

## Optimization Model

### Constraints

$$\text{(Max Battery Limit)} \quad b_n^k \leq b_{\text{full}} \quad (1)$$

$$\text{(Min Battery Limit)} \quad b_n^k \geq e_{\text{base}} \quad (2)$$

$$\text{(Turn vs Move)} \quad y_{\text{turn},n}^k + y_{\text{mov},n}^k \leq 1 \quad (3)$$

$$\text{(Exchange vs No-Exchange)} \quad Y_{\text{exchange},n}^k + Y_{\text{noexchange},n}^k \leq 1 \quad (4)$$

$$\text{(Binary Turn Limit)} \quad y_{\text{turn},n}^k \geq 0 \quad (5)$$

$$\text{(Binary Move Limit)} \quad y_{\text{mov},n}^k \geq 0 \quad (6)$$

$$\text{(Binary Exchange Limit)} \quad Y_{\text{exchange},n}^k \geq 0 \quad (7)$$

$$\text{(Binary No-Exchange Limit)} \quad Y_{\text{noexchange},n}^k \geq 0 \quad (8)$$

$$\text{(Exchange implies station presence)} \quad Y_{\text{exchange},n}^k \leq z_{\text{base\_station},n}^k \quad (9)$$

### Battery Update Rule

$$\begin{aligned} b_n^{k+1} = & Y_{\text{noexchange},n}^k \cdot (b_n^k - y_{\text{turn},n}^k \cdot b_{\text{turn}} - y_{\text{mov},n}^k \cdot b_{\text{mov}}) \\ & + Y_{\text{exchange},n}^k \cdot b_{\text{full}} \end{aligned} \quad (10)$$

### Objective Function (Multi-Objective)

$$\max \quad \sum_{i=1}^M c_i, \quad (11)$$

$$\min \quad \sum_{n,k} \left( y_{\text{turn},n}^k \cdot b_{\text{turn}} + y_{\text{mov},n}^k \cdot b_{\text{mov}} + Y_{\text{exchange},n}^k \cdot (b_{\text{full}} - b_n^k) \right) \quad (12)$$