K-means 聚类

1.找到数据中每个实例最接近的聚类中心的函数。

ax. scatter(cluster2[:,0], cluster2[:,1], s=30, color='g', label='Cluster 2')

```
In [1]:
          import numpy as np
          import pandas as pd
          import matplotlib.pyplot as plt
          import seaborn as sb
          from scipy.io import loadmat
 In [2]:
          def find_closest_centroids(X, centroids):
              m = X. shape[0]
              k = centroids. shape[0]
              idx = np. zeros(m)
              for i in range(m):
                  min_dist = 1000000
                  for j in range(k):
                      dist = np. sum((X[i,:] - centroids[j,:]) ** 2) # **2一平方
                      if dist < min_dist:</pre>
                          min_dist = dist
                          idx[i] = j
              return idx
 In [3]:
          data = loadmat('data/machine-learning-ex7/ex7/ex7data2.mat')
          X = data['X']
          initial_centroids = initial_centroids = np. array([[3, 3], [6, 2], [8, 5]])
          idx = find_closest_centroids(X, initial_centroids)
          idx[0:3]
 Out[3]: array([0., 2., 1.])
 In [4]:
          data2 = pd. DataFrame(data.get('X'), columns=['X1', 'X2'])
          data2. head()
 Out[4]:
                 X1
                         X2
          0 1.842080 4.607572
          1 5.658583 4.799964
          2 6.352579 3.290854
          3 2.904017 4.612204
          4 3.231979 4.939894
 In [5]:
          sb. set(context="paper", style="white") #绘图风格
          sb. lmplot(x='X1', y='X2', data=data2, fit_reg=False) #sb. lmplot:多图叠加,一个x多个y
          plt.show()
          Ŋ 3
          def compute_centroids(X, idx, k):
              m, n = X. shape
              centroids = np. zeros((k, n))
              for i in range(k):
                  indices = np. where(idx == i) #只有条件 (condition),没有x和y,则输出满足条件(即非0)元素的坐标
                  centroids[i,:] = (np. sum(X[indices,:], axis=1) / len(indices[0])).ravel()
                  #[i,:]第一维度元素保留到i,保留第二个维度所有元素,
              return centroids
          compute_centroids(X, idx, 3)
 Out[7]: array([[2.42830111, 3.15792418],
                 [5.81350331, 2.63365645],
                [7.11938687, 3.6166844]])
 In [8]:
          #为了运行算法,只需要在将样本分配给最近的簇并重新计算簇的聚类中心。
          def run_k_means(X, initial_centroids, max_iters):
              m, n = X. shape
              k = initial_centroids.shape[0]
              idx = np. zeros(m)
              centroids = initial_centroids
              for i in range(max_iters):
                  idx = find_closest_centroids(X, centroids)
                  centroids = compute_centroids(X, idx, k)
              return idx, centroids
 In [9]:
          idx, centroids = run_k_means(X, initial_centroids, 10)
          centroids
 Out[9]: array([[1.95399466, 5.02557006],
                 [3.04367119, 1.01541041],
                 [6.03366736, 3.00052511]])
In [10]:
          cluster1 = X[np. where(idx == 0)[0], :]
          cluster2 = X[np. where(idx == 1)[0], :]
          cluster3 = X[np. where(idx == 2)[0], :]
          fig, ax = plt. subplots(figsize=(12, 8))
          ax. scatter(cluster1[:,0], cluster1[:,1], s=30, color='r', label='Cluster 1')
```

```
ax. scatter(cluster3[:,0], cluster3[:,1], s=30, color='b', label='Cluster 3')
          ax.legend()
          plt. show()

    Cluster 1

                                                                                         Cluster 2

    Cluster 3

In [11]:
          #初始化聚类中心的过程可以影响算法的收敛,因此,创建一个选择随机样本并将其用作初始聚类中心的函数。
          def init_centroids(X, k):
             m, n = X. shape
             centroids = np. zeros((k, n))
             idx = np. random. randint(0, m, k)
             for i in range(k):
                 centroids[i,:] = X[idx[i],:]
             return centroids
In [12]:
          init_centroids(X, 3)
Out[12]: array([[1.82975993, 4.59657288],
               [0.10511804, 4.72916344],
[1.70725482, 4.04231479]])
        2.将K-means应用于图像压缩。
         使用聚类来找到最具代表性的少数颜色,并使用聚类分配将原始的24位颜色映射到较低维的颜色空间。
In [13]:
          from IPython.display import Image
          Image(filename='data/machine-learning-ex7/ex7/bird_small.png')
Out[13]:
In [14]: #像素点数值
          image_data = loadmat('data/machine-learning-ex7/ex7/bird_small.mat')
[226, 186, 110],
                 [ 14, 15, 13],
                 [ 13, 15, 12],
[ 12, 14, 12]],
                [[230, 193, 119], [224, 192, 120],
                 [226, 192, 124],
                 [ 16, 16, 13],
[ 14, 15, 10],
                 [ 11, 14, 9]],
                [[228, 191, 123], [228, 191, 121],
                 [220, 185, 118],
                 [ 14, 16, 13],
                 [ 13, 13, 11],
                 [ 11, 15, 10]],
                ...,
                 [[ 15, 18, 16],
                 [ 18, 21, 18],
                 [ 18, 19, 16],
                 ...,
[ 81, 45, 45],
                 [ 70, 43, 35],
                 [ 72, 51, 43]],
                 [[ 16, 17, 17],
                 [ 17, 18, 19],
                 [ 20, 19, 20],
                 [ 80, 38, 40],
                 [ 68, 39, 40],
                 [ 59, 43, 42]],
                [[ 15, 19, 19],
                 [ 20, 20, 18],
                 [ 18, 19, 17],
                 [ 65, 43, 39],
                 [ 58, 37, 38],
                 [ 52, 39, 34]]], dtype=uint8)}
In [15]:
          A = image_data['A']
          A. shape
Out[15]: (128, 128, 3)
In [16]:
          #预处理
          # normalize value ranges
```

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A = A / 255.
          # reshape the array
          X = np. reshape(A, (A. shape[0] * A. shape[1], A. shape[2])) #在不改变数据内容的情况下,改变一个数组的格式,参数及返回值
Out[16]: (16384, 3)
In [17]:
          # randomly initialize the centroids
          initial_centroids = init_centroids(X, 16)
          # run the algorithm
          idx, centroids = run_k_means(X, initial_centroids, 10)
          \# get the closest centroids one last time
          idx = find_closest_centroids(X, centroids)
          # map each pixel to the centroid value
          X_recovered = centroids[idx.astype(int),:] #astype: 转换数组的数据类型。
          X_recovered. shape
Out[17]: (16384, 3)
In [18]:
          # reshape to the original dimensions
          X_recovered = np. reshape(X_recovered, (A. shape[0], A. shape[1], A. shape[2]))
          X_recovered. shape
Out[18]: (128, 128, 3)
In [19]:
          plt.imshow(X recovered)
          plt. show()
          #对图像进行了压缩,但图像的主要特征仍然存在,这就是K-means。
          60
                20 40 60 80 100
         下面用scikit-learn实现K-means。
In [20]:
          from skimage import io
          # cast to float, you need to do this otherwise the color would be weird after clustring
          pic = io. imread('data/machine-learning-ex7/ex7/bird_small.png') /255.
          io. imshow(pic)
          plt.show()
          100
          120
          data = pic.reshape(128*128, 3)
          data. shape
Out[21]: (16384, 3)
In [22]:
          from sklearn.cluster import KMeans#导入kmeans库
          model = KMeans(n_clusters=16, n_init=100)
          model. fit (data)
Out[22]: KMeans(n_clusters=16, n_init=100)
In [23]:
          centroids = model.cluster_centers_ #KMeans.cluster_centers_返回中心的坐标
          print(centroids. shape)
          C = model. predict(data)
          print(C. shape)
          print(centroids[C]. shape)
          (16, 3)
          (16384,)
          (16384, 3)
In [24]:
          compressed_pic = centroids[C].reshape((128, 128, 3))
In [25]:
          fig, ax = plt. subplots(1, 2)
          ax[0]. imshow(pic)
          ax[1]. imshow(compressed_pic)
          plt.show()
```

Principal component analysis (主成分分析)

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```
In [26]:
          data = loadmat('data/machine-learning-ex7/ex7/ex7datal.mat')
[4.52787538, 5.8541781],
                [2.65568187, 4.41199472],
                [2.76523467, 3.71541365],
                [2.84656011, 4.17550645],
                [3.89067196, 6.48838087],
                [3.47580524, 3.63284876],
                [5.91129845, 6.68076853],
                [3.92889397, 5.09844661],
                [4.56183537, 5.62329929],
                [4.57407171, 5.39765069],
                [4.37173356, 5.46116549],
                [4.19169388, 4.95469359],
                [5. 24408518, 4. 66148767],
                [2.8358402 , 3.76801716],
                [5.63526969, 6.31211438],
                [4.68632968, 5.6652411],
                [2.85051337, 4.62645627],
                [5.1101573 , 7.36319662],
                [5.18256377, 4.64650909],
                [5.70732809, 6.68103995],
                [3.57968458, 4.80278074],
                [5.63937773, 6.12043594],
                [4.26346851, 4.68942896],
                [2.53651693, 3.88449078],
                [3.22382902, 4.94255585],
                [4.92948801, 5.95501971],
                [5.79295774, 5.10839305],
                [2.81684824, 4.81895769],
                [3.88882414, 5.10036564],
                [3.34323419, 5.89301345],
                [5.87973414, 5.52141664],
                [3.10391912, 3.85710242],
                [5. 33150572, 4. 68074235],
                [3.37542687, 4.56537852],
                [4.77667888, 6.25435039],
                [2.6757463 , 3.73096988],
                [5.50027665, 5.67948113],
                [1.79709714, 3.24753885],
                [4.3225147 , 5.11110472],
                [4.42100445, 6.02563978],
                [3.17929886, 4.43686032],
                [3.03354125, 3.97879278],
                [4.6093482 , 5.879792 ],
                [2.96378859, 3.30024835],
                [3.97176248, 5.40773735],
                [1.18023321, 2.87869409],
                [1.91895045, 5.07107848],
                [3.95524687, 4.5053271],
                [5.11795499, 6.08507386]])}
In [27]:
          X = data['X']
          fig, ax = plt. subplots(figsize=(12, 8))
          ax. scatter (X[:, 0], X[:, 1])
          plt.show()
In [28]:
          #PCA的算法相当简单。 在确保数据被归一化之后,输出仅仅是原始数据的协方差矩阵的奇异值分解。
          def pca(X):
             #均值归一化
             X = (X - X. mean()) / X. std()
             #计算协方差矩阵
             X = np. matrix(X)
             cov = (X. T * X) / X. shape[0]
             奇异值分解SVD, U叫做左奇异值, S叫做奇异值, V叫做右奇异值。
             其中s是对矩阵a的奇异值分解。s除了对角元素不为0,其他元素都为0,并且对角元素从大到小排列。
             s中有n个奇异值,一般排在后面的比较接近0,所以仅保留比较大的r个奇异值。
             U, S, V = np. linalg. svd(cov)
             return U, S, V
In [29]:
          U, S, V = pca(X)
          U, S, V
Out[29]: (matrix([[-0.79241747, -0.60997914],
                 [-0.60997914, 0.79241747]]),
          array([1.43584536, 0.56415464]),
          matrix([[-0.79241747, -0.60997914],
                 [-0.60997914, 0.79241747]]))
In [30]:
          #现在我们有主成分(矩阵U),我们可以用这些来将原始数据投影到一个较低维的空间中。
          #对于这个任务,我们将实现一个计算投影并且仅选择顶部K个分量的函数,有效地减少了维数。
          def project_data(X, U, k):
             U_reduced = U[:,:k]
             return np. dot(X, U_reduced)
In [31]:
         Z = project_data(X, U, 1)
          Z
```

```
Out[31]: matrix([[-4.74689738],
                    -7.15889408],
                   [-4.79563345],
                   [-4.45754509],
                   [-4.80263579],
                   [-7.04081342],
                    [-4.97025076],
                    [-8.75934561],
                    [-6.2232703],
                    [-7.04497331],
                    [-6.91702866],
                    [-6.79543508],
                    [-6.3438312],
                    [-6.99891495],
                    [-4.54558119],
                    [-8.31574426],
                    -7.16920841],
                    [-5.08083842],
                    [-8.54077427],
                    [-6.94102769],
                    [-8.5978815],
                    [-5. 76620067],
                    -8.2020797 ],
                    [-6.23890078],
                    [-4.37943868],
                    [-5.56947441],
                    [-7.53865023],
                    [-7.70645413],
                    [-5.17158343],
                    [-6.19268884],
                    -6.24385246],
                    [-8.02715303],
                    [-4.81235176],
                    [-7.07993347],
                    [-5.45953289],
                   [-7.60014707],
                   [-4.39612191],
                    [-7.82288033],
                    [-3.40498213],
                    [-6.54290343],
                    -7.17879573],
                    [-5.22572421],
                    [-4.83081168],
                    [-7.23907851],
                   [-4.36164051],
                    [-6.44590096],
                    [-2.69118076],
                   [-4.61386195],
                   [-5.88236227],
                   [-7.76732508]]
In [32]:
           #也可以通过反向转换步骤来恢复原始数据。
           def recover_data(Z, U, k):
               U_{reduced} = U[:,:k]
               return np. dot(Z, U_reduced. T)
In [33]:
           X_recovered = recover_data(Z, U, 1)
           X_recovered
 Out[33]: matrix([[3.76152442, 2.89550838],
                   [5.67283275, 4.36677606],
                   [3.80014373, 2.92523637],
                   [3.53223661, 2.71900952],
                   [3.80569251, 2.92950765],
                   [5.57926356, 4.29474931],
                   [3.93851354, 3.03174929],
                   [6.94105849, 5.3430181],
                   [4.93142811, 3.79606507],
                   [5.58255993, 4.29728676],
                   [5.48117436, 4.21924319],
                   [5. 38482148, 4. 14507365],
                   [5.02696267, 3.8696047],
                   [5.54606249, 4.26919213],
                    [3.60199795, 2.77270971]
                   [6.58954104, 5.07243054],
                   [5.681006 , 4.37306758],
                   [4.02614513, 3.09920545],
                   [6.76785875, 5.20969415],
                   [5.50019161, 4.2338821],
                   [6.81311151, 5.24452836],
                   [4.56923815, 3.51726213],
                   [6.49947125, 5.00309752],
                   [4.94381398, 3.80559934],
                   [3.47034372, 2.67136624],
                   [4.41334883, 3.39726321],
                   [5. 97375815, 4. 59841938],
                   [6.10672889, 4.70077626],
                   [4.09805306, 3.15455801],
                   [4.90719483, 3.77741101],
                   [4.94773778, 3.80861976],
                   [6.36085631, 4.8963959],
                   [3.81339161, 2.93543419],
                   [5.61026298, 4.31861173],
                   [4. 32622924, 3. 33020118],
                   [6.02248932, 4.63593118],
                   [3.48356381, 2.68154267],
                   [6.19898705, 4.77179382],
                   [2.69816733, 2.07696807],
                   [5.18471099, 3.99103461],
                   [5.68860316, 4.37891565],
                   [4.14095516, 3.18758276],
                   [3.82801958, 2.94669436],
                   [5.73637229, 4.41568689],
                   [3.45624014, 2.66050973],
                   [5.10784454, 3.93186513],
                   [2.13253865, 1.64156413],
                   [3.65610482, 2.81435955],
                   [4.66128664, 3.58811828],
                   [6.1549641 , 4.73790627]])
In [34]:
           fig, ax = plt. subplots(figsize=(12, 8))
           ax. scatter(list(X_recovered[:, 0]), list(X_recovered[:, 1]))
           plt.show()
           #第一主成分的投影轴基本上是数据集中的对角线,当将数据减少到一维时,失去了该对角线周围的变化,所以在再现中,一切都沿着该对角线。
```

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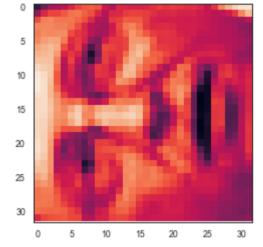
44

56

67
```

将PCA应用于脸部图像。 通过使用相同的降维技术,我们可以使用比原始图像少得多的数据来捕获图像的"本质"。

In [37]:
 face = np. reshape(X[3,:], (32, 32))
 plt. imshow(face)
 plt. show()



```
In [38]: #在面数据集上运行PCA,并取得前100个主要特征。
U, S, V = pca(X)
Z = project_data(X, U, 100)
Z
```

```
Out[38]: matrix([[ 526.09608833, 734.37008142, 194.48322788, ..., -19.27422565, -3.22314155, 20.93551538], [ 304.5906028, 493.0633805, -162.10424193, ..., -20.94839919, 17.86358442, -8.14045979], [ -389.99893833, 600.20010851, -293.91694459, ..., -27.86998851, 48.74829475, 17.98452065], ..., [ 487.55926046, 430.86037345, 490.71749378, ..., -31.76395627, 23.77770829, 51.74592358], [ 1358.99575656, 402.85437502, -136.10305216, ..., -10.45305753, -2.76084233, 2.96467067], [ 372.01599145, 360.59923883, 105.10564415, ..., -48.29644614, -8.75071522, -30.24094867]])
```

In [39]: #尝试恢复原来的结构并再次渲染
X_recovered = recover_data(Z, U, 100)
face = np.reshape(X_recovered[3,:], (32, 32))
plt.imshow(face)
plt.show()

