

Name: Paul Anderson

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Purpose: *Experiment with Greedy Best-First Search and A* algorithm*

Problem 1:

Greedy Best-First Search (GBFS)

g=0 h=18	g=1 h=17	g=2 h=16	g=3 h=15	g=4 h=14	g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	
				g=5 h=13					
	g=inf h=0	g=inf h=0	g=inf h=0	g=6 h=12	g=7 h=11	g=8 h=10	g=9 h=9	g=10 h=8	g=inf h=0
	g=inf h=0							g=11 h=7	
g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	g=16 h=10	g=15 h=9	g=14 h=8	g=13 h=7	g=12 h=6	
				g=17 h=9					
	g=inf h=0	g=inf h=0	g=inf h=0	g=18 h=8	g=inf h=0	g=inf h=0	g=inf h=0		g=inf h=0
				g=19 h=7					g=inf h=0
g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	g=20 h=6	g=21 h=5	g=22 h=4	g=23 h=3	g=24 h=2	g=25 h=1
g=inf h=0									g=26 h=0

A* Search

g=0 h=18	g=1 h=17	g=2 h=16	g=3 h=15	g=4 h=14	g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	
				g=5 h=13					
	g=9 h=15	g=8 h=14	g=7 h=13	g=6 h=12	g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0
	g=10 h=14							g=inf h=0	
g=inf h=0	g=11 h=13	g=12 h=12	g=13 h=11	g=14 h=10	g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	
				g=15 h=9					
	g=inf h=0	g=inf h=0	g=inf h=0	g=16 h=8	g=inf h=0	g=inf h=0	g=inf h=0		g=inf h=0
				g=17 h=7					g=inf h=0
g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	g=18 h=6	g=19 h=5	g=20 h=4	g=21 h=3	g=22 h=2	g=23 h=1
g=inf h=0									g=24 h=0

GBFS tries to find the path it deems closest to the exit, even if it is not the best available path. Meanwhile A* analyses the path and factors in the $g(n)$. GBFS analyses using $f(n) = h(n)$, while A* is $f(n) = g(n) + h(n)$. Adding the $g(n)$, or the cost from the start to the current node, optimizes the algorithm and ensures the best possible path with a minimum cost is taken.

To Create GBFS algorithm, I simply modified the find_path code in the following way

```
### Update the evaluation function for the cell n:  $f(n) = g(n) + h(n)$ 
self.cells[new_pos[0]][new_pos[1]].f = new_g + self.cells[new_pos[0]][new_pos[1]].h
self.cells[new_pos[0]][new_pos[1]].parent = current_cell
```

Changed to, removing the 'new_g' section

```
# Removing  $g(n)$  makes A* Greedy Best-First Search because it is  $f(n) = h(n)$ 
self.cells[new_pos[0]][new_pos[1]].f = self.cells[new_pos[0]][new_pos[1]].h
self.cells[new_pos[0]][new_pos[1]].parent = current_cell
```

Greedy Best-First Search (GBFS)

[illegible][illegible]

Similar to problem 1, GBFS tries to get to the end by choosing the closest possible h value to 0, while A* factors in the g value as well. Both g values are considerably smaller. With A* end g value ending at 17, the previous algorithm had a g value of 24. Similarly, GBFS had an ending g value of 19 and previously had a g value of 26.

For this problem, the two algorithm ‘find_path’ functions remained as they were with one exception

Both GBFS and A* used this modification

```
##### Agent goes E, W, N, and S, whenever possible
# Additionally, nw, ne, sw, and se have been added for Euclidean
for dx, dy in [(0, 1), (0, -1), (1, 0), (-1, 0), (1,1), (-1,-1), (-1,1), (1,-1)]:
    new_pos = (current_pos[0] + dx, current_pos[1] + dy)
```

The 'heuristic' function was change to

```
def heuristic(self, pos):
    return (m.sqrt(((pos[0] - self.goal_pos[0]) ** 2) + ((pos[1] - self.goal_pos[1]) ** 2)))
    #return (abs(pos[0] - self.goal_pos[0]) + abs(pos[1] - self.goal_pos[1]))
```

From

```
def heuristic(self, pos):  
    return (abs(pos[0] - self.goal_pos[0]) + abs(pos[1] - self.goal_pos[1]))
```

To use the Euclidean distance (first picture) function instead of the Manhattan distance function (second picture)

Problem 3:

Alpha, the α , affects how much weight goes toward the total cost up to n . Bravo, the β , affects the algorithm in a way that makes it greedier, with $\beta > \alpha$ resembling GBFS. $\alpha > \beta$ resembling A^* search. If the values are big enough and close enough together, the search will always resemble A^* search algorithm

A	B	Observed Behavior
5	1	A^* search pattern
5	10	GBFS pattern
2	1	A^* search pattern
300	301	A^* search pattern

$A = 5 \ B = 1$

g=0 h=18	g=1 h=17	g=2 h=16	g=3 h=15	g=4 h=14	g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	
				g=5 h=13					
	g=9 h=15	g=8 h=14	g=7 h=13	g=6 h=12	g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0
	g=10 h=14							g=inf h=0	
g=inf h=0	g=11 h=13	g=12 h=12	g=13 h=11	g=14 h=10	g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	
				g=15 h=9					
	g=inf h=0	g=inf h=0	g=inf h=0	g=16 h=8	g=inf h=0	g=inf h=0	g=inf h=0		g=inf h=0
				g=17 h=7					g=inf h=0
g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	g=18 h=6	g=19 h=5	g=20 h=4	g=21 h=3	g=22 h=2	g=23 h=1
g=inf h=0									g=24 h=0

$A = 5 \ B = 10$

g=0 h=18	g=1 h=17	g=2 h=16	g=3 h=15	g=4 h=14	g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	
				g=5 h=13					
	g=inf h=0	g=inf h=0	g=inf h=0	g=6 h=12	g=7 h=11	g=8 h=10	g=9 h=9	g=10 h=8	g=inf h=0
	g=inf h=0							g=11 h=7	
g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	g=16 h=10	g=15 h=9	g=14 h=8	g=13 h=7	g=12 h=6	
				g=17 h=9					
	g=inf h=0	g=inf h=0	g=inf h=0	g=18 h=8	g=inf h=0	g=inf h=0	g=inf h=0		g=inf h=0
				g=19 h=7					g=inf h=0
g=inf h=0	g=inf h=0	g=inf h=0	g=inf h=0	g=20 h=6	g=21 h=5	g=22 h=4	g=23 h=3	g=24 h=2	g=25 h=1
g=inf h=0									g=26 h=0

See the problem 3 paragraph for an explanation of what is occurring.

The following variable were created for ease of access at the top of code

```
# Alfa and Bravo for the equation
# f(n) = alfa * g(n) + bravo * h(n) where bravo >= 0
alfa = 5
bravo = 10
```

The code in the 'find_path' function was changed to

```
### Update the evaluation function for the cell n:  $f(n) = g(n) + h(n)$ 
# added Bravo and Alfa to equation:  $f(n) = \text{alfa} * g(n) + \text{bravo} * h(n)$  where  $\text{bravo} \geq 0$ 
self.cells[new_pos[0]][new_pos[1]].f = (alfa * new_g) + (bravo * self.cells[new_pos[0]][new_pos[1]].h)
self.cells[new_pos[0]][new_pos[1]].parent = current_cell
```

From

```
### Update the evaluation function for the cell n:  $f(n) = g(n) + h(n)$ 
self.cells[new_pos[0]][new_pos[1]].f = new_g + self.cells[new_pos[0]][new_pos[1]].h
self.cells[new_pos[0]][new_pos[1]].parent = current_cell
```

In order to add a and b into the mix

Conclusion:

While both A* and GBFS are complete, only A* is optimal. When GBFS is optimized it becomes A*.