#### ECE653

# Software Testing, Quality Assurance, and Maintenance Assignment 2 (50 Points), Version 4

Instructor: Patrick Lam Release Date: June 14, 2022 Modified: June 21, 2022

Version history: v2: made some questions not-to-be-handed-in; v3: note on sym.py in Q4; v4: use crowdmark.

Due: July 4, 2022 Submit: An electronic copy on GitLab

Source code and test cases for the assignment will be released in the skeleton repository at https://git.uwaterloo.ca/stqam-1225/skeleton.

I expect each of you to do the assignment independently. I will follow UW's Policy 71 for all cases of plagiarism.

#### **Submission Instructions:**

Please read the following instructions carefully.

Submit code by pushing your changes to the main branch of your GitLab repository in directory a2/. Make sure to use a web browser to check that your changes have been committed! The submission must contain the following:

- a user.yml file with your UWaterloo user information (-5 points if your user.yml is incorrect);
- a directory a2q3 that includes your code for Question 3 (optional bonus); and
- a directory wlang that includes your code for Question 4.

Submit text (Q1, Q2) on crowdmark.

After submission, review your submissions on GitLab web interface to make sure you have uploaded the right files/versions.

You can push changes to the repository before and after the deadline. If you want to use late days, push a README.md to the a2 directory with "Submission date: 5 July 2022" (or 6 July) and I will take the state of the git repo as of a few minutes after 5 July 23:59 (or 6 July).

## Question 1 (10 points)

Consider the following program Prog1:

```
havoc x, y;
   if x + y > 15 then {
     x = x + 7;
 4
     y = y - 12
 5
   else {
 6
     y = y + 10;
 7
     x = x - 2;
8
9
   x = x + 2;
10
   if 2 * (x + y) > 21 then {
11
12
     x = x * 3;
13
     y = y * 2
14
   else {
15
     x = x * 4;
     y = y * 3 + x };
17
   skip
```

- (a) (3) How many execution paths does Prog1 have? List all the paths as a sequence of line numbers taken on the path.
- (b) (4) Symbolically execute each path and provide the resulting path condition. Show the steps of symbolic execution as a table. An example of executing the first line is given below:

Edge	Symbolic State (PV)	Path Condition (PC)
$1 \rightarrow 2$	$x \mapsto X_0, y \mapsto Y_0$	true

(c) (3) For each path in part (b), indicate whether it is feasible or not. For each feasible path, give values for  $X_0$  and  $Y_0$  that satisfy the path condition.

### Question 2 (15 points)

(a) (2) The constraint  $at\text{-}most\text{-}one(a_1,\ldots,a_n)$  is satisfied if at most one of the Boolean variables  $a_1,\ldots,a_n$  is true. For example,  $at\text{-}most\text{-}one(\top,\bot,\bot)$  is true, and  $at\text{-}most\text{-}one(\top,\bot,\top)$  is false. Encode the constraint

$$at\text{-}most\text{-}one(a_1, a_2, a_3, a_4)$$

into an equivalent set of clauses (i.e., in CNF).

(b) (4) Show whether the following First Order Logic (FOL) sentence is valid or not. Either give a proof of validity, or show a model in which the sentence is false.

$$(\forall x \cdot \exists y \cdot P(x) \lor Q(y)) \iff (\forall x \cdot P(x)) \lor (\exists y \cdot Q(y))$$

(c) (Not to be handed in, but a useful exercise:) Show whether the following First Order Logic (FOL) sentence is valid or not. Either give a proof of validity, or show a model in which the sentence is false.

$$(\forall x \cdot \exists y \cdot P(x,y) \lor Q(x,y)) \implies (\forall x \cdot \exists y \cdot P(x,y)) \lor (\forall x \cdot \exists y \cdot Q(x,y))$$

(d) (3) Consider the following FOL formula  $\Phi$ :

$$\exists x \exists y \exists z (P(x,y) \land P(z,y) \land P(x,z) \land \neg P(z,x))$$

For each of the following FOL models, explain whether they satisfy or violate the formula  $\Phi$ .

- (a) (Not to be handed in):  $M_1 = \langle S_1, P_1 \rangle$ , where  $S_1 = \mathbb{N}$ , and  $P_1 = \{(x, y) \mid x, y \in \mathbb{N} \land x < y\}$ . Does  $M_1 \models \Phi$ ?
- (b)  $M_2 = \langle S_2, P_2 \rangle$ , where  $S_2 = \mathbb{N}$  and  $P_2 = \{(x, x+1) \mid x \in \mathbb{N}\}$ . Does  $M_2 \models \Phi$ ?
- (c)  $M_3 = \langle S_3, P_3 \rangle$ , where  $S_3 = \mathcal{P}(\mathbb{N})$ , the powerset of natural numbers, and  $P_3 = \{(A, B) \mid A, B \in \mathcal{P}(\mathbb{N}) \land A \subseteq B\}$ . Does  $M_3 \models \Phi$ ?
- (e) (Bonus question) Extend your encoding from part (a) to n variables and use at most O(n) clauses and variables. If your solution is based on external resources, make sure to properly reference them.

### Question 3 (Bonus, 12 points)

I've made this question a bonus. If you submit it, we will mark it and give you marks for it. You don't lose marks for not doing it. I recommend doing it, but I also need to preserve TA resources.

In recreational mathematics, a **magic square** is a  $n \times n$  square grid filled with distinct positive integers from 1 to  $n^2$  inclusive such that each cell contains a different integer, and the sum of the integers in each row, column, and diagonal is equal.

The following is an example of  $3 \times 3$  magic square:

8	1	6
3	5	7
4	9	2

- (a) (Not to be handed in:) Write down quantifier free constraints in First Order Logic to solve the puzzle above for any positive integer n.
- (b) (10) Use the Z3 Python API to implement a solver for magic square puzzles. Your solver should accept four parameters: n, r, c, val, where:
  - n is the size of the puzzle—number of cells on each side, n>0
  - r is a row number,  $0 \le r \le n$
  - c is a column number,  $0 \le c < n$
  - val is an integer value,  $1 \le val \le n^2$

Your program should find a magic square of the given size n with the value val filled at location (r, c), assuming the top left corner corresponds to (0, 0).

Your solver should return a 2D array of integers corresponding to the solution. If there is more than one solution, just return any one of them. If there is no such magic square, your solver should return None. For example,

```
>>> res = solve_magic_square(3, 1, 1, 5)
>>> print_square(res, 3)
4 9 2
3 5 7
8 1 6
```

The skeleton for the solver is provided in a2q3/magic\_square.py.

You might find it helpful to use Z3 z3.Distinct(x) to create a constraint that states that all constants in the list x have distinct values. For example,

```
>>> x, y = z3.Ints ('x y')
>>> z3.Distinct (x, y)
x != y
```

(c) (2) Extend the test suite in a2q3/puzzle\_tests.py with two additional set of parameters, and one extra set of parameters that does not have a solution (i.e., the solver returns None).

Recall that you can execute the test suite using the following command:

```
python -m a2q3.test
```

### Question 4 (30 points)

Your GitHub repository includes an implementation of a parser and interpreter for the WHILE language from the lecture notes. Your task is to write a symbolic execution engine for it.

The implementation of the interpreter is located in directory wlang. You can execute the interpreter using the following command:

```
(venv) $ python3 -m wlang.int wlang/test1.prg
x: 10
```

A sample program is provided for your convenience in wlang/test1.prg

You can execute the interpreter using the following command:

```
(venv) $ python3 -m wlang.sym wlang/test1.prg
```

A skeleton for a symbolic interpreter is given in wlang/sym.py. It includes an implementation of a symbolic state in a class SymState. You need to modify the skeleton, but please (1) keep the run() method as the external interface, and (2) use mk\_error() to report error states e.g. assertion failures.

You may find it helpful to look at the implementation of the concrete interpreter in wlang/int.py. Note that the concrete interpreter takes a State as input, and returns a single State as output. On the other hand, the symbolic interpreter takes a symbolic state State as input, and returns a **list** of symbolic states as output, where each output state corresponds to some execution of the program. In general, the number of output states will be proportional to the number of execution paths in the program.

- (a) (6) Implement symbolic execution of straight line code (i.e., programs without if- and while-statements);
- (b) (6) Extend your answer to symbolic execution of programs with if-statements;
- (c) (12) Extend your answer to symbolic execution of programs with while-statements. To handle arbitrary loops, assume that the loop is executed at most 10 times. That is, your symbolic execution engine should explore all feasible program paths in which the body of each loop is executed no more than 10 times.
- (d) (3) Extend the test suite test\_sym.py to achieve 100% branch coverage of your implementation in parts (a), (b), and (c). Recall that you can run the test suite using

```
(venv) $ python3 -m wlang.test
```

and measure coverage of the test suite using

```
(venv) $ coverage run -m wlang.test
(venv) $ coverage html
```

(e) (3) In file wlang/diverge.wl, provide a program on which your symbolic execution engine diverges (for our purposes: takes longer than a few seconds to run).