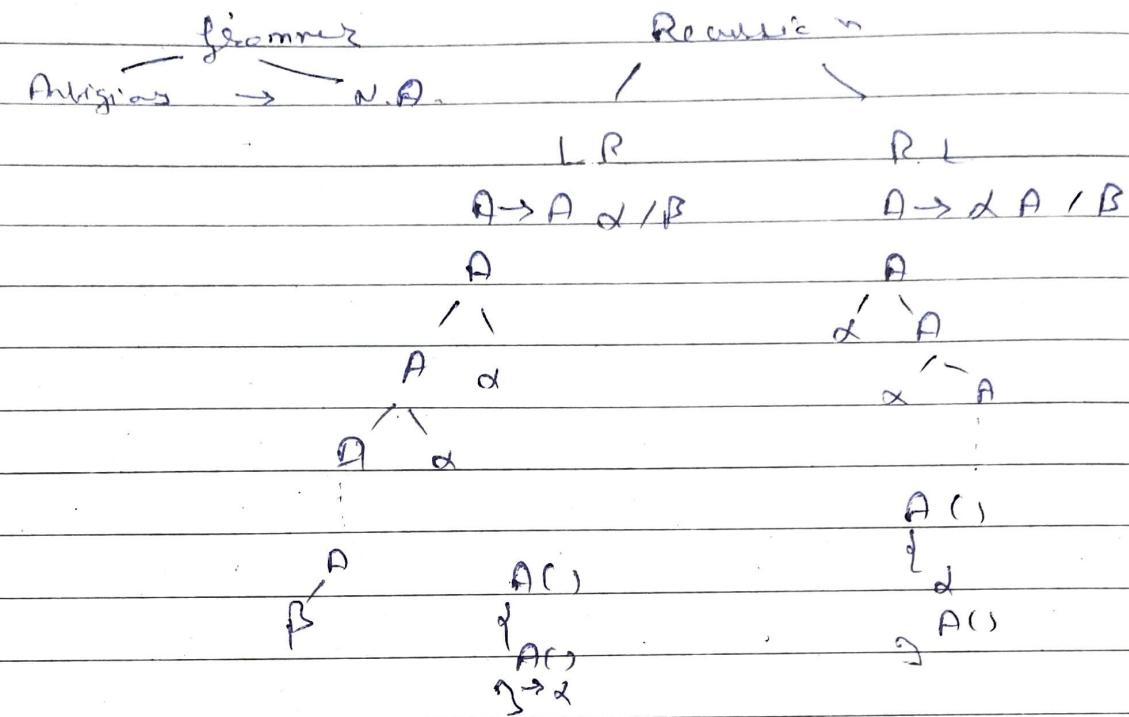
$/ F$

Associativity

$* > *$

$+ < * +$

- (Ambiguous Grammar)



Infinite Loop

Not desired in parser

Language:  $B^* \alpha^*$

Change Gramm:

$A \rightarrow B A'$

$A' \rightarrow E / \alpha A'$

Right Recursion

B.g.  $E \rightarrow B + T / T$

$T \rightarrow T * F / F$

$F \rightarrow id$

$A \rightarrow B A'$

$A' \rightarrow E / \alpha A'$

Conversion:

$R \rightarrow TB'$

$E' \rightarrow E / TB'$

$T \rightarrow FT'$

$F \rightarrow FT' / C$

$C \rightarrow id$

Ex.  $S \rightarrow S \alpha S \mid S \beta \mid \alpha$

Generalize form:

$A \rightarrow A \alpha_1 / A \alpha_2 / A \alpha_3 \quad / B, / B_2 / B_3 \dots$

①

$A \rightarrow B, A' / B_2, A' / B_3 A' \dots$

$A' \rightarrow \alpha, A' / \alpha_2 A' / \alpha_3 A'$

Left Recursion

Direct LR

$A \rightarrow A \alpha / B$

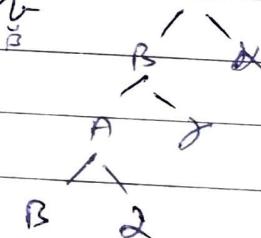
Indirect LR

$A \rightarrow B \alpha$

$B \rightarrow A \gamma / B$

Q.L.R.

A



$B \rightarrow B^d \gamma / B$

$B = b F'$

$B' = \alpha \gamma B' / E$

$A \rightarrow B^d$

Ex.  $S \rightarrow A \alpha / b \quad (\text{I LR})$

$A \rightarrow S \alpha / a$

↓

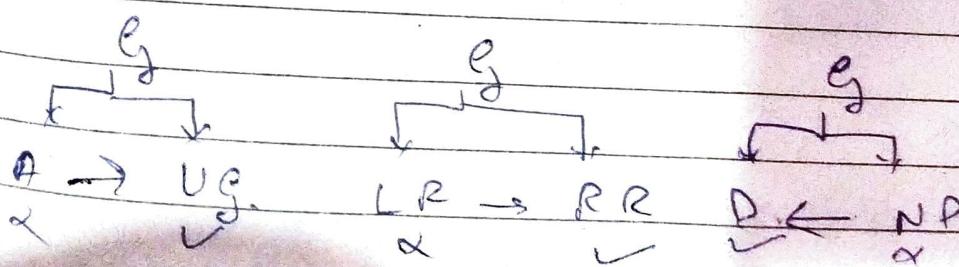
$A \rightarrow A \alpha d / b \alpha / a \quad (\text{LR})$

↓

$A \rightarrow b \alpha A' / a A' \quad (\text{Non-LR})$

$A' \rightarrow \alpha d A' / E$

$S \rightarrow A \alpha / b$



~~#~~ Left-factoring  $\rightarrow$  Converting ND  $\rightarrow$  D.

$$A \rightarrow \lambda A'$$

$$A' \rightarrow B_1/B_2/B_3$$

Bg:  $S \rightarrow iB + s / iE + es / a$   
 $B \rightarrow b$

$\downarrow$

$$S \rightarrow iB + SS' / a$$

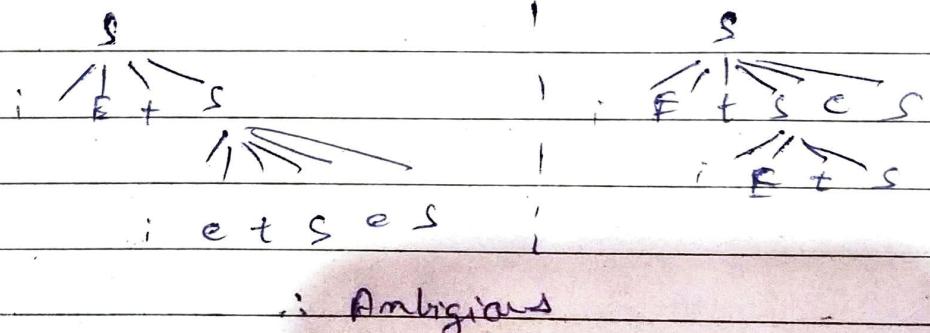
$$S' \rightarrow E / es$$

$$E \rightarrow b$$

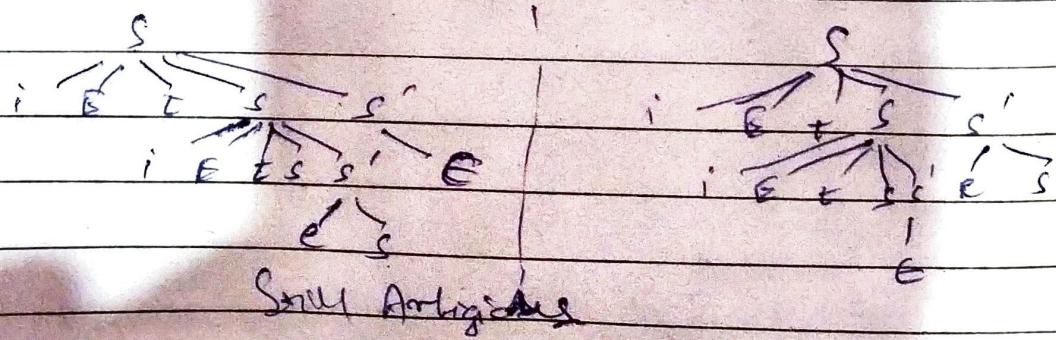
Note: Remaining the Non-Deterministic nature of grammar  
doesn't remove ambiguity.

By  $\rightarrow iB + s : iB + es$

①  $S \rightarrow iE + / iE + es / a$



②  $S \rightarrow iE + ss' / a \quad S' \rightarrow E / es$



Eg:  $S \rightarrow aSs \cup s$

1 aSaSs

1 aSs

1 s

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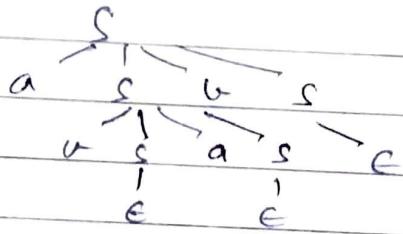
C. D.

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Eg:  $S \rightarrow aSs \cup s \cup a \epsilon$

abcde

→ Multiple Productions



To determine which production to select - first sets calculated.

\* First Set () : Rules to calculate first set

a) First (terminal) = terminal

b)  $A \rightarrow a\alpha$

$$\text{First}(A) = \{a\}$$

c)  $A \rightarrow B\alpha$ ,  $B \not\rightarrow \epsilon$  (directly, or indirectly)

$$\text{First}(A) = \text{First}(B)$$

d)  $A \rightarrow B\alpha$ ,  $B \rightarrow \epsilon$

$$\text{First}(A) = \{\text{First}(B) - \epsilon\} \cup \{\text{First}(\alpha)\}$$

Ex.: (i)  $S \rightarrow AA$        $\text{First}(S) = \{a\}$   
 $A \rightarrow b/c$        $\text{First}(A) = \{b, c\}$   
 $B \rightarrow d$        $\text{First}(B) = \{d\}$

Ex.: (ii)  $S \rightarrow AB$        $\text{First}(S) = \text{First}(A) \cup \{a\} \cup$   
 $A \rightarrow a$        $\text{First}(A) = \{a\}$   
 $B \rightarrow b/c$        $\text{First}(B) = \{b, c\}$

Ex.: (iii)  $S \rightarrow A B$        $\text{First}(S) = \{\text{First}(A) - \epsilon\} \cup \text{First}(B) = \{a, b\}$   
 $A \rightarrow a/c$        $\text{First}(A) = \{a, c\}$   
 $B \rightarrow b$        $\text{First}(B) = \{b\}$

Ex.: (iv)  $S \rightarrow aAa/bBb/a / Bb/Ba$        $\text{First}(S) = \{\text{First}(A) - \epsilon\} \cup \text{First}(a) \cup$   
 $A \rightarrow \epsilon$        $\{\text{First}(B) - \epsilon\} \cup \text{First}(a)$   
 $B \rightarrow \epsilon$        $= \{(\epsilon - \epsilon) \cup a\} \cup \{(\epsilon - \epsilon) \cup b\} = \{a, b\}$   
 $\text{First}(A) = \{\epsilon\}$        $\text{First}(B) = \{\epsilon\}$

(v).  $A \rightarrow B \cup / cd$   
 $B \rightarrow aB/b$   
 $C \rightarrow dc/c$

\* Follow Set(): Rules to calculate Follow Set

a)  $\text{Follow}(S) = \{\$\}$

b)  $A \rightarrow \alpha B \beta, B \rightarrow \epsilon$

$\text{Follow}(B) = \text{First}(F)$

c)  $A \rightarrow \alpha B$

$\text{Follow}(B) = \text{Follow}(A)$

d)  $A \rightarrow \alpha B \beta, B \rightarrow \epsilon$

$\text{Follow}(B) = \{\text{First}(B) - \epsilon\} \cup \{\text{Follow}(A)\}$

Ex: (i)  $E \rightarrow TE'$  $B' \rightarrow +TB'/\epsilon$  $T \rightarrow FT'$  $T' \rightarrow *FT'/\epsilon$  $F \rightarrow id$ 

$$\text{Follow}(B) = \{ \$ \}$$

$$\text{Follow}(B') = \text{Follow}(B) - \{ \$ \}$$

$$\text{Follow}(T) = \{\text{First}(B') - E^g\} \cup \text{Follow}(B)$$

$$= \{(+, \epsilon) - E^g \cup \{ \$ \}\} = \{+, \$\}$$

$$\text{Follow}(T') = \text{Follow}(T) = \{+, \$\}$$

$$\text{Follow}(F) = \text{Follow}(T) - \{\text{First}(T') - E^g\} \cup$$

$$\text{Follow}(T)$$

$$= \{(*, \epsilon) - E^g \cup \{ +, \$ \}\}$$

$$= \{ *, +, \$ \}$$

Ex: (ii)  $S \rightarrow aABb$  $A \rightarrow c/\epsilon$  $B \rightarrow d/\epsilon$ 

$$\text{Follow}(S) = \{ \$ \}$$

$$\text{Follow}(A) = \{\text{First}(B) - E^g\} \cup \text{Follow}(B)$$

$$= \{(d, \epsilon) - E^g \cup \{ b \}\} = \{d, b\}$$

$$\text{Follow}(B) = \text{First}(b) = \{b\}$$

Q.1  $S \rightarrow A$  $A \rightarrow aB/a$  $B \rightarrow bB/C$  $C \rightarrow g$ Q.2.  $S \rightarrow iE + SS'/a$  $S' \rightarrow eS/\epsilon$  $E \rightarrow b$

# \* Parsing Techniques

(a) Universal Parsing



CYK Parsing Barley's Parsing

$O(n^3)$

(b) Top-Down Parsing



with Backtracking

w/o Backtracking

(c) Bottom-up Parsing



LR Parsing

operator precedence

LR(0)

SLR(1)

LALR(1)

LLR(1)

Brute-force

Recursive

Non-Recursive

Descent

Descent

Predictive

Predictive

Passing

Passing

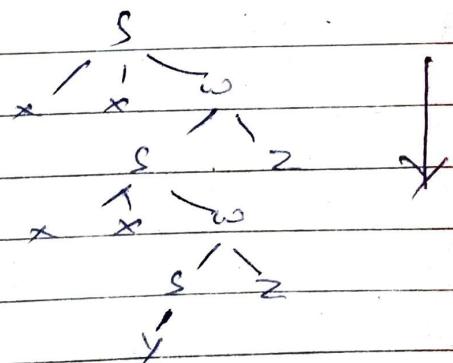
Ex. (i)  $S \rightarrow xxw$

$S \rightarrow y$

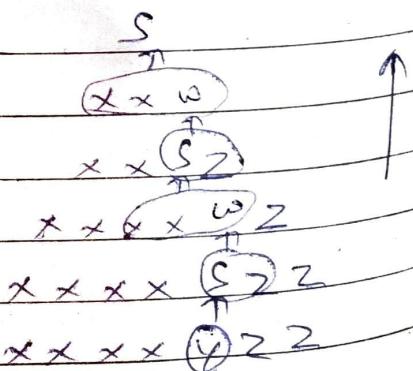
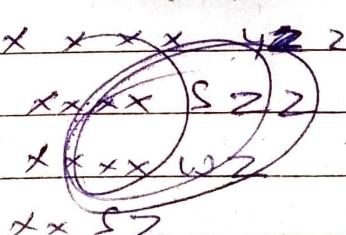
$w \rightarrow Sz$

$xxxxyzz$

Top-Down



Bottom-up



## \* Top-Down Parsing

- Construct the parser table which starts from the starting symbol & proceeds until the required string is produced by replacing every non-terminal by its corresponding R.H.S.
- It uses left most derivation in the construction of parser.

## \* Bottom-Up Parsing

- Construct the parse tree starting from the given string & proceeds until the starting symbol is reached by replacing the substring by its corresponding L.H.S. non-terminal.
- It uses right most derivation in reverse order.

## Top-Down Parsing

with Backtracking

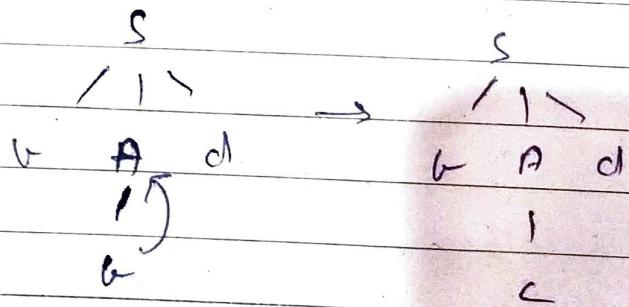
### 1. Brute force Parsing $\Theta(2^n)$ :

$$\text{Ex.: } S \rightarrow bAd/aB$$

$$A \rightarrow b/c$$

$$B \rightarrow ccd/odd c$$

ccd:



→ Exponential Time Complexity is not used in practical compilers

→ Higher Powers of Parser: No. of grammars a parsing technique can handle is known as power of a parser

→ Powerful compared to all the remaining techniques as it handles A + B strings

## Without Backtracking

### 1. Recursive Descent Predictive Parsing

→ Very simple to design

→ First compiler - FORTRAN

$B_T : E \rightarrow \text{num}^+ T$

$T \rightarrow * \text{num}^+ T / E$

$E(), T()$

Procedure  $E()$

{

if (lookahead == num)

{

advance();

$T()$ ;

}

else {error();}

, if (lookahead == \$)

{ pf ("Success"); }

, else {error();}

advance()

lookahead = NextToken;

}

error()

{ pf ("Syntax error"); }

error

error

34\*

\* 34

Procedure  $T()$

{

if (lookahead == \$)

{

advance();

, if (lookahead == num)

{

advance();

$T()$ ;

}

, else {error();}

, else {null;}

{

- Recursive Program uses Runtime memory (Activation Record)
  - Not advised, may occupy lot of runtime memory in the compile time itself
  - Very difficult to debug recursive program.
  - To avoid this, we use non recursive descent parsing.

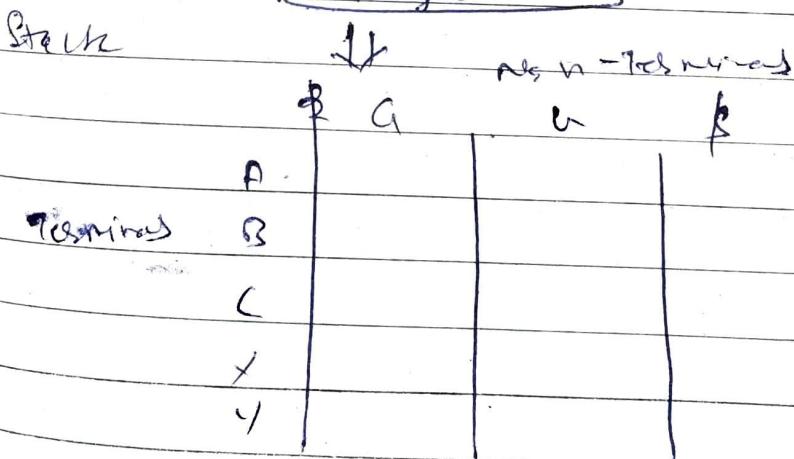
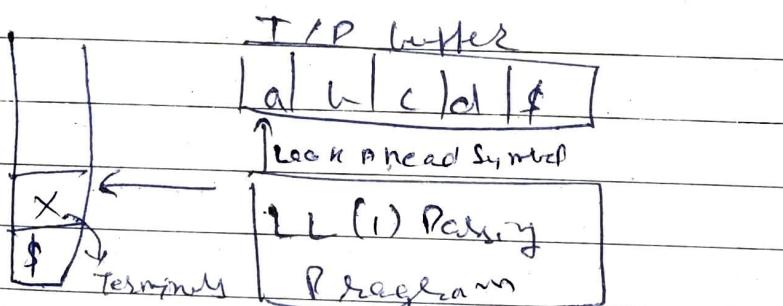
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C.D.

11

## 2. Non-Recursive Descent Predictive Parsing or LL(1) Parsing

left to right      ↴      Length of backtracking symbol.  
                        ↴      Left most derivation



## LL(1) Parsing Table

Length of table = # of Non Terminal \* # of terminals

Dt. \_\_\_\_\_  
Pg. \_\_\_\_\_

Let  $x$  be the symbol on the top of the stack &  $\alpha$  is look ahead symbol then.

(a) if  $x = a = \epsilon$

TIP: string is valid & parsing is successful

(b) if  $x = a \neq \epsilon$

Pop  $x$  from stack & increment L.A.S.

(c) If  $x$  is non-terminal on the stacks, then parser takes the decision from the parsing table

$$[x, a] \Rightarrow x \rightarrow UVW$$

$x$  is replaced by  $UVW$  such that  $U$  appears on the top of the stack.

(d) if  $[x, a] \Rightarrow \text{Blank}$

Syntax error, & return to the error handler.

→ To apply this algorithm initially starting symbol will be pushed on the stack.

$$B_1: S \rightarrow A B$$

3x3 → length of parsing table

$$A \rightarrow a$$

$$B \rightarrow b$$

Apply parsing for the string  $a b$  by considering following grammar in LL(1) parsing table & also identify total no. of actions.

|   | a                  | b | \$ |
|---|--------------------|---|----|
| S | $S \rightarrow AB$ | / | /  |
| A | $A \rightarrow a$  | / | /  |
| B | $B \rightarrow b$  | / | /  |

Stack

|    |     |
|----|-----|
| \$ | S   |
| \$ | B A |
| \$ | B a |
| \$ | B   |
| \$ | v   |
| \$ |     |

T/P stack

ab \$

ab \$

Take \$

v \$

b \$

\$

Action

1

2

3

4

5

6. Accep +

E.  $F \rightarrow T E'$  $F' \rightarrow + T B' / E$  $T \rightarrow R T'$  $T' \rightarrow * R T' / E$  $F \rightarrow id / ( E )$ T/P stack  $\rightarrow id + id \# id$ 

|    |                       |           |                       |                           |
|----|-----------------------|-----------|-----------------------|---------------------------|
| E  | $E \rightarrow T B'$  | $+ *$     | $( )$                 | \$                        |
| E' | $E' \rightarrow T B'$ |           | $E' \rightarrow T B'$ | $E' \rightarrow + B' / E$ |
| T  | $T \rightarrow F T'$  |           | $T \# T'$             |                           |
| T' |                       | $T' \# E$ | $T' \# T'$            | $T' \# E$                 |
| F  | $F \rightarrow id$    |           | $F \rightarrow ( B )$ | $F \rightarrow id$        |

Stack

|    |          |
|----|----------|
| \$ | E        |
| \$ | R' T     |
| \$ | R' T' F  |
| \$ | R' T' id |
| \$ | R' T'    |
| \$ | R'       |
| \$ | R' T +   |
| \$ | R' T     |
| \$ | R' T' F  |
| \$ | R' T' id |
| \$ | R' T'    |
| \$ | R' T' F  |
| \$ | R' T' F  |

T/P

id + id  $\#$  id \$id + id  $\#$  id \$id + id  $\#$  id \$+ id  $\#$  id \$+ id  $\#$  id \$+ id  $\#$  id \$id  $\#$  id \$id  $\#$  id \$id  $\#$  id \$id  $\#$  id \$

\* id \$

\* id \$

id \$

Action

1

2

3

4 POP

5

6

7 POP

8

9

10 - POP

11

12

13

$\$ E T' id$ 

id \$

14 Poo

 $\$ E T'$ 

\$

15

 $\$ B'$ 

\$

16

 $\$$ 

\$

17 Accept

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CD

(12)

\* Construct LL(1) Parsing Table for the Grammar

B1.  $E \rightarrow T E'$

$E' \rightarrow + T E' / \epsilon$

$T \rightarrow F T'$

$T' \rightarrow * F T' / \epsilon$

$F \rightarrow id / C(E)$

|      | $id$                 | $+$                     | $*$                     | $($                  | $)$  | $\$$                      |
|------|----------------------|-------------------------|-------------------------|----------------------|--|---------------------------|
| $E$  | $E \rightarrow T E'$ |                         |                         | $E \rightarrow T E'$ | <del><math>E \rightarrow T E'</math></del> |                           |
| $E'$ |                      | $E' \rightarrow + T E'$ |                         |                      | $E' \rightarrow + T E'$                    | $E' \rightarrow \epsilon$ |
| $T$  | $T \rightarrow F T'$ |                         |                         | $T \rightarrow F T'$ |  | $T \rightarrow F T'$      |
| $T'$ |                      | $T' \rightarrow E$      | $T' \rightarrow * F T'$ |                      | $T' \rightarrow E$                         | $T' \rightarrow * E$      |
| $F$  | $F \rightarrow id$   |                         |                         | $F \rightarrow id$   |  |                           |

$First(E) = \{ id, C \}$

$Follow(E) = \{ \$, ) \}$

$First(E') = \{ +, \epsilon \}$

$Follow(E') = \{ \$, ) \}$

$First(T) = \{ id, C \}$

$Follow(T) = \{ +, \$, ) \}$

$First(T') = \{ *, \epsilon \}$

$Follow(T') = \{ +, \$, ) \}$

$First(F) = \{ id, C \}$

$Follow(F) = \{ *, +, \$, ) \}$

→ If first has  $E$ , we follow  $Follow$

→ No multiple entry → LL(1)

→ Once grammar is LL(1) is强壮的, But not true

- Left Recursive grammar is not LL(1)
- NP (Non-left) factored → Not LL(1)
- Single production for each N.T. → LL(1)
- $A \rightarrow \alpha_1 / \alpha_2 / \alpha_3 / \dots / \alpha_n$   
 $\text{First}(\alpha_1) \cap \text{Follow}(\alpha_2) \cap \dots \cap (\text{First}(\alpha_n) \neq \emptyset \rightarrow \text{LL}(1))$
- $A \rightarrow \alpha / \beta$   
 $\text{First}(A) \cap \text{Follow}(\beta) \neq \emptyset \rightarrow \text{LL}(1)$

Ex.: (i)  $S \rightarrow aSbS \mid bSaS \mid \epsilon$   
 LL(1) grammar as not  
 $\text{First}(aSbS) = \{a\}$   
 $\text{First}(bSaS) = \{b\}$   
 $\text{First}(\epsilon) = \text{Follow}(S) = \{a, b, \$\}$   
 $[S, a] \Rightarrow S \rightarrow aSbS, S \not\in E$   
 $[S, b] \Rightarrow S \rightarrow bSaS, S \rightarrow E$   
 $[S, \$] \Rightarrow S \rightarrow \epsilon$

Ex.: (ii)  $S \rightarrow aB\bar{B}b$   
 $A \rightarrow C/E$   
 $B \rightarrow d/E$

Single grammar production is always LL(1)  
 $\text{Follow}(A) = \{C\} \cap \text{Follow}(B) = \{b, d\}$

Ex.: (iii)  $S \rightarrow aB/\epsilon$        $\text{Follow}(S) = \text{Follow}(C) = \text{Follow}(B) = \{\$\}$   
 $B \rightarrow bC/\epsilon$   
 $C \rightarrow cS/\epsilon$

G.1  $S \rightarrow A B$

$A \rightarrow d / G$

$B \rightarrow b / G$

G.2.  $S \rightarrow A S A / G$

$A \rightarrow C / G$

G.3.  $S \rightarrow A$

$A \rightarrow B C / G$

$B \rightarrow A B / G$

$C \rightarrow C C / G$

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(13)

G.4.  $S \rightarrow A B$

$A \rightarrow a b / a c$

$B \rightarrow b b / b a$

$LL(2)$  as not

~~First(s) = { first(A), first(B) }~~ Always  $LL(2)$

~~First(A) = { a, first(ac) }~~

~~First(B) = { b, b }, { b-a }~~

~~First(ac) < First(b)~~

$First(ac) \geq First(b)$

$First(b) = \{ b, b \}$

$\{ ba \} = \{ ba \}$

$\therefore LL(2) \sim$

$LL(1) \alpha$

Powers of  $LL(2)$  parser is more than  $LL(1)$  parser

## \* Bottom-Up Parsing Tree (Shift Reduce Parser)

→ Based on handle detection & handle pruning mechanism.

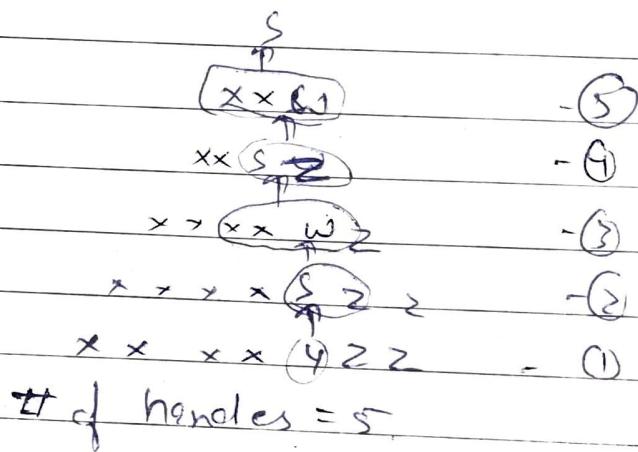
Handle: Substring in the I/P string that is matched with RHS part of the grammar.

→ When handle is detected, replace it by its corresponding left non-terminal. This is known as handle pruning.

Ex (-)  $S \rightarrow x x w$

$S \rightarrow y$

$x x \rightarrow S z$



Actions in Bottom-up

- Shift: Shift the symbol from I/P buffer into the stack
- Reduce: When a handle is detected on the stack, replace it by its corresponding left non-terminal
- Accept: If stack contain the starting symbol & look ahead symbol, I/P string is accepted.
- Errors: Parser halts w/o accepting the string

- Q. How many shift-reduce actions taken by shift-reduce parser to reduce the I/P string

int id, id;

S → TL;

T → int / float

L → L, id / id

# Shift = 5

# Reduce = 4

# of operation = 10

Stack

\$

\$ | int

( | T |

\$ ( T ) id |

\$ ( T ) L |

| id | C | , |

\$ ( T ) L | , | id |

\$ ( T ) L

\$ ( T ) L | ;

\$ ( S )

I/P Buffer

int id, id; \$

LAS

id, id; \$

Action

shift

reduce

Shift

Reduce

Shift

Shift

Reduce

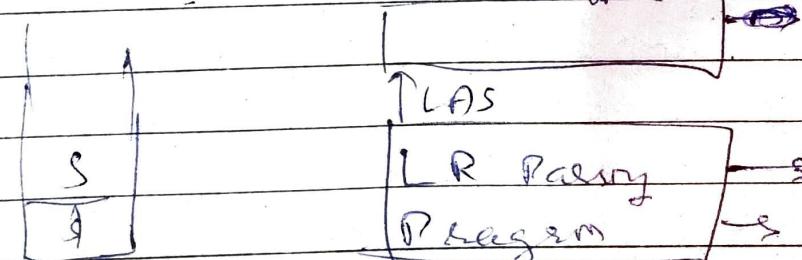
Shift

Reduce

Accept

## LR Parsing Technique:

I/P buffer



Stack

| Terminals            | Action | Go To | Non-Terminals |
|----------------------|--------|-------|---------------|
| State I <sub>0</sub> | a → r  | s → B |               |
| I <sub>1</sub>       |        |       |               |
| .                    |        |       |               |
| I <sub>n</sub>       |        |       |               |

d) Initially push initial/start state of the parsing table onto the stack.

b) Let S be the state ~~cont~~ at the top of the stack & A is the L.A.S. in T/P buffer, then LR parser will take decision from the LR parsing table as follows.

i) if Action [S, q] = Shift + J

Shift a onto the stack & then shift J onto the top of the stack & increment the L.A.S.

ii) if [S, q] = Reduce (A → β)

then pop 2+ |P| (2+ns of length of β symbol from the stack) & push α onto the stack & then push gate of (J, A) onto the top of the stack.

iii) if [S, q] = Accept

T/P string is valid → stop parsing

iv) if [S, q] = Blank

Syntax errors → return to error handler