## Paragraph Ran in the Queries

**Paper Title:** Nanoprecipitates enhanced the yield strength and output work of (TiHfZr)50(NiCu)50 high-entropy shape memory alloys

Content:

## Mechanical properties

Fig. 7 shows the compressive engineering stress \_\_strain curves of the fifteen as-cast and aged samples. Each sample exhibits the typical double yield shape characteristic of superelastic alloys. The results show that alloy composition and aging treatment have great influences on its mechanical properties. With increasing Zr content, the fracture strength ( $\sigma$ max) and fracture strain ( $\varepsilon$ max) decrease due to the increase in secondary phase precipitation during solidification, but the yield strength ( $\sigma_s$ ) and the critical strength ( $\sigma LC$ ) of stress-induced martensite transformation increase significantly. For the as-cast alloys, ternary TiNiCu alloys have the highest  $\sigma_{max}$  (3391.6 MPa) and  $\varepsilon_{max}$ (44.2 %), but their  $\sigma LC$  (310.2 MPa) and  $\sigma_S$  (660.5 MPa) are the lowest. The  $\sigma_{max}$ (2863.1 MPa) and  $\varepsilon_{max}$  (33.4 %) of the quaternary Zro alloy decrease, but  $\sigma_s$  and  $\sigma_{LC}$ increase greatly, reaching 481.2 MPa and 1530.1 MPa, respectively. With the increase in Zr, the  $\sigma_s$  and the  $\sigma_{LC}$  of HESMA continue to increase (Fig. 7(f)), and the  $\sigma_s$  of alloys Zr1, Zr5, and Zr10 reach 1500.2 MPa, 1760.5 MPa, 1870.3 MPa, respectively, and  $\sigma LC$  reaches 373.5 MPa, 570.1 MPa, and 648.5 MPa. This should be due to the combined effect of the enhanced solid solution strengthening effect caused by the increase in Zr content and the enhanced dispersion strengthening effect caused by the increase in the solidified secondary phase

Moreover, due to the precipitation of the nanoscale phases, the  $\sigma_8$  and  $\sigma_{LC}$  of aging alloys (especially for the samples aged at 400 °C) increase obviously, but the plasticity decreases, which is more obvious in HESMAs. The reason for the more significant decrease in plasticity of alloy HESMAs, may be that the number and size of nanoprecipitates is larger, so the hindrance effect on dislocation slip is stronger when the alloy undergoes plastic deformation. Compared with the as-cast alloys, the  $\sigma_8$  of the Zr1–300 and Zr5–300 samples increases by 10.4 MPa and 110.2 MPa, and the  $\sigma_{LC}$  of the Zr1–300, Zr5–300, and Zr10–300 alloys increases by 7.1 MPa, 60.0 MPa and 113.5 MPa, respectively. For the alloys aged at 400 °C, the  $\sigma_8$  of the Zr1–400, and Zr5–400 samples increases by 205.4 MPa and 180.2 MPa, and the  $\sigma_{LC}$  of the Zr1–400, Zr5–400, and Zr10–400 samples increases by 43.1 MPa, 310.0 MPa, and 350.5 MPa, respectively. The reason is that the quantity and scale of the nanoprecipitates in HESMAs aged at 400 °C (approximately 45–50 particles per  $\mu$ m² and 80–150 nm in length) are much larger than the samples aged at 300 °C (approximately 5–10/ $\mu$ m² and

40–80 nm in length) (as shown in Fig. 3), so the dispersion strengthening effect of the nanoprecipitates is stronger.

## Superelasticity properties

Fig. 8(a)-(e) show the loading \_\_unloading compressive curves of the five as-cast shape memory alloys with prestrains from 2 % to 15 %. For the first five cycles, the strain step size is 2 %, and for the last five cycles, it is 1 %. Fig. 8(f)-(i) show the evolutions of total recoverable strain  $(\varepsilon r)$ , superelastic recovery strain  $(\varepsilon s E)$ , elastic recovery strain  $(\varepsilon E)$ , residual strain ( $\varepsilon_i$ ), and shape recovery rate ( $\eta$ ) during cyclic compression. Fig. 9, Fig. 10 show the corresponding results of HESMAs aged at 300 °C and 400 °C, respectively. The results of Fig. 8, Fig. 9, Fig. 10 indicate that the load prestrain has a significant effect on the superelasticity behaviors during cyclic compression. With increasing prestrain, the  $\varepsilon_r$  and  $\varepsilon_{SE}$  increase significantly at first, and then increase slowly or even decrease slightly. For example, as the load strain increases from 2 % to 10 %, the  $\varepsilon_r$  of the as-cast Zr5 sample increases from 1.1 % to 7.7 %, and ESE increases from 0.3 % to 4.9 %. When the loading strain increases from 10 % to 15 %,  $\varepsilon r$  increases from 7.7 % to 8.7 %, and ESE decreases from 4.9 % to 4.8 %. On the one hand, the amount of austenite participating in the stress-induced martensite transformation gradually increases with the increasing prestrain; therefore, the  $\varepsilon_r$  and  $\varepsilon_{SE}$  increase with the loading prestrain at the initial stage. However, with a further increase in load strain (more than 10 %), the increment of newly added austenite participating in stress-induced martensitic transformation gradually decreases, and the deformation gradually exceeds the elastic deformation limit of the alloy, so the increase rates of  $\varepsilon_r$  and  $\varepsilon_{SE}$  decrease and tend to be gradually stabilize. On the other hand, with increasing loading strain, the plastic deformation of austenite and martensite and the dislocation accumulation in the cyclic compression process hinders the reverse transformation of stress-induced martensite, which may result in the stabilization of stress-induced martensite [48], [49], [50], [51], [52], so  $\varepsilon r$  and  $\varepsilon s \varepsilon E$  may drop slightly.

Moreover, the results in Fig. 8, Fig. 9, Fig. 10 also indicate that the superelasticity of the  $(Ti_{40-x}Hf_{10}Zr_x)_{50}(NiCu)_{50}$  HESMAs is much better than that of the ternary alloy and further improved after aging. Taking the as-cast alloys as an example (Fig. 8), the maximum  $\varepsilon_r$  and  $\varepsilon_{SE}$  of the ternary TiNiCu alloy in the cycle process are only 2.6 % and 0.9 %, respectively,  $\varepsilon_i$  reaches 12.4 % and the maximum  $\eta$  is only 52.3 % in the cyclic process. While the  $\varepsilon_r$  of  $(Ti_{40-x}Hf_{10}Zr_x)_{50}(NiCu)_{50}$  HESMAs is 7.2–8.8 %, the  $\varepsilon_{SE}$  is 3.6–4.8 %, and the maximum  $\eta$  can reach 75.5–77.8 %. For the results of the aged samples at 300 °C (Fig. 9), the maximum  $\varepsilon_r$  and  $\varepsilon_{SE}$  of the ternary TiNiCu-300 samples in the cycle process are only 3.9% and 1.8 %, while the corresponding values of HESMAs are 6.4–9.7 % and 2.4–5.4 %, respectively. For the results of the aged samples at 400 °C (Fig. 10), the maximum  $\varepsilon_r$  and  $\varepsilon_{SE}$  of the ternary TiNiCu-400 samples are only 4.2 %

and 2.1 %, while the corresponding values of HESMAs are 7.1–9.3 % and 3.2–5.1 %, respectively. Similar to the mechanical properties, the memory performances of HESMAs are better than those of ternary Ti-Ni-Cu and quaternary Zro samples, possibly for two reasons. First, the solution strengthening effect of HEAs is enhanced by the increase in Zr content; second, the dispersion strengthening effect caused by the secondary solidification phases is enhanced with the increase in Zr content. The reason for the further improvement of the aging sample is due to the dispersion strengthening effect of nanoprecipitates. It should be noted that among all the samples, the Zr<sub>5</sub> cast and aged HESMAs samples have the best superelasticity properties, and their maximum  $\varepsilon r$  and  $\varepsilon s \varepsilon E$  are 8.8–9.7 % and 4.9–5.4 %, respectively. In addition, the precipitation of coherent compound phases shown in Fig. 5 may also be one of the reasons for its strengthening. In addition to the above reasons, there is another possible reason for the better performance of Zr10 and Zr5 HESMAs. We measured the compositions of the 400 °C aged samples containing O through EDS. The oxygen contents of alloys TiNiCu-400, Zr0-400, Zr1-400, Zr5-400 and Zr10-400 are 4.8 %, 4.8 %, 4.96 %, 7.76 %, and 5.51 %, respectively. The results indicate that the Zr5-400 and Zr10-400 alloys with the best performance have the highest oxygen content. Ambient oxygen can also enter the HEA lattice as interstitial impurities, causing the formation of ordered oxygen complexes that can enhance both the strength and ductility of the alloys [53], [54], [55]. Therefore, the strength effect of interstitial oxygen may be one of the reasons for strengthening Zr5 and Zr10 HESMAs. However, further research is needed on the existing form and strengthening mechanism of oxygen in alloys in the future.

It should be noted that, compared with the increase in yield strength, the improvement in  $\varepsilon_r$  and  $\varepsilon_{SE}$  of HESMAs after aging treatment is slightly lower. One possible reason is that the phase transformation of the superelastic alloy in the cyclic loading process must be completed by the phase boundary migration of austenite and martensite. However, grain boundary migration is sometimes hindered by some factors, such as the precipitated phase [56], [57], [58], antiphase boundaries [59], or twin boundaries [60], [61], [62]. In this article, the nanoscale precipitates pin the phase boundary and hinder its migration, leading to the stabilization of martensite during reverse transformation [56], [57], [58], thus reducing the  $\varepsilon_r$  and  $\varepsilon_{SE}$  of the aged HESMAs to a certain extent. To understand the fracture mechanism of the prepared alloys, the samples after cyclic compression with 2-15 % prestrain were compressed to fracture and the morphology of the compression fracture surfaces is shown in Fig. 11. Most alloy samples exhibit <u>cleavage fracture</u> morphology, but due to the presence of vein-like fractures, a small amount of plastic slip traces can also be observed. In addition, it was found that aging treatment and an increase in Zr content both led to a decrease in vein patterns and a small increase in cracks. It should be noted that the Zr10-300 and Zr10-400 samples exhibit only brittle fracture morphology with no plastic slip traces visible, which is consistent with the mechanical performance test results.

Superelastic SMAs are widely used in medical devices, seismic structures, mechanical connections, damping devices, and other fields. Output work (Wout) is one of the important indicators to measure its performance, which is equal to the product of applied stress and recoverable strain ( $Wout = \sigma_{out} \times \varepsilon_r$ ) [26], [35], [44]. Fig. 12 shows the comparisons of Wout of the three groups of samples during cyclic compression. Compared with the as-cast alloys, the compressive strength ( $\sigma_{out}$ ) of all alloys and the recoverable strain  $(\varepsilon_r)$  of most alloys are improved after aging, which can lead to a higher Wout. For example, when the compressive prestrain is 15 %, the  $\sigma_{out}$  of the aged Zr5 alloy reaches 1693.8–1976.2 MPa,  $\varepsilon r$  reaches 9.1–9.7 %, and  $W_{out}$  reaches 179.6–188.5 J/cm3, while the corresponding values of the as-cast alloy are 1591.4 MPa, 8.7 %, and 163.7 J/cm<sub>3</sub>, respectively. Moreover, in comparison to reported HESMAs and SMAs [15], [23], [24], [25], [26], [28], [29], [31], [32], [35], [44], [63], [64], [65], [66], [67], [68], [69], [70], [71], [72], [73], [74] shown in Fig. 13, the (Ti<sub>40-x</sub>Hf<sub>10</sub>Zr<sub>x</sub>)<sub>50</sub>(NiCu)<sub>50</sub> HESMAs show an excellent combination of maximum output work (WMout) and maximum recoverable strain (EMr). The WMout and EMr of TiNiCu samples are only 17.4–35.8 J/cm<sub>3</sub> and 2.6–4.2 %, respectively, which are close to the values reported in the literature. The results of the Zro and Zr1 samples are relatively close and obviously higher than the literature values. The value of W<sub>Mout</sub> reaches 99.8–146.8 J/cm<sub>3</sub> and  $\varepsilon$ Mr reaches 6.4–7.98 %. The Zr<sub>5</sub> and Zr<sub>10</sub> samples have the highest  $W_{Mout}$  (151.7–188.5 J/cm<sub>3</sub>) and  $\varepsilon_{Mr}$  (7.9–9.7 %), respectively. In summary, the HESMAs have much higher  $W_{Mout}$  and  $\varepsilon_{Mr}$  than the existing TiNi-based memory alloys due to the combination of high strength and large recoverable strain. The reason for the high W<sub>Mout</sub> is that the lattice distortion effect of HEAs increases the strength of the alloy, and the dispersion strengthening effect of nanoprecipitates after aging further increases the critical stress and yield strength, making the HESMAs possess both high strength and large recoverable strain, thus possessing high Wout. Moreover, the load strains in this paper are higher than most of the literature values due to the good plasticity and high yield strength of the HESMAs, which also leads to the possibility of higher  $\varepsilon_r$ . However, it should be noted that the performance of the Zr1 sample is not significantly improved compared with that of Zro, which may be due to the weak lattice distortion caused by the low Zr content, so the solution strengthening effect is also weak. In addition, the performance of the Zr10 alloy decreased compared to that of the Zr5 alloy, possibly due to a decrease in plasticity caused by more secondary phase