

DNA_06.2

August 29, 2016

1 Dynamic Network Analysis of Enron Email Network Comparisons

```
In [1]: import pandas as pd
import numpy as np
import networkx as nx
import seaborn as sns
import matplotlib.pyplot as plt
import scipy as sc
import random
from scipy.signal import *
from numpy.linalg import *
from sklearn.decomposition import *
from sklearn.metrics import mean_squared_error
from sklearn import ensemble
#plotting parameters
%matplotlib inline
sns.set(style="whitegrid", color_codes=True, context='paper')

In [2]: from matplotlib import rcParams
rcParams['font.family'] = 'serif'
rcParams['font.sans-serif'] = ['CMU Serif']
rcParams['font.weight']=['heavy']
import matplotlib.pyplot as plt

In [4]: plt.rc('axes', grid=False, titlesize='large', labelsizsize='large',labelweight
plt.rc('lines', linewidth=4)
plt.rc('figure', figsize = (12,6),titlesize='large',titleweight='black')
plt.rc('font', weight='heavy', size=11)
plt.rc('grid',linewidth=5)

In [7]: sns.set_palette(sns.cubehelix_palette(10, hue=0.3, reverse=True, rot=-0.55,
```

2 Get attribute data

```
In [71]: lap = pd.read_excel('attribute_data/lap_att.xlsx')
adj = pd.read_excel('attribute_data/adj_att.xlsx')
mod = pd.read_excel('attribute_data/mod_att.xlsx')
```

```
In [72]: lap.head()
```

```
Out [72]:
```

	AvgDeg	AvgBet	AvgClo	AvgLoad	AvgKatz	AvgDensity	AvgAlgCon
0	0.475524	1.000000	0.810523	0.475524	0.267944	-0.318532	1.0
1	-0.027972	0.250903	0.509903	-0.027972	0.069435	-0.419219	1.0
2	0.388112	1.000000	0.785809	0.388112	0.282044	-0.622808	1.0
3	1.000000	1.000000	1.000000	1.000000	1.000000	1.000000	1.0
4	0.559441	1.000000	0.835787	0.559441	0.423789	-0.054825	1.0

	AvgClustCoff	AvgEig	InstAmp	...	StatRat	MeanCurv	\
0	-1.000000	0.177194	0.679834	...	0.407864	-0.242635	
1	-0.000165	-0.044891	0.305093	...	0.570795	-0.269438	
2	-1.000000	-0.127797	0.450396	...	0.836955	-0.337965	
3	-1.000000	1.000000	1.000000	...	-1.000000	1.000000	
4	-1.000000	0.403160	0.860240	...	0.074177	0.108395	

	SubgraphStat	1-Zeta	LogKPCARatioChg	NormNMFRatioChg	NormFabel	\
0	-1.000000	1.000000	-0.015620	-1.000000	-0.543745	
1	0.766117	-0.766117	-0.059551	-0.573875	-0.352246	
2	0.873376	-0.873376	0.012093	-0.780922	-0.276008	
3	0.421859	-0.421859	-0.079774	-0.869723	-1.000000	
4	0.763599	-0.763599	0.019315	-0.673657	-0.702049	

	NRMS	RMS	Emergence
0	0.000000	0.722464	0.000000
1	0.134441	0.551228	-0.205409
2	0.045739	0.604070	0.390743
3	0.189878	0.887236	1.000000
4	0.126025	0.688637	-0.972473

```
[5 rows x 33 columns]
```

```
In [73]: coldrop = lap.columns[:9]
```

```
In [74]: lap.drop(coldrop, axis=1, inplace=True)
mod.drop(coldrop, axis=1, inplace=True)
adj.drop(coldrop, axis=1, inplace=True)
```

```
In [75]: lap.head()
```

```
Out [75]:
```

	InstAmp	InstPhase	InstFreq	Power	dInstAmp	d2InstAmp	InstAcc
0	0.679834	0.535455	-1.000000	0.021345	-0.565983	-0.539313	-0.707491
1	0.305093	-0.578269	-0.393695	-0.364336	-0.587010	-0.455499	0.708190
2	0.450396	0.214700	-0.052958	-0.367204	-0.566478	-0.483079	-0.006052
3	1.000000	-0.207114	1.000000	1.000000	-0.560284	1.000000	0.103005
4	0.860240	0.812100	-0.845407	0.340239	-1.000000	0.122943	-0.161020

	cosInstPhase	A_wt_IF	A_wt_IP	...	StatRat	MeanCurv	\
0	0.249334	-1.000000	0.796844	...	0.407864	-0.242635	

1	-0.261313	-0.235448	-0.838336	...	0.570795	-0.269438
2	-0.457223	0.015942	0.204171	...	0.836955	-0.337965
3	1.000000	1.000000	-0.359857	...	-1.000000	1.000000
4	0.560408	-0.708792	0.771960	...	0.074177	0.108395

	SubgraphStat	1-Zeta	LogKPCARatioChg	NormNMFRatioChg	NormFabel	\
0	-1.000000	1.000000	-0.015620	-1.000000	-0.543745	
1	0.766117	-0.766117	-0.059551	-0.573875	-0.352246	
2	0.873376	-0.873376	0.012093	-0.780922	-0.276008	
3	0.421859	-0.421859	-0.079774	-0.869723	-1.000000	
4	0.763599	-0.763599	0.019315	-0.673657	-0.702049	

	NRMS	RMS	Emergence
0	0.000000	0.722464	0.000000
1	0.134441	0.551228	-0.205409
2	0.045739	0.604070	0.390743
3	0.189878	0.887236	1.000000
4	0.126025	0.688637	-0.972473

[5 rows x 24 columns]

In [76]: mod.max()

```
Out [76]: InstAmp          1.000000
InstPhase          1.000000
InstFreq           1.000000
Power              1.000000
dInstAmp           1.000000
d2InstAmp          1.000000
InstAcc            1.000000
cosInstPhase       1.000000
A_wt_IF            1.000000
A_wt_IP            1.000000
PowerSpecDen       1.000000
ResDist            1.000000
ZeroCrossRate      1.000000
LogSpecCentroid    1.000000
StatRat            1.000000
MeanCurv          1.000000
SubgraphStat       1.000000
1-Zeta             1.000000
LogKPCARatioChg    1.000000
NormNMFRatioChg    1.000000
NormFabel          1.000000
NRMS               0.193777
RMS                0.745719
Emergence          1.000000
dtype: float64
```

```
In [77]: months = ['Nov98', 'Dec98', 'jan_99', 'feb_99', 'mar_99', 'apr_99', 'may_99',
                  'nov_99', 'dec_99', 'jan_2k', 'feb_2k', 'mar_2k', 'apr_2k', 'may_2k',
                  'nov_2k', 'dec_2k', 'jan_2k1', 'feb_2k1', 'mar_2k1', 'apr_2k1', 'may_2k1',
                  'oct_2k1', 'nov_2k1', 'dec_2k1', 'jan_2k2', 'feb_2k2', 'mar_2k2']
```

```
In [78]: att_only = lap.join(adj,rsuffix='_Adj').join(mod,rsuffix='_Mod')
        att_only.sortlevel(axis=1, inplace=True);
```

```
In [79]: att_only.head()
```

```
Out [79]:
```

	1-Zeta	1-Zeta_Adj	1-Zeta_Mod	A_wt_IF	A_wt_IF_Adj	A_wt_IF_Mod	\
0	1.000000	1.000000	1.000000	-1.000000	-0.065973	-0.578144	
1	-0.766117	-0.500770	-0.562061	-0.235448	0.000403	-0.270839	
2	-0.873376	-0.808032	-0.688113	0.015942	-0.065973	-0.578144	
3	-0.421859	-0.009407	0.339333	1.000000	-0.065973	-0.578144	
4	-0.763599	-0.427517	-0.195048	-0.708792	0.101108	-0.578144	

	A_wt_IP	A_wt_IP_Adj	A_wt_IP_Mod	Emergence	...	\
0	0.796844	0.402595	0.448481	0.000000	...	
1	-0.838336	-1.000000	-1.000000	-0.205409	...	
2	0.204171	1.000000	0.448481	0.390743	...	
3	-0.359857	-0.245437	0.448481	1.000000	...	
4	0.771960	-0.359158	0.448481	-0.972473	...	

	ZeroCrossRate_Mod	cosInstPhase	cosInstPhase_Adj	cosInstPhase_Mod	\
0	-1.000000	0.249334	0.912276	0.869867	
1	-0.904762	-0.261313	-0.339427	-0.038949	
2	-0.952381	-0.457223	-0.597742	0.009933	
3	-0.952381	1.000000	0.795405	0.243197	
4	-0.952381	0.560408	0.741131	1.000000	

	d2InstAmp	d2InstAmp_Adj	d2InstAmp_Mod	dInstAmp	dInstAmp_Adj	\
0	-0.539313	-0.741787	-0.070128	-0.565983	0.375510	
1	-0.455499	-0.811824	0.594556	-0.587010	0.465306	
2	-0.483079	-0.602222	-0.070128	-0.566478	0.375510	
3	1.000000	1.000000	-0.070128	-0.560284	0.375510	
4	0.122943	0.342754	-0.070128	-1.000000	-0.107077	

	dInstAmp_Mod
0	0.197628
1	0.007620
2	0.197628
3	0.197628
4	0.197628

[5 rows x 72 columns]

```
In [106]: snr_lap = lap.mean()/lap.std()
          snr_mod = mod.mean()/mod.std()
          snr_adj = adj.mean()/adj.std()
```

```

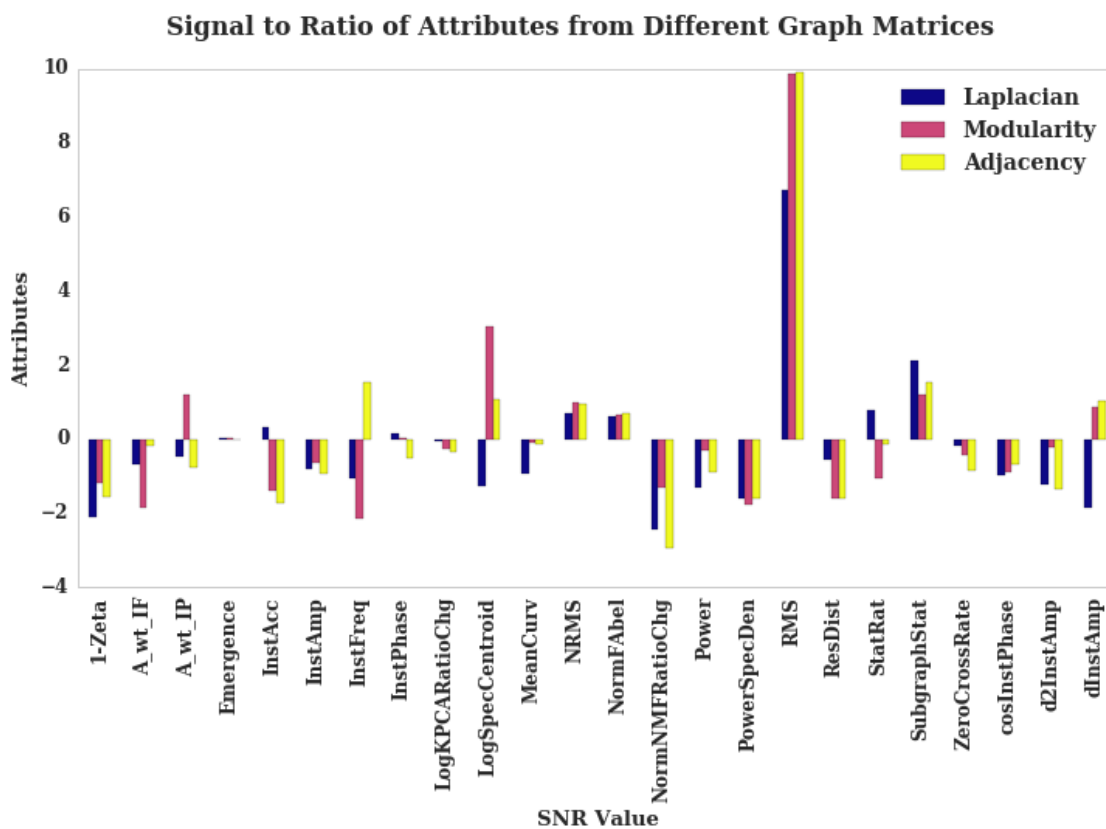
In [111]: snr_df = pd.DataFrame([snr_lap, snr_mod, snr_adj])

In [114]: cname = ['Laplacian', 'Modularity', 'Adjacency']

In [129]: snr_df = snr_df.T
           snr_df.columns = cname
           snr_df.sortlevel(inplace=True)

In [248]: snr_df.plot.bar(figsize=(12,6), fontsize=12, cmap='plasma')
           plt.suptitle("Signal to Ratio of Attributes from Different Graph Matrices")
           plt.legend(fontsize=14)
           plt.xlabel('SNR Value')
           plt.ylabel('Attributes')
           plt.savefig('images/snr_allatt_3mat.png')

```



```

In [247]: mad_lap = lap.mad()
           mad_adj = adj.mad()
           mad_mod = mod.mad()

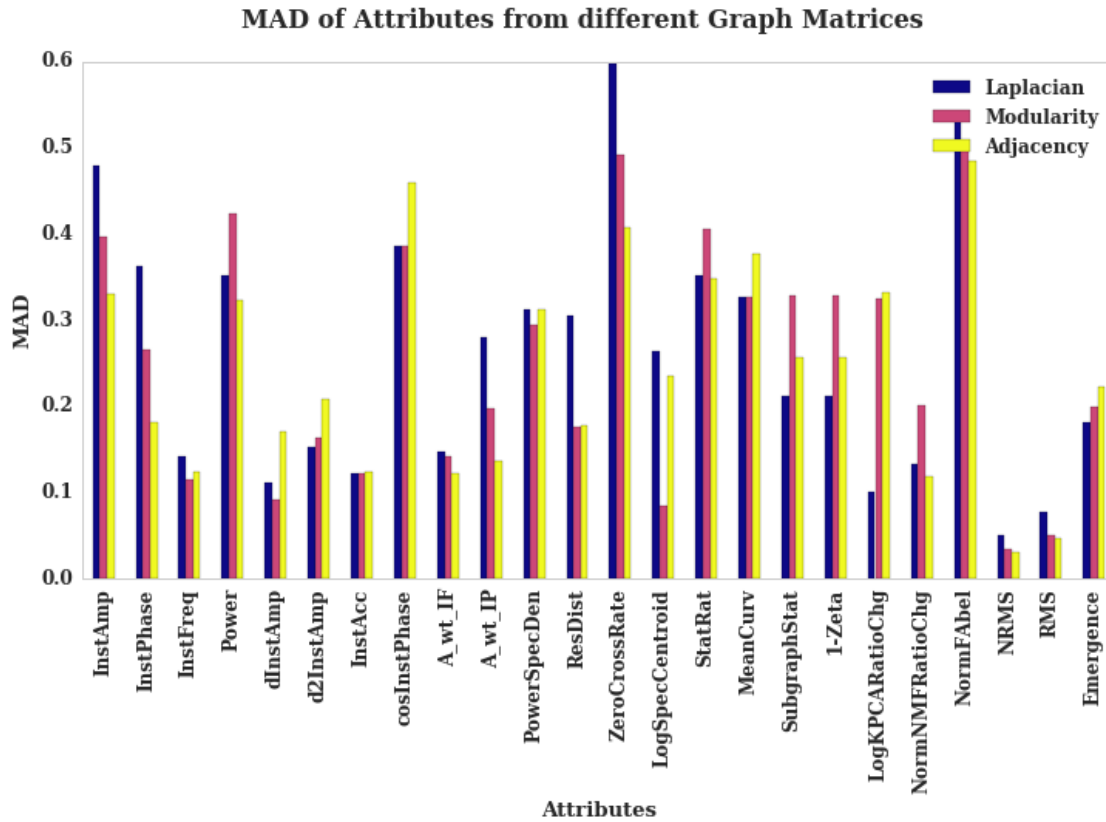
           mad_all = pd.DataFrame([mad_lap, mad_mod, mad_adj]).T
           mad_all.columns = ['Laplacian', 'Modularity', 'Adjacency']

```

```

mad_all.plot.bar(fontsize=12, cmap='plasma',figsize=(12,6))
plt.suptitle('MAD of Attributes from different Graph Matrices', fontsize=
plt.xlabel('Attributes')
plt.ylabel('MAD')
plt.legend(loc=1,fontsize=12)
plt.savefig('images/mad_allatt_3mat.png')

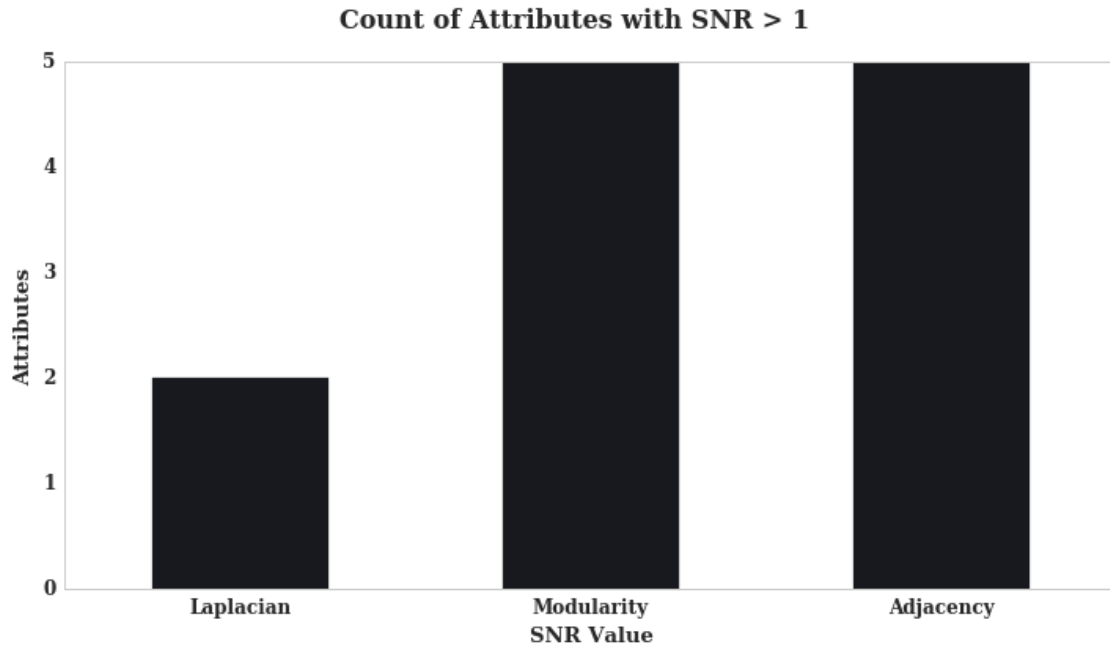
```



```

In [232]: snr_df[snr_df > 1].count().plot.bar(rot=0, fontsize=12)
plt.suptitle("Count of Attributes with SNR > 1", fontsize=16)
plt.xlabel('SNR Value')
plt.ylabel('Attributes')
plt.savefig('images/snrcount.png')

```



```
In [164]: mad_all.max()/2
```

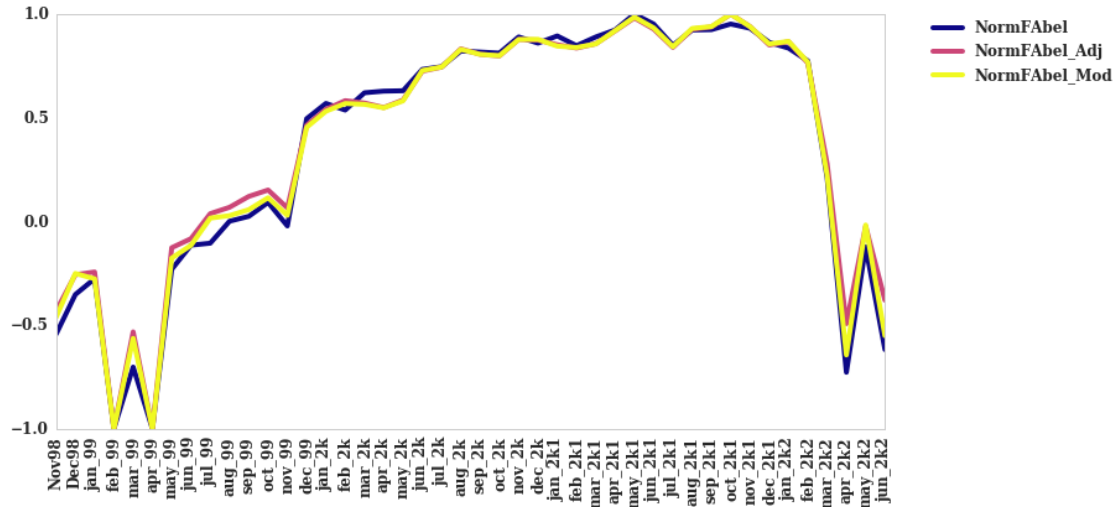
```
Out[164]: Laplacian      0.299199
          Modularity    0.252281
          Adjacency     0.242036
          dtype: float64
```

```
In [168]: att_only.columns[36:39]
```

```
Out[168]: Index(['NormFLabel', 'NormFLabel_Adj', 'NormFLabel_Mod'], dtype='object')
```

```
In [187]: att_only.iloc[:,36:39].plot.line(fontsize=12,cmap='plasma',rot=90)
          plt.xticks(np.arange(len(months)), months);
          plt.legend(fontsize=12, bbox_to_anchor=(1.05, 1), loc=2, borderaxespad=0.)
```

```
Out[187]: <matplotlib.legend.Legend at 0x7f63f26db7f0>
```

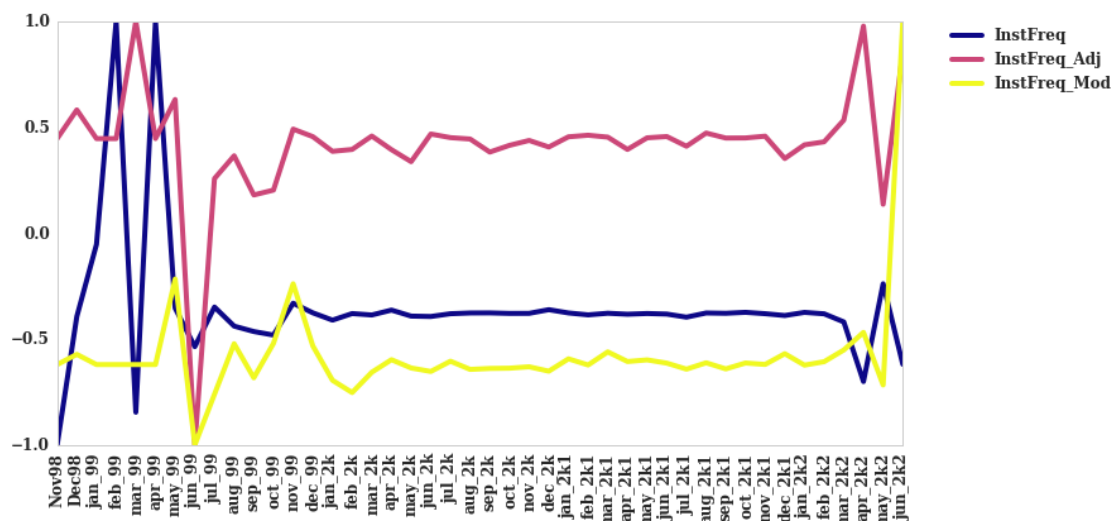


```
In [175]: att_only.columns[18:21]
```

```
Out[175]: Index(['InstFreq', 'InstFreq_Adj', 'InstFreq_Mod'], dtype='object')
```

```
In [186]: att_only.iloc[:,18:21].plot.line(fontsize=12,cmap='plasma', rot=90)
plt.xticks(np.arange(len(months)), months);
plt.legend(fontsize=12, bbox_to_anchor=(1.05, 1), loc=2, borderaxespad=0.)
```

```
Out[186]: <matplotlib.legend.Legend at 0x7f63f26ee080>
```



```
In [195]: from sklearn.preprocessing import *
```



```

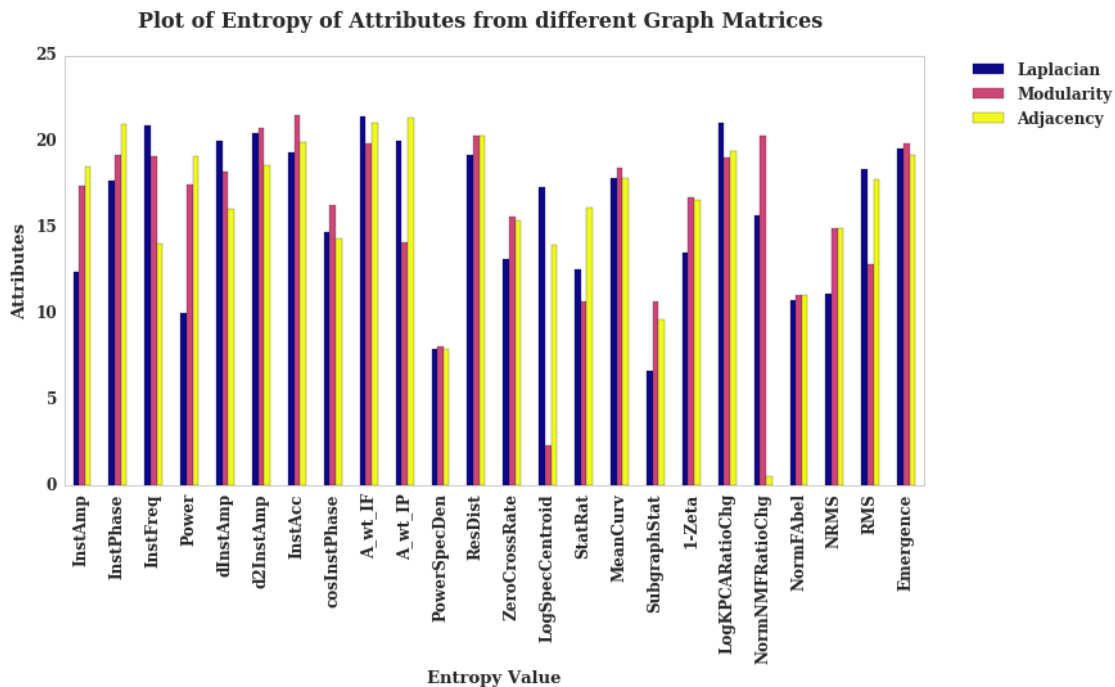
In [201]: px_lap = lap.apply(lambda x: minmax_scale(x, feature_range=[0,1]))
          px_mod = mod.apply(lambda x: minmax_scale(x, feature_range=[0,1]))
          px_adj = adj.apply(lambda x: minmax_scale(x, feature_range=[0,1]))

In [202]: ent_lap = -1* np.sum(px_lap*np.log2(px_lap))
          ent_mod = -1* np.sum(px_mod*np.log2(px_mod))
          ent_adj = -1* np.sum(px_adj*np.log2(px_adj))

In [203]: entropy_df = pd.DataFrame([ent_lap,ent_mod,ent_adj]).T
          entropy_df.columns = ['Laplacian', 'Modularity', 'Adjacency']

In [243]: entropy_df.plot.bar(figsize=(12,6), fontsize=12, cmap='plasma')
          plt.legend(fontsize=12, bbox_to_anchor=(1.05, 1), loc=2, borderaxespad=0)
          plt.suptitle("Plot of Entropy of Attributes from different Graph Matrices")
          plt.xlabel('Entropy Value')
          plt.ylabel('Attributes')
          plt.savefig('images/entropy.png')

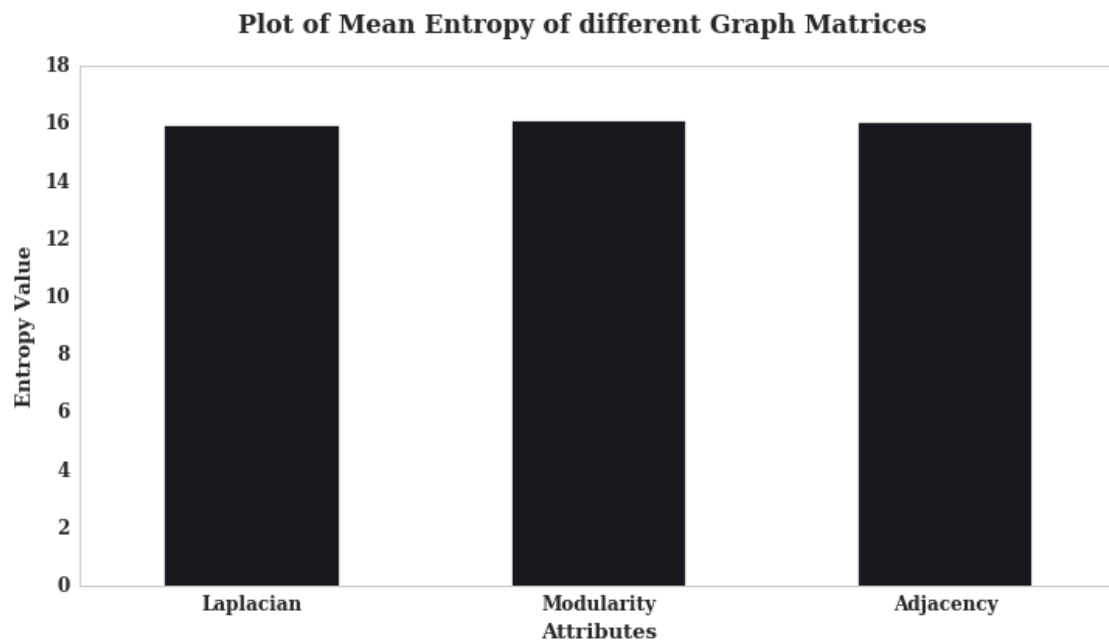
```



```

In [234]: entropy_df.mean().plot.bar(legend=False, fontsize=12, rot=0)
          plt.suptitle("Plot of Mean Entropy of different Graph Matrices", fontsize=12)
          plt.ylabel('Entropy Value')
          plt.xlabel('Attributes')
          plt.savefig('images/entropy_mean.png')

```



In []: