

*A Pathfinding Algorithm Report**

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Introduction:

Pathfinding is a crucial technique in computer science, widely used in robotics, video games, and AI applications. The *A (A-Star) Algorithm** is a popular pathfinding algorithm that finds the shortest path from a start node to a goal node efficiently by combining **Dijkstra's algorithm** and **Greedy Best-First Search**.

This report presents the implementation of the A* algorithm on a grid-based environment to compute the shortest path. The algorithm considers both the actual movement cost and an estimated heuristic cost to reach the goal, ensuring optimal performance.

Methodology:

1. Grid Representation:

- The environment is represented as a **2D grid**, where each cell is a node.
- Nodes can be **walkable (white)** or **obstacles (black)**.

2. A Algorithm Working:*

- Each node maintains three costs:
 - **$g(n)$** : Cost from the start node to the current node.
 - **$h(n)$** : Estimated heuristic cost from current node to goal.
 - **$f(n) = g(n) + h(n)$** : Total estimated cost.
- A **priority queue (min-heap)** is used to expand the node with the lowest cost.
- The **Manhattan Distance** heuristic is used:
$$h(n) = |x_1 - x_2| + |y_1 - y_2|$$
$$h(n) = |x_1 - x_2| + |y_1 - y_2|$$

- The algorithm terminates when the goal node is reached, and the shortest path is reconstructed.

Code:

```
import heapq
```

```
# Define the grid size
```

```
ROWS, COLS = 5, 5
```

```
# Directions for moving: right, left, down, up
```

```
DIRECTIONS = [(0, 1), (0, -1), (1, 0), (-1, 0)]
```

```
class Node:
```

```
    def __init__(self, row, col):
```

```
        self.row, self.col = row, col
```

```
        self.g = float("inf") # Cost from start to current  
node
```

```
        self.h = 0 # Heuristic cost to goal
```

```
        self.f = float("inf") # Total cost
```

```
self.parent = None # Parent node for path tracking
```

```
def __lt__(self, other):  
    return self.f < other.f # Comparison for priority queue
```

```
def heuristic(a, b):  
    """ Manhattan Distance heuristic """  
    return abs(a.row- b.row) + abs(a.col- b.col)
```

```
def a_star(grid, start, goal):  
    open_set = []  
    heapq.heappush(open_set, (0, start)) # Push start node  
    start.g, start.h, start.f = 0, heuristic(start, goal),  
    heuristic(start, goal)
```

```
while open_set:  
    current = heapq.heappop(open_set)[1]
```

```

# Goal reached
if current == goal:
    path = []
    while current:
        path.append((current.row, current.col))
        current = current.parent
    return path[::-1] # Reverse path

# Check neighbors
for dr, dc in DIRECTIONS:
    r, c = current.row + dr, current.col + dc
    if 0 <= r < ROWS and 0 <= c < COLS: # Within
bounds
        neighbor = grid[r][c]
        temp_g = current.g + 1

        if temp_g < neighbor.g: # Found a better
path

```

```
        neighbor.g, neighbor.h = temp_g,  
        heuristic(neighbor, goal)  
        neighbor.f = neighbor.g + neighbor.h  
        neighbor.parent = current  
        heapq.heappush(open_set, (neighbor.f,  
neighbor))
```

```
    return None # No path found
```

```
# Create grid
```

```
grid = [[Node(r, c) for c in range(COLS)] for r in  
range(ROWS)]
```

```
start, goal = grid[0][0], grid[ROWS- 1][COLS- 1]
```

```
# Run A* Algorithm
```

```
path = a_star(grid, start, goal)
```

```
# Print the path
```

```
if path:
```

```
print("Path found:", path)
else:
    print("No path found")
```

Result :

The program finds the shortest path from the start position (0,0) to the goal (4,4). Below is an example output of the execution:

Path found: [(0, 0), (1, 0), (2, 0), (3, 0), (4, 0), (4, 1), (4, 2), (4, 3), (4, 4)]

References/Credits:

1. A* Algorithm:

https://en.wikipedia.org/wiki/A*_search_algorithm

2. Python Heapq (Priority Queue):

<https://docs.python.org/3/library/heapq.html>

3. Artificial Intelligence: A Modern Approach by
Stuart Russell & Peter Norvig

Conclusion:

The A* algorithm efficiently finds the shortest path in a grid environment. By balancing cost and heuristic estimation, it ensures an optimal and fast solution. This implementation can be extended to handle obstacles, larger grids, and real-world applications such as game development and robotics.