

# Climate Prediction Markets and Convergence of Predictive Models

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## Abstract

We present an agent-based model of a climate prediction market in which traders adapt their belief about the climate based on the monetary performance of their neighboring traders in a social network. We analyze the model to determine how a variety of factors affect whether climate prediction markets foster a convergence of market participants' beliefs regarding a true model of the earth's climate. We find that only the imposed "true model" itself significantly affects the convergence of beliefs. If the true model from which the temperature data is generated is auto-regressive, with no human-induced effects, participation in the prediction market, on average, does not cause convergence of traders' beliefs. On other hand, if anthropogenic climate change is real, traders' beliefs are more likely than not to converge toward the correct climate model due to participation in the market.

## Introduction

The previous two decades saw a strong polarization of the climate change debate. Although the scientific consensus on the anthropogenic nature of climate change strongly increased, the average belief about anthropogenic climate change did not evolve much within the public [18]. In addition, the divide on anthropogenic climate change between liberals and conservatives has grown steadily, indicating that the question is becoming increasingly politicized and potentially disconnected from scientific evidence. This is troubling given the costs of a misinformed climate policy. If anthropocentric climate change is a myth but is taken to be true, a tremendous amount of public resources will be wasted on adaptation and mitigation efforts. On the other hand, if climate change is human induced but not recognized as so, the costs of inaction would be huge. Given that effective climate policies require long-lasting measures to be taken, the importance of an accurate consensus on the issue is manifest.

Attempts to foster such consensus face many social and psychological challenges. Recently, people have argued that such challenges could be met by set-

ting up climate prediction markets [8, 18]. The idea of using prediction markets to efficiently aggregate information about uncertain events has been discussed for decades [7]. Prediction markets have been shown to have interesting theoretical properties [15, 4] and to perform well in terms of prediction accuracy in experiments [5, 6], agent-based models (ABM) [10, 9], and in the real-world [19].

However, to the best of our knowledge, the idea that prediction markets can generate consensus *on the factors* affecting uncertain events has never been quantitatively explored. ABMs of prediction markets have been studied [10, 17, 9], some of which feature communication between agents. In these models, however, beliefs about the uncertain outcomes are constructed in rather abstract ways. In particular, beliefs are not based on structural models from which agents could derive causal implications, and therefore these models are not suitable for investigating the convergence of the underlying explanatory models agents employ for prediction.

From a public policy perspective, changing the explanatory models of market participants is one of the most important roles that prediction markets might play.<sup>1</sup> Effective climate policy not only requires an accurate consensus on future climate *outcomes*. It also requires an accurate consensus on the causal *mechanisms* influencing such outcomes. If people agree that temperature will rise, but some believe it will be due to greenhouse gases, while others believe that it will be caused by increased solar activity, inconsistent and ineffective policies may be implemented. Our model is designed to investigate whether, and under what conditions, prediction markets can foster such convergence in predictive models.

## Model Design

TODO: Martin use this text below (it is commented out) from the original document and flesh it out for the Supplementary Material and then write a couple paragraph summary and the key equations to put in this main article right here.

In particular, lets go over main design and then define what each of these mean in our model:

- `ideo`  $\sim \text{Unif}(0, 1)$
- `market.complet`  $\sim \text{Unif}(0, 1000)$  (mapped into integer)
- `n.edge`  $\sim \text{Unif}(100, 200)$  (mapped into integer)
- `n.traders`  $\sim \text{Unif}(50, 250)$  (mapped into integer)
- `risk.tak`  $\sim \text{Unif}(0, 1)$

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<sup>1</sup>and perhaps the most important potential social benefit of prediction markets given the comparable predictive power of statistical models, which are less expensive than setting up and maintaining prediction markets [3].

- `seg`  $\sim Unif(0, 1)$
- `true.model`  $\sim Binom(0.5)$

## Model Analysis

We estimated the effects of the parameters of our model on the difference between the fraction of traders who believe in the true model at the beginning of the experiment and the fraction who believe in the true model at the end of all trading sequences. The sensitivity analysis is based on a Latin Hypercube Sampling of 10,000 parameter sets from the following distributions [1, 2].

- `ideo`  $\sim Unif(0, 1)$
- `market.complet`  $\sim Unif(0, 1000)$  (mapped into integer)
- `n.edge`  $\sim Unif(100, 200)$  (mapped into integer)
- `n.traders`  $\sim Unif(50, 250)$  (mapped into integer)
- `risk.tak`  $\sim Unif(0, 1)$
- `seg`  $\sim Unif(0, 1)$
- `true.model`  $\sim Binom(0.5)$

We use the model to simulate 10,000 outcomes based on the input parameter sets and then conduct a partial rank correlation coefficient analysis on the relationship between the input matrix,  $X$ , resulting simulated vector,  $y$  [11, 12, 14]. Partial correlation computes the linear relationship between the part of the variation of  $X_i$  and  $y$  that are linearly independent of other  $X_j$  ( $j \neq i$ ). The only difference with the partial correlation and partial *rank* correlation (which we use here), is that the outcome variable  $y$  is first ranked-transformed in order to allow us capture potentially non-linear relationships.<sup>2</sup>

Our sensitivity analysis, illustrated by Fig. 1, strongly suggests that the magnitude of convergence to the true model is conditional on what the true model actually is: if anthropogenic climate change is true, a prediction market is likely to cause convergence to the true model; while if anthropogenic climate change is false, and the model of the climate is in fact auto-regressive, convergence to this true model is unlikely (Fig. 2).

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<sup>2</sup>That is every value,  $y_s$ , in the data set is replace by a number  $f(y_s) \equiv |\{y_r \mid y_s > y_r\}|$ , where  $y_r$  are the other observed values of  $y$  in the data set.

## Discussion

Proponents of climate prediction markets argue that climate prediction markets will foster convergence to the best approximate model, whatever the actual true model is. It is framed as an apartisan proposal: if climate change is not anthropogenic, traders will converge to non-anthropogenic beliefs similar to how they would converge to anthropogenic beliefs if the climate is truly influenced by human activities. Our findings contradict this assumption.

TODO: Jonathan, perhaps talk about the policy implications of this finding...

## Acknowledgements

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## References

- [1] Brian Beachkofski and Ramana Grandhi. Improved Distributed Hypercube Sampling. In *43rd AIAA/ASME/ASCE/AHS/ASC Structures, Structural Dynamics, and Materials Conference*. American Institute of Aeronautics and Astronautics, 2002.
- [2] Rob Carnell. lhs Latin Hypercube Samples, July 2012.
- [3] Sharad Goel, Daniel M. Reeves, Duncan J. Watts, and David M. Pennock. Prediction Without Markets. In *Proceedings of the 11th ACM Conference on Electronic Commerce*, EC '10, pages 357–366, New York, NY, USA, 2010. ACM.
- [4] Robin Hanson. Logarithmic market scoring rules for modular combinatorial information aggregation. *The Journal of Prediction Markets*, pages 3–15, 2012.
- [5] Robin Hanson, Ryan Oprea, and David Porter. Information aggregation and manipulation in an experimental market. *Journal of Economic Behavior & Organization*, 60(4):449–459, August 2006.
- [6] Paul J. Healy, Sera Linardi, J. Richard Lowery, and John O. Ledyard. Prediction markets: Alternative mechanisms for complex environments with few traders. *Management Science*, 56(11):1977–1996, November 2010.
- [7] Christian Franz Horn, Bjoern Sven Ivens, Michael Ohneberg, and Alexander Brem. Prediction markets – a literature review 2014. *The Journal of Prediction Markets*, 8(2):89–126, September 2014.

- [8] Shi-Ling Hsu. Prediction market for climate outcomes, a. *University of Colorado Law Review*, 83:179, 2011.
- [9] Janyl Jumadinova and Prithviraj Dasgupta. A multi-agent system for analyzing the effect of information on prediction markets. *International Journal of Intelligent Systems*, 26(5):383–409, 2011.
- [10] Frank MA Klingert and Matthias Meyer. Comparing prediction market mechanisms using an experiment-based multi-agent simulation. In *ECMS*, pages 654–661, 2012.
- [11] Simeone Marino, Ian B. Hogue, Christian J. Ray, and Denise E. Kirschner. A methodology for performing global uncertainty and sensitivity analysis in systems biology. *Journal of Theoretical Biology*, 254(1):178–196, September 2008.
- [12] Gilles Pujol, Bertrand Iooss, Alexandre Janon with contributions from Paul Lemaitre, Laurent Gilquin, Loic Le Gratiet, Taieb Touati, Bernardo Ramos, and Jana Fruth and Sebastien Da Veiga. sensitivity: Sensitivity Analysis, August 2014.
- [13] R Core Team. *R: A Language and Environment for Statistical Computing*. R Foundation for Statistical Computing, Vienna, Austria, 2014.
- [14] A. Saltelli, K. Chan, and E. M. Scott. *Sensitivity Analysis*. Wiley, Chichester, 1 edition edition, March 2009.
- [15] Reinhard Set and Reinhard Selten. Axiomatic characterization of the quadratic scoring rule. *Experimental Economics*, 1(1):43–62, June 1998.
- [16] Victoria Stodden, Friedrich Leisch, and Roger D. Peng, editors. *Implementing Reproducible Computational Research*. Chapman & Hall/CRC, Boca Raton, 2014.
- [17] Jie-Jun Tseng, Chih-Hao Lin, Chih-Ting Lin, Sun-Chong Wang, and Sai-Ping Li. Statistical properties of agent-based models in markets with continuous double auction mechanism. *Physica A: Statistical Mechanics and its Applications*, 389(8):1699–1707, April 2010.
- [18] Michael P. Vandenbergh, Kaitlin E. Toner, and Jonathan M. Gilligan. Energy and climate change: A climate prediction market. SSRN Scholarly Paper ID 2372321, Social Science Research Network, Rochester, NY, December 2013.
- [19] Justin Wolfers and Eric Zitzewitz. Prediction markets in theory and practice. 2006.
- [20] Yihui Xie. *Dynamic Documents with R and knitr*. Chapman & Hall/CRC, Boca Raton, 2014.

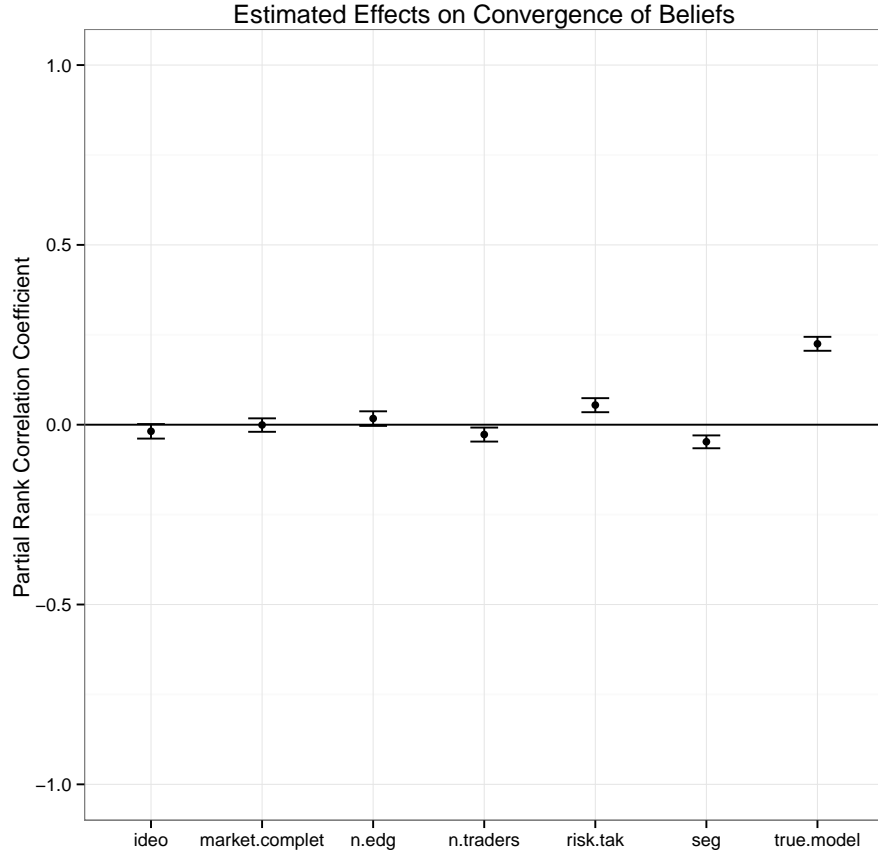


Figure 1: Partial rank correlation coefficient analysis based on 10,000 simulated parameter sets [12, 14] of the effects of ideology, market completeness, number of edges in social network, number of traders in market, risk taking propensities, segregation measure of the social network, and the true climate model on the convergence of traders' beliefs. Lines are bootstrapped 95% confidence intervals.

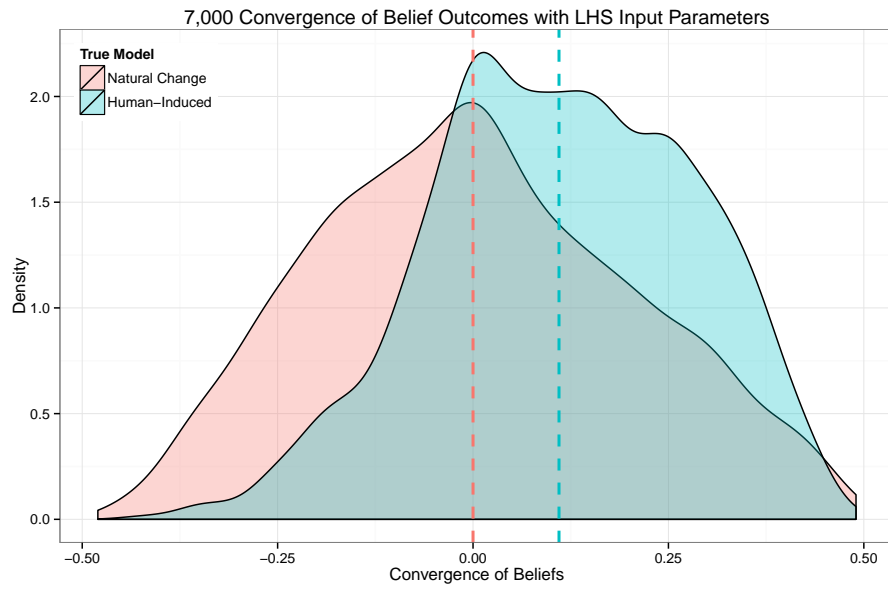


Figure 2: Density of 7,000 convergence of belief model outcomes with 7,000 Latin Hypercube Sampled input parameter sets. 3,500 of the Latin Hypercube Sampled input parameter sets have “human-induced” climate change as the true model and 3,500 have “natural change” climate change as the true model. Dashed lines are the medians of the two densities (0, 0.11). Possible values of convergence of beliefs range from -1 to 1.

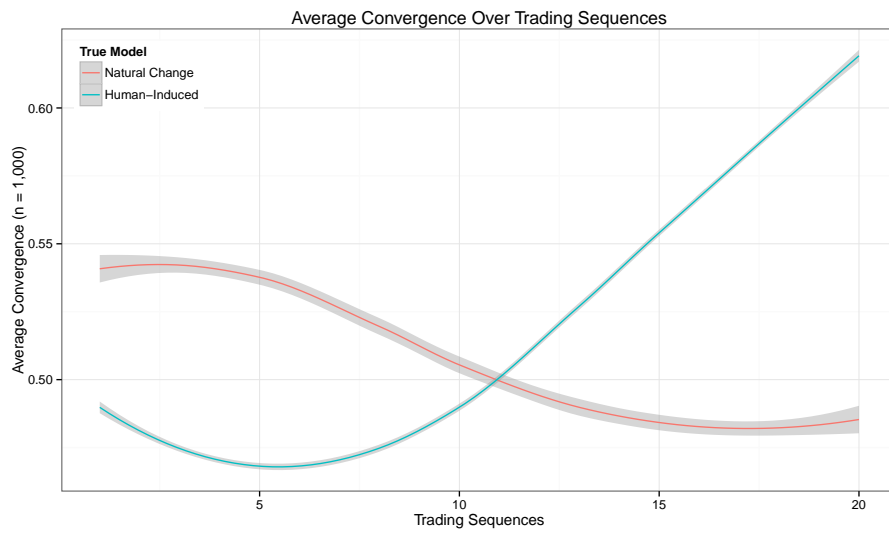


Figure 3: Temporal evolution of convergence of beliefs.