Computational Photography

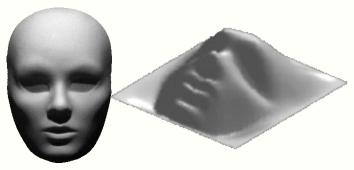
Instructor: Sanjeev J. Koppal

MWF 1145am-1235pm BEN 328

Acknowledgements

Some slides from
Narasimhan (Carnegie Mellon),
Zickler (Harvard),
and
Efros (Berkeley)

Methods Relying on Surface Reflectance



Shape from Shading

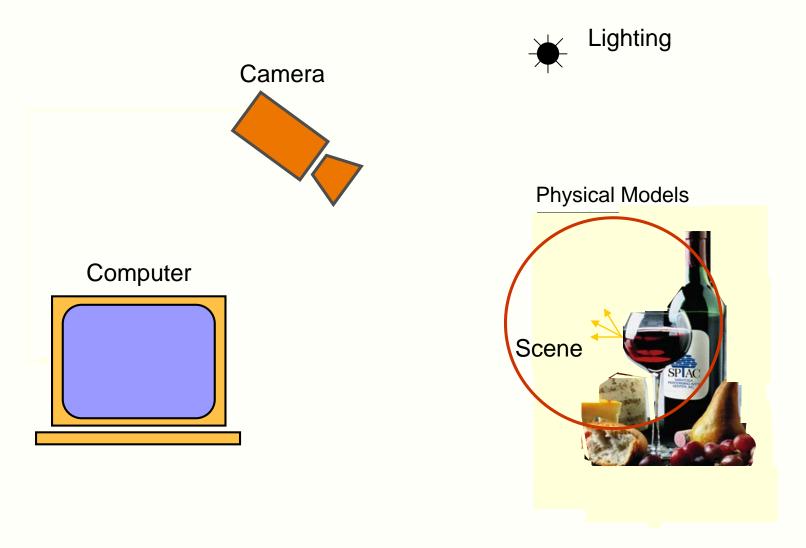


Photometric Stereo



Reflection Separation

Computer Vision: Building Machines that See



We need to understand the relation between the lighting, surface reflectance and medium and the image of the scene.

Surface Appearance

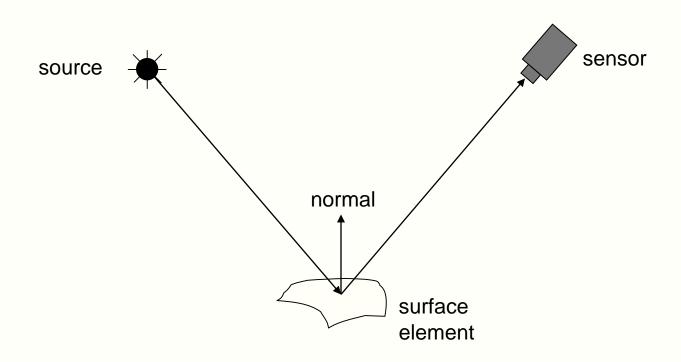
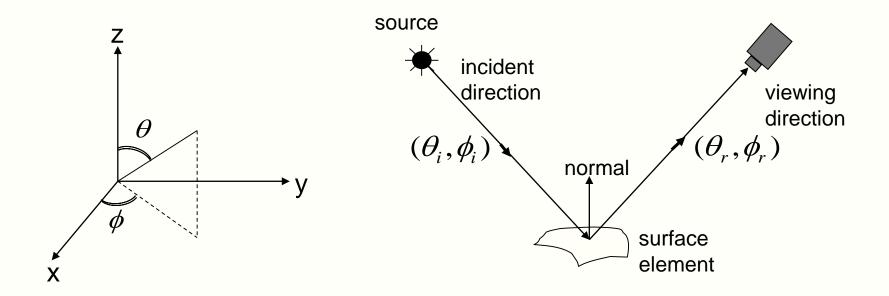


Image intensities = f (normal, surface reflectance, illumination)

Surface Reflection depends on both the viewing and illumination direction.

BRDF: Bidirectional Reflectance Distribution Function



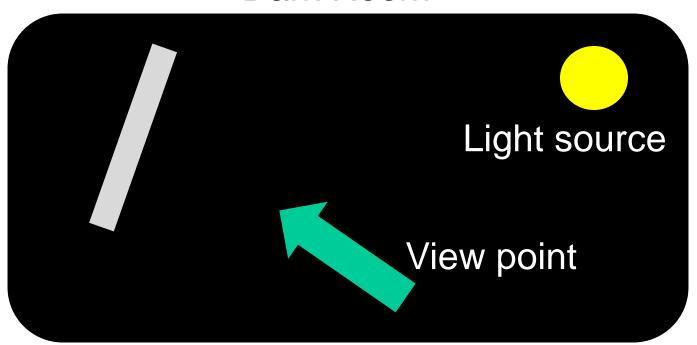
 $E^{surface}(\theta_i, \phi_i)$ Irradiance at Surface in direction (θ_i, ϕ_i)

 $L^{ ext{surface}}(heta_r,\phi_r)$ Radiance of Surface in direction $(heta_r,\phi_r)$

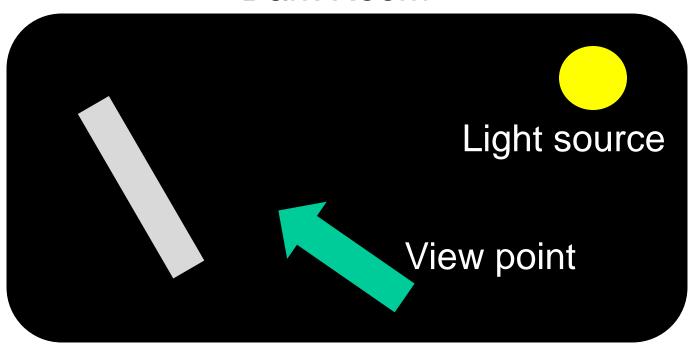
$$\mathsf{BRDF} : f(\theta_i, \phi_i; \theta_r, \phi_r) = \frac{L^{\mathit{surface}}(\theta_r, \phi_r)}{E^{\mathit{surface}}(\theta_i, \phi_i)}$$

What is the BRDF of a mirror?

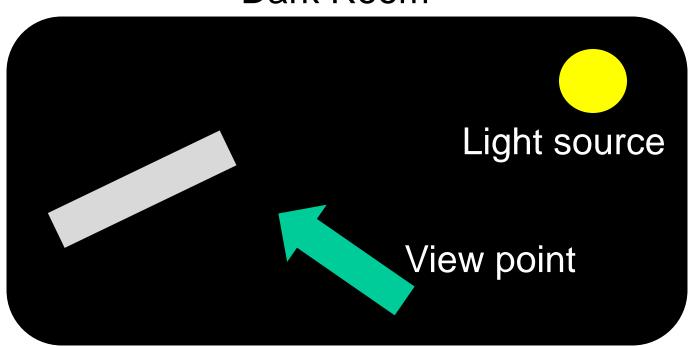
What do we see?



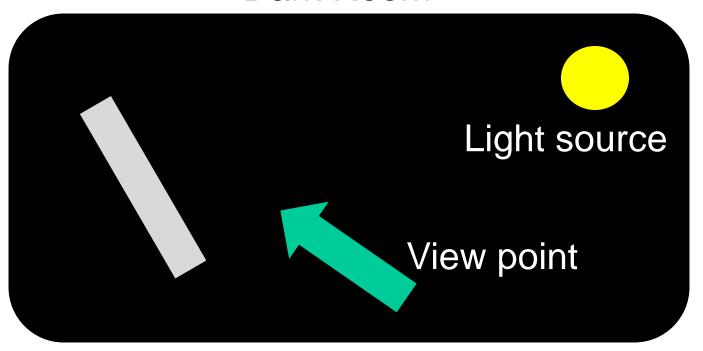
Now?

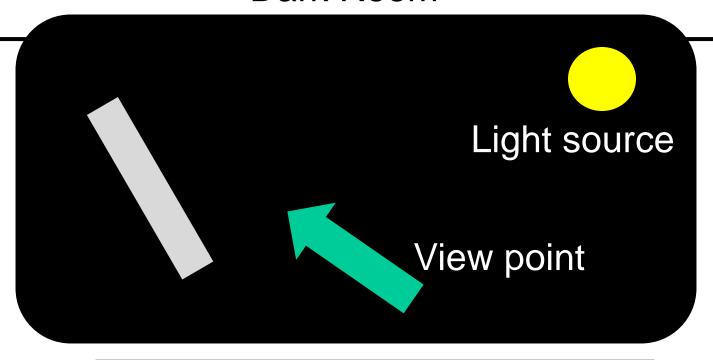


Now?

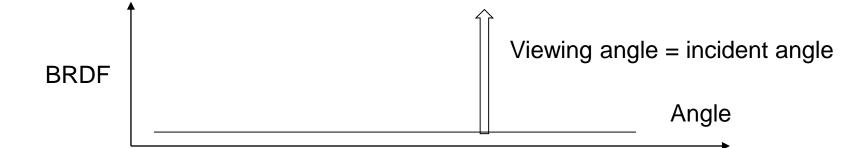


Over angle?

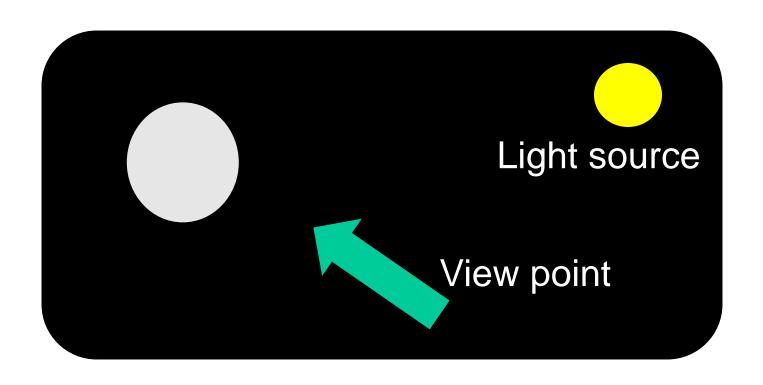




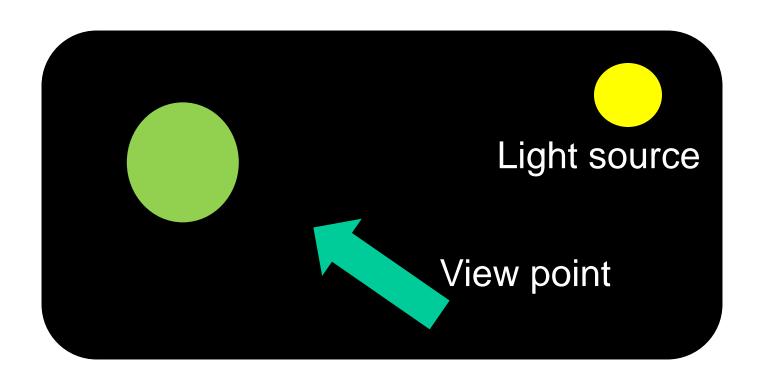
BRDF:
$$f(\theta_i, \phi_i; \theta_r, \phi_r) = \frac{L^{surface}(\theta_r, \phi_r)}{E^{surface}(\theta_i, \phi_i)}$$



The reflectance of a mirror sphere?



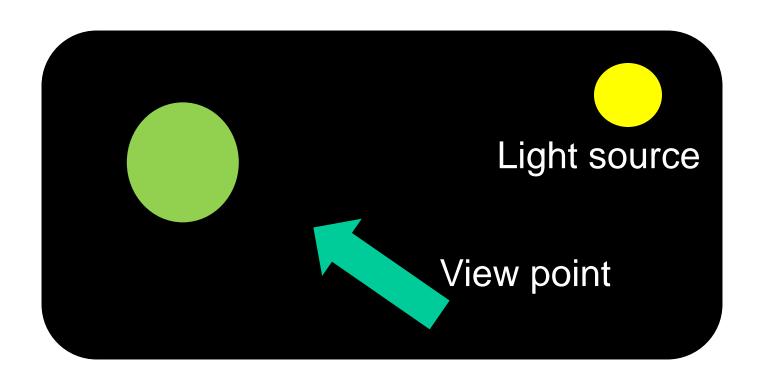
What if I change the color of the sphere?



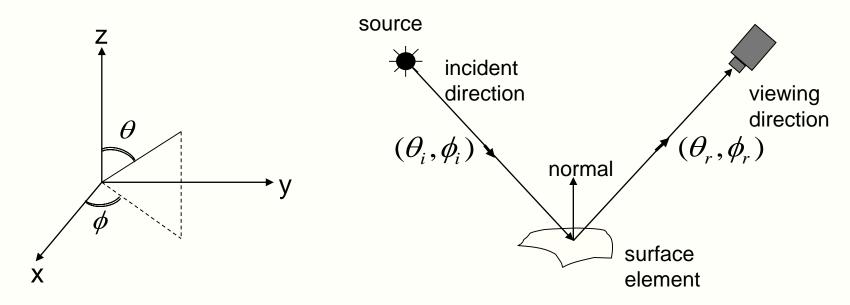
Colored metal



What if I change the color of the sphere?



Important Properties of BRDFs



Rotational Symmetry:

BRDF does not change when surface is rotated about the normal.

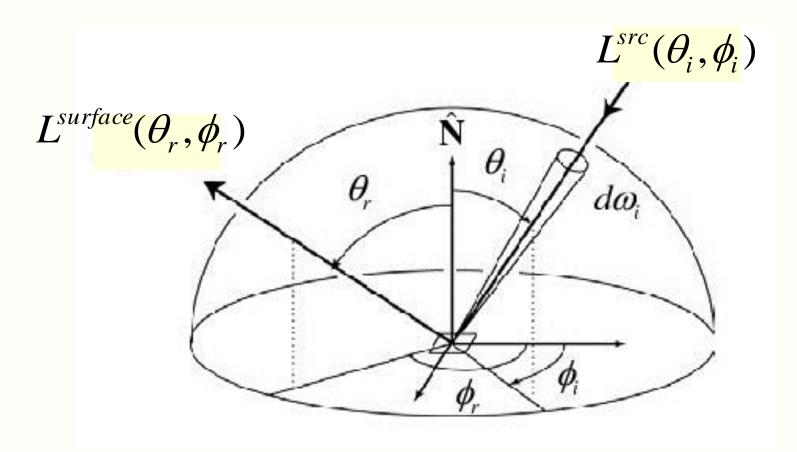
BRDF is only a function of 3 variables : $f(\theta_i, \theta_r, \phi_i - \phi_r)$

Helmholtz Reciprocity: (follows from 2nd Law of Thermodynamics)

BRDF does not change when source and viewing directions are swapped.

$$f(\theta_i, \phi_i; \theta_r, \phi_r) = f(\theta_r, \phi_r; \theta_i, \phi_i)$$

Derivation of the Scene Radiance Equation



From the definition of BRDF:

$$L^{surface}(\theta_r, \phi_r) = E^{surface}(\theta_i, \phi_i) f(\theta_i, \phi_i; \theta_r, \phi_r)$$

Derivation of the Scene Radiance Equation – Important!

From the definition of BRDF:

$$L^{surface}(\theta_r, \phi_r) = E^{surface}(\theta_i, \phi_i) f(\theta_i, \phi_i; \theta_r, \phi_r)$$

Write Surface Irradiance in terms of Source Radiance:

$$L^{surface}(\theta_r, \phi_r) = L^{src}(\theta_i, \phi_i) f(\theta_i, \phi_i; \theta_r, \phi_r) \underline{\cos \theta_i d\omega_i}$$

Why the cosine term?

Foreshortening



Derivation of the Scene Radiance Equation – Important!

From the definition of BRDF:

$$L^{surface}(\theta_r, \phi_r) = E^{surface}(\theta_i, \phi_i) f(\theta_i, \phi_i; \theta_r, \phi_r)$$

Write Surface Irradiance in terms of Source Radiance:

$$L^{surface}(\theta_r, \phi_r) = L^{src}(\theta_i, \phi_i) f(\theta_i, \phi_i; \theta_r, \phi_r) \underline{\cos \theta_i d\omega_i}$$

Integrate over entire hemisphere of possible source directions:

$$L^{surface}(\theta_r, \phi_r) = \int_{2\pi} L^{src}(\theta_i, \phi_i) f(\theta_i, \phi_i; \theta_r, \phi_r) \cos \theta_i \, \underline{d\omega_i}$$

Convert from solid angle to theta-phi representation:

$$L^{surface}(\theta_r, \phi_r) = \int_{-\pi}^{\pi} \int_{0}^{\pi/2} L^{src}(\theta_i, \phi_i) f(\theta_i, \phi_i; \theta_r, \phi_r) \cos \theta_i \sin \theta_i d\theta_i d\phi_i$$

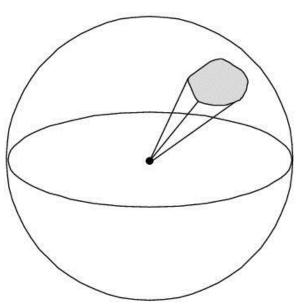
Lesson 1

Reflectance depends on surface normals, and involves lots of angles.

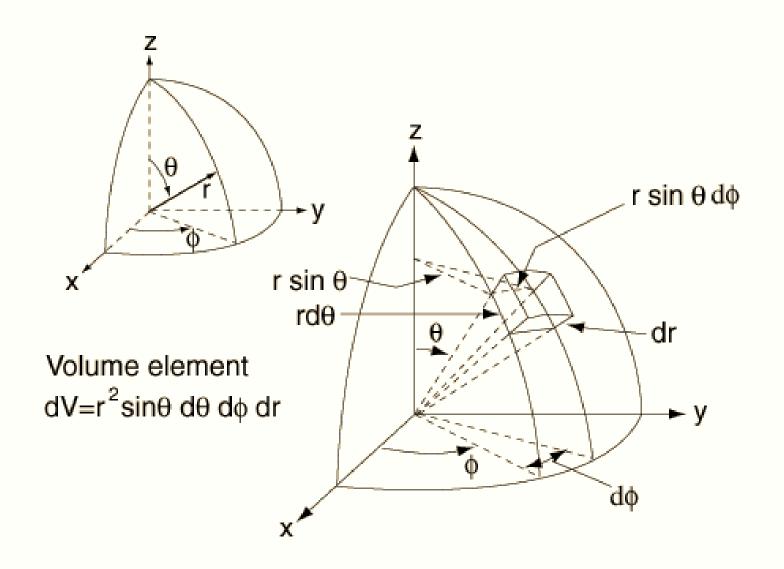
Angles and Solid Angles

- Angle $\theta = \frac{l}{r}$
 - \Rightarrow circle has 2π radians
- Solid angle $\Omega = \frac{A}{R^2}$

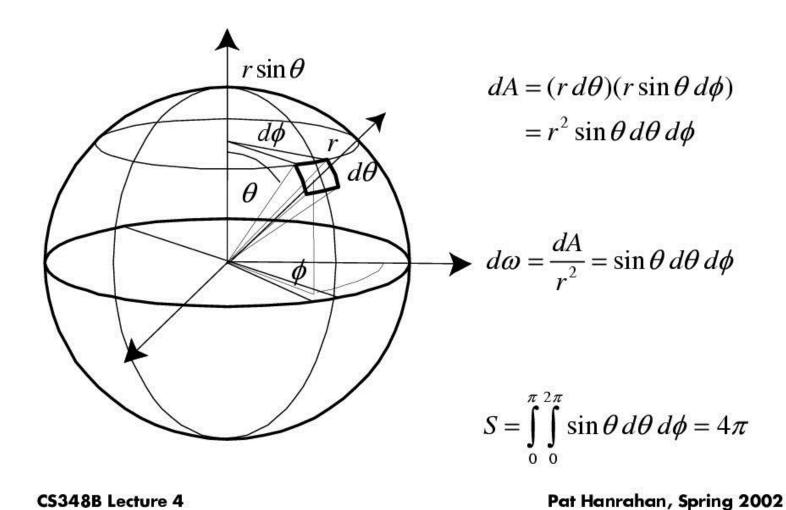
 \Rightarrow sphere has 4π steradians



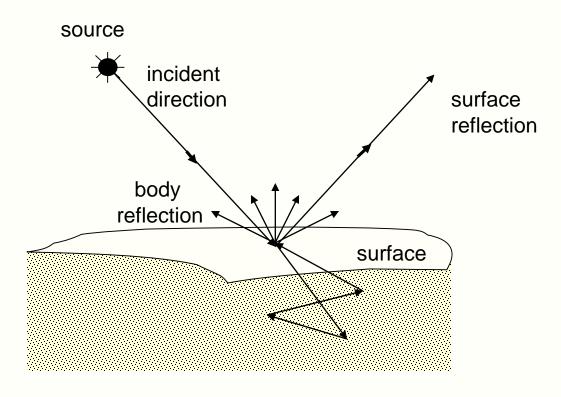
Differential Solid Angle and Spherical Polar Coordinates



Differential Solid Angles



Mechanisms of Reflection



Body Reflection:

Diffuse Reflection
Matte Appearance
Non-Homogeneous Medium
Clay, paper, etc

Surface Reflection:

Specular Reflection Glossy Appearance Highlights Dominant for Metals

Image Intensity = Body Reflection + Surface Reflection

Mechanisms of Surface Reflection

Body Reflection:

Diffuse Reflection
Matte Appearance
Non-Homogeneous Medium
Clay, paper, etc



Many materials exhibit both Reflections:

Surface Reflection:

Specular Reflection Glossy Appearance Highlights Dominant for Metals

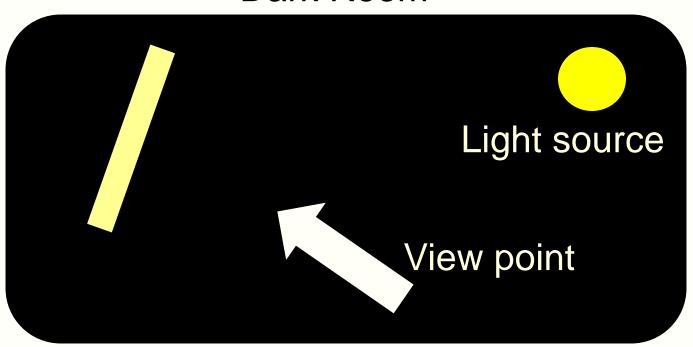




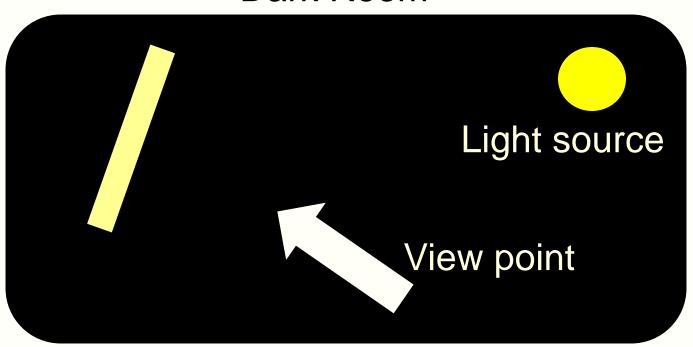


What is the BRDF of a slab of chalk?

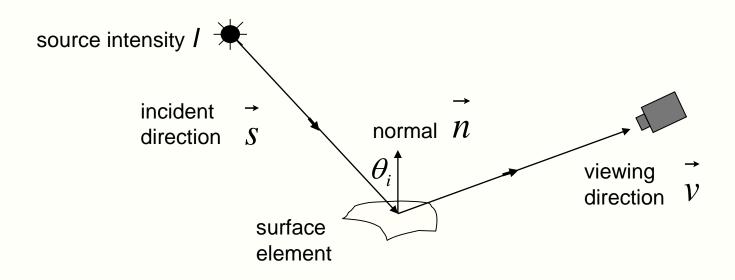
What do we see?



What do we see?

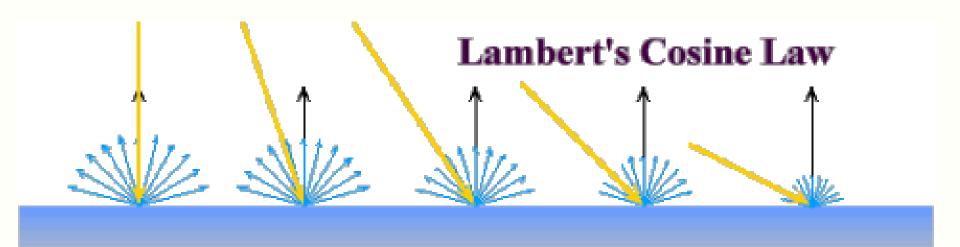


Diffuse Reflection and Lambertian BRDF



- Surface appears equally bright from ALL directions! (independent of $\,v_{i}$
- Lambertian BRDF is simply a constant : $f(\theta_i, \phi_i; \theta_r, \phi_r) = \frac{\rho_d}{\pi}$
- Surface Radiance : $L = \frac{\rho_d}{\pi} I \cos \theta_i = \frac{\rho_d}{\pi} I \dot{n} \dot{s}$ source intensity
- Commonly used in Vision and Graphics!

Diffuse Reflection and Lambertian BRDF



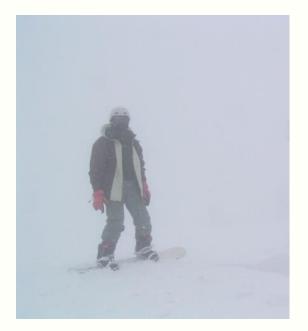
Lesson 2

Diffuse reflectance is easy to compute.

A lot of vision is trying to "filter"

images into a diffuse image.

White-out Conditions from an Overcast Sky





CAN'T perceive the shape of the snow covered terrain!



CAN perceive shape in regions lit by the street lamp!!

Why can we perceive shape in the last picture?

Diffuse Reflection from Uniform Sky

$$L^{surface}(\theta_r, \phi_r) = \int_{-\pi}^{\pi} \int_{0}^{\pi/2} L^{src}(\theta_i, \phi_i) f(\theta_i, \phi_i; \theta_r, \phi_r) \cos \theta_i \sin \theta_i d\theta_i d\phi_i$$

Assume Lambertian Surface with Albedo = 1 (no absorption)

$$f(\theta_i, \phi_i; \theta_r, \phi_r) = \frac{1}{\pi}$$

Assume Sky radiance is constant

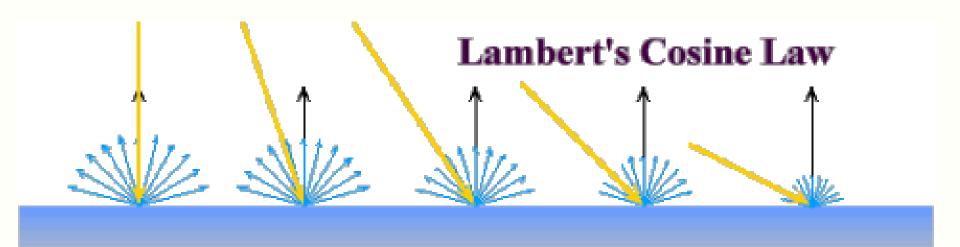
$$L^{src}(\theta_i, \phi_i) = L^{sky}$$

Substituting in above Equation:

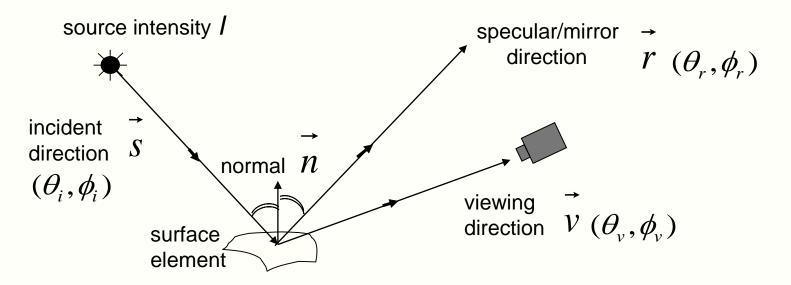
$$L^{surface}(\theta_r,\phi_r) = L^{sky}$$

Radiance of any patch is the same as Sky radiance !! (white-out condition)

Diffuse Reflection and Lambertian BRDF



Specular Reflection and Mirror BRDF

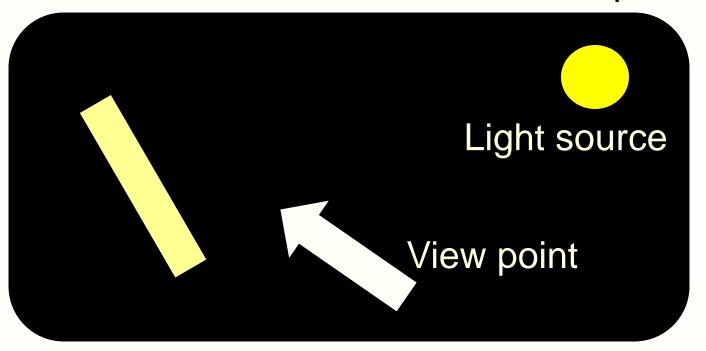


- · Very smooth surface.
- All incident light energy reflected in a SINGLE direction. (only when V=V
- Mirror BRDF is simply a double-delta function :

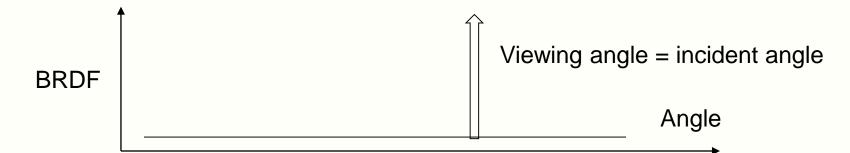
specular albedo
$$f(\theta_i,\phi_i;\theta_v,\phi_v)=\rho_s \ \delta(\theta_i-\theta_v) \ \delta(\phi_i+\pi-\phi_v)$$

• Surface Radiance : $L = I \rho_s \delta(\theta_i - \theta_v) \delta(\phi_i + \pi - \phi_v)$

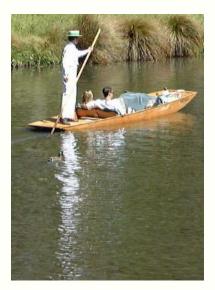
Remember the Dark Room example



$$\mathsf{BRDF} : f(\theta_i, \phi_i; \theta_r, \phi_r) = \frac{L^{\mathit{surface}}(\theta_r, \phi_r)}{E^{\mathit{surface}}(\theta_i, \phi_i)}$$



Specular Reflections in Nature





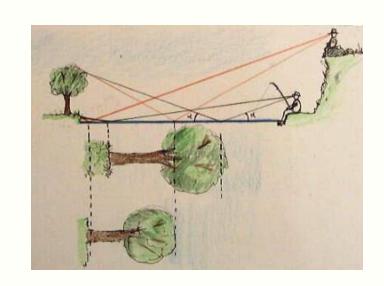




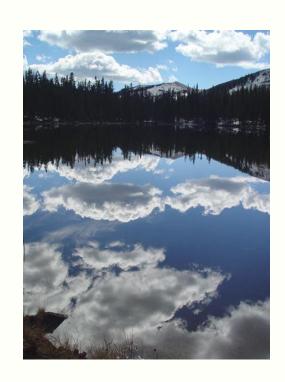
It's surprising how long the reflections are when viewed sitting on the river bank.

Compare sizes of objects and their reflections!

The reflections when seen from a lower view point are always longer than when viewed from a higher view point.



Specular Reflections in Nature



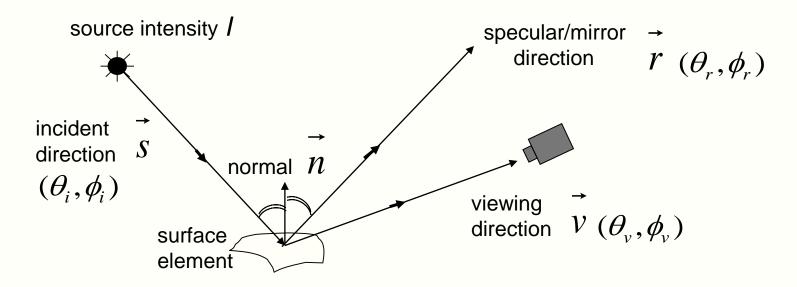


The reflections of bright objects have better perceived contrast.

Intensity of reflected light is a fraction of the direct light – [Fresnel term (derivation in a later class)]

More advanced BRDFs (micro facets)

Specular Reflection and Mirror BRDF - RECAP



- · Very smooth surface.
- All incident light energy reflected in a SINGLE direction. (only when V=V)
- Mirror BRDF is simply a double-delta function :

specular albedo
$$f(\theta_i,\phi_i;\theta_v,\phi_v) = \rho_s \ \delta(\theta_i-\theta_v) \ \delta(\phi_i+\pi-\phi_v)$$

• Surface Radiance : $L = I \rho_s \delta(\theta_i - \theta_v) \delta(\phi_i + \pi - \phi_v)$

Glossy Surfaces

- Delta Function too harsh a BRDF model (valid only for highly polished mirrors and metals).
- Many glossy surfaces show broader highlights in addition to mirror reflection.

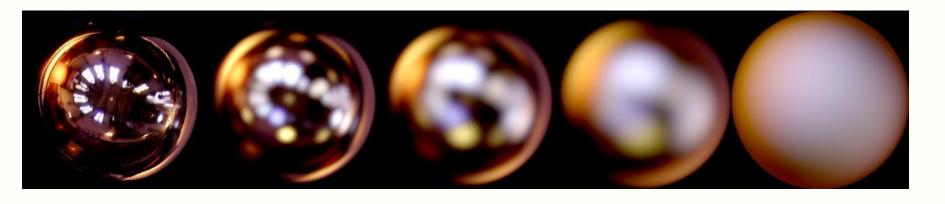




- Surfaces are not perfectly smooth they show micro-surface geometry (roughness).
- Example Models : Phong model

Torrance Sparrow model

Blurred Highlights and Surface Roughness



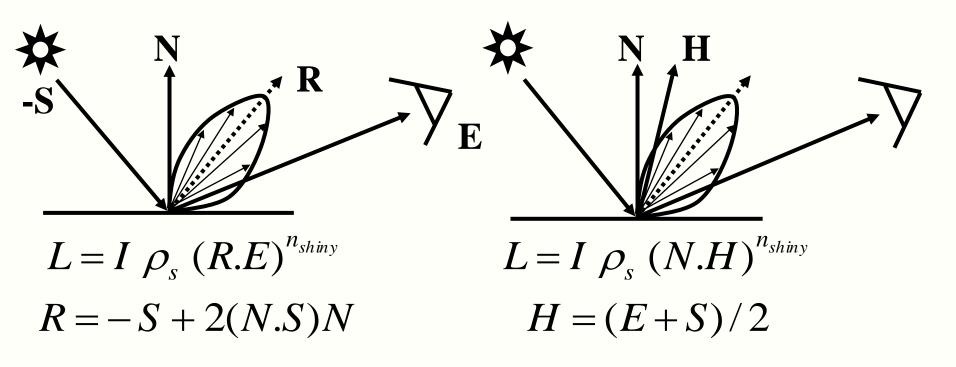
Roughness

Participation

Does this remind you of anything?

Phong Model: An Empirical Approximation

How to model the angular falloff of highlights:



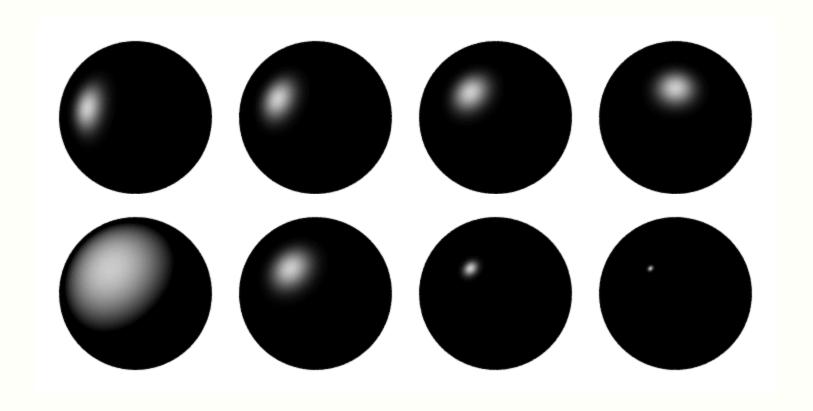
Phong Model

Blinn-Phong Model

- Sort of works, easy to compute
- But not physically based (no energy conservation and reciprocity).
- Very commonly used in computer graphics.

Phong Examples

• These spheres illustrate the Phong model as *lighting direction* and n_{shiny} are varied:



Participation

Why are the spheres so dark?

Those Were the Days

• "In trying to improve the quality of the synthetic images, we do not expect to be able to display the object exactly as it would appear in reality, with texture, overcast shadows, etc. We hope only to display an image that approximates the real object closely enough to provide a certain degree of realism."

– Bui Tuong Phong, 1975

Torrance-Sparrow Model – Main Points

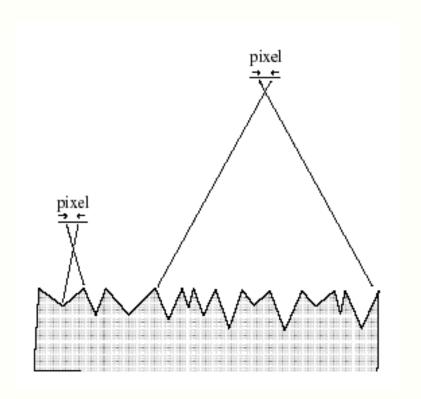
- Physically Based Model for Surface Reflection.
- Based on Geometric Optics.
- Explains off-specular lobe (wider highlights).
- •Works for only rough surfaces.

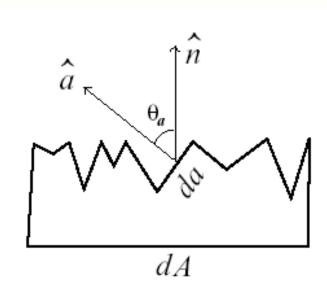
•For very smooth surfaces, electromagnetic nature of light must be used

Beckmann-Spizzichinno model.

Beyond the scope of this course.

Modeling Rough Surfaces - Microfacets





- •Roughness simulated by Symmetric V-groves at Microscopic level.
- •Distribution on the slopes of the V-grove faces are modeled.
- •Each microfacet assumed to behave like a perfect mirror.

Torrance-Sparrow BRDF – Different Factors

Fresnel term: allows for wavelength dependency

Geometric Attenuation: reduces the output based on the amount of shadowing or masking that occurs.

$$f = \frac{F(\theta_i)G(\omega_i, \omega_r)D(\theta_h)}{4\cos(\theta_i)\cos(\theta_r)}$$

How much of the macroscopic surface is visible to the light source

How much of the macroscopic surface is visible to the viewer Distribution:
distribution function
determines what
percentage of
microfacets are
oriented to reflect
in the viewer
direction.

Torrance-Sparrow BRDF – Different Factors

Fresnel term: allows for wavelength dependency Geometric Attenuation: reduces the output based on the amount of shadowing or masking that occurs.

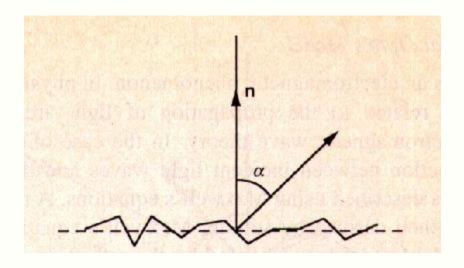
$$f = \frac{F(\theta_i)G(\omega_i, \omega_r)D(\theta_h)}{4\cos(\theta_i)\cos(\theta_r)}$$

How much of the macroscopic surface is visible to the light source

How much of the macroscopic surface is visible to the viewer

Distribution:
distribution function
determines what
percentage of
microfacets are
oriented to reflect
in the viewer
direction.

Slope Distribution Model



- Model the distribution of slopes as Gaussian.
- Mean is Zero, Variance represents ROUGHNESS.

$$\rho_{\alpha}(\alpha) = \frac{1}{\sqrt{2\pi\sigma_{\alpha}}} e^{-\frac{\alpha^2}{2\sigma_{\alpha}^2}}.$$

Torrance-Sparrow BRDF – Different Factors

Fresnel term: allows for wavelength dependency Geometric Attenuation: reduces the output based on the amount of shadowing or masking that occurs.

 $f = \frac{F(\theta_i)G(\omega_i, \omega_r)D(\theta_h)}{4\cos(\theta_i)\cos(\theta_r)}$

How much of the macroscopic surface is visible to the light source

How much of the macroscopic surface is visible to the viewer Distribution:
distribution function
determines what
percentage of
microfacets are
oriented to reflect
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direction.

Fresnel Reflectance

Metal (Aluminum)

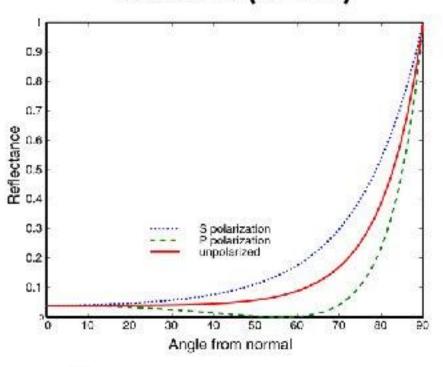
50

Angle from normal

70

80

Dielectric (N=1.5)



Gold F(0)=0.82 Silver F(0)=0.95

30

20

Glass n=1.5 F(0)=0.04 Diamond n=2.4 F(0)=0.15

Schlick Approximation $F(\theta) = F(0) + (1 - F(0))(1 - \cos \theta)^5$

CS348B Lecture 10

10

0.2

0.1

Pat Hanrahan, Spring 2002

Experiment

Reflections from a shiny floor







From Lafortune, Foo, Torrance, Greenberg, SIGGRAPH 97

Lesson 3

The effect of Fresnel reflectance increases greatly at grazing angles.

Torrance-Sparrow BRDF – Different Factors

Fresnel term: allows for wavelength dependency Geometric Attenuation: reduces the output based on the amount of shadowing or masking that occurs.

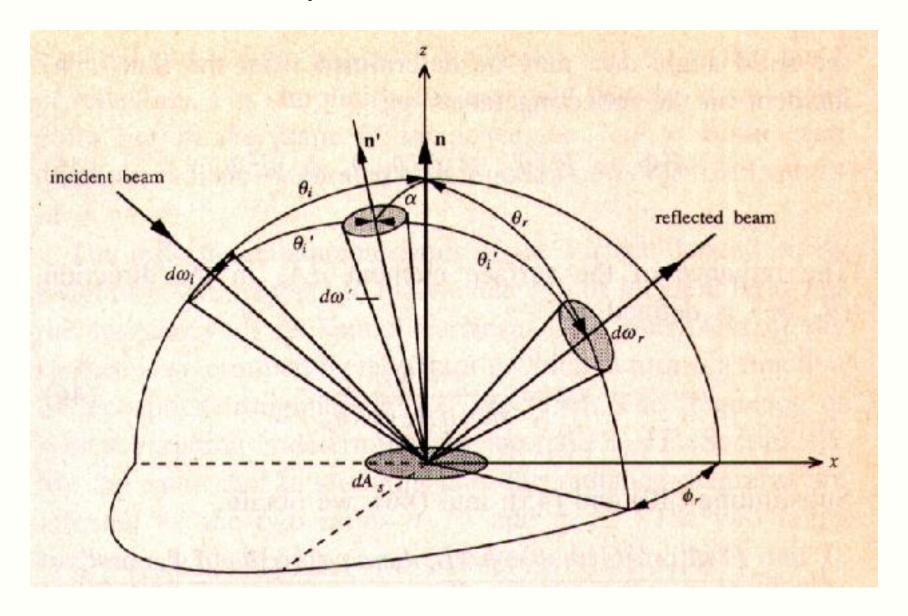
$$f = \frac{F(\theta_i) \mathbf{G}(\omega_i, \omega_r) D(\theta_h)}{4\cos(\theta_i)\cos(\theta_r)}$$

How much of the macroscopic surface is visible to the light source

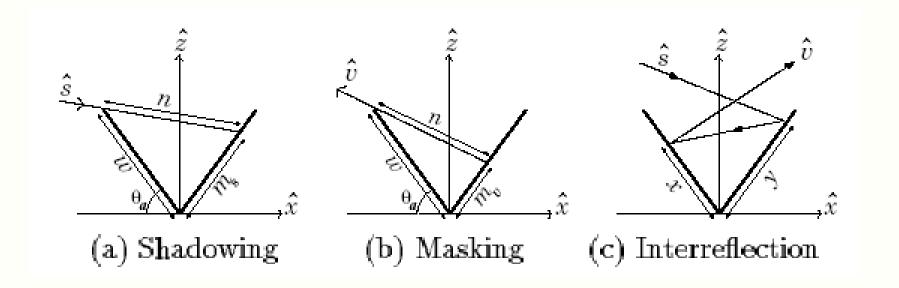
How much of the macroscopic surface is visible to the viewer

Distribution:
distribution function
determines what
percentage of
microfacets are
oriented to reflect
in the viewer
direction.

Coordinate System needed to derive T-S model



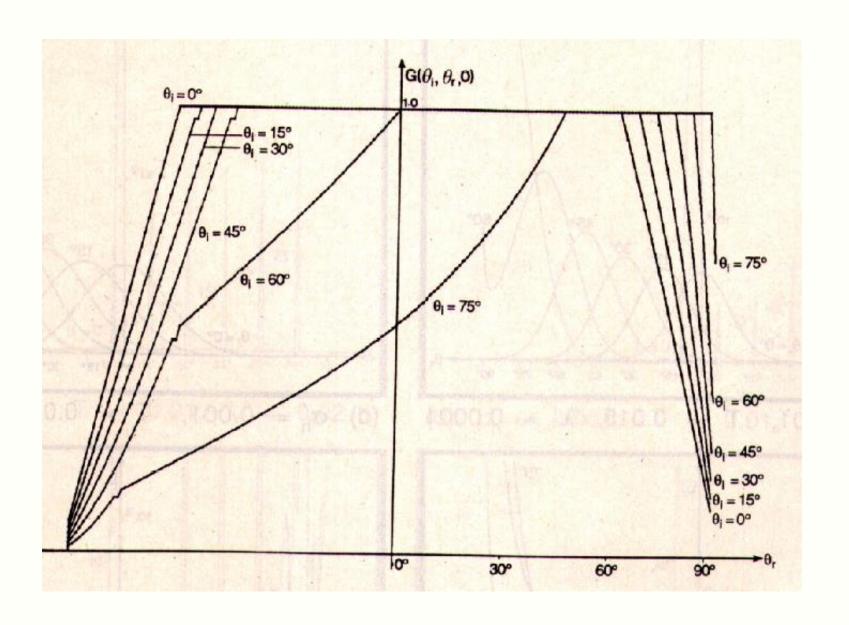
Geometric Attenuation Factor



$$G(\theta_i, \theta_r, \phi_r) = \min \left(1, \frac{2\cos\alpha\cos\theta_r}{\cos\theta_i'}, \frac{2\cos\alpha\cos\theta_i}{\cos\theta_i'} \right).$$

- No interreflections taken into account in above function.
- Derivation found in 1967 JOSA paper (read if interested).

Geometric Attenuation Factor



Torrance Sparrow Model - Final Expression

$$L_r = \kappa_{\rm spec} \frac{L_i d\omega_i}{\cos \theta_r} e^{-\frac{\alpha^2}{2\sigma_{\alpha}^2}}$$

$$\kappa_{\text{spec}} = \frac{ca_f F'(\theta_i', \eta') G(\theta_i, \theta_r, \phi_r)}{4}.$$

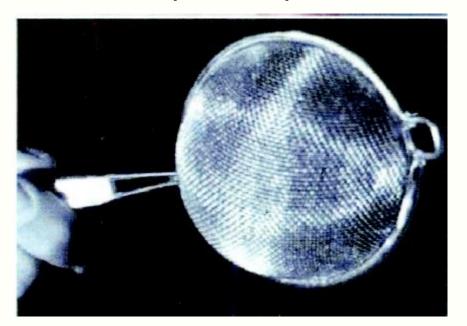
Reflections on water surfaces - Glittering

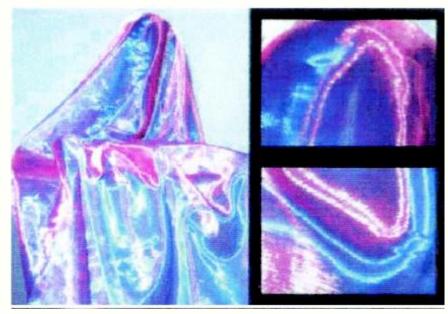






Split off-specular Reflections in Woven Surfaces



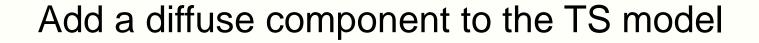




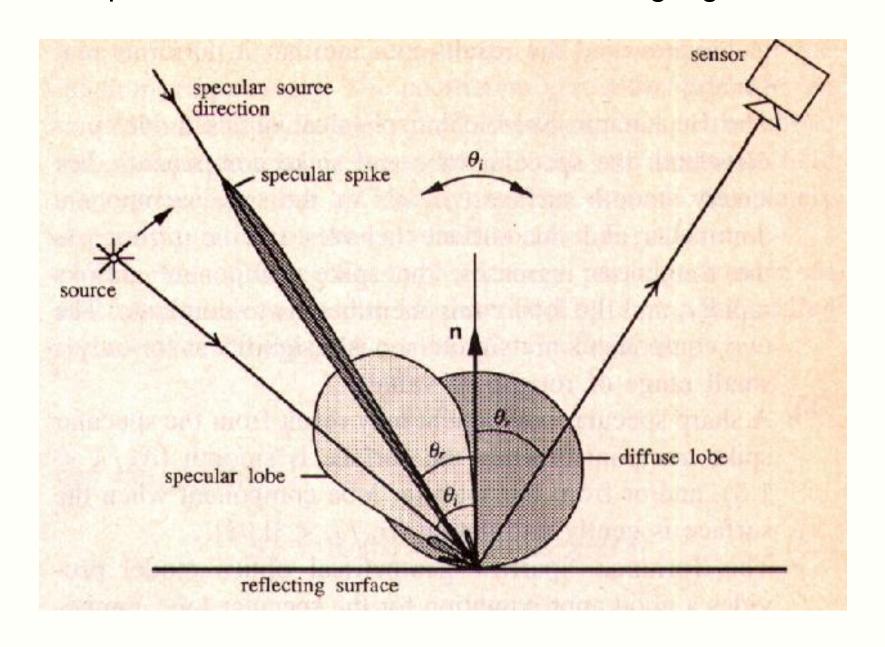
Lesson 4

Many scenes do not have diffuse reflectance and cannot be easily made diffuse.

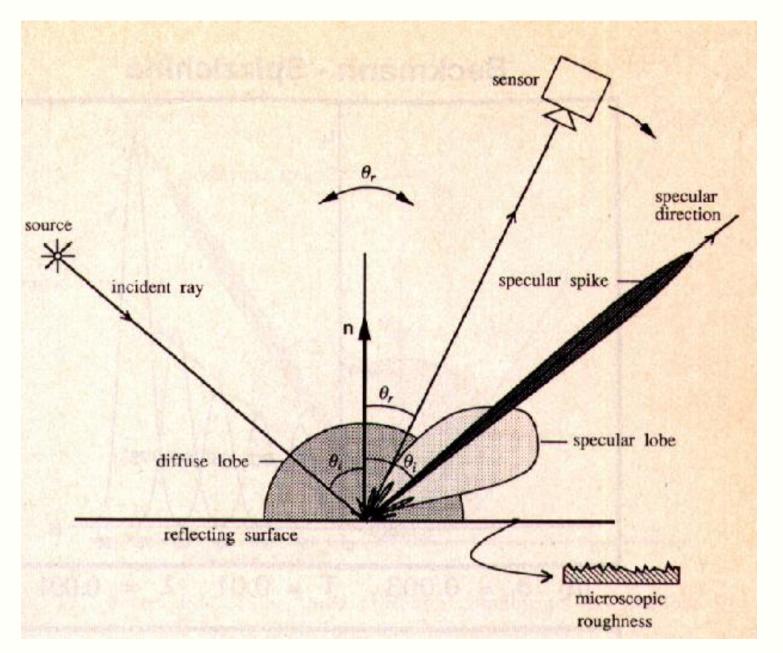
So we need to do more work.



Components of Surface Reflection – Moving Light Source



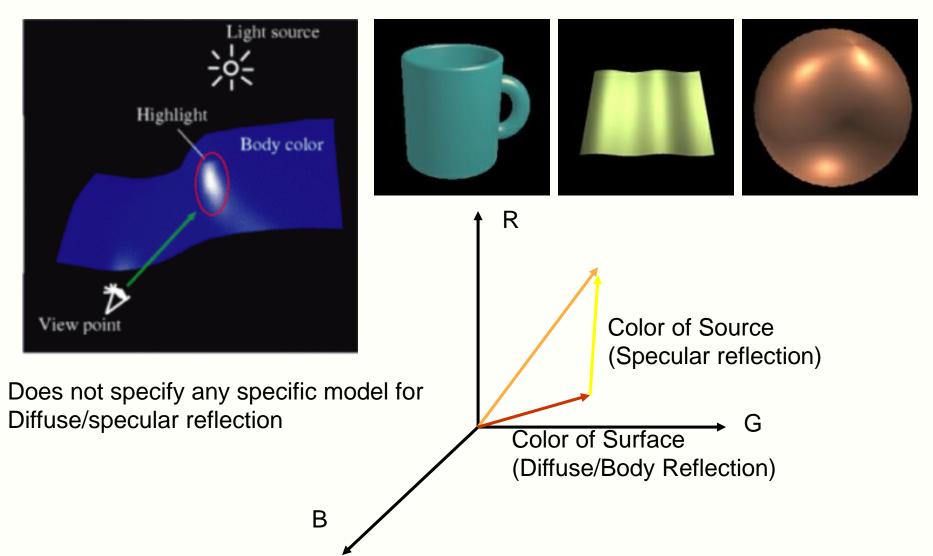
Components of Surface Reflection – Moving Camera



A Simple Reflection Model - Dichromatic Reflection

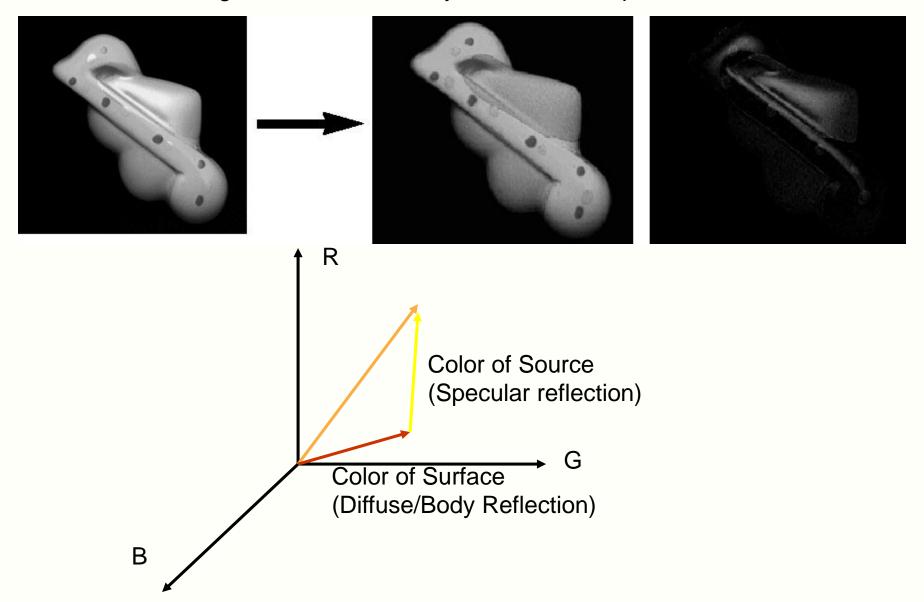
Observed Image Color = $a \times Body Color + b \times Specular Reflection Color$

Klinker-Shafer-Kanade 1988



Separating Diffuse and Specular Reflections

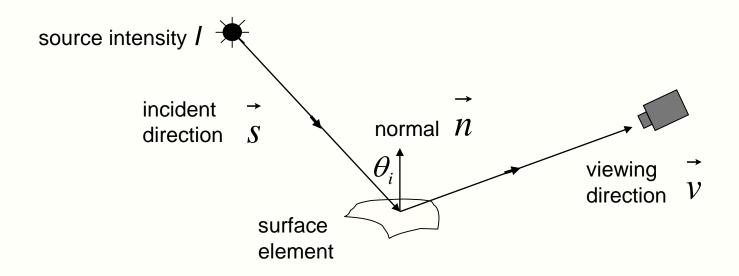
Observed Image Color = $a \times Body Color + b \times Specular Reflection Color$



We looked at rough specular things, and we added diffuse stuff to them.

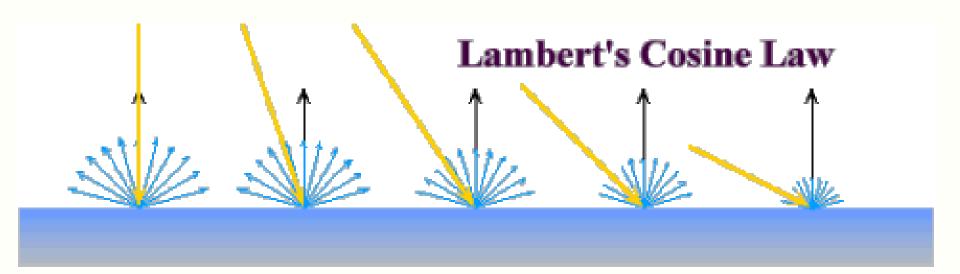
What about rough diffuse things?

Diffuse Reflection and Lambertian BRDF - Recap



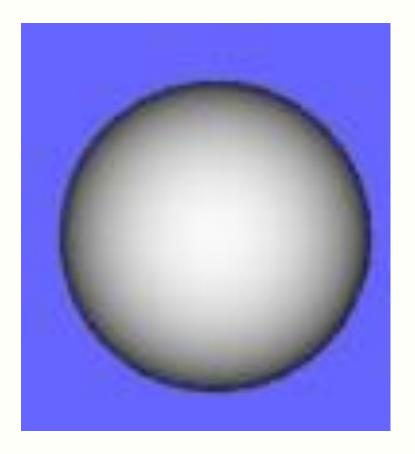
- Surface appears equally bright from ALL directions! (independent of $\,v_{i}$
- Lambertian BRDF is simply a constant : $f(\theta_i, \phi_i; \theta_r, \phi_r) = \frac{\rho_d}{\pi}$
- Surface Radiance : $L = \frac{\rho_d}{\pi} I \cos \theta_i = \frac{\rho_d}{\pi} I \dot{n} \dot{s}$ source intensity
- Commonly used in Vision and Graphics!

Diffuse Reflection and Lambertian BRDF - Recap



Radiance decreases with increase in angle between surface normal and source

Rendered Sphere with Lambertian BRDF



- Edges are dark (N.S = 0) when lit head-on
- See shading effects clearly.

Why does the Full Moon have a flat appearance?



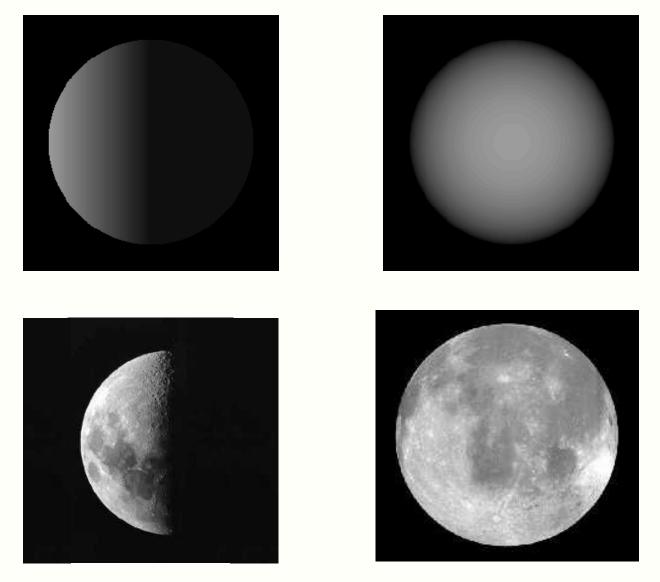


- The moon appears matte (or diffuse)
- But still, edges of the moon look bright (not close to zero) when illuminated by earth's radiance.



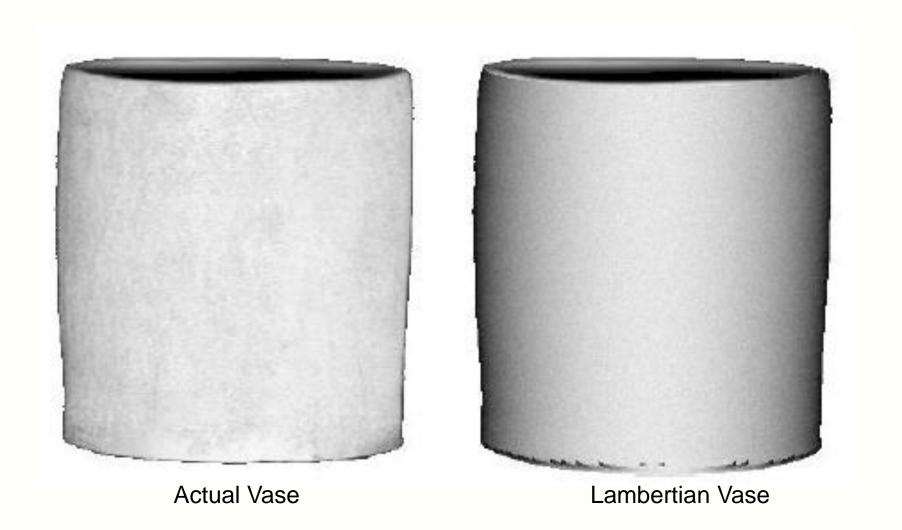


Why does the Full Moon have a flat appearance?

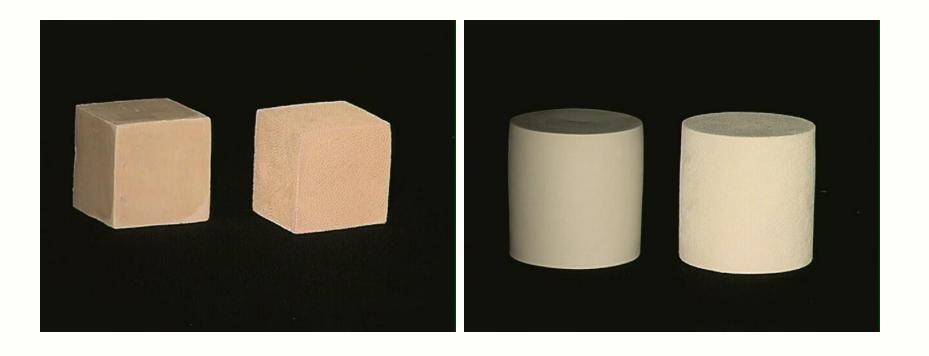


Lambertian Spheres and Moon Photos illuminated similarly

Surface Roughness Causes Flat Appearance



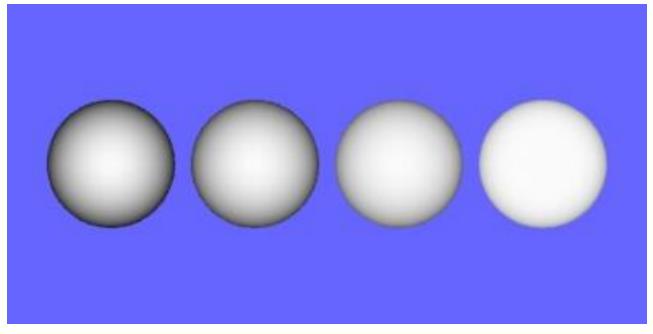
Surface Roughness Causes Flat Appearance – More Examples



Lesson 5

Local reflectance properties can create surprising global effects.

Surface Roughness Causes Flat Appearance



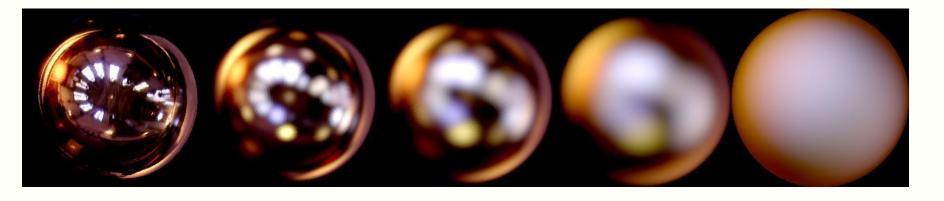
Increasing surface roughness

Lambertian model

Valid for only SMOOTH MATTE surfaces.

Bad for ROUGH MATTE surfaces.

Blurred Highlights and Surface Roughness - RECAP

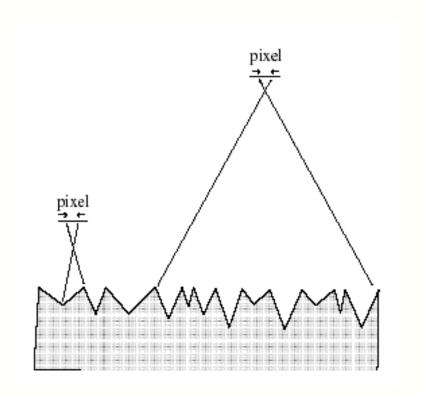


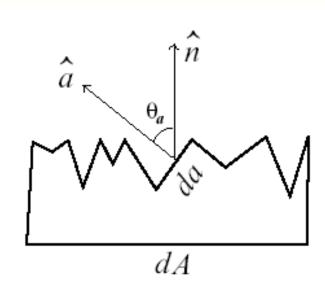
Roughness

Oren-Nayar Model – Main Points

- Physically Based Model for Diffuse Reflection.
- Based on Geometric Optics.
- •Explains view dependent appearance in Matte Surfaces
- Take into account partial interreflections.
- Roughness represented like in Torrance-Sparrow Model
- •Lambertian model is simply an extreme case with roughness equal to zero.

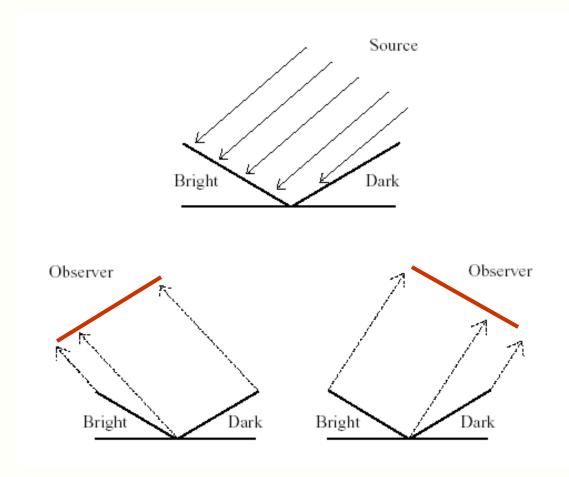
Modeling Rough Surfaces - Microfacets





- •Roughness simulated by Symmetric V-groves at Microscopic level.
- •Distribution on the slopes of the V-grove faces are modeled.
- •Each microfacet assumed to behave like a perfect lambertian surface.

View Dependence of Matte Surfaces - Key Observation



- Overall brightness increases as the angle between the source and viewing direction decreases. WHY?
- Pixels have finite areas. As the viewing direction changes, different mixes between dark and bright are added up to give pixel brightness.

Torrance-Sparrow BRDF – Different Factors (RECAP)

Fresnel term: allows for wavelength dependency

Geometric Attenuation: reduces the output based on the amount of shadowing or masking that occurs.

$$f = \frac{F(\theta_i)G(\omega_i, \omega_r)D(\theta_h)}{4\cos(\theta_i)\cos(\theta_r)}$$

How much of the macroscopic surface is visible to the light source

How much of the macroscopic surface is visible to the viewer

Distribution:
distribution function
determines what
percentage of
microfacets are
oriented to reflect
in the viewer
direction.

Fresnel term: allows for wavelength dependency Geometric Attenuation: reduces the output based on the amount of shadowing or masking that occurs.

$$f = \frac{F(\theta_i)G(\omega_i, \omega_r)D(\theta_h)}{4\cos(\theta_i)\cos(\theta_r)}$$

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How much of the macroscopic surface is visible to the light source

How much of the macroscopic surface is visible to the viewer Distribution:
distribution function
determines what
fraction of the
surface area do the
facets of the same
orientation cover?

Fresnel term: allows for wavelength dependency

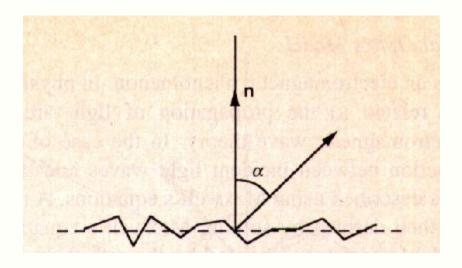
Geometric Attenuation: reduces the output based on the amount of shadowing or masking that occurs.

$$f = \frac{F(\theta_i)G(\omega_i, \omega_r)D(\theta_h)}{4\cos(\theta_i)\cos(\theta_r)}$$

How much of the macroscopic surface is visible to the light source

How much of the macroscopic surface is visible to the viewer Distribution:
distribution function
determines what
fraction of the
surface area do the
facets of the same
orientation cover?

Slope Distribution Model



- Model the distribution of slopes as Gaussian.
- Mean is Zero, Variance represents ROUGHNESS.

$$\rho_{\alpha}(\alpha) = \frac{1}{\sqrt{2\pi\sigma_{\alpha}}} e^{-\frac{\alpha^2}{2\sigma_{\alpha}^2}}.$$

Fresnel term: allows for wavelength dependency

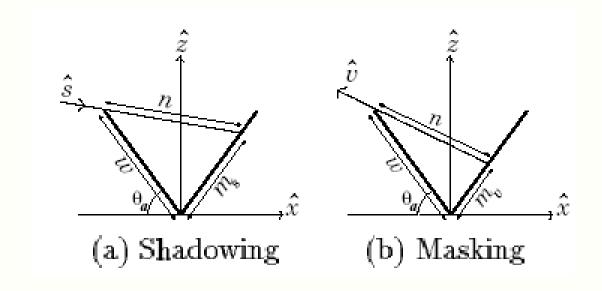
Geometric Attenuation: reduces the output based on the amount of shadowing or masking that occurs.

$$f = \frac{F(\theta_i)G(\omega_i, \omega_r)D(\theta_h)}{4\cos(\theta_i)\cos(\theta_r)}$$

How much of the macroscopic surface is visible to the light source

How much of the macroscopic surface is visible to the viewer Distribution:
distribution function
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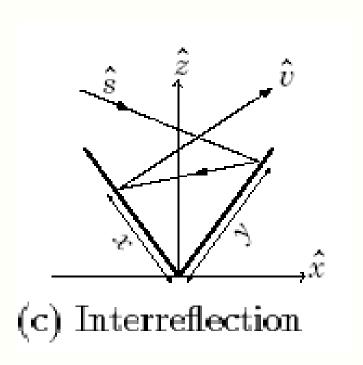
TS Geometric Attenuation Factor - RECAP



$$G(\theta_i, \theta_r, \phi_r) = \min \biggl(1, \, \frac{2\cos\alpha\cos\theta_r}{\cos\theta_i'}, \, \frac{2\cos\alpha\cos\theta_i}{\cos\theta_i'} \biggr).$$

- No interreflections taken into account in above function.
- Derivation found in 1967 JOSA paper (read if interested).

Oren-Nayar Model – Different Factors (contd.)



- Take into account two light bounces (reflections).
- Hard to solve analytically, so they find a functional approximation.

Oren-Nayar Model – Final Expression

$$L(\theta_r, \theta_i, \phi_r - \phi_i; \rho, \sigma) = \frac{\rho}{\pi} E_0 \cos \theta_i (A + BMax \left[0, \cos (\phi_r - \phi_i) \right] \sin \alpha \tan \beta),$$

$$A = 1.0 - 0.5 \frac{\sigma^2}{\sigma^2 + 0.33}, \qquad \alpha = Max(\theta_r, \theta_i)$$

$$B = 0.45 \frac{\sigma^2}{\sigma^2 + 0.09}, \qquad \beta = Min(\theta_r, \theta_i).$$

Lambertian model is simply an extreme case with roughness equal to zero.

Comparison to Ground Truth

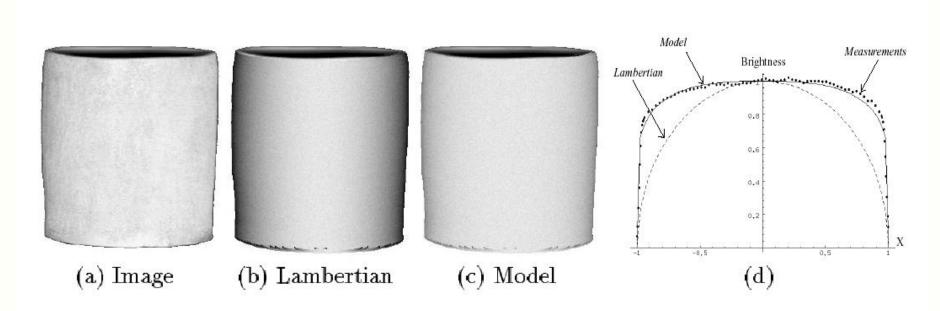
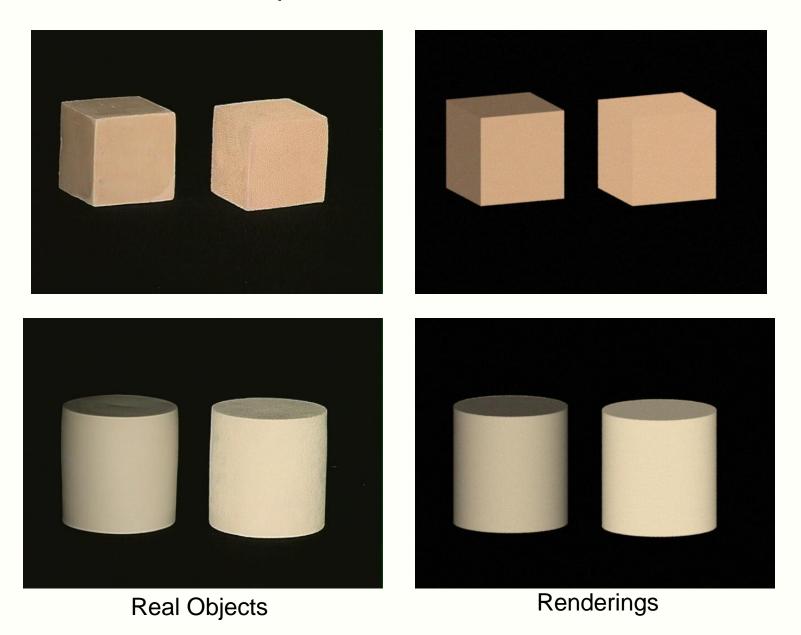
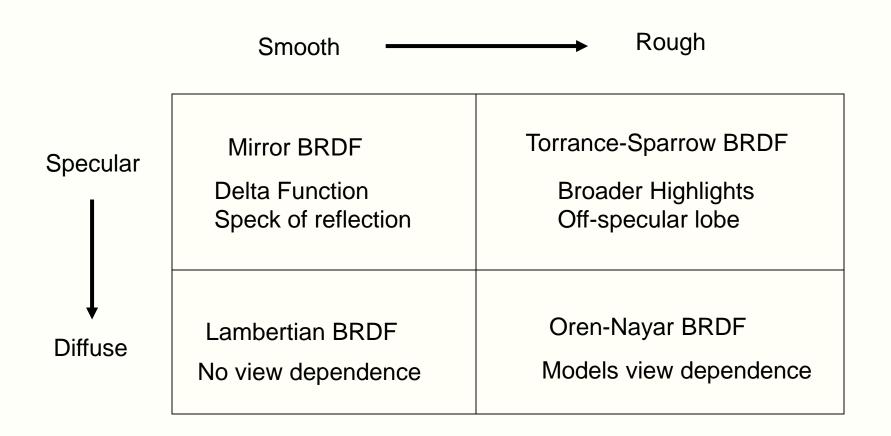


Fig. 7. (a-c) Real image of a cylindrical clay vase compared with images rendered using the Lambertian and proposed models. Illumination is from the direction $\theta_i = 0^{\circ}$. (d) Comparison between image brightness along the cross-sections of the three vases.

Comparison to Ground Truth

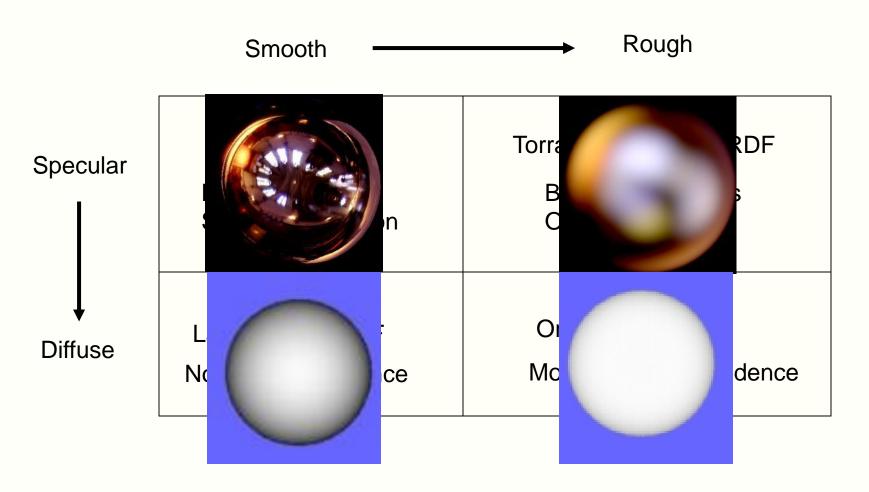


Summary of Surfaces and BRDFs



Many surfaces may be rough and show both diffuse and surface reflection.

Summary of Surfaces and BRDFs



Many surfaces may be rough and show both diffuse and surface reflection.

Thank you

Lesson summary:

- 1. Reflectance depends on surface normals, and involves lots of angles.
- 2. Diffuse reflectance is easy to compute.
 A lot of vision is trying to "filter" images into a diffuse image.
- 3. The effect of Fresnel reflectance increases greatly at grazing angles.
- 4. Many scenes do not have diffuse reflectance and cannot be easily made diffuse. So algorithms need to model the reflectance.
- 5. Local reflectance properties can create surprising global effects.