

ASSIGNMENT (INNOVATIVE METHOD)

Group No. : 4

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Subject : PAI

Aim : Write a Program to implement A* algorithm for 8 puzzle problem.

Theory:

1) Problem Formulation

1.1 Introduction

8-puzzle

It is 3x3 matrix with 8 square blocks containing 1 to 8 and a blank square. The main idea of 8 puzzle is to reorder these squares into a numerical order of 1 to 8 and last square as blank. Each of the squares adjacent to blank block can move up, down, left or right depending on the edges of the matrix.

1 3	=>	1 3	=>	1 2 3	=>	1 2 3	=>	1 2 3
4 2 5		4 2 5		4 5		4 5		4 5 6
7 8 6		7 8 6		7 8 6		7 8 6		7 8
initial								goal

A*

The project is about solving 8-puzzle using A* search algorithm. A* is a recursive algorithm which finds the shortest path to the goal state. In this algorithm we consider two heuristic functions, misplaced tiles heuristic and manhattan distance heuristic. Misplaced tiles heuristic measures the number of tiles of the current state as compared to the goal state. Manhattan distance heuristic function measures the least steps needed for each of the tiles in the current state to arrive to the goal state position. In this project we will implement the space generation using both the heuristics.



We are also calculating $g(n)$ which is a measure of step cost for each move made from current state to next state, initially it is set to zero. For each of the heuristic we have implemented $f(n) = g(n) + h(n)$, where $g(n)$ is step cost and $h(n)$ is the heuristic function used. Each of the states is explored using priority queue, which stores the position and $f(n)$ value as key value pair. Then using merge sort technique priority queue is sorted and the next node to be explored is selected based on the least $f(n)$ value.

In this project, we have used the optimality of A* by not allowing any node generation of previously traversed nodes. We have used two sets they are closed set and open set to implement this functionality of A* algorithm. Closed set stores all the previously expanded nodes and open set (priority queue in source code) which stores all of the non-duplicate nodes and sorts them according to $f(n)$ value.

The reason for this project to be unique is the functionality it offers to user to enter initial state and goal state, thus offering the generalized solution for any initial state against any goal state. The program comes to an end if the A* algorithm has not found an optimal path within a runtime limit of two minutes.

2. Program structure

2.1 Global variables

Variable name	Variable type
puzzle	Integer list (user input for initial state from [0-8])
goal	Integer list (user input for goal state from [0-8])
bestpath	Integer list of state space after every optimal move
visit	Integer value containing total number of explored nodes
totalmoves	Integer value that holds the total number of moves made to reach the solution

2.2 Functions and Procedures



Description
<p>This function solves the 8-puzzle problem using manhattan heuristic.</p> <p>In this function $g(n)$, $h(n)$ and $f(n)$ is calculated and a priority queue is used to store the node $f(n)$ and position value as key value pair. We use the merge sort technique to find the least cost node and explore that node first if it hasn't already been explored.</p> <p>We call <code>all()</code> to check for repeats. We call the <code>manhattan()</code> to compute the manhattan distance. We identify the blank tile and then check for the next available steps. Then generate the new nodes and check if this new node is the goal state or not.</p> <p>Here, $f(n) = g(n) + h(n)$</p> <p>$h(n)$ calculates the sum of number of steps each tile in the current state needs to take to reach to goal state.</p> <p>$g(n)$ is the step cost of each step made.</p>

coordinates(<value>)	This function assigns integer value as coordinates to any input that has been passed as the parameter and returns the single integer value of the coordinates.
manhattan(initial, goal)	This function calculates the mahanttan distance of each element in the initial matrix by calculating the optimal moves each element should do to reach the position as mentioned in the goal state.
all()	This function uses set method in python to check if the current state is a duplicate of any other state that has been traversed in past or not and returns 1 if it is true and 0 if it is not.
misplaced_tiles()	This function takes current and goal state as input and returns the count of number of misplaced tiles. If there are no misplaced tiles then zero is returned.
evaluate_misplaced()	<p>This function solves the 8-puzzle problem using Misplaced Tiles heuristic.</p> <p>In this function $g(n)$, $h(n)$ and $f(n)$ is calculated and a priority queue is used to store the node fn and position value as key value pair.</p> <p>We use the merge sort technique to find the least cost node and explore that node first if it hasn't already been explored.</p> <p>We call <code>all()</code> to check for repeats.</p> <p>We call the <code>misplaced_tiles()</code> to compute the misplaced tile cost .</p> <p>We identify the blank tile and then check for the next available steps and generate the new nodes and check if this new node is the goal state or not.</p> <p>Here, $f(n) = g(n) + h(n)$ $h(n)$ calculates the number of misplaced tiles in current state as compared to goal state. $g(n)$ is the path cost for each step made.</p>



ent states and evaluvates the best path to goal state

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int).reshape(-1, 9)
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count = len(state) - 1
while count != -1:
    bestsol = np.insert(bestsol, 0, state[count]['puzzle'], 0)
    count = (state[count]['parent'])
return bestsol.reshape(-1, 3, 3)

# this function checks for the uniqueness of the iteration(it) state, weather it
has been previously traversed or not.
def all(checkarray):
    set=[]
    for it in set:
        for checkarray in it:
            return 1
        else:
            return 0

# calculate Manhattan distance cost between each digit of puzzle(start state) and
the goal state
def manhattan(puzzle, goal):
    a = abs(puzzle // 3 - goal // 3)
    b = abs(puzzle % 3 - goal % 3)
    mhcost = a + b
    return sum(mhcost[1:])

# will calculates the number of misplaced tiles in the current state as compared
to the goal state
def misplaced_tiles(puzzle,goal):
    mscost = np.sum(puzzle != goal) - 1
    return mscost if mscost > 0 else 0

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] else [on_false]

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linates of each of goal or initial state values

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))
puzzle):

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        pos[q] = p
    return pos

# start of 8 puzzle evaluation, using Manhattan heuristics
def evaluvate(puzzle, goal):
    steps = np.array([('up', [0, 1, 2], -3), ('down', [6, 7, 8], 3), ('left', [0,
3, 6], -1), ('right', [2, 5, 8], 1)],
        dtype = [('move', str, 1), ('position', list), ('head', int)])

    dtstate = [('puzzle', list), ('parent', int), ('gn', int), ('hn', int)]

    # initializing the parent, gn and hn, where hn is manhattan distance
function call
    costg = coordinates(goal)
    parent = -1
    gn = 0
    hn = manhattan(coordinates(puzzle), costg)
    state = np.array([(puzzle, parent, gn, hn)], dtstate)

# We make use of priority queues with position as keys and fn as value.
    dtpriority = [('position', int), ('fn', int)]
    priority = np.array([(0, hn)], dtpriority)

    while 1:
        priority = np.sort(priority, kind='mergesort', order=['fn',
'position'])
        position, fn =
priority[0]
        priority = np.delete(priority, 0, 0)
        # sort priority queue using merge sort, the first element is picked for
exploring remove from queue what we are exploring
        p, hn = state[position]
        puzzle =
        blank square in input
        (puzzle == 0)[0])

        time()

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        if blank not in s['position']:
            # generate new state as copy of current
            openstates = deepcopy(puzzle)
            openstates[blank], openstates[blank + s['head']] =
openstates[blank + s['head']], openstates[blank]
            # The all function is called, if the node has been previously
explored or not
            if ~(np.all(list(state['puzzle']) == openstates, 1)).any():
                end_time = time.time()
                if ((end_time - start_time) > 2):
                    print(" The 8 puzzle is unsolvable ! \n")
                    exit
                # calls the manhattan function to calculate the cost
                hn = manhattan(coordinates(openstates), costg)
                # generate and add new state in the list
                q = np.array([(openstates, position, gn, hn),
dtstate)

                state = np.append(state, q, 0)
                # f(n) is the sum of cost to reach node and the cost to reach
from the node to the goal state
                fn = gn + hn

                q = np.array([(len(state) - 1, fn)], dtpriority)
                priority = np.append(priority, q, 0)
                # Checking if the node in openstates are matching the goal
state.
                if np.array_equal(openstates,
goal):

                    print(' The 8 puzzle is solvable ! \n')
                    return state, len(priority)

return state, len(priority)

```



```

ation, using Misplaced tiles heuristics
puzzle, goal):
    ('', [0, 1, 2], -3), ('down', [6, 7, 8], 3), ('left', [0,
, 8], 1)],
    ('move', str, 1), ('position', list), ('head', int)])

    list), ('parent', int), ('gn', int), ('hn', int)]
    al)

```

```

    # initializing the parent, gn and hn, where hn is misplaced_tiles function
    call
    parent = -1
    gn = 0
    hn = misplaced_tiles(coordinates(puzzle), costg)
    state = np.array([(puzzle, parent, gn, hn)], dtype)

    # We make use of priority queues with position as keys and fn as value.
    dtpriority = [ ('position', int), ('fn', int) ]

    priority = np.array([(0, hn)], dtpriority)

    while 1:
        priority = np.sort(priority, kind='mergesort', order=[ 'fn',
        'position' ])
        position, fn = priority[0]
        # sort priority queue using merge sort, the first element is picked for
        exploring.
        priority = np.delete(priority, 0, 0)
        puzzle, parent, gn, hn = state[position]
        puzzle = np.array(puzzle)
        # Identify the blank square in input
        blank = int(np.where(puzzle == 0)[0])
        # Increase cost g(n) by 1
        gn = gn + 1
        c = 1
        start_time = time.time()
        for s in steps:
            c = c + 1
            if blank not in s[ 'position' ]:
                # generate new state as copy of current
                openstates = deepcopy(puzzle)
                openstates[blank], openstates[blank + s[ 'head' ]] =
                openstates[blank + s[ 'head' ]], openstates[blank]
                # If blank function is called, if the node has been previously
                visited
                if list(state[ 'puzzle' ]) == openstates,
                # If time taken is more than 2 seconds
                if (time.time() - start_time) > 2):
                    print(" The 8 puzzle is unsolvable \n")
                    break
                # Call the Misplaced_tiles function to calculate the cost
                hn = misplaced_tiles(coordinates(openstates), costg)

```



```

        # generate and add new state in the list
        q = np.array([(openstates, position, gn, hn)],
dtstate)

        state = np.append(state, q, 0)
        # f(n) is the sum of cost to reach node and the cost to reach
        # from the node to the goal state
        fn = gn + hn

        q = np.array([(len(state) - 1, fn)], dtpriority)
        priority = np.append(priority, q, 0)
        # Checking if the node in openstates are matching the goal
        # state.

        if np.array_equal(openstates, goal):
            print(' The 8 puzzle is solvable \n')
            return state, len(priority)

    return state, len(priority)

# ----- Program start -----

# User input for initial state
puzzle = []
print(" Input vals from 0-8 for start state ")
for i in range(0,9):
    x = int(input("enter vals :"))
    puzzle.append(x)

# User input of goal state
goal = []
print(" Input vals from 0-8 for goal state ")
for i in range(0,9):
    x = int(input("Enter vals :"))

    # Print the distance and the number of misplaced tiles
    print(" distance \n2. Misplaced tiles"))

    # Call the solve function
    solve(puzzle, goal)
    print(" state")

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print(str(bestpath).replace('[', ' ').replace(']', ''))
totalmoves = len(bestpath) - 1
print('Steps to reach goal:',totalmoves)
visit = len(state) - visited
print('Total nodes visited: ',visit, "\n")
print('Total generated:', len(state))

if(n == 2):
    state, visited = evaluvate_misplaced(puzzle, goal)
    bestpath = bestsolution(state)
    print(str(bestpath).replace('[', ' ').replace(']', ''))
    totalmoves = len(bestpath) - 1
    print('Steps to reach goal:',totalmoves)
    visit = len(state) - visited
    print('Total nodes visited: ',visit, "\n")
    print('Total generated:', len(state))

```

Sample Output : 1

```

PS C:\Users\HP\Desktop\python> python -u "c:\Users\HP\Desktop\python\PAI Assignment.py"
Input vals from 0-8 for start state
enter vals :1
enter vals :2
enter vals :3
enter vals :4
enter vals :5
enter vals :6
enter vals :7
enter vals :0
enter vals :8
Input vals from 0-8 for goal state
Enter vals :1
Enter vals :2
Enter vals :3
Enter vals :4
Enter vals :5
Enter vals :6

```



Sample Output : 2

```
PROBLEMS  OUTPUT  DEBUG CONSOLE  TERMINAL

PS C:\Users\HP\Desktop\python> python -u "c:\Users\HP\Desktop\python\PAI Assignment.py"
  Input vals from 0-8 for start state
enter vals :1
enter vals :2
enter vals :3
enter vals :4
enter vals :5
enter vals :6
enter vals :0
enter vals :7
enter vals :8
  Input vals from 0-8 for goal state
Enter vals :1
Enter vals :2
Enter vals :3
Enter vals :4
Enter vals :5
Enter vals :6
Enter vals :7
Enter vals :8
Enter vals :0
1. Manhattan distance
2. Misplaced tiles 2
  The 8 puzzle is solvable

  1 2 3
  4 5 6
  0 7 8

  1 2 3
  4 5 6
  7 0 8
```



Sample Output : 3

```
PROBLEMS  OUTPUT  DEBUG CONSOLE  TERMINAL

Try the new cross-platform PowerShell https://aka.ms/powershell

PS C:\Users\HP\Desktop\python> python -u "c:\Users\HP\Desktop\python\PAI Assignment.py"
Input vals from 0-8 for start state
enter vals :1
enter vals :2
enter vals :3
enter vals :0
enter vals :4
enter vals :5
enter vals :6
enter vals :7
enter vals :8
Input vals from 0-8 for goal state
Enter vals :1
Enter vals :2
Enter vals :0
Enter vals :3
Enter vals :4
Enter vals :5
Enter vals :6
Enter vals :7
Enter vals :8
1. Manhattan distance
2. Misplaced tiles 1
The 8 puzzle is solvable !
```

```
PROBLEMS  OUTPUT  DEBUG CONSOLE  TERMINAL

1. Manhattan distance
2. Misplaced tiles 1
The 8 puzzle is solvable !

1 2 3
0 4 5
6 7 8

0 2 3
1 4 5
6 7 8

2 0 3
1 4 5
```

```
1 2 5
3 0 4
6 7 8

1 2 5
3 4 0
6 7 8

1 2 0
3 4 5
6 7 8
Steps to reach goal: 11
Total nodes visited: 53

Total generated: 94
```



CONCLUSION

The 8 puzzle algorithm is solved using A* algorithm which uses heuristics such as manhattan distance and misplaced tile.

