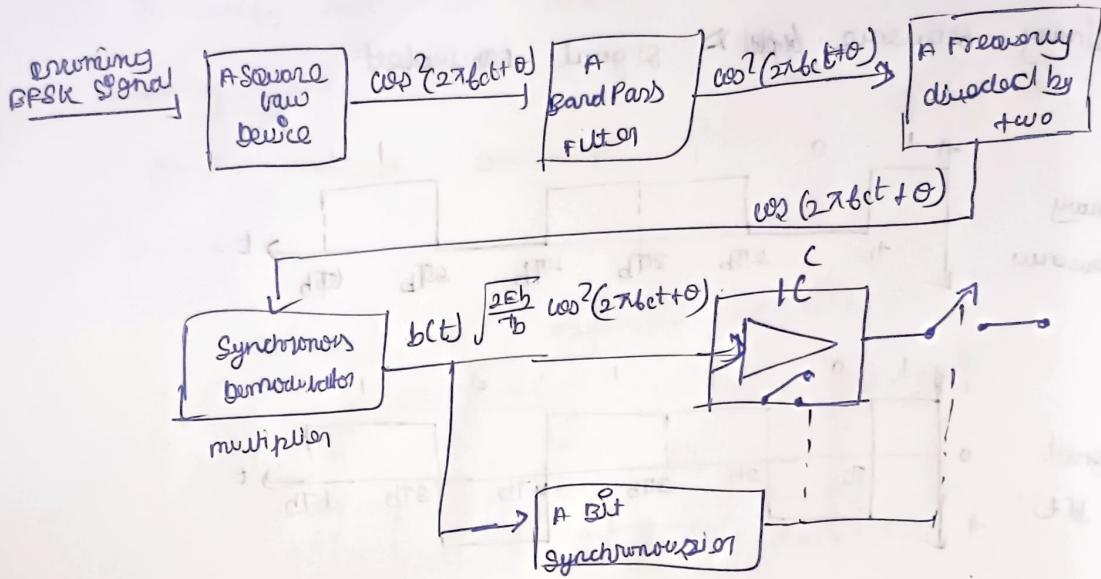


NO	Input Binary	Bipolar NRZ signal	BPSK output signal
1	Binary 0	$b(t) = -1$	$-\sqrt{\frac{2E_b}{Tb}} \cos 2\pi f_c t$
2	Binary 1	$b(t) = +1$	$\sqrt{\frac{2E_b}{Tb}} \cos 2\pi f_c t$

Reception of BPSK signal:



* consider a 'θ' phase shift, the input signal

can be written as

$$s(t) = b(t) \sqrt{\frac{2E_b}{Tb}} \cos(2\pi f_c t + \theta)$$

* the carrier signal is separated from the input to the receiver, now it is sent to the square law device.

$$\Rightarrow \cos^2(2\pi f_c t + \theta)$$

$$\cos^2 \theta = \frac{1 + \cos 2\theta}{2}$$

$$= \frac{1 + \cos 2(2\pi f_c t + \theta)}{2}$$

$$= \frac{1}{2} + \frac{1}{2} \cos 2(2\pi f_c t + \theta).$$

- ⇒ At Band Pass filter is connected to base of V₁, the output is
- $\Rightarrow \cos 2(\omega_f t + \theta)$
- ⇒ At frequency divider, it is divided by 2 and thus output is
- $\cos(\omega_f t + \theta)$.

⇒ Synchronous demodulator, input signal and recovered carrier

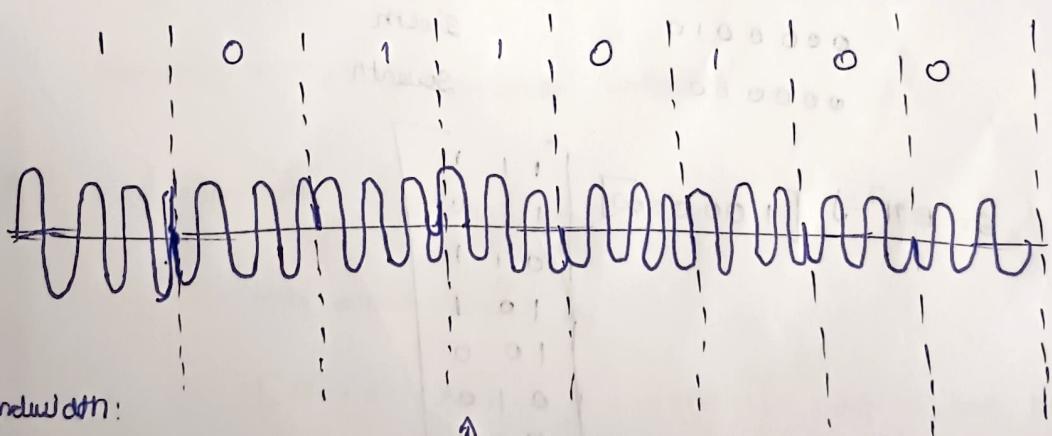
$$b(t) = \sqrt{\frac{2E_b}{T_b}} \cos(\omega_f t + \theta) \times \cos(\omega_f t + \theta)$$

$$\Rightarrow b(t) = \sqrt{\frac{2E_b}{T_b}} \cos^2(\omega_f t + \theta)$$

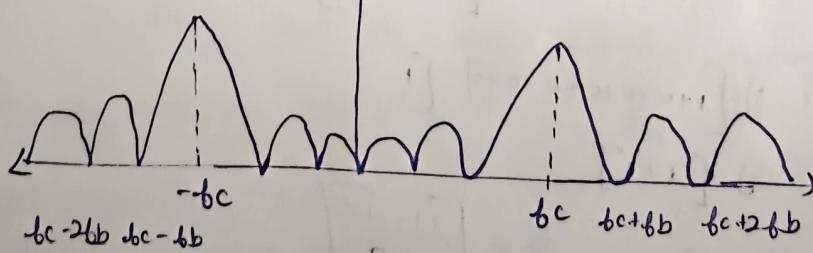
$$= b(t) \sqrt{\frac{2E_b}{T_b}} \times \left[\frac{1 + \cos 2(\omega_f t + \theta)}{2} \right]$$

$$= b(t) \sqrt{\frac{E_b}{T_b}} [1 + \cos 2(\omega_f t + \theta)]$$

output [waveform]



Bandwidth:



$$\text{Bandwidth} = H.F - L.F$$

$$= (f_c + f_b) - (f_c - f_b)$$

$$\boxed{B_w = 2f_b}$$

16/9
History Frequency 1 Shift 1 Hop

N of Frequency 10, 11 can be 1 (Infinite possibility)

The parity check matrix $(7,4)$ hamming code.

$$H = \begin{bmatrix} 1 & 1 & 0 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 & 0 & 0 & 1 \end{bmatrix}, \text{ calculate the syndrome vector}$$

For single bit errors.

$$S = E H^T$$

Error vector

$$E = [1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

0 1 0 0 0 0 0

0 0 1 0 0 0 0

0 0 0 1 0 0 0

0 0 0 0 1 0 0

0 0 0 0 0 1 0

0 0 0 0 0 0 1

Bit 1 error

First

Second

Third

Fourth

Fifth

Sixth

Seventh

$$S = EH^T = [1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0] \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\Rightarrow [1 + 0 + 0 + 0 + 0 + 0 + 0] [1]$$

$$\Rightarrow [1 \ 1 \ 1]$$

$$= [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

$$\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\Rightarrow [0 + 0 + 1 + 0 + 0 + 0 + 0] [0]$$

$$\Rightarrow [0 + 0 + 1 + 0 + 0 + 0 + 0] [0]$$

$$\Rightarrow [0 + 0 + 1 + 0 + 0 + 0 + 0] [0]$$

$$\Rightarrow [0 \ 1 \ 1]$$

Error vector:

1 0 0 0 0 0 0
0 1 0 0 0 0 0
0 0 1 0 0 0 0
0 0 0 1 0 0 0
0 0 0 0 1 0 0
0 0 0 0 0 1 0
0 0 0 0 0 0 1

Syndrome vector

1 1 1
1 1 0
0 1 1
1 0 1
1 0 0
0 1 0
0 0 1

Relation with M

1st row
2nd row
3rd row
4th row
5th row
6th row
7th row

cyclic code:

A binary code said to be a cyclic code if it exhibits the following properties

i) Linearity property \Rightarrow A code is said to be linear if

ii) cyclic property sum of any two code is also a code word

A code is said to be cyclic if any cyclic

shift of the code word results in the

Formation of the another codeword.

Code word polynomial

* The code word given by:

$[x_0, x_1, x_2, \dots, x_{n-1}]$, which can be

Expressed in the form of code word polynomial as

$$c(x) = x_0 + x_1 p + x_2 p^2 + \dots + x_{n-1} p^{n-1}$$

Generator polynomial

$$* x(p) = m(p) \cdot g(p)$$

$$\text{where: } g(p) = 1 + g_1 p + g_2 p^2 + \dots + g_{n-k-1} p^{n-k-1} + p^{n-k}$$

$$m(p) = 1 + \sum_{i=1}^{n-k-1} g_i p^i + p^{n-k}$$

non - systematic code vectors (or words)

$$\alpha_1(P) = m_1(P) \cdot \alpha_1(P)$$

$$\alpha_2(P) = m_2(P) \cdot \alpha_1(P)$$

$$\alpha_3(P) = m_3(P) \cdot \alpha_1(P)$$

$$\vdots$$

generation of

systematic code words

$$\left[P^{n-k} \underline{m(P)} \right] \oplus c(P) = x(P)$$

$c(P) \Leftrightarrow$ remainder polynomial

$$\frac{P^{n-k} m(P)}{\alpha_1(P)} = \alpha_2(P) \oplus \frac{c(P)}{\alpha_1(P)}$$

problem

- 1) The generated polynomial for an $(7,4)$ cyclic Hamming code is given by $\alpha_1(P) = 1 + P + P^3$, determine all systematic and non systematic code vectors.

Non systematic:

$$x_1(P) = M_1(P) \cdot \alpha_1(P)$$

$$m(0000) \Leftrightarrow$$

$$M_1(P) = 0 + 0P + 0P^2 + 0P^3$$

$$\alpha_1(P) = 1 + P + P^3$$

$$\alpha_1(P) = m(P) \cdot \alpha_1(P)$$

$$= 0 + \overbrace{0P}^{\text{parity}} + \overbrace{0P^3}^{\text{parity}} + \overbrace{0P}^{\text{message}} + \overbrace{0P^2}^{\text{message}} + \overbrace{0P^4}^{\text{message}} + \overbrace{0P^2}^{\text{message}} + \overbrace{0P^3}^{\text{message}} + \overbrace{0P^5}^{\text{message}}$$

$$\Rightarrow 0 + 0P + 0P^3 + 0P^4 + 0P^5 + 0P^6 + 0P^2$$

$$\underbrace{0 + 0P + 0P^2 + 0P^3 + 0P^4 + 0P^5 + 0P^6}_{\text{parity}} + \underbrace{0P^2}_{\text{message}}$$

message:

$$m(1100)$$

$$\begin{aligned}m(p) &= 1 + p + \underline{op^2} + \underline{op^3} \\o_1(p) &= 1 + p + \underline{p^3}\end{aligned}$$

$$x(p) = m(p) \cdot o_1(p)$$

$$= 1 + p + \underline{p^3} + \underline{p} + \underline{p^2} + \underline{p^4} + \underline{op^2} + \underline{op^3} + \underline{op^5}$$

$$+ \underline{op^3} + \underline{op^4} + \underline{op^6}$$

$$= 1 + op + \underline{p^2} + \underline{p^3} + \underline{p^4} + \underline{op^5} + \underline{op^6}$$

$$m \Rightarrow \left[\begin{array}{c|cc} 1 & 0 & 1 & 1 & 1 & 0 & 0 \\ \hline \text{parity} & \text{message} \end{array} \right]$$

$$1 + op + \underline{p^2} + \underline{op^3}$$

$$m(1010)$$

$$m(p) = 1 + op + \underline{p^2} + \underline{op^3}$$

$$o_1(p) = 1 + p + \underline{p^3}$$

$$x(p) = m(p) \cdot o_1(p)$$

$$= 1 + p + \underline{p^3} + \underline{op} + \underline{op^2} + \underline{op^4} + \underline{p^2} + \underline{p^3} + \underline{pp}$$

$$+ \underline{op^3} + \underline{op^4} + \underline{op^6}$$

$$\Rightarrow 1 + 1p + 1p^2 + op^3 + op^4 + op^5 + op^6$$

$$\Rightarrow \left[\begin{array}{c|cc} 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ \hline \text{parity} & \text{message} \end{array} \right]$$

$$m(0010)$$

$$m(p) = 0 + op + \underline{p^2} + \underline{op^3}$$

$$o_1(p) = 1 + p + \underline{p^3}$$

$$x(p) = m(p) \cdot o_1(p)$$

$$= 0 + \underline{op} + \underline{op^3} + \underline{op} + \underline{op^2} + \underline{op^4} + \underline{p^2} + \underline{p^3} + \underline{p^5}$$

$$+ \underline{op^3} + \underline{op^4} + \underline{op^6}$$

$$\Rightarrow 0 + op + 1p^2 + 1p^3 + op^4 + 1p^5 + op^6$$

$$\Rightarrow \left[\begin{array}{c|cc} 0 & 0 & 1 & 1 & 0 & 1 & 0 \\ \hline \text{parity} & \text{message} \end{array} \right]$$

$$g_{\text{stomachic}} = m(1010) \Rightarrow 1 + P^2$$

$$x(cP) = c(P) \oplus P^{n+1} \otimes m(P)$$

$$\alpha(p) = c(p) \oplus p^{\beta} (1 + p^2)$$

$$c(p) = \frac{p^{n-k} (m(p))}{61(p)} \Rightarrow \frac{p^3 (1+p^2)}{1+p+p^3} \Rightarrow \frac{p^3 + p^5}{1+p+p^3}$$

[non systematic] generated and parity check matrices of cyclic codes.

$$G(P) = P^{n-k-1} + P^{n-k} g_{n-k-1} + \dots + g_1 P^2 + g_0 P + 1$$

$$P^k \times G(P) = P^{n-k+i} + P^{n-k+i-1} \dots + g_2 P^{2+i} + g_1 P^{1+i} + 1$$

$$i = (m-1), (k-2), \dots, 0, 1, 2, 3, 0.$$

Problem

1) For a $(7,4)$ cyclic code determine the

generated matrix & $G(P)$ if $\alpha(P) = 1 + P + P^3$

$$n=7$$

$$k=4$$

$$i = (0, 1, 2, 3)$$

$$i=3 \quad \alpha(P) \times P^3$$

$$\alpha(P) \times P^3 = P^3 + P^4 + P^6$$

$$\text{Case } i=3 \quad P^3 + P^4 + P^6 + P^3 + OP^2 + OP + 0 \\ P^6 + OP^5 + P^4 + P^3 + OP^2 + OP + 0$$

$$i=2 \quad P^2 \times \alpha(P)$$

$$P^2 \times [1 + P + P^3]$$

$$P^2 + P^3 + P^5$$

$$OP^6 + P^5 + OP^4 + P^3 + P^2 + OP + 0$$

$$i=1 \quad P^1 \times G(P)$$

$$P^1 \times [1 + P + P^3]$$

$$P + P^2 + P^4$$

$$i=0 \quad P^0 \times G(P)$$

$$P^0 \times (1 + P + P^3)$$

$$1 + P + P^3$$

$$OP^6 + OP^5 + OP^4 + P^3 + OP^2 + P + 1$$

$G_1(N \times n)$

$$G_1(4 \times 7) = \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix}$$

Code word :

$$R = m \times \underline{G_1} \quad (m, n) = 2^k \cdot 2^l = 16.$$

$m(0110)$

$$x = [0110] \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix}$$

$$\Rightarrow [0] [0+1+0+0] [0+0+1+0] [0+1+0+0] \\ [0+1+1+0] [0+0+1+0] [0+0+0+0] \\ = [0 \ 1 \ 1 \ 1 \ 0 \ 1 \ 0]$$

$m(0010)$:-

$$x = [0010] \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix}$$

$$\Rightarrow [0+0+0+0] [0+0+0+0] [0+0+1+0] [0+0+0+0] \\ [0+0+1+0] [0+0+1+0] [0+0+0+0] \\ = [0 \ 0 \ 1 \ 0 \ 1 \ 1 \ 0]$$

$m(0101)$

$$x = [0 \ 1 \ 0 \ 1] \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix}$$

$$= [0+0+0+0] [0+1+0+0] [0+0+0+0] [0+1+0+1] [0+1+0+0]$$

$$[0+0+0+1] [0+0+0+1]$$

$$= [0 \ 1 \ 0 \ 0 \ 1 \ 1]$$

$m(1100)$

$$x = [1 \ 1 \ 0 \ 0] \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix}$$

$$= [1+0+0+0] [0+1+0+0] [1+0+0+0] [1+0+0+0] [0+1+0+0]$$

$$[0+0+0+0] [0+0+0+0]$$

$$= [1 \ 1 \ 1 \ 0 \ 1 \ 0 \ 0]$$

$m(1010)$

$$x = [1 \ 0 \ 1 \ 0] \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix}$$

$$= [1 \ 0 \ 0 \ 1 \ 1 \ 0]$$

$m(1110)$

$$x = [1 \ 1 \ 1 \ 0] \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix}$$

$$= [1 \ 1 \ 0 \ 0 \ 0 \ 1 \ 0]$$

$m(1011)$

$$x = [1 \ 0 \ 1 \ 1] \begin{bmatrix} 1 & 0 & 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix}$$

$$= [1 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0]$$

Code

generated matrix for the systematic codes:

$$P^{(n-i)} \oplus R_i(P) = Q_i(P) \cdot \alpha_i(P)$$

where $i = 1, 2, 3, \dots, k$

$$\frac{P^{(n-i)}}{\alpha_i(P)} = Q_i(P) \oplus \frac{R_i(P)}{\alpha_i(P)}$$

augmented matrix (continued)

Problems:

Q1. For a $(7, 4)$ systematic cyclic code, determine the generated matrix, parity check matrix.

Given $\alpha_i(P) = P^3 + P + 1$

$$P^{(n-i)} \oplus R_i(P) = Q_i(P) \cdot \alpha_i(P)$$

$$i = 1, 2, 3, 4 \quad n = 7$$

$$i=1$$

$$P^6 \oplus R_1(P) = Q_1(P) \cdot \alpha_1(P)$$

$$\Rightarrow \frac{P^{(n-i)}}{\alpha_i(P)} = Q_i(P) + \frac{R_i(P)}{\alpha_i(P)}$$

$$\Rightarrow \frac{P^6}{\alpha_1(P)}$$

$$\begin{array}{c}
 p^3 + op^2 + p + 1 \\
 \hline
 p^6 + op^5 + op^4 + op^3 + op^2 + op + o \\
 p^6 + p^4 + p^3 \\
 \hline
 op^5 + p^4 + p^3 + op^2 \\
 op^5 + op^3 + op^2 \\
 \hline
 p^4 + p^3 + op + o \\
 p^4 + p^2 + p \\
 \hline
 p^3 + p^2 + p + o \\
 p^3 + p + 1 \\
 \hline
 p^2 + 1
 \end{array}$$

$i = 1$

$$\begin{aligned}
 & p^{(n-i)} \oplus R_i(p) = Q_i(p) \cdot O_i(p) \\
 & p^6 \oplus p^2 + 1 = (p^3 + p + 1) (p^3 + p + 1) \\
 & p^6 \oplus p^2 + 1 = p^6 + p^4 + p^3 + p^4 + p^2 + p + p^3 + p + 1 \\
 & = p^6 + p^2 + 1 \quad \boxed{100010}
 \end{aligned}$$

$i = 2$

$$\begin{aligned}
 & p^{(n-i)} \oplus R_i(p) = Q_i(p) \cdot O_i(p) \\
 & r^5 \oplus R_2(p) = Q_2(p) \cdot O_2(p) \\
 & \frac{p^5}{O_2(p)} = Q_2(p) \oplus \frac{R_2(p)}{O_2(p)}
 \end{aligned}$$

$$P^2 + OP + 1$$

$$P^3 + P + 1$$

$$P^9 + P^2 + P + 1$$

$$\Rightarrow [010011]$$

$$\begin{array}{r}
 P^4 + OP^3 + OP^2 + OP + 1 \\
 \underline{P^3 + P^2 + P^1 + P} \\
 OP^4 + 1P^3 + P^2 + OP \\
 OP^4 + OP^3 + OP^2 + OP \\
 \underline{1P^3 + 1P^2 + 0} \\
 1P^2 + 1P + 1 \\
 \hline
 1P^3 + P + 1
 \end{array}$$

$$i = 3 :$$

$$P^4 \oplus R_i(P) = Q_i(P) \cdot G(P)$$

$$\frac{P^{(n-i)}}{G(P)} = R_i(P)$$

$$\frac{P^4}{P^2 + P + 1} = R_i(P)$$

$$\begin{array}{r}
 P^2 + P + 1 \\
 | \\
 P^4 + OP^3 + OP^2 + OP + 1 \\
 | \\
 P^4 + P^3 + P^2 \\
 | \\
 OP^3 + P^2 + OP \\
 | \\
 P + 0
 \end{array}$$

$$P^3 + P + 1$$

$$\begin{array}{r}
 P^4 + OP^3 + OP^2 + OP + 0 \\
 | \\
 P^4 + P^3 + P^2 + P \\
 | \\
 OP^3 + P^2 + P + 0 \\
 | \\
 OP + 0 \\
 | \\
 P^2 + P + 0
 \end{array}$$

$$P^4 \oplus (P^2 + P + 0) = (1P) \cdot (P^3 + P + 1)$$

$$= P^4 + P^2 + P$$

$$\Rightarrow [0\ 0\ 1\ 0\ 1\ 0]$$

$i = n:$

$$\frac{P^3}{a_1(P)} = Q(P) + \frac{R_4(P)}{G_1(P)}$$

$$P^3 + P + 1$$

$$\overline{\left(\begin{array}{c} P^3 + 0P^2 + 0P + 0 \\ P^3 + P + 1 \\ \hline 0P^2 + P^2 + 1 \end{array} \right)}$$

$$P^3 \oplus (P^2 + 1) = 1 \cdot P^3 + P + 1$$

$$= P^3 + P + 1$$

$$= [0\ 0\ 0\ 1\ 0\ 1\ 1]$$

$$a_1 = \left[\begin{array}{cccccc} P^6 & P^5 & P^4 & P^3 & P^2 & P^1 & P^0 \\ 1 & 0 & 0 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{array} \right] \quad a = [1\ 1\ 1\ | \ P]$$

$$P = \left[\begin{array}{ccc} 1 & 0 & 1 \\ 1 & 1 & 1 \\ 1 & 0 & 1 \\ 0 & 1 & 1 \end{array} \right] \quad u = [P^T \ | \ P^{n-k}]$$

$$H = \left[\begin{array}{cccc|cc} 1 & 1 & 1 & 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & 1 & 0 \\ 1 & 0 & 1 & 1 & 0 & 0 & 1 \end{array} \right]$$

obtain the code vector for a (7,4) cyclic having

$$\text{the } \text{GCD} = 1 + p + p^3$$

$$2^4 \Rightarrow 16.$$

$$x = m \alpha_1$$

take α_1 from the previous sum:

$$\alpha_1 = \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix}$$

$$x = \begin{bmatrix} 1 & 1 & 1 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \end{bmatrix} \\ = \begin{bmatrix} 1 & 1 & 0 & 1 & 0 & 0 & 0 \end{bmatrix}$$

Encoder for cyclic codes.

Encoder is useful for generating the systematic cyclic codes.

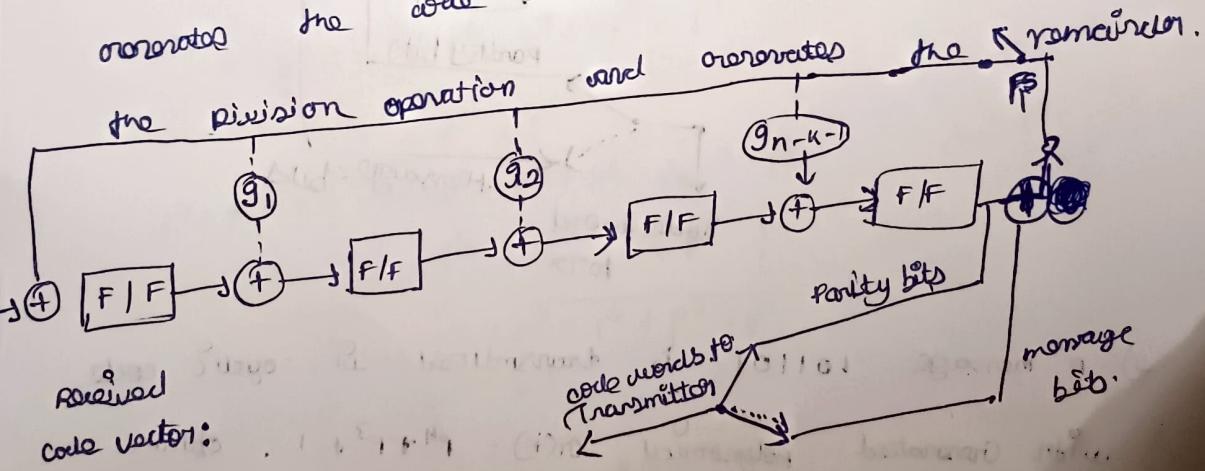
Flipflops are used to construct a shift register, operations of all these flipflops are controlled by the external clock.

The flipflop contents will get shifted in the direction of arrow corresponding to each clock pulse.

All the flipflops are initialised to zero state.

After shifting the 'k' message bits the shift register will contain $n-k$ parity (or) check bits. Therefore after shifting the message bits circuited. and the feedback switch is open the output switch is thrown to Parity bit position.

now every shift the parity bits one encoder transmitted over the channel thus the encoder performs error detection on the code word. The encoder performs the division operation and generates the remainder.



Problems:

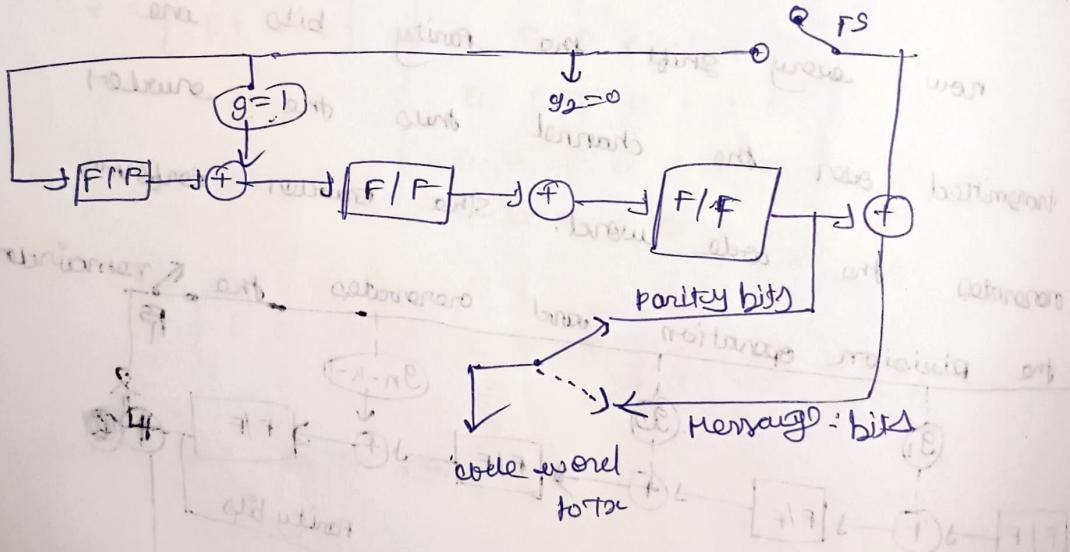
- i) Draw the encoder for a $(7, n)$ cyclic hamming code generated by the generator polynomial $g(p) = 1 + p + p^3$

generator polynomial

$$g(p) = 1 + \sum_{i=1}^{n-k-1} g_i p^i + p^{n-k}$$

$$= 1 + \sum_{i=1}^2 g_i p^i + p^3$$

$$g(p) = 1 + g_1 p + g_2 p^2 + p^3$$



- 2) A message 101101 is transmitted in a cyclic code with generator polynomial $g(p) = p^4 + p^3 + 1$. obtain the transmitted code word.

i) how many check (or) parity bits does the encoded message contain

ii) draw the encoding arrangement for the same.

Systematic code:

$$H = 101101$$

$k = 6$ $n-k = \text{Parity bits}$

length of $n-k = 4 \rightarrow$ highest degree of polynomial.

$$\text{Degree of } h = n-k \\ (n, k) = (10, 6) \quad \boxed{n=10}$$

$$x(P) = P^{n-k} M(P) \oplus C(P)$$

$$\frac{P^{n-k} M(P)}{C(P)} = Q(P) + \frac{C(P)}{G(P)}$$

$$\frac{P^4 \times (101101)}{P^4 + P^3 + 1} \rightarrow M(P) = 1 + OP + P^2 + P^3 + OP^4 + OP^5$$

$$\Rightarrow \frac{(1 + OP + P^2 + P^3 + OP^4 + OP^5) \times (P^4)}{P^4 + P^3 + 1}$$

$$= P^4 + OP^5 + P^6 + P^7 + OP^8 + P^9.$$

$$P^4 + P^3 + 1 \left[\begin{array}{c} P^5 + P^4 + P^2 \\ P^9 + OP^8 + P^7 + P^6 + OP^5 + P^1 \\ P^9 + P^8 \\ \hline P^8 + P^7 + P^6 + P^5 + P^4 \\ P^8 + P^7 \\ \hline P^6 + P^5 \\ P^4 + P^6 + P^2 \\ \hline P^2 \end{array} \right]$$

$$P^5 + P^4 + P^2 + P^6 + P^3 + 1$$

$$Q(P) = P^5 + P^4 + P^2$$

$$C(P) = P^2$$

$$x(P) = P^4(1 + OP + P^2 + P^3 + OP^4 + OP^5) \oplus P^2$$

$$= (P^4 + OP^5 + P^6 + P^7 + OP^8 + OP^9) \oplus P^2$$

$$= P^9 + OP^8 + P^7 + P^6 + OP^5 + P^4 + P^2$$

$$x = \underbrace{\begin{matrix} 1 & 0 & 1 & 1 & 0 & 1 \end{matrix}}_{\text{msg bits}} \underbrace{\begin{matrix} 0 & 1 & 0 & 0 \end{matrix}}_{\text{parity bits}}$$

115 → A
210 → A
100 → B
200 → B
100 → A
95 → C
500

Problems:

i) why are cyclic codes effectively detecting error Burst.
 (The message .1001001010 is to be transmitted)

In a cyclic code with a generator polynomial
 $g(x) = x^2 + 1$

i) how many check bits does the encoded message contain

ii) obtain the transmitted code word.

iii) draw encoding arrangement to obtain remainder bits

iv) after the receive word is divided to one remainder word what should be content of register stored.

$$m = 1001001010 \quad \{k=10\}$$

$n-k =$ parity bits

$$n-k = 2$$

$$n = 10 + 2$$

$$\boxed{n = 12}$$

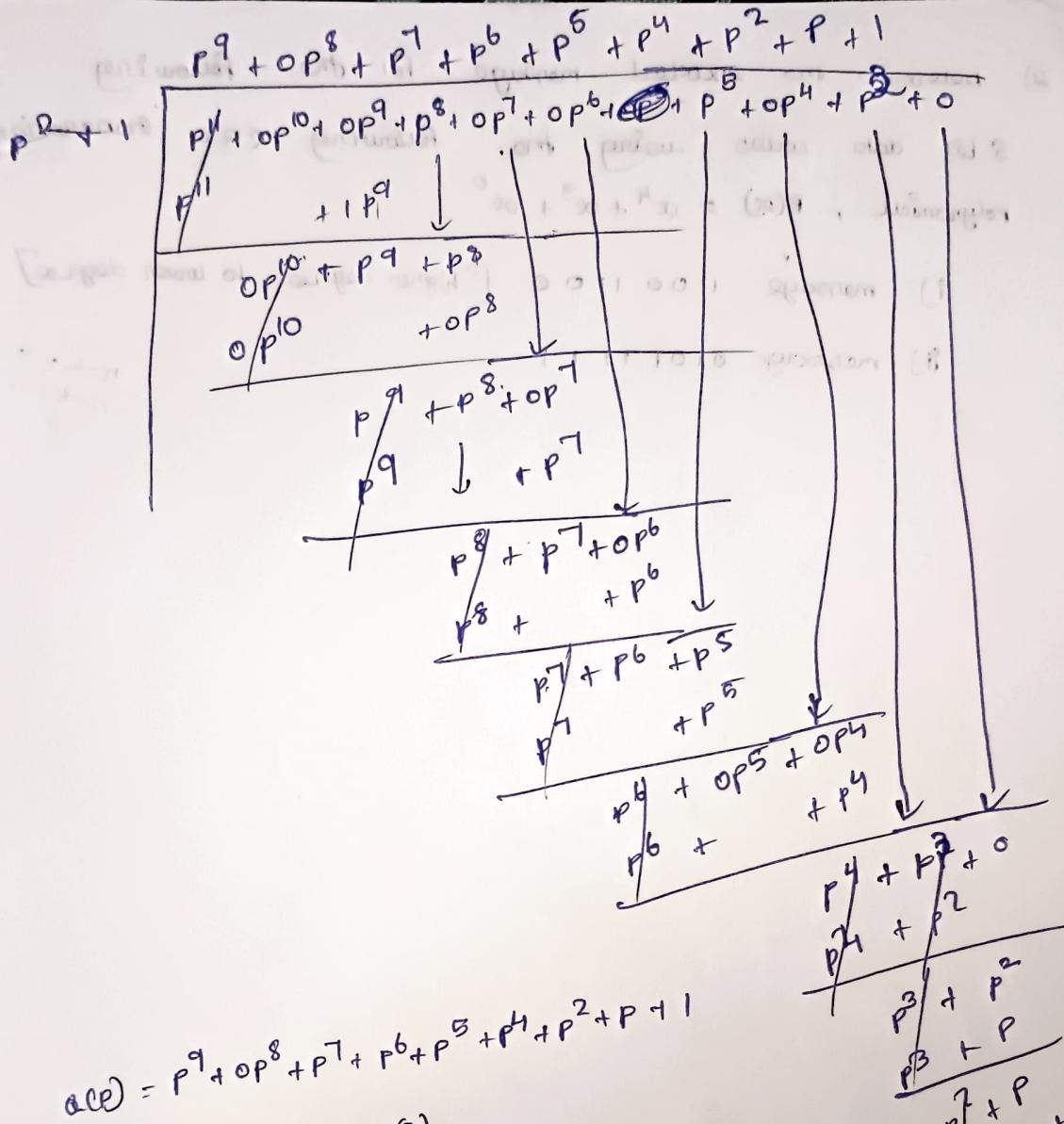
$$x(P) = P^{n-k} M(P) \oplus C(P)$$

$$\frac{P^{n-k} M(P)}{G(P)} = Q(P) + \frac{C(P)}{G(P)}$$

$$P^2 \times \underbrace{(1001001010)}_{x^2 + 1}$$

$$P^2 \times \underbrace{\left(p^9 + p^8 + p^7 + p^6 + p^5 + p^4 + p^3 + p^2 + p \right)}_{x^2 + 1}$$

$$\underbrace{p^{11} + p^{10} + p^9 + p^8 + p^7 + p^6 + p^5 + p^4 + p^3}_{10} \quad \frac{1}{x^2 + 1}$$



$$\alpha(P) = P^9 + OP^8 + P^7 + P^6 + P^5 + P^4 + P^2 + P + 1$$

$$\alpha(P) = P^{n-k} m(P) \oplus \overset{\text{c}(P)}{\underline{c(P)}}$$

$$= P^2 \times [P^9 + OP^8 + OP^7 + P^6 + OP^5 + OP^4 + P^3 + OP^2 + P + O] \oplus [P+1]$$

$$= P^{11} + OP^{10} + OP^9 + P^8 + OP^7 + OP^6 + P^5 + OP^4 + P^3 + O + P + 1$$

$$= P^{11} + OP^{10} + OP^9 + P^8 + OP^7 + OP^6 + P^5 + OP^4 + P^3 + P + 1$$

$$\alpha(P) = \underbrace{1 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1 \ 0 \ 1 \ 0 \ 1 \ 1}_{\text{message}} \underbrace{\sim}_{\text{parity}}$$

2) determine the encoded message for the following 8 bit data codes using the following generator polynomial, $P(x) = x^4 + x^3 + x^0$

i) message 1100 1100 [higher degree to lower degree]

ii) message 0101 1111

$$n-k=2^4$$

$$n=8=4$$

$$\begin{array}{r}
 & & & & 1 & 1 & 0 & 0 \\
 & & & & \times & x^4 & + & x^3 & + & x^0 \\
 & & & & \hline
 & & 0 & 1 & 0 & 1 & 1 & 1 & 1 \\
 & & & & \times & x^4 & + & x^3 & + & x^0 \\
 & & & & \hline
 & & 0 & 1 & 0 & 1 & 1 & 1 & 1 \\
 & & & & \times & x^4 & + & x^3 & + & x^0 \\
 & & & & \hline
 & & 0 & 1 & 0 & 1 & 1 & 1 & 1
 \end{array}$$

$$(1+g+x^3+x^4) + x^7 + x^9 + x^{10} + P_1 = (1)$$

$$(D_2 \oplus D_m) x^{2^4-1} = (1)$$

$$(1+g)(1+g) + x^7 + x^9 + x^{10} + P_1 + x^0 + P_1$$

$$(1+g + x^3 + x^4 + x^7 + x^9 + x^{10} + P_1) + x^0 + P_1$$

$$(1+g + x^3 + x^4 + x^7 + x^9 + x^{10} + P_1) + x^0 + P_1$$

1101001001