

### **Tasks for 29/08/2022:**

**\*Root finding 2:** Solve the equation  $f(x) = x^3 - 0.165x^2 + 3.993 \times 10^{-4}$  using Newton-Raphson method for a given error limit of  $e=0.0001$ .

- 1) With initial guess of  $x(0) = 0.05$ .
- 2) With initial guess of  $x(0)=0.11$ ,

Why does the 2<sup>nd</sup> case do not offer any solution? You may start of by plotting the function.

- 3) Can you find another initial guess which will lead to no solution? Explain why.
- 4) Now take  $e = [0.1 \ 0.01 \ 0.001 \ 0.0001 \ 0.00001 \ 0.000001 \ \dots]$  and plot  $e$  vs the number of steps needed for convergence ( $N$ ).

**Root finding 3:** Now find the roots for the polynomial of last problem (root finding 2) by method of bisection. See if choosing  $x(0)=0.11$  as one of the initial bound work. Compare the number of iterations it takes to converge to a root. Also check  $x= 1.8$  as the starting point

**\*Newton-Raphson for finding reciprocal of a number:** The reciprocal of a real number  $a$  is defined as a zero of the function:  $f(x) = 1/x - a$ .

The function converges for an initial estimate in the range  $0 < x_0 < 2/a$ .

a) Write a matlab code that will be able to find the reciprocal of any real number using Newton-Raphson method. Do not set an error limit. Rather let the code run for a fixed number of 50 iterations

b) Plot the error propagation (by comparing the outcome of the code and  $1/a$ ) and plot is as a function of the iteration

**\*Diagonal dominance of matrix:** Consider the square matrices:

$A = [-6 \ 2 \ 1 \ 2 \ 1;$

$3 \ 8 \ -4 \ 1 \ 0;$

$-1 \ 1 \ 4 \ 10 \ 1;$

```
3 -4 1 9 2;  
2 0 1 3 10]
```

```
B=[18 3 6 -3;  
9 13 -5 2;  
-3 -2 4 9;  
6 0 11 3]
```

Write a code to see if the matrices A and B are diagonally dominant. In case if they are not, make the code display a message like “Not strictly diagonally dominant on row (row number)”