

Betting and Belief: Prediction Markets and Attribution of Climate Change

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Prediction Markets

**Who will be the 2016 Democratic nominee?**

Top Predictions 13815 Comments

Clinton	790	82¢ ↓ 2¢
Sanders	1337	19¢ ↑ 1¢

**Who will be the 2016 Republican nominee?**

Top Predictions 67708 Comments

Trump	3087	46¢ ↑ 1¢
Cruz	577	32¢ ↓ 2¢

**Who will win the 2016 U.S. presidential election?**

Top Predictions 9106 Comments

Clinton	481	59¢ NC
Trump	1226	20¢ ↑ 2¢

**Who'll win the Wisconsin Republican primary?**


Top Predictions 15959 Comments

Cruz	59	86¢ NC
Trump	106	15¢ ↑ 1¢

**Who'll win the Wisconsin Democratic primary?**

Top Predictions 3646 Comments

Sanders	20	88¢ NC
Clinton	18	13¢ ↓ 1¢

**Who'll win the Pennsylvania Republican primary?**

Top Predictions 592 Comments

Trump	1	69¢ NC
Kasich		22¢ ↑ 2¢

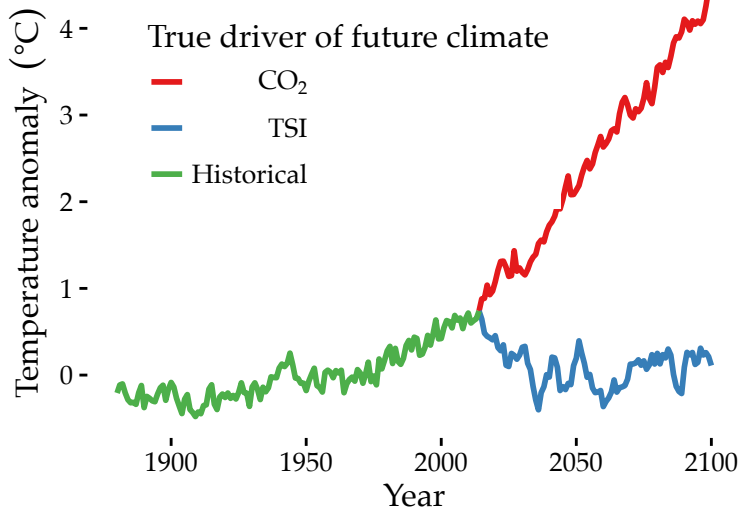
Climate Change and Prediction Markets

- ▶ Scientific consensus on anthropogenic climate change increased.
- ▶ BUT, beliefs about climate change did not evolve much within public.
- ▶ Prediction markets: participants can “put their money where their mouths are.”
- ▶ High prediction accuracy, efficient information aggregation.
- ▶ Do they also change beliefs?

Prediction Market Simulation

- ▶ *Whether, and under what social and climate conditions, might prediction markets be useful for increasing convergence of climate beliefs?*
- ▶ Prediction markets focus on near term events such as elections months away, so difficult to extrapolate to climate case.
- ▶ Investigating unobservable beliefs of traders.
- ▶ So, simulation modeling informed by climate and economic theory.

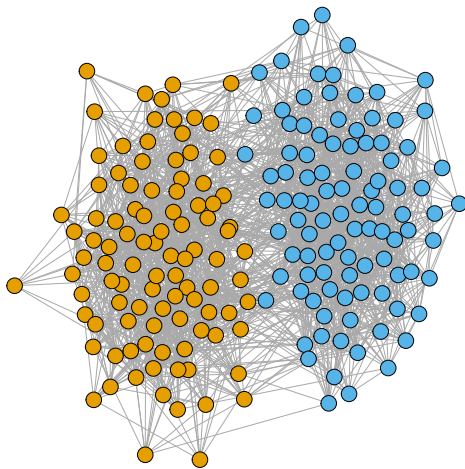
Two Alternate Realities



Trader Beliefs

- ▶ At initialization approximately half of traders use true data-generating model to make predictions.
- ▶ Traders using true model not necessarily perfectly accurate.
- ▶ Although correct *functional form* of model, still need to calibrate on limited noisy data.

Social Network



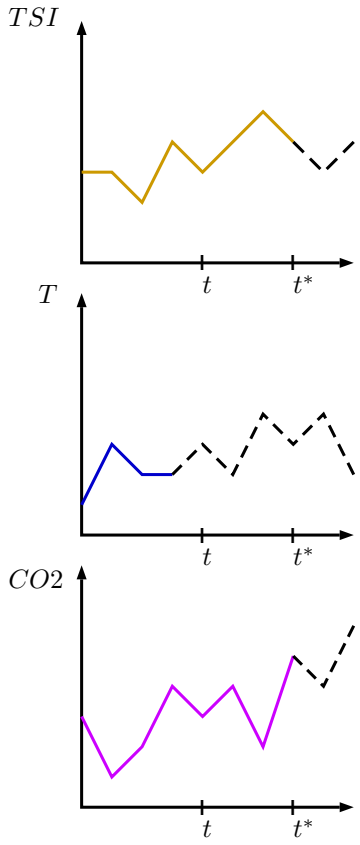
Model

1. Trader agents estimate forecasting model.
2. Make predictions for climate for 6 yrs from now to assign expected value to temp securities.
3. Trade.
4. Payoffs for owners of security that was correct.
5. Decide whether to adopt neighbors model based on cumulative earnings.



$$F_{(t-1)}^{TSI}$$

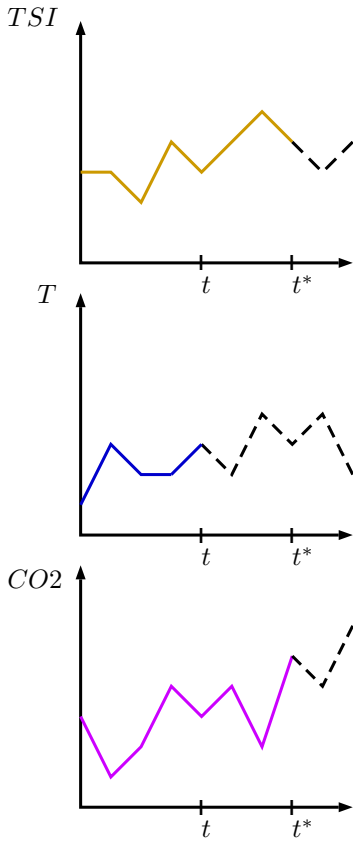
$$F_{(t-1)}^{CO2}$$





$$F_{(t-1)}^{TSI}$$

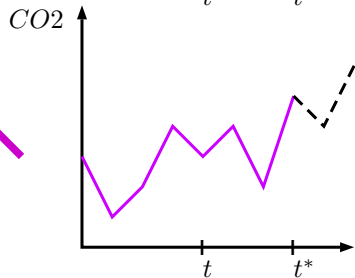
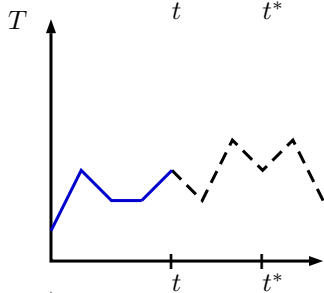
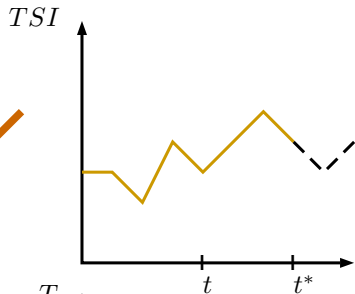
$$F_{(t-1)}^{CO_2}$$

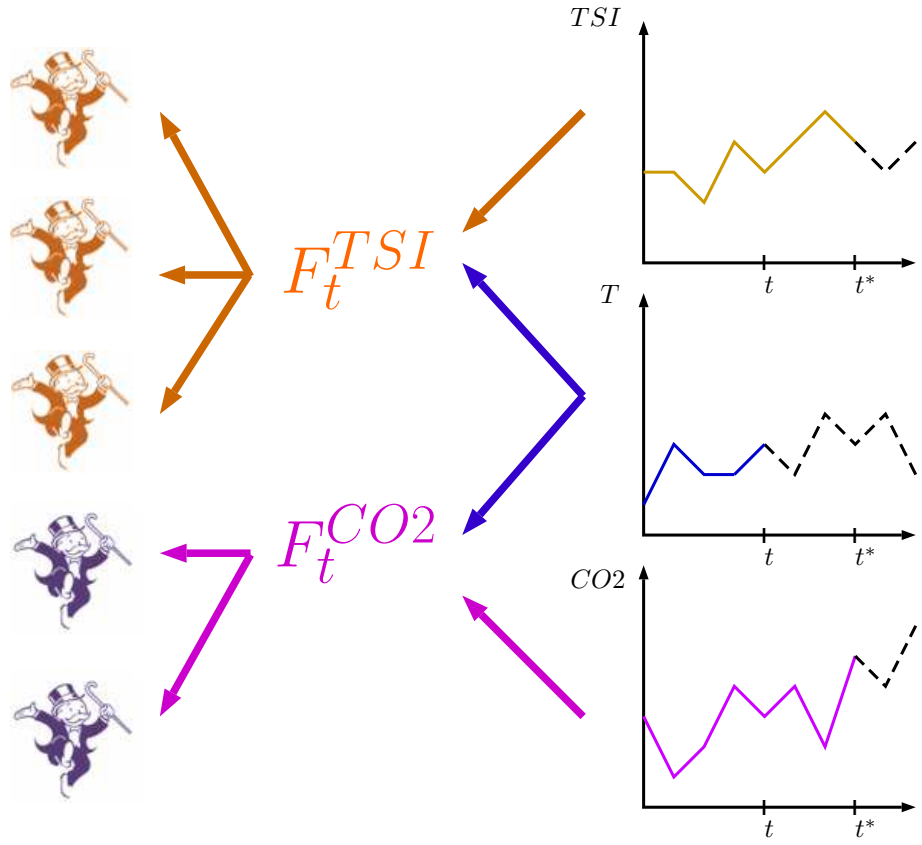




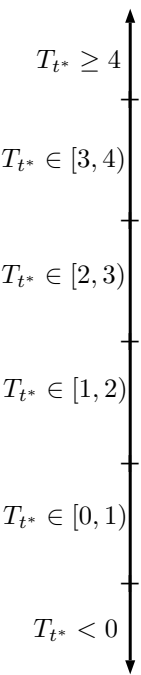
$F_{(t-1)}^{TSI}$

$F_{(t-1)}^{CO2}$



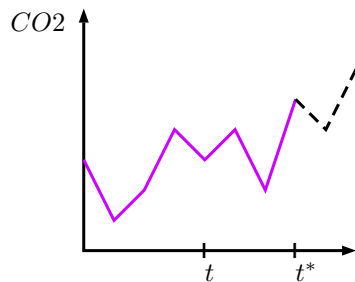
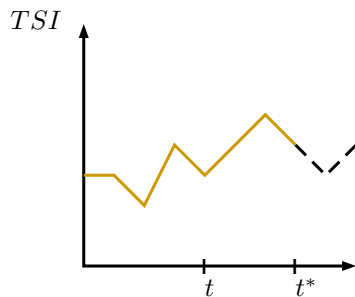


1\$ if

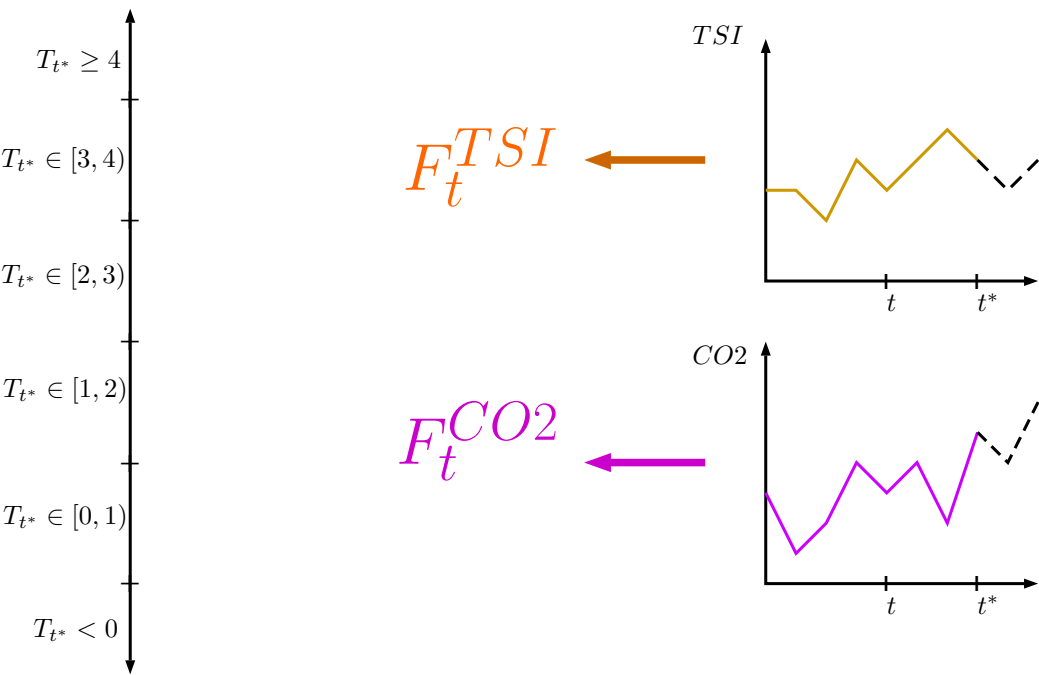


F_t^{TSI}

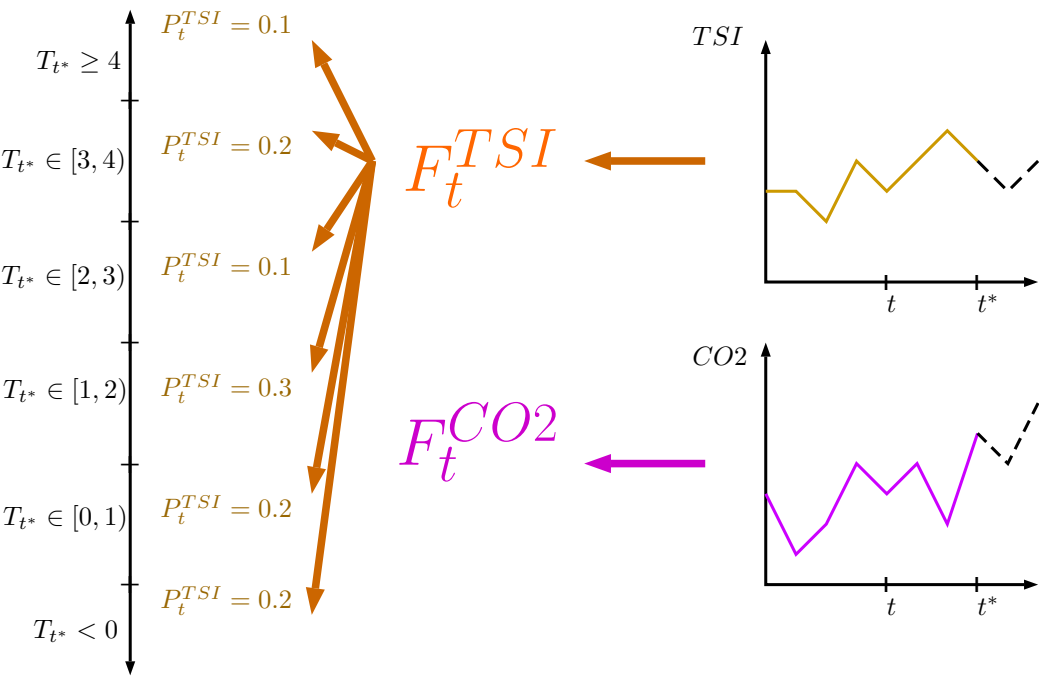
F_t^{CO2}



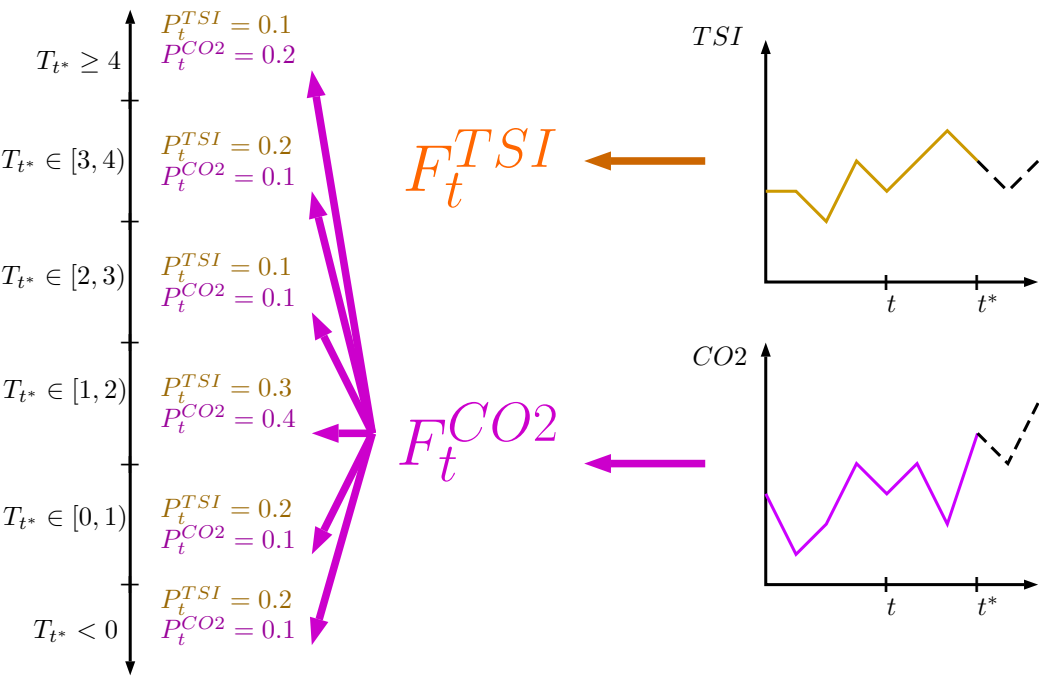
1\$ if



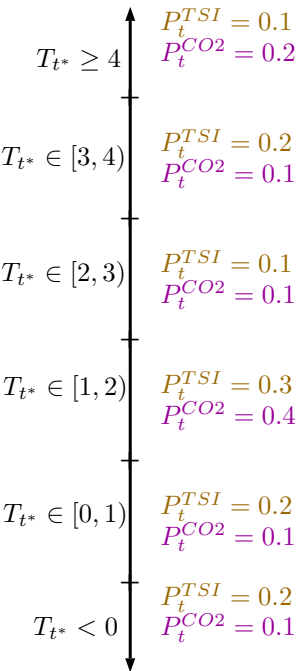
1\$ if



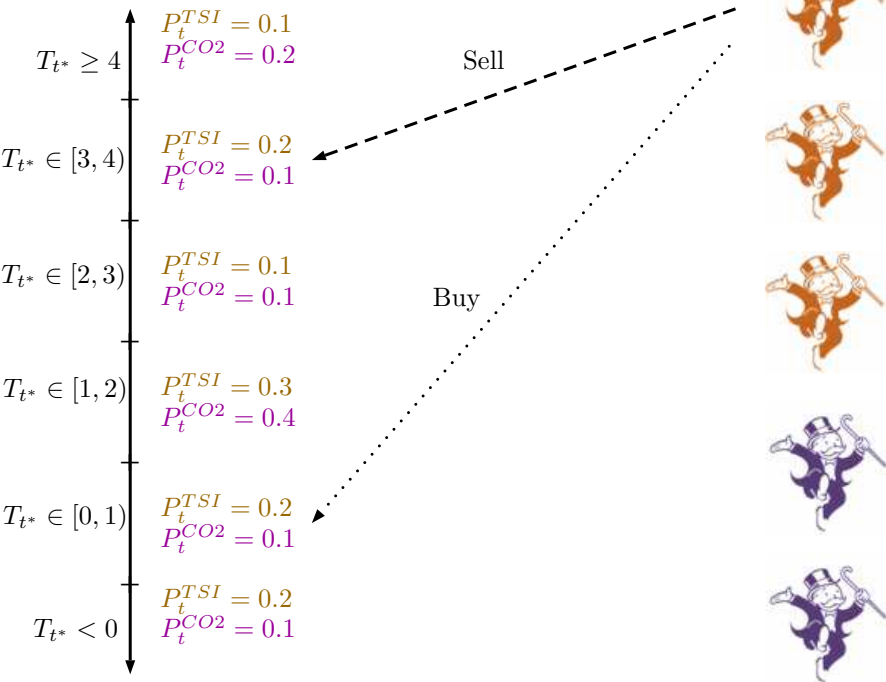
1\$ if



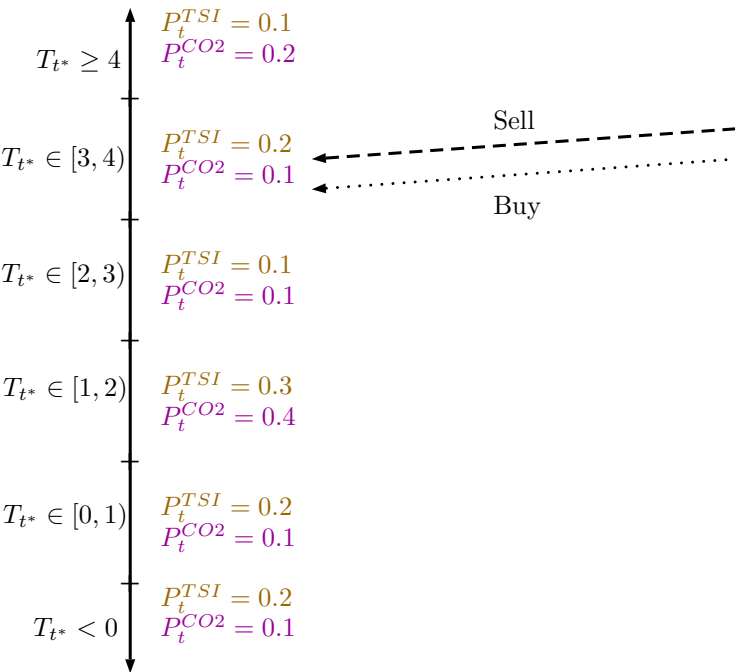
1\$ if



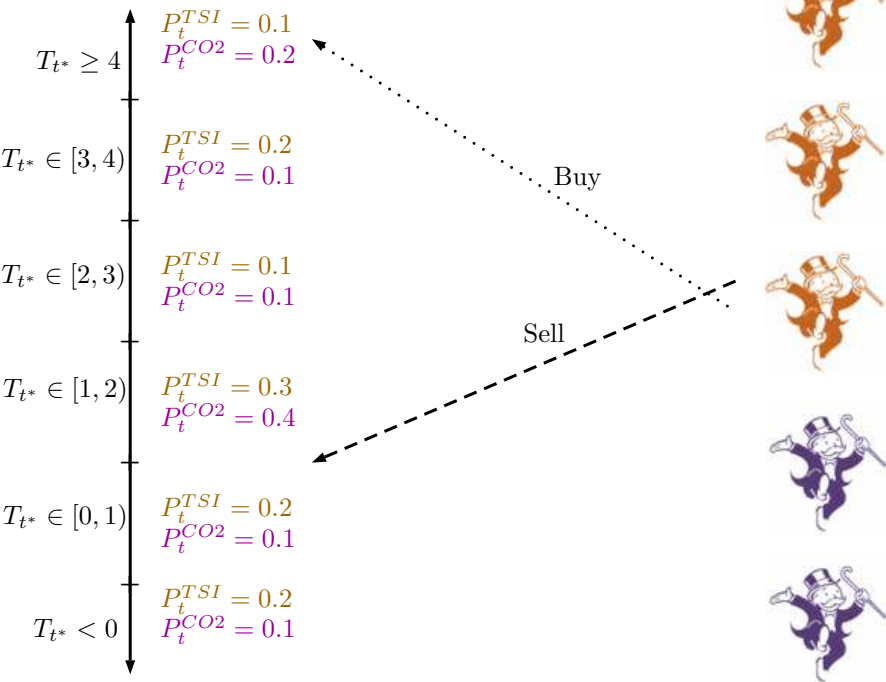
1\$ if



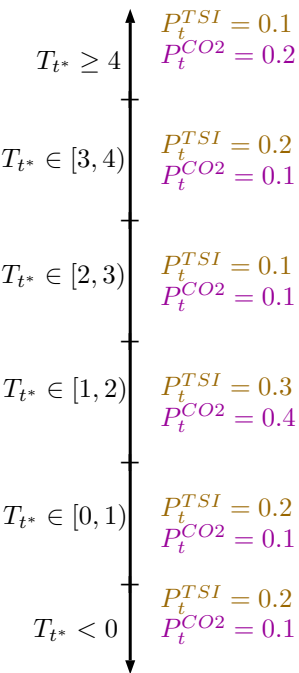
1\$ if



1\$ if



1\$ if

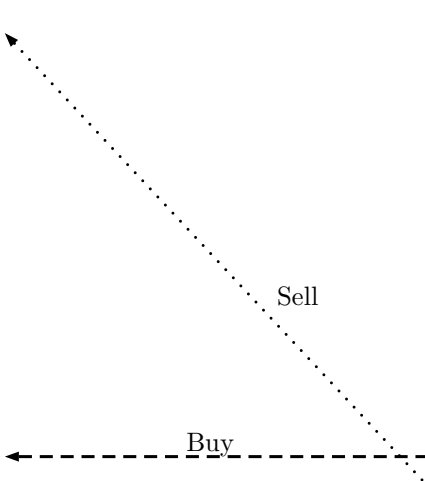
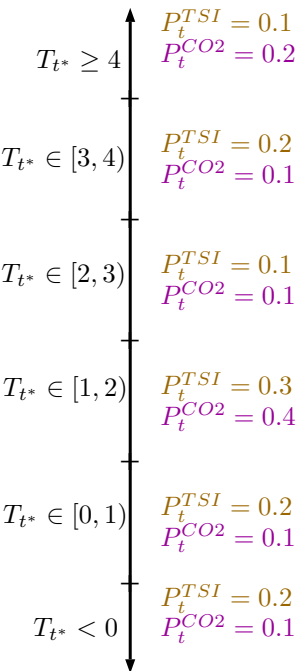


Sell

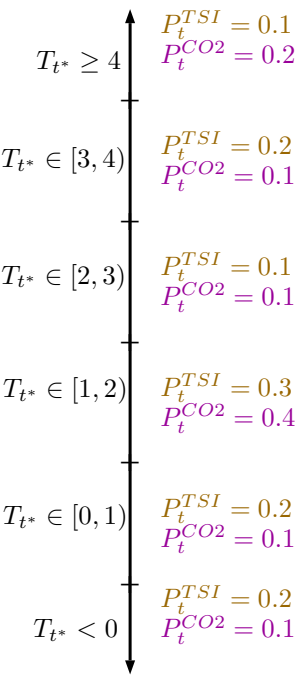
Buy



1\$ if



1\$ if



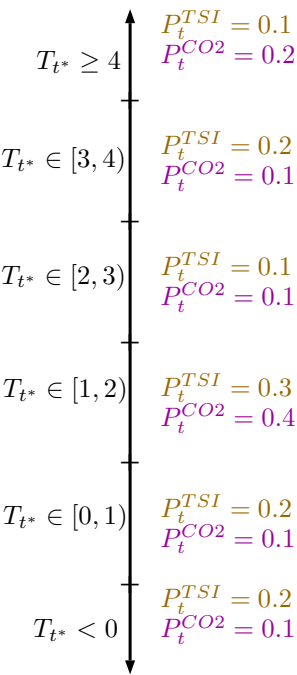
Order Book



Sell Orders

Buy Orders

1\$ if



Order Book



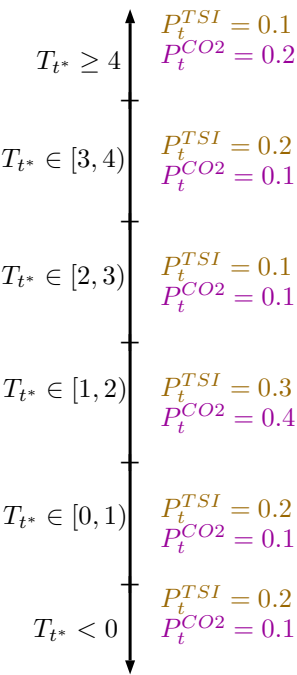
Sell Orders

Sell $\{T_{t^*} \in [3, 4)\}$ above 0.3

Buy Orders

Buy $\{T_{t^*} \in [0, 1)\}$ below 0.15

1\$ if



Order Book



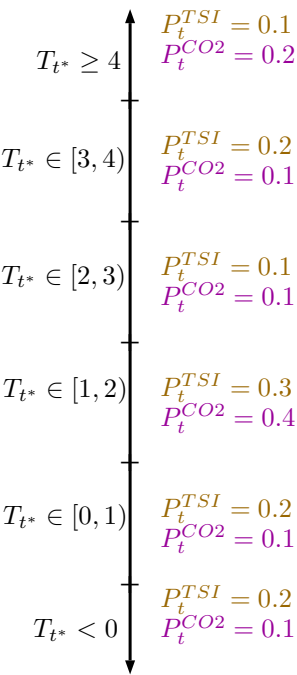
Sell Orders

Sell $\{T_{t^*} \in [3, 4)\}$ above 0.3
Sell $\{T_{t^*} \in [3, 4)\}$ above 0.25

Buy Orders

Buy $\{T_{t^*} \in [0, 1)\}$ below 0.15
Buy $\{T_{t^*} \in [3, 4)\}$ below 0.15

1\$ if



Order Book



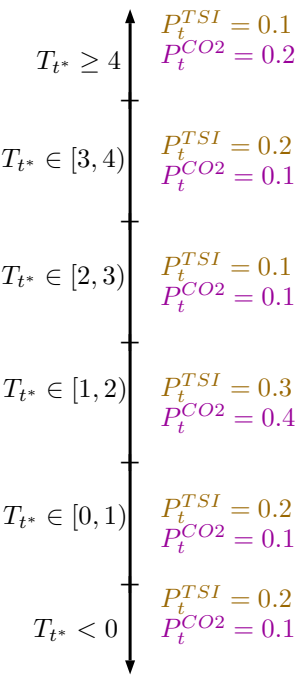
Sell Orders

- Sell $\{T_{t^*} \in [3, 4)\}$ above 0.3
- Sell $\{T_{t^*} \in [3, 4)\}$ above 0.25
- Sell $\{T_{t^*} \geq 4\}$ above 0.2

Buy Orders

- Buy $\{T_{t^*} \in [0, 1)\}$ below 0.15
- Buy $\{T_{t^*} \in [3, 4)\}$ below 0.15
- Buy $\{T_{t^*} \in [0, 1)\}$ below 0.1

1\$ if



Order Book



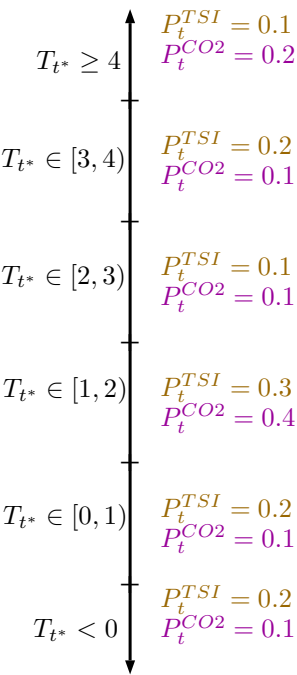
Sell Orders

- Sell $\{T_{t^*} \in [3, 4)\}$ above 0.3
- Sell $\{T_{t^*} \in [3, 4)\}$ above 0.25
- Sell $\{T_{t^*} \geq 4\}$ above 0.2
- Sell $\{T_{t^*} \in [0, 1)\}$ above 0.12

Buy Orders

- Buy $\{T_{t^*} \in [0, 1)\}$ below 0.15
- Buy $\{T_{t^*} \in [3, 4)\}$ below 0.15
- Buy $\{T_{t^*} \in [0, 1)\}$ below 0.1
- Buy $\{T_{t^*} < 0\}$ below 0.05

1\$ if



Order Book



Sell Orders

Sell $\{T_{t^*} \in [3, 4)\}$ above 0.3

Sell $\{T_{t^*} \in [3, 4)\}$ above 0.25

Sell $\{T_{t^*} \geq 4\}$ above 0.2

Sell $\{T_{t^*} \in [0, 1)\}$ above 0.12

Buy Orders

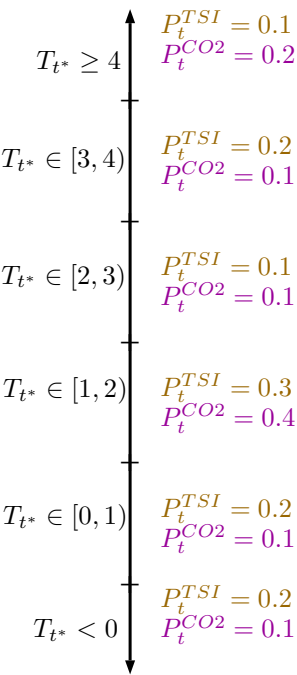
Buy $\{T_{t^*} \in [0, 1)\}$ below 0.15

Buy $\{T_{t^*} \in [3, 4)\}$ below 0.15

Buy $\{T_{t^*} \in [0, 1)\}$ below 0.1

Buy $\{T_{t^*} < 0\}$ below 0.05

1\$ if



0.12 \$

Order Book



Sell Orders

Sell $\{T_{t^*} \in [3, 4)\}$ above 0.3

Sell $\{T_{t^*} \in [3, 4)\}$ above 0.25

Sell $\{T_{t^*} \geq 4\}$ above 0.2

Sell $\{T_{t^*} \in [0, 1)\}$ above 0.12

Buy Orders

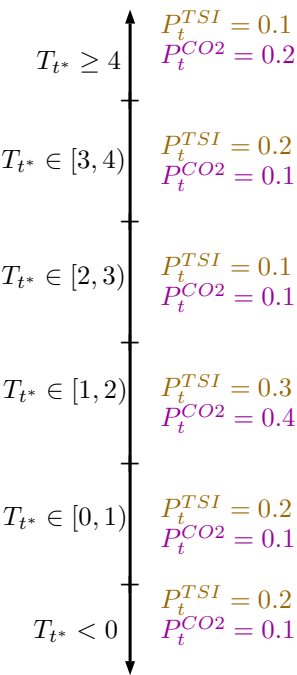
Buy $\{T_{t^*} \in [0, 1)\}$ below 0.15

Buy $\{T_{t^*} \in [3, 4)\}$ below 0.15

Buy $\{T_{t^*} \in [0, 1)\}$ below 0.1

Buy $\{T_{t^*} < 0\}$ below 0.05

1\$ if



1 security $\{T_{t^*} \in [0, 1)\}$

Order Book



Sell Orders

Sell $\{T_{t^*} \in [3, 4)\}$ above 0.3

Sell $\{T_{t^*} \in [3, 4)\}$ above 0.25

Sell $\{T_{t^*} \geq 4\}$ above 0.2

Sell $\{T_{t^*} \in [0, 1)\}$ above 0.12

Buy Orders

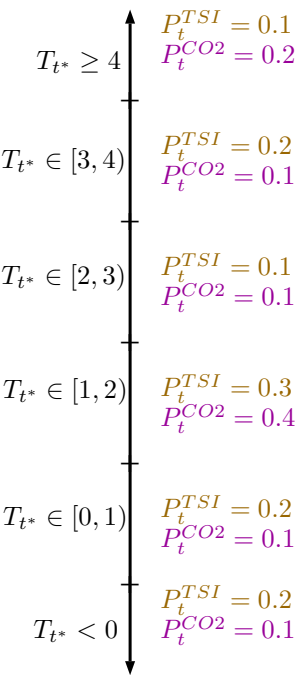
Buy $\{T_{t^*} \in [0, 1)\}$ below 0.15

Buy $\{T_{t^*} \in [3, 4)\}$ below 0.15

Buy $\{T_{t^*} \in [0, 1)\}$ below 0.1

Buy $\{T_{t^*} < 0\}$ below 0.05

1\$ if



Order Book



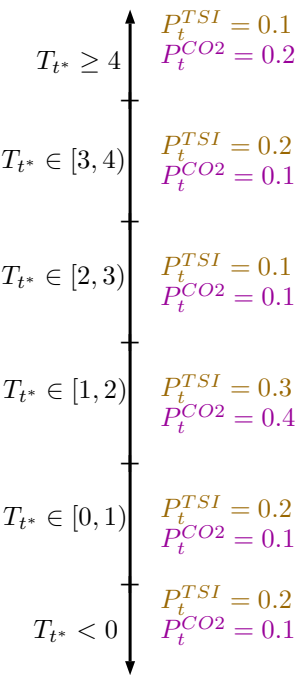
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- Sell $\{T_{t^*} \geq 4\}$ above 0.2

Buy Orders

- Buy $\{T_{t^*} \in [3, 4)\}$ below 0.15
- Buy $\{T_{t^*} \in [0, 1)\}$ below 0.1
- Buy $\{T_{t^*} < 0\}$ below 0.05

1\$ if



Order Book



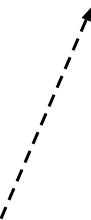
Sell Orders

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- Sell $\{T_{t^*} \in [3, 4)\}$ above 0.25
- Sell $\{T_{t^*} \geq 4\}$ above 0.2

Sell $\{T_{t^*} < 0\}$ above 0.15

Buy Orders

- Buy $\{T_{t^*} \in [3, 4)\}$ below 0.15
- Buy $\{T_{t^*} \in [0, 1)\}$ below 0.1
- Buy $\{T_{t^*} < 0\}$ below 0.05



Buy $\{T_{t^*} \in [3, 4)\}$ below 0.05

1\$ if



$$T_{t^*} \geq 4 \quad \begin{array}{l} P_t^{TSI} = 0.1 \\ P_t^{CO2} = 0.2 \end{array}$$



$$T_{t^*} \in [3, 4) \quad \begin{array}{l} P_t^{TSI} = 0.2 \\ P_t^{CO2} = 0.1 \end{array}$$



$$T_{t^*} \in [2, 3) \quad \begin{array}{l} P_t^{TSI} = 0.1 \\ P_t^{CO2} = 0.1 \end{array}$$



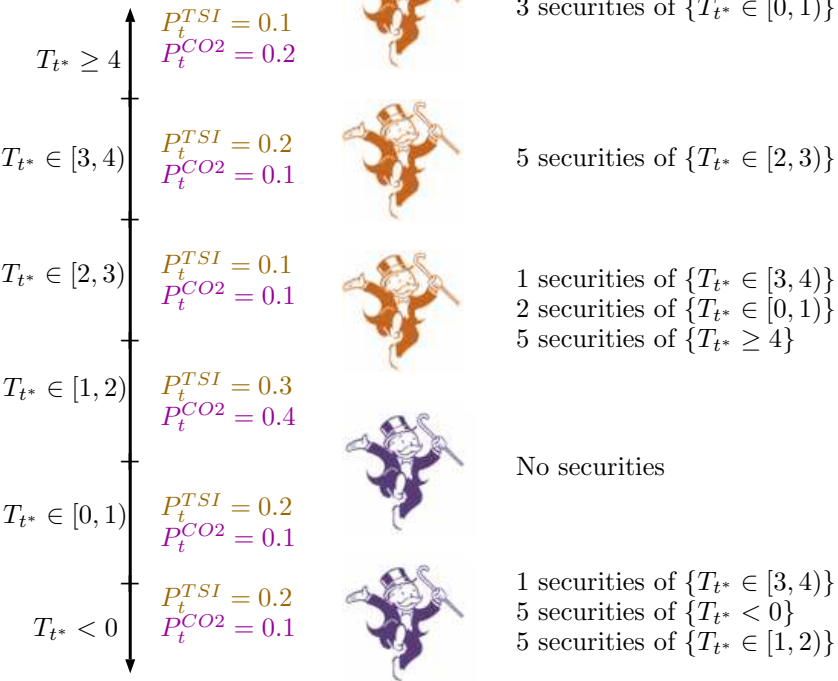
$$T_{t^*} \in [1, 2) \quad \begin{array}{l} P_t^{TSI} = 0.3 \\ P_t^{CO2} = 0.4 \end{array}$$



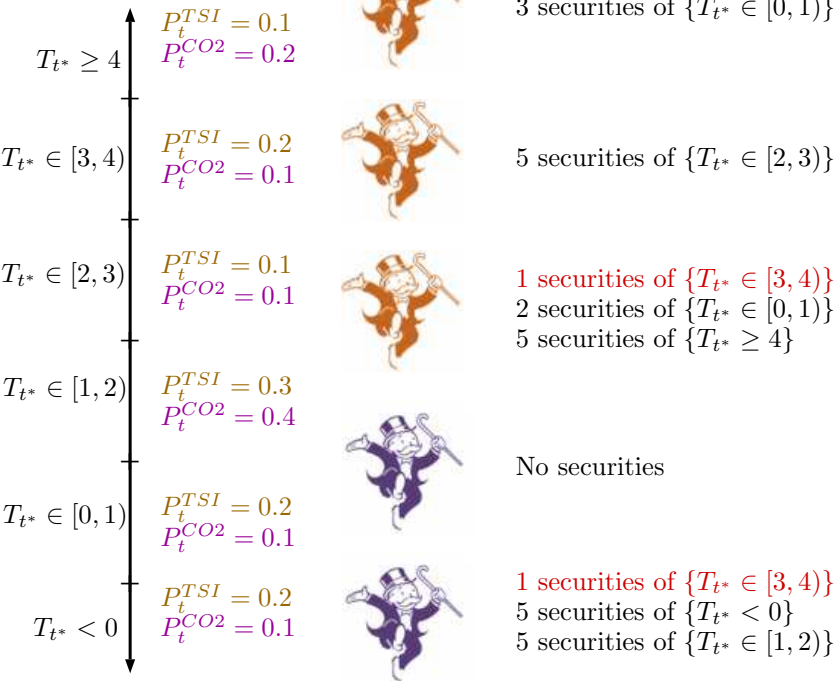
$$T_{t^*} \in [0, 1) \quad \begin{array}{l} P_t^{TSI} = 0.2 \\ P_t^{CO2} = 0.1 \end{array}$$

$$T_{t^*} < 0 \quad \begin{array}{l} P_t^{TSI} = 0.2 \\ P_t^{CO2} = 0.1 \end{array}$$

1\$ if

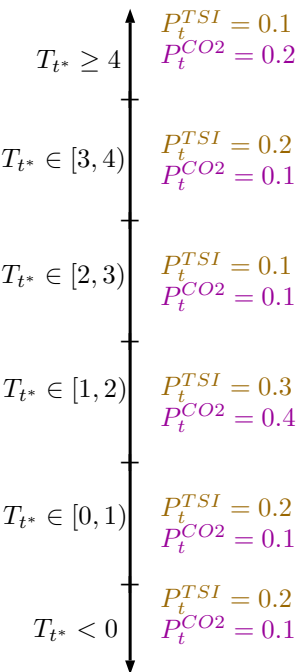


1\$ if



True Temperature at t^*
 $3.12 \in [3, 4)$

1\$ if



3 securities of $\{T_{t^*} \in [3, 4)\}$
 3 securities of $\{T_{t^*} \in [0, 1)\}$

+ 3\$



5 securities of $\{T_{t^*} \in [2, 3)\}$



1 securities of $\{T_{t^*} \in [3, 4)\}$
 2 securities of $\{T_{t^*} \in [0, 1)\}$
 5 securities of $\{T_{t^*} \geq 4\}$

+ 1\$



No securities



1 securities of $\{T_{t^*} \in [3, 4)\}$
 5 securities of $\{T_{t^*} < 0\}$
 5 securities of $\{T_{t^*} \in [1, 2)\}$

+ 1\$

True Temperature at t^*
 $3.12 \in [3, 4)$

11\$



7\$



21\$

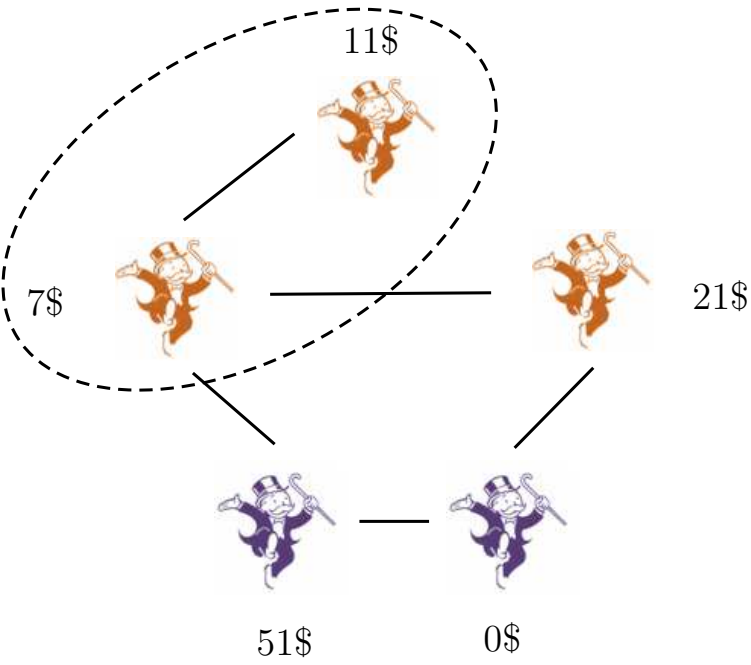


51\$



0\$





11\$



7\$



21\$



51\$



0\$



11\$



7\$



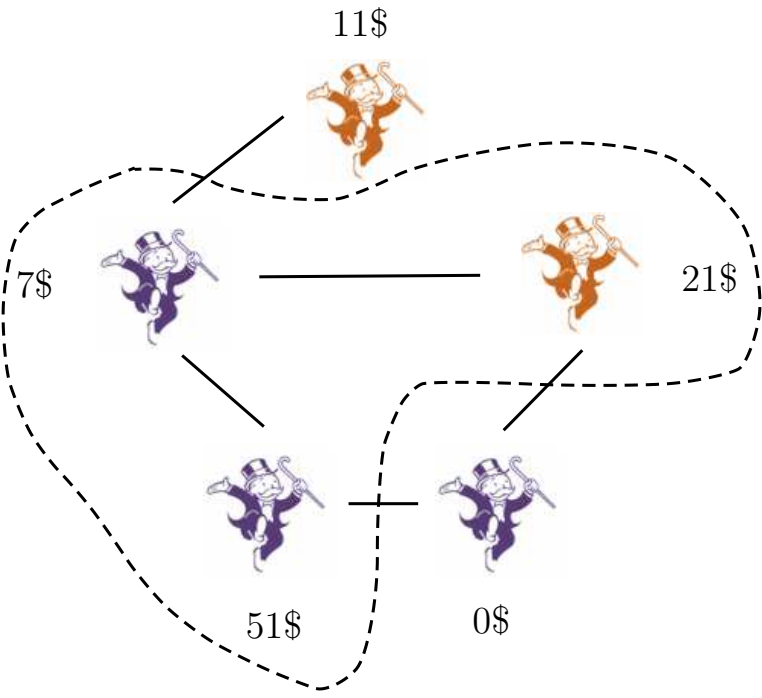
21\$



51\$



0\$



11\$



7\$



21\$



51\$



0\$

11\$



21\$



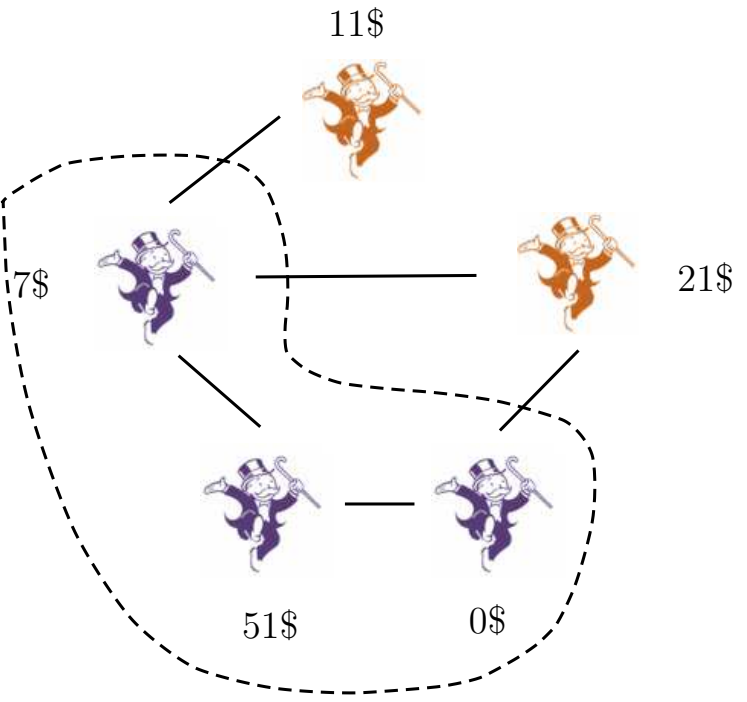
7\$

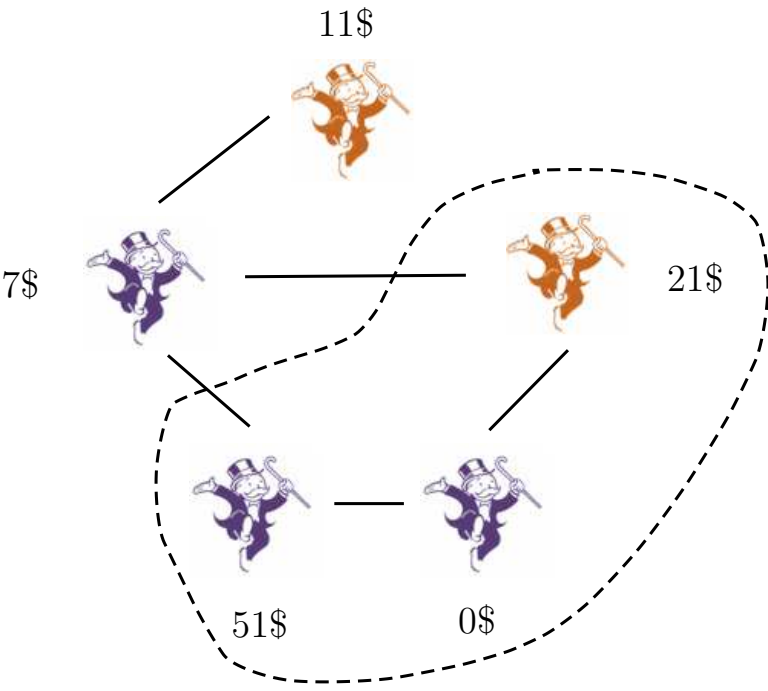


51\$



0\$



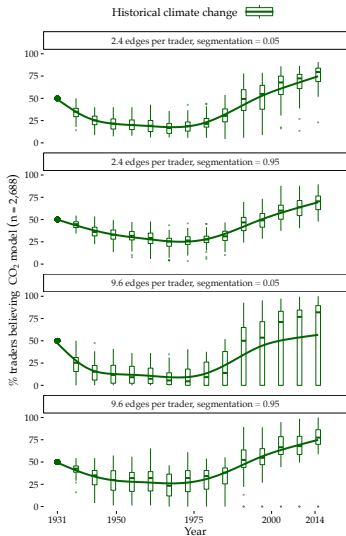


Parameters

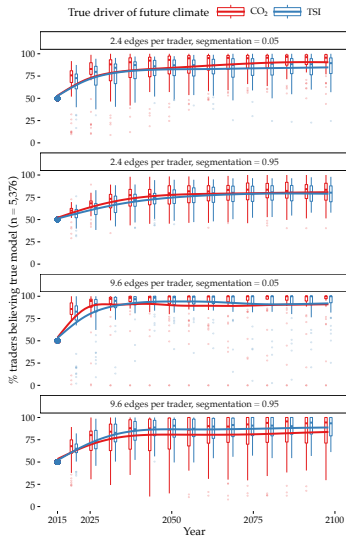
- ▶ $ideo \sim \text{Uniform}(0, 1)$
- ▶ $n.edge \sim \text{Uniform}(100, 200)$ (mapped into integer)
- ▶ $n.traders \sim \text{Uniform}(50, 250)$ (mapped into integer)
- ▶ $risk.tak \sim \text{Uniform}(0, 1)$
- ▶ $seg \sim \text{Uniform}(0, 1)$
- ▶ $true.model \sim \text{Bernoulli}(0.5)$

Convergence Over Time

1931–2014



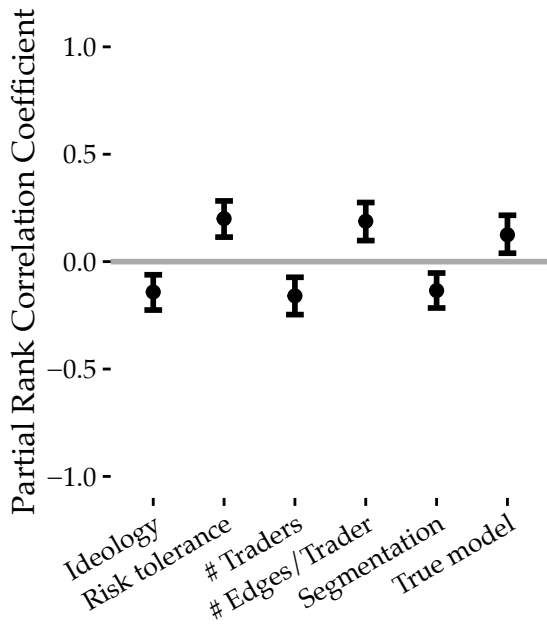
2015–2098



Sensitivity Analysis Design

- ▶ Stochasticity in temperature data, social network structure, and agent decision models.
- ▶ 10 full simulations for each of 500 input parameter sets and average.
- ▶ Partial rank correlation coefficient analysis on relationship between input matrix, X , and resulting simulated outcome vector of mean belief convergence scores, y .
- ▶ Partial correlation: linear relationship between part of variation of X_i and y that are linearly independent of other X_j ($j \neq i$).
- ▶ To allow potentially non-linear relationships y is first rank-transformed.
- ▶ 1,000 bootstrapped estimations of PRCC to obtain 95% confidence intervals.

Sensitivity Analysis Results



References