

$$I \equiv \{(0 \leq \lambda \leq |S|) \wedge (\text{result} = \text{true} \iff (\forall k: \mathbb{Z})(0 \leq k < \lambda \rightarrow S[k] \neq 7))\}$$

$$(I \wedge \neg B) \rightarrow Q_c$$

$$I \wedge \neg B \equiv (\lambda = |S|) \wedge \text{result} = \text{true} \iff (\forall k: \mathbb{Z})(0 \leq k < |S| \rightarrow S[k] \neq 7)$$

↑
porque
 $0 \leq \lambda \leq |S| \wedge \lambda \geq |S|$

↑
porque
 $\lambda = |S|$

Por lo que $I \wedge \neg B \rightarrow Q_c$ ya que $I \wedge \neg B \equiv (\lambda = |S| \wedge Q_c)$

$$\{I \wedge B\} S \{I\} \quad (I \wedge B) \rightarrow \text{up}(\lambda := \lambda + 1, \text{up}(\text{result} := \text{result} \wedge (S[\lambda-1] \neq 7), I))$$

↑
cuerpo
del ciclo

E_1

trabaja la expresión del postcondición
cada vez que se ejecuta el ciclo

$$E_1 \equiv \underbrace{\text{def}(\text{result})}_{\text{true}} \wedge \underbrace{\text{def}(S[\lambda-1])}_{0 \leq \lambda-1 < |S|} \wedge I_{\text{result} \wedge (S[\lambda-1] \neq 7)}$$

$$\begin{aligned} &\equiv 0 \leq \lambda-1 < |S| \wedge (0 \leq \lambda \leq |S| \wedge ((\text{result} \wedge S[\lambda-1] \neq 7) = \text{true} \iff \\ &\quad (\forall k: \mathbb{Z})(0 \leq k < \lambda \rightarrow S[k] \neq 7))) \equiv \\ &\equiv -1 \leq \lambda \leq |S| \wedge ((\text{result} \wedge S[\lambda-1] \neq 7) = \text{true} \iff (\forall k: \mathbb{Z})(0 \leq k < \lambda \rightarrow S[k] \neq 7)) \end{aligned}$$

$$\mathbb{Z} \ 0 \leq \lambda \leq |S| \wedge (\text{result} = \text{true})$$

$$\text{wp}(\lambda := \lambda + 1, E_1) \equiv E_2$$

$$E_2 = \text{def}(\lambda + 1) \wedge E_{1, \lambda+1} \equiv -1 \leq \lambda + 1 \leq |S| \wedge ((\text{result} \wedge S[\lambda] \neq 7) = \text{true} \rightarrow (\forall k: \mathbb{Z})(0 \leq k < \lambda + 1 \rightarrow S[k] \neq 7))$$

$$\equiv 0 \leq \lambda < |S| \wedge (\text{result} = \text{true} \wedge \underline{S[\lambda] \neq 7}) \rightarrow ((\forall k: \mathbb{Z})(0 \leq k < \lambda \rightarrow \underline{S[k] \neq 7}) \wedge \underline{S[\lambda] \neq 7}) \equiv$$

$$S[\lambda] \neq 7 \rightarrow S[\lambda] \neq 7$$

es una tautología

$$\equiv 0 \leq \lambda < |S| \wedge (\text{result} = \text{true}) \rightarrow (\forall k: \mathbb{Z})(0 \leq k < \lambda \rightarrow S[k] \neq 7) \equiv I \wedge B$$

se puede decir, entonces, que $I \wedge B \rightarrow E_2$ ya que $I \wedge B \equiv E_2$

~~esto es trivial~~ por lo que vale la triple de Hoare $\{I \wedge B\} S \{I\}$