HMM in Speech Recognition

Speech Recognition 1/2

In acoustic model,

- each word consists of syllables
- each syllable consists of phonemes
- each phoneme consists of some (hypothetical) states.

$$\text{“青色”} \rightarrow \text{“青 (くーㄥ) 色 (ㄙさˋ)”} \rightarrow \text{“く”} \rightarrow \{s_1, s_2, \ldots\}$$

Each phoneme can be described by a HMM (acoustic model). Given a sequence of observation (MFCC vectors), each of them can be mapped to a corresponding state.

Speech Recognition 2/2

Hence, there are

- state transition probabilities (a_{ij}) and
- observation distribution ($b_j[o_t]$)

in each phoneme acoustic model (HMM).

Usually in speech recognition we restrict the HMM to be a *left-to-right model*, and the observation distribution is assumed to be a continuous Gaussian mixture model.

Review

- Left-to-right
- The observation distribution is a continuous Gaussian mixture model.

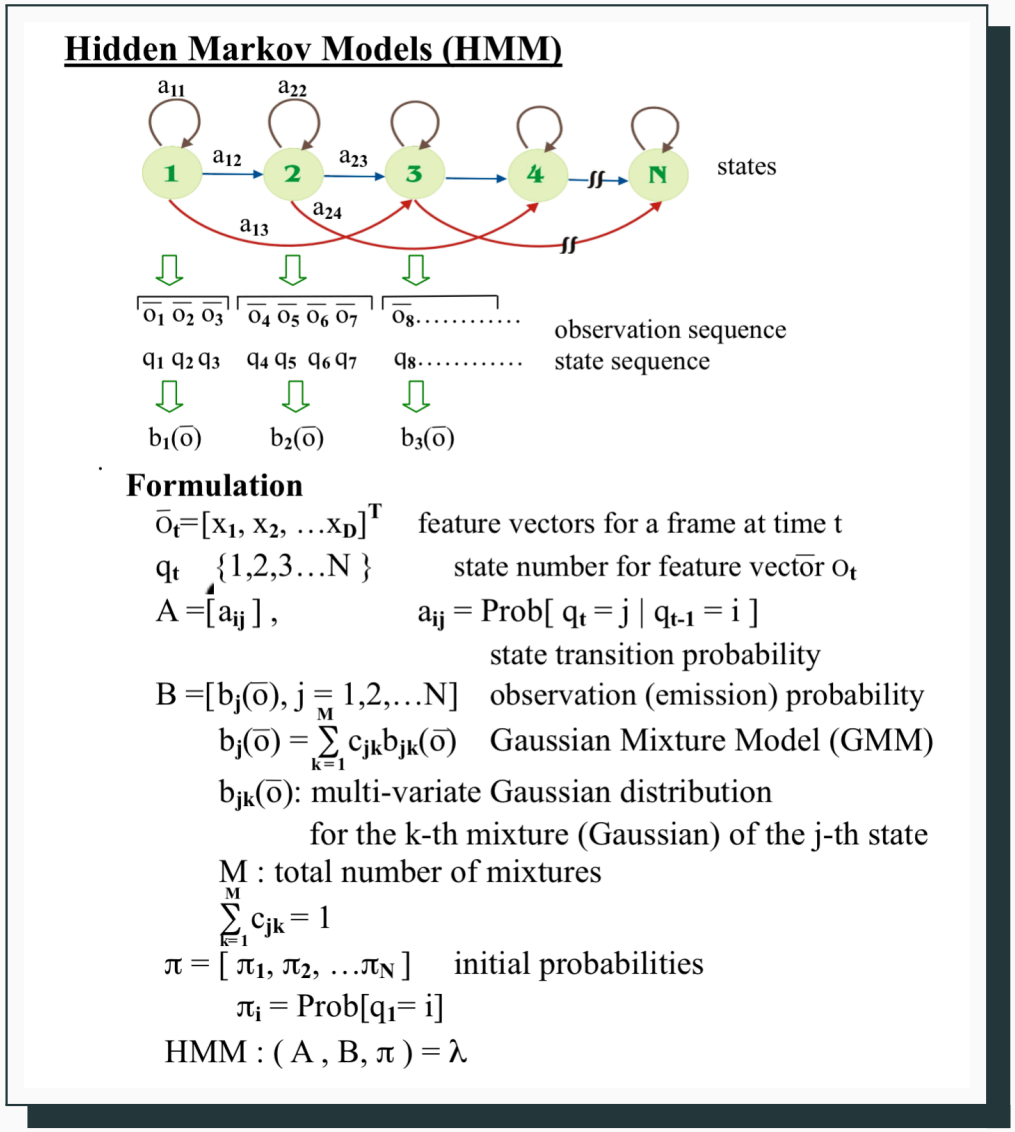


Figure 1: HMM from lecture 2.0

General Discrete HMM

$$a_{ij} = P(q_{t+1} = j \mid q_t = i), \forall\, t, i, j \tag{1}$$

$$b_j(A) = P(o_t = A \mid q_t = j), \forall\, t, A, j \tag{2}$$

Given q_t, the probability distributions of q_{t+1} and o_t are completely determined. (independent of other states or observation)

HW1 v.s. Speech Recognition

	Homework	*Speech Recognition*
λ **set**	5 models	initial-final
λ	model_01-05	“ㄑ”
$\{\mathbf{o}_t\}$	A, B, C, D, E, F	39-dim MFCC
unit	an alphabet	a time frame
observation	sequence	voice wave

Homework of HMM

Flowchart

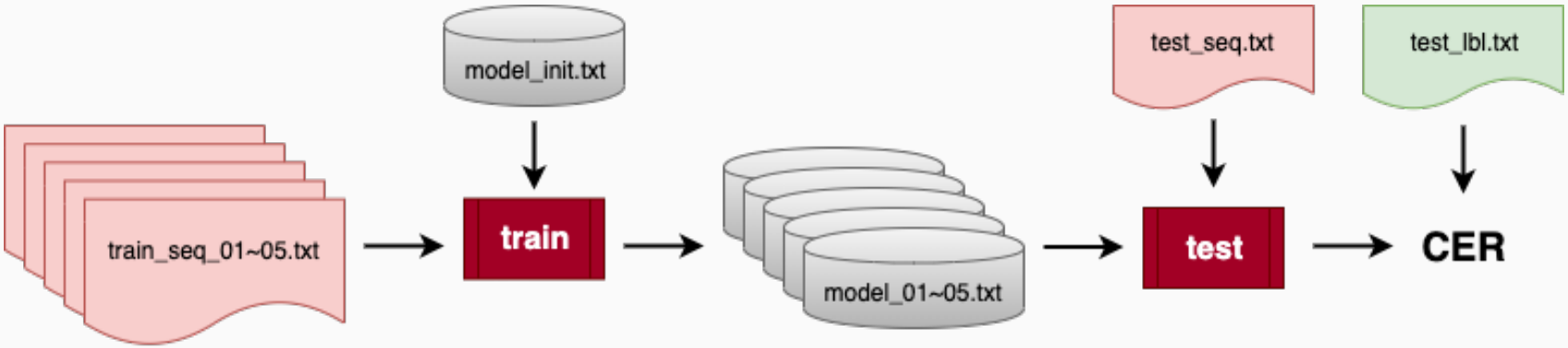


Figure 2: Training and testing models

Problems of HMM

Training

- Basic problem 3 in lecture 4.0
  - Given observations O and an initial model $\lambda = (A, B, \pi)$, adjust λ to maximize $P(O \mid \lambda)$.

$$A_{ij} = a_{ij},\ B_{jt} = b_j[o_t],\ \pi_i = P(q_1 = i)$$

- Baum-Welch algorithm

Testing

- Basic problem 2 in lecture 4.0
  - Given λ and O, find the best state sequences to maximize $P(O \mid \lambda, q)$.
- Viterbi algorithm

Homework of HMM

Training

Training

- Basic problem 3
- *Baum-Welch algorithm*: A generalized expectation-maximization (EM) algorithm[1]
  - Calculate α (forward probabilities) and β (backward probabilities) given the observations
  - Find temporary variables ϵ and γ from α and β
  - Update model parameters $\lambda' = (A', B', \pi')$

[1] `http://en.wikipedia.org/wiki/Baum-Welch_algorithm`

Forward Procedure

Forward algorithm: define a forward variable $\alpha_t(i)$

$$\alpha_t(i) = P(o_1, o_2, \ldots, o_t,\ q_t = i \mid \lambda) \tag{3}$$

$$= \text{Prob[observing } o_1, o_2, \ldots, o_t, \text{ state } i \text{ at time } t \mid \lambda \text{]} \tag{4}$$

Initialization

$$\alpha_1(i) = \pi_i b_i(o_1),\ 1 \le i \le N \tag{5}$$

Induction

$$\alpha_{t+1}(j) = \left[\sum_{i=1}^{N} \alpha_t(i) a_{ij} \right] \cdot b_j(o_{t+1}),$$

$$1 \le t \le T-1,\ 1 \le j \le N \tag{6}$$

Termination

$$P\left(\bar{O} \mid \lambda\right) = \sum_{i=1}^{N} \alpha_T(i) \tag{7}$$

Backward Procedure

Backward algorithm: define a backward variable $\beta_t(i)$

$$\beta_t(i) = P(o_{t+1}, o_{t+2}, \ldots, o_T \mid q_t = i, \lambda) \tag{8}$$

$$= \text{Prob[observing } o_{t+1}, o_{t+2}, \ldots, o_T \mid \text{state } i \text{ at time } t,\ \lambda \text{]} \tag{9}$$

Initialization

$$\beta_T(i) = 1,\ 1 \leq i \leq N \tag{10}$$

Induction

$$\beta_t(i) = \sum_{j=1}^{N} a_{ij}\ b_j(o_{t+1})\ \beta_{t+1}(j),$$

$$t = \{T-1, T-2, \ldots, 1\},\ 1 \leq i \leq N \tag{11}$$

Calculate γ

Define a temporary variable $\gamma_t(i) = P\left(q_t = i \mid \bar{O}, \lambda\right)$

$$\gamma_t(i) = \frac{\alpha_t(i)\beta_t(i)}{\sum_{i=1}^{N} \alpha_t(i)\beta_t(i)} = \frac{P\left(\bar{O}, q_t = i \mid \lambda\right)}{P\left(\bar{O} \mid \lambda\right)} \tag{12}$$

It should be a $N \times T$ matrix!

Calculate ε

The probability of transition from state i to state j given observation and model.

$$\epsilon_t(i,j) = P\left(q_t = i, q_{t+1} = j \mid \bar{O}, \lambda\right) \tag{13}$$

$$= \frac{\alpha_t(i)\ a_{ij}\ b_j(o_{t+1})\ \beta_{t+1}(j)}{\sum_{i=1}^{N}\sum_{j=1}^{N}\alpha_t(i)\ a_{ij}\ b_j(o_{t+1})\ \beta_{t+1}(j)} \tag{14}$$

$$= \frac{\text{Prob}\left[\bar{O},\ q_t = i,\ q_{t+1} = j \mid \lambda\right]}{P\left(\bar{O} \mid \lambda\right)} \tag{15}$$

In total $T-1$ matrices (each $N \times N$)

Accumulate ε and γ

Recall $\gamma_t(i) = P\left(q_t = i \mid \bar{O}, \lambda\right)$

$$\sum_{t=1}^{T-1} \gamma_t(i) = \text{expected number of times that state } i \text{ is visited in } \bar{O} \text{ from } t = 1 \text{ to } t = T - 1 \tag{16}$$

$$\sum_{t=1}^{T-1} \epsilon_t(i, j) = \text{expected number of transitions from state } i \text{ to state } j \text{ in } \bar{O} \tag{17}$$

Re-estimate Model Parameters

$$\lambda' = (A', B', \pi') \tag{18}$$

$$\pi_i = \frac{\sum \gamma_1(i)}{N}, \text{ where } N \text{ is number of samples} \tag{19}$$

$$a_{ij} = \frac{\sum \epsilon(i,j)}{\sum \gamma(i)} = \frac{\mathbb{E}\left[\text{ Number of transition from } i \text{ to } j \text{ }\right]}{\mathbb{E}\left[\text{ Number of visiting state } i \text{ }\right]} \tag{20}$$

$$b_i(k) = \frac{\sum_{O=k} \gamma(i)}{\sum \gamma(i)} = \frac{\mathbb{E}\left[\text{ Number of observation } O = k \text{ in state } i \text{ }\right]}{\mathbb{E}\left[\text{ Number of visiting state } i \text{ }\right]} \tag{21}$$

Accumulate ϵ and γ through all samples!!!
Not just the observations in one sample!

Homework of HMM

Testing

Testing

- Basic problem 2
  - Given λ and O, find the best state sequences to maximize $P(O \mid \lambda, q)$.
- Calculate $P(O \mid \lambda) \approx \max P(O \mid \lambda, q)$ for each of the five models
- The model with the highest probability for the most probable path usually also has the highest probability for all possible paths.

Viterbi Algorithm

Complete procedure for Viterbi algorithm[2]

Initialization

$$\delta_1(i) = \pi_i b_i(o_1),\ 1 \leq i \leq N \tag{22}$$

Recursion

$$\delta_t(j) = \max_{1 \leq i \leq N} [\ \delta_{t-1}(i)\ a_{ij}\ ] \cdot b_j(o_t),\ 2 \leq t \leq T,\ 1 \leq j \leq N \tag{23}$$

Termination

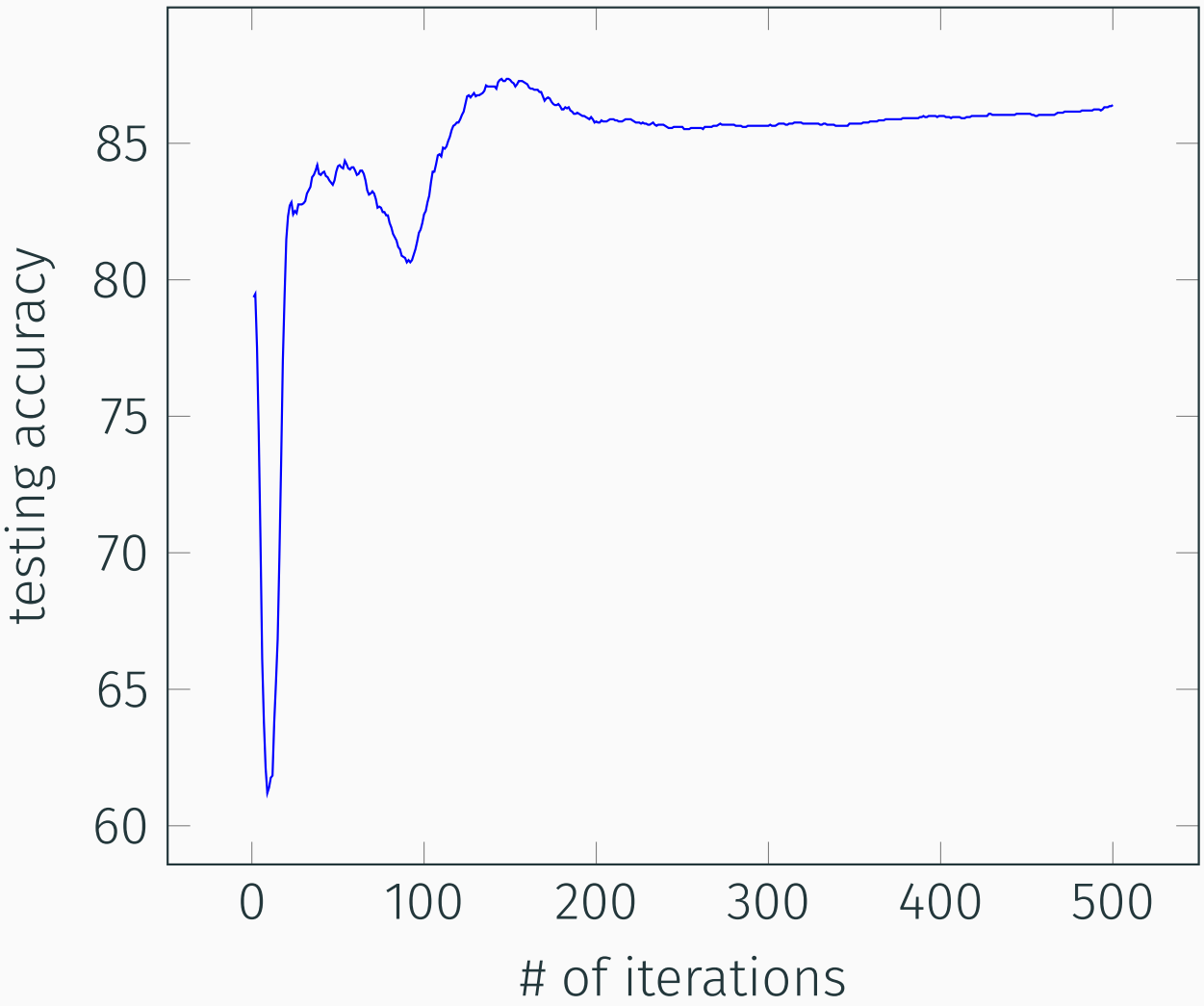
$$P^* = \max_{1 \leq i \leq N} [\ \delta_T(i)\ ] \tag{24}$$

$$\delta_t(i) = \max_{q_1, \ldots, q_{t-1}} P[\ q_1, q_2, \ldots, q_{t-1}, q_t = i, o_1, o_2, \ldots, o_t \mid \lambda\ ] \tag{25}$$

$$= \text{the highest probability along a certain single path ending at state } i \text{ at time } t \text{ for the first } t \text{ observations, given } \lambda \tag{26}$$

[2] http://en.wikipedia.org/wiki/Viterbi_algorithm

Test Accuracy v.s. # of Training Iterations



Requirements

Provided Files

`data/train_seq_0X.txt`

- Training data (10K observation sequences)

`data/test_lbl.txt`

- Testing labels

`data/test_seq.txt`

- Testing data (2.5K observation sequences)

`inc/hmm.h`

- Provided by TA, please work with it!
- You can load/dump models with functions within.

`model_init.txt`

- Initial model parameters

`modellist.txt`

- Paths to model files

`src/test_hmm.c`

- A showcase of the usage of `hmm.h`

```
dsp-hw1
├── data
│   ├── test_lbl.txt
│   ├── test_seq.txt
│   ├── train_seq_01.txt
│   ├── train_seq_02.txt
│   ├── train_seq_03.txt
│   ├── train_seq_04.txt
│   └── train_seq_05.txt
├── inc
│   └── hmm.h
├── Makefile
├── model_init.txt
├── modellist.txt
└── src
    └── test_hmm.c
```

Input and Output of Your Program

Training

Input
1. number of iterations
2. initial model (`model_init.txt`)
3. observation sequences (`train_seq_01~05.txt`)

Output Five files of parameters for 5 models, each contains $\lambda = (A, B, \pi)$ (e.g. `model_01~05.txt`)

Testing

Input
1. a file of paths to the models trained in the previous step (`modellist.txt`)
2. observation sequences (`test_seq.txt`)

Output best answer labels and $P(O \mid \lambda)$ (e.g. `result.txt`)

Training Details

```
./train <iter> <model_init_path> <seq_path> <output_model_path>
```

`iter`	# of iterations
`model_init_path`	path to the initial model params
`seq_path`	path to sequence data
`output_model_path`	path to dump trained models

Testing Details

```
./test <models_list_path> <seq_path> <output_result_path>
```

`models_list_path`	path to the model list file
`seq_path`	path to sequence data
`output_result_path`	path to output testing result

Program Execution Example

Compiling

```
make  # type this in the root directory of the project
```

Training

```
./train 100 model_init.txt data/train_seq_01.txt model_01.txt
```

Testing

```
./test modellist.txt data/test_seq.txt result.txt
```

Notice!

Command-line arguments are not fixed, read them during runtime. (e.g. Use `argv` in main function to pass the arguments.)

Also the paths in arguments need to be variable path.

Requirements

File Format

Observation Sequence Format

The given `data/train_seq_01~05.txt` and `data/test_seq.txt` look like this.

```
ACCDDDDFFCCCCBCFFFCCCCCEDADCCAEFCCCACDDFFCCDDFFCCD
CABACCAFCCFFCCCDFFCCCCCDFFCDDDDFCDDCCFCCCEFFCCCCBC
ABACCCDDCCCDDDDFBCCCCCDDAACFBCCBCCCCCCCFFFCCCCCDBF
AAABBBCCFFBDCDDFFACDCDFCDDFFFFFCDFFFCCCDCFFFFCCCCD
AACCDCCCCCCCCDCEDCBFFFCDCDCDAFBCDCFFCCDCCCEACDBAFFF
...
```

Each of the former has 10000 sequences and the latter has 2500 sequences.

Model Format 1/2

`initial: 6`

$$\pi = [\, \pi_1,\ \pi_2,\ \pi_3,\ \pi_4,\ \pi_5,\ \pi_6 \,]$$

`transition: 6`

$$A = \begin{bmatrix} a_{11} & \dots & a_{16} \\ \vdots & \ddots & \vdots \\ a_{61} & \dots & a_{66} \end{bmatrix}$$

`observation:` 6^3

$$B = \begin{bmatrix} b_1(o_1) & \dots & b_6(o_1) \\ \vdots & \ddots & \vdots \\ b_1(o_6) & \dots & b_6(o_6) \end{bmatrix}$$

[3] The sum of column is 1 here.

Model Format 2/2

A model file (e.g. `model_0X.txt`) should look like this.

```
initial: 6
0.2     0.1     0.2     0.2     0.2     0.1

transition: 6
0.3     0.3     0.1     0.1     0.1     0.1
0.1     0.3     0.3     0.1     0.1     0.1
0.1     0.1     0.3     0.3     0.1     0.1
0.1     0.1     0.1     0.3     0.3     0.1
0.1     0.1     0.1     0.1     0.3     0.3
0.3     0.1     0.1     0.1     0.1     0.3

observation: 6
0.2     0.2     0.1     0.1     0.1     0.1
0.2     0.2     0.2     0.2     0.1     0.1
0.2     0.2     0.2     0.2     0.2     0.2
0.2     0.2     0.2     0.2     0.2     0.2
0.1     0.1     0.2     0.2     0.2     0.2
0.1     0.1     0.1     0.1     0.2     0.2
```

Model List Format

The given `modellist.txt` looks like this.

```
model_01.txt
model_02.txt
model_03.txt
model_04.txt
model_05.txt
```

Your testing program should be able to read a list like this and load models from the specified paths for testing. (Don't worry! If you use `hmm.h`, all of these are done by calling function `load_models()`. For more details please refer to `hmm.h`.)

Output Format

Your testing program should output these to the specific path (e.g. `result.txt`) given as a command-line argument while executing the program.

```
model_01.txt 7.822367e-34
model_05.txt 1.094896e-40
model_01.txt 7.928724e-33
model_02.txt 4.262100e-37
model_02.txt 5.914689e-42
...
```

Each line consists of the hypothesis model and its likelihood. They should be separated by a space.

Label File Format

The first few lines of the given `data/test_lbl.txt` looks like this.

```
model_01.txt
model_05.txt
model_01.txt
model_02.txt
model_02.txt
...
```

Makefile Format

The Makefile you submit should be capable to compile your program using `make`. The provided one can compile `train.c` and `test.c` in directory `src` into two executables `train` and `test`.

```
1  .PHONY: all clean run
2  CC=gcc
3  CFLAGS=-std=c99 -O2
4  LDFLAGS=-lm
5  TARGET=train test
6
7  all: $(TARGET)
8
9  train: src/train.c
10     $(CC) -o $@ $^ $(CFLAGS) $(LDFLAGS) -Iinc
11
12 test: src/test.c
13     $(CC) -o $@ $^ $(CFLAGS) $(LDFLAGS) -Iinc
14
15 clean:
16     rm -f $(TARGET)
```

Report Format

Please write a **one-page** report in **PDF** format, name it `report.pdf` and submit with your source code.

State your name, student ID and any challenges you encounter or attempts you try. A good report may grant you bonus of extra 5%.

File Structure

All of your source code files must be placed under `inc/` and `src/`.

Let's say you only have two implementation files and use the functions provided in `hmm.h`. You should put your source code under `src/` and leave `hmm.h` in `inc/`.

```
.
├── inc
│   ├── hmm.h
│   └── [other *.h or *.hpp]
├── Makefile
├── model_init.txt
├── report.pdf
└── src
    ├── test.c
    ├── train.c
    └── [other *.c, *.cc or *.cpp]
```

Requirements

Submission Requirement

Submission Requirement 1/2

1. Create a directory named `hw1_[STUDENT_ID]`.
2. Put
   - `inc/`
   - `Makefile`
   - `model_init.txt`
   - `report.pdf`
   - `src/`

   into the directory. [4]
3. Compress the directory into a ZIP file named `hw1_[STUDENT_ID].zip`.
4. Upload this ZIP file to CEIBA.

[4] Put every source code files in `inc/` and `src/`.

Submission Requirement 2/2

Let's say your student ID is `r01234567`.

```
hw1_r01234567.zip
└── hw1_r01234567
    ├── inc
    │   └── [*.h or *.hpp]
    ├── Makefile
    ├── model_init.txt
    ├── report.pdf
    └── src
        └── [*.c, *.cc or *.cpp]
```

Grading

Grading Method

Your training and testing program will be tested respectively. We will specify `100` as the number of iterations while testing your training program. And each of your program is allowed to run for 1 min.

Here's TA's environment.

Kernel	Linux 5.3.1-arch1-1-ARCH [5]
Processors	Intel Core i7-9700K (2 Cores)
RAM	4096 MB
GCC Version	9.1.0

[5] You can download the OVA file here if need be: `https://ppt.cc/fl7drx`. The user is *root* and its password is *ntudsp*

Grading Policy

File Format 20%

- ZIP file name
- directory name
- separated header and implementation files
- `Makefile`
- `model_init.txt`

Program 20%

- compiled and executed without error
- output files generated after execution

Report 10%

and bonus of extra 5% for the impressive ones

Accuracy 50%

30% for your training program and 20% for your testing program

Late Submission

Due on November 1, 2019

You are still allowed to submit after *2019-11-01 23:59*. The penalty for late submission is an exponential decay with decay rate 1.5%[6] of the maximum grade applicable for the assignment, for each hour that the assignment is late.

An assignment submitted more than 3 days after the deadline will have a grade of zero recorded for that assignment.

$$\text{SCORE}_{final}(hr) = \begin{cases} \text{SCORE}_{original} \times 0.985^{hr} & , \ hr \leq 72 \\ 0 & , \ hr > 72 \end{cases}$$

[6] less than 70% after 24 hrs, 48% for 48 hrs and 33% for 72 hrs

Please Note...

File Frmat

- All of your source code files should be placed under `inc/` and `src/`.
- `model_init.txt` must be submitted, even if it's not needed for your program.

Program

- Make sure your program can be compiled with the `Makefile` you submit.
- The paths in command-line arguments have to be relative path.
- Each of your program is allowed to run for 1 min.

Accuracy

- Make sure your training program saves models within time limit.

Should you have any questions, please read the FAQ[7] first.

[7] http://speech.ee.ntu.edu.tw/DSP2019Autumn/hw1/FAQ.html

DO NOT CHEAT

Any form of cheating, lying, or plagiarism will not be tolerated.