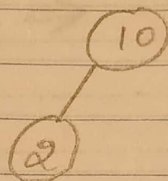


HOMEWORK 5 \Rightarrow ARSHITHA BASAVARAJ

Q1
a)

(10)

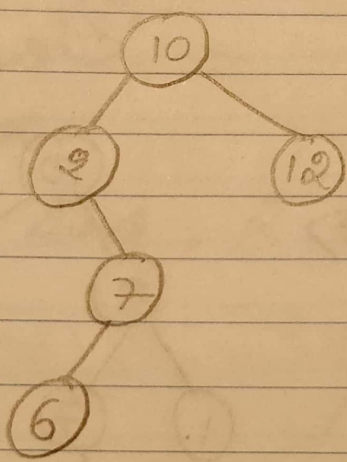
\Rightarrow



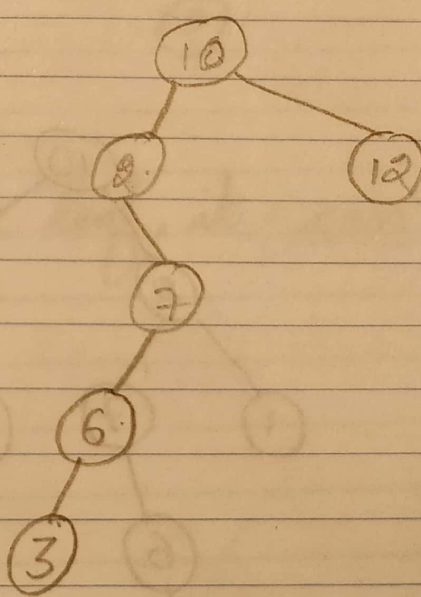
\Rightarrow



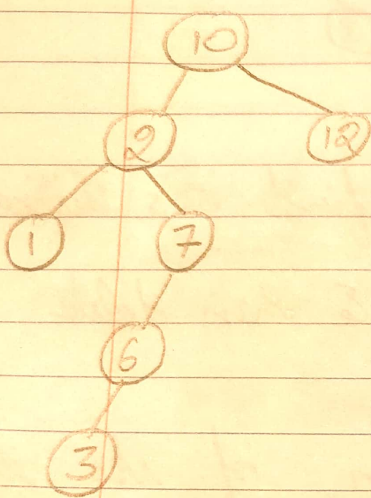
\Rightarrow



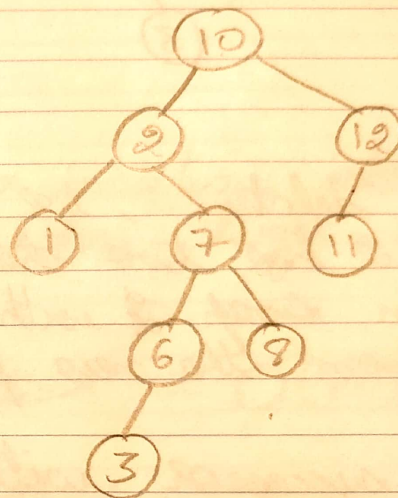
\Rightarrow



\Rightarrow

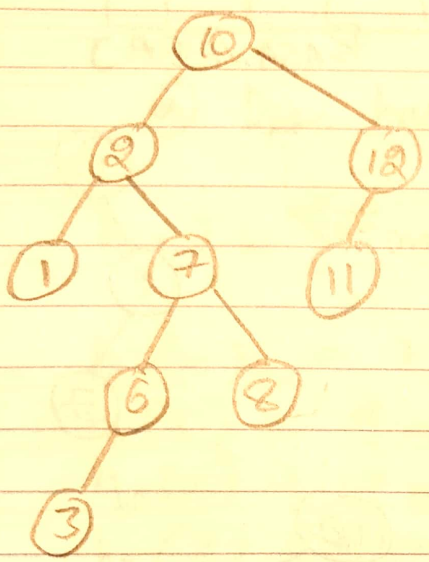


⇒

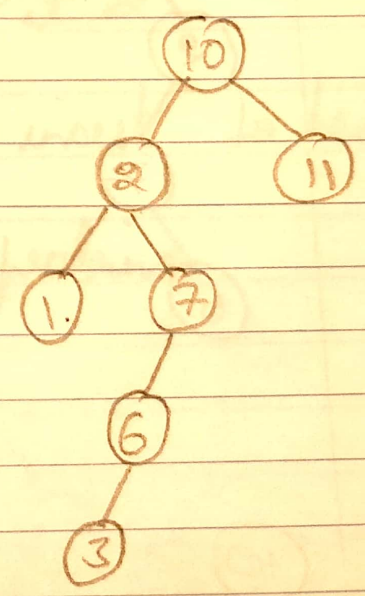
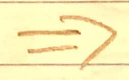
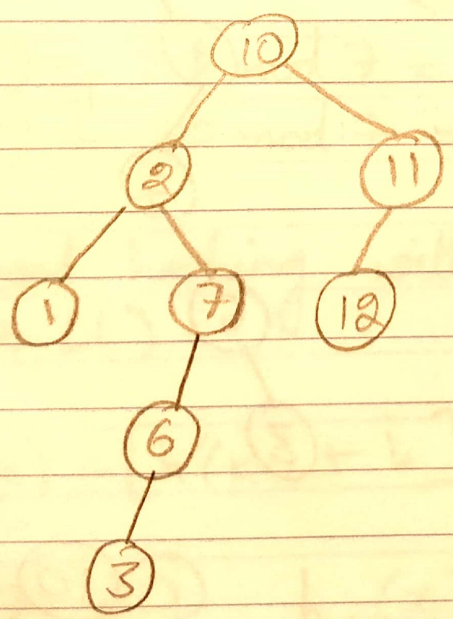
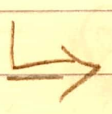


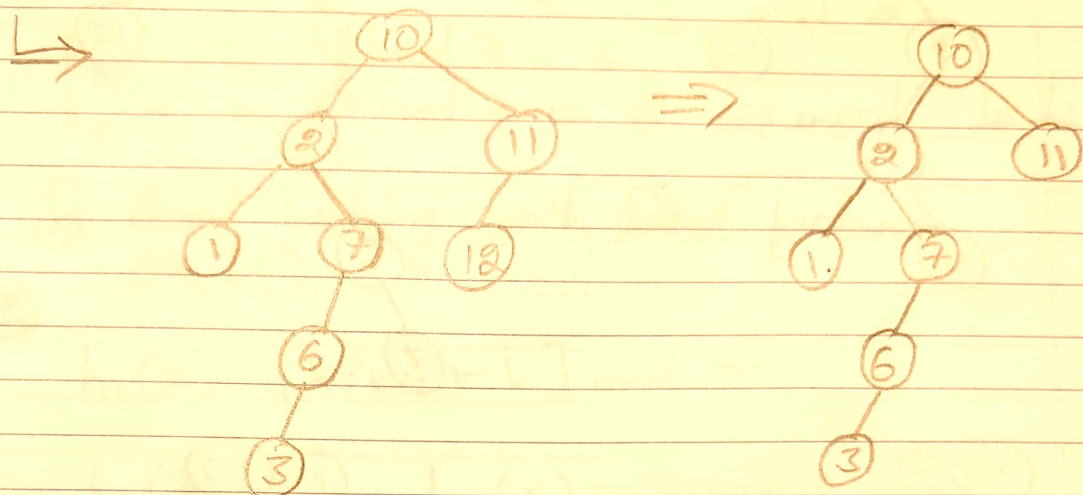
Binary Search Tree after
insertion

67



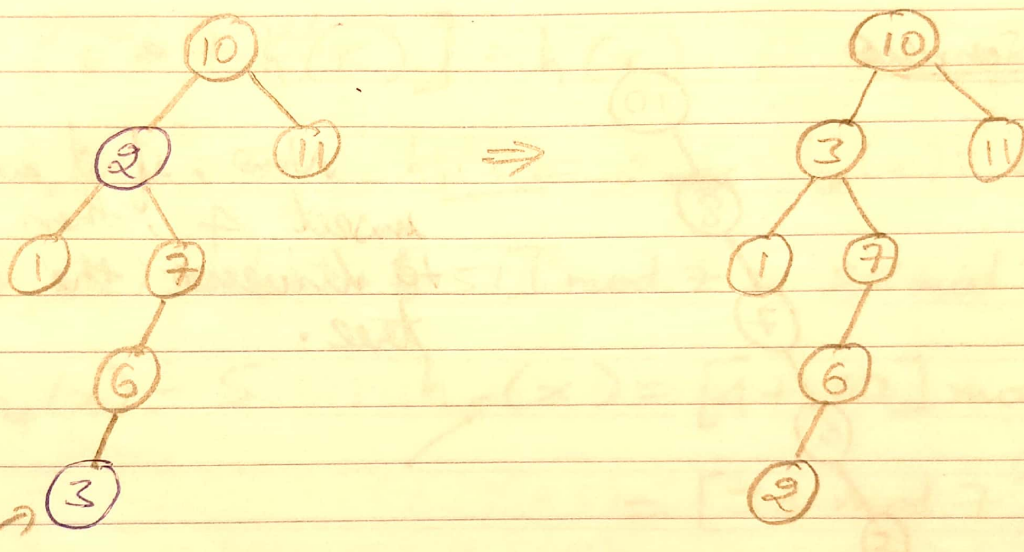
\therefore 12 has one child 11, 12 will be replaced with 11 & then 12 will be deleted





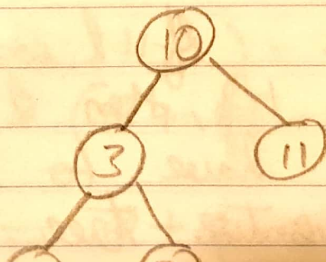
c> To delete 2, we first need to find 2's successor (\because 2 has two children).
Then swap 2 with its successor & then delete 2 from the new position.

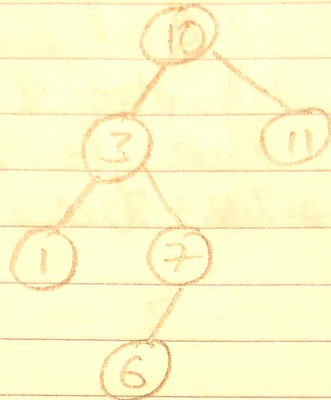
2's successor will be the minimum of its right subtree.



Successor
of 3

Since, 2 is now a leaf, it can be removed.



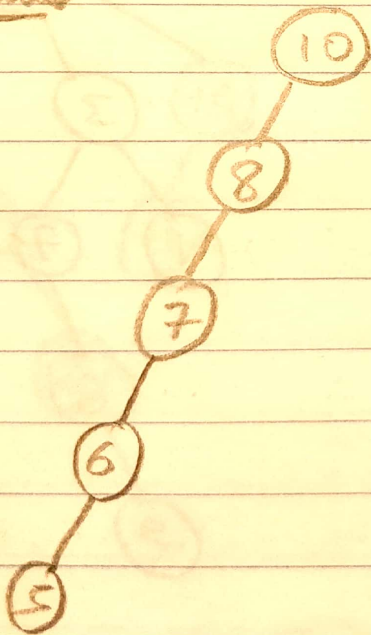


3> Worst-case run time for insertion into Binary Search Tree occurs when height of the tree =, n .

\Rightarrow Runtime for insertion = $O(n)$ (worst-case)

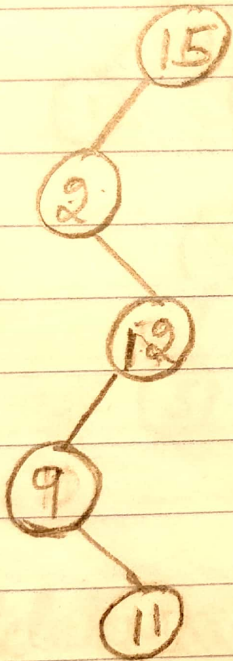
This occurs in the following two scenarios:

1st Scenario



Now, if I wish to insert 4, then I to traverse the entire tree.

2nd scenario



If I want to insert 10, then I'll have to traverse the entire tree.

a) 4)

7, 9, 18, 51, 33, 30

$$h(x) = x \bmod 7$$

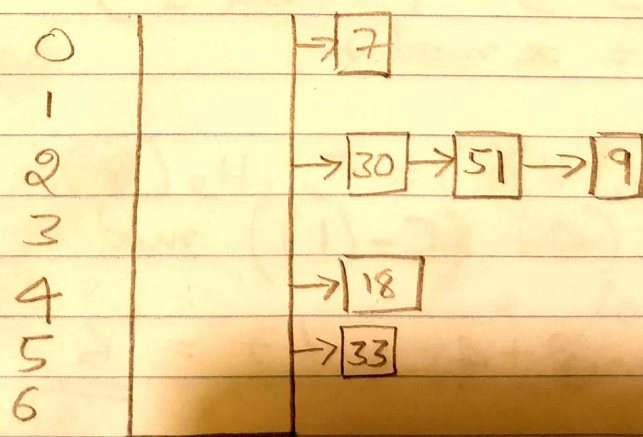
$$h(7) = 7 \bmod 7 = 0 ; h(9) = 9 \bmod 7 = 2$$

$$h(18) = 18 \bmod 7 = 4 ; h(51) = 51 \bmod 7 = 2$$

↑ insert to head

$$h(33) = 33 \bmod 7 = 5 ;$$

$$h(30) = 30 \bmod 7 = 2 \Rightarrow \text{insert to head}$$



b) Closed hashing with linear probing.

$$H(x) = (h(x) + i) \bmod 7 \quad i = \text{no. of collision}$$

$$H(7) = 0; H(9) = 2; H(18) = 4$$

$$H(51) = (51 \bmod 7 + i) \bmod 7 = (2 + 1) \bmod 7 = 3$$

$$H(33) = 5$$

$$H(30) = (30 \bmod 7 + i) \bmod 7 = (2 + 2) \bmod 7 = 4$$

$$\therefore H(4) = (4 + 1) \bmod 7$$

$$= 5$$

\Rightarrow again a collision

$$H(5) = (5 + 1) \bmod 7 = 6 \quad (\text{no collision})$$

0	7
1	
2	9
3	51
4	18
5	33
6	30

resulting hash table

$$c) \quad H(x) = [h(x) + i^2 c_0] = [h(x) + i^2] \bmod 7$$

$$H(7) = 0; \quad H(9) = 2; \quad H(18) = 4;$$

$$H(51) = [51 + 1^2] \bmod 7 = 52 \bmod 7 = 3;$$

$$H(33) = 5; \quad H(30) = [30 + 2^2] \bmod 7 \\ = 34 \bmod 7 = 6;$$

$$c) \quad H(x) = [h(x) + i^2 c_0] \mod 7 = [h(x) + i^2] \mod 7$$

$$H(7) = 0; \quad H(9) = 2; \quad H(18) = 4;$$

$$H(51) = [51 + 1^2] \mod 7 = 52 \mod 7 = 3;$$

$$H(33) = 5; \quad H(30) = [30 + 2^2] \mod 7 = 34 \mod 7 = 6;$$

0	7
1	
2	9
3	51
4	18
5	33
6	30

resulting hash table

$$d) \quad H(x) = [h_1(x) + i h_2(x)] \mod 7$$

$$h_1(x) = x \mod 7$$

$$h_2(x) = 5 - (x \mod 5)$$

$$H(7) = 7 \bmod 7 = 0 ; H(9) = 9 \bmod 7 = 2$$

$$H(18) = 4 ; H(51) = [51 \bmod 7 + 2 \cdot 5 - (51 \bmod 5)] \bmod 7$$

$$= [2 + 2 \cdot 5 - 1] \bmod 7$$

$$H(51) = 6 \bmod 7 = 6$$

$$H(33) = 5 ;$$

$$H(30) = [30 \bmod 7 + 2 \cdot 5 - (30 \bmod 5)] \bmod 7$$

$$= [2 + 2 \cdot 5 - 0] \bmod 7 = 12 \bmod 7 = 5$$

$$= [2 + 2\{5-0\}] \bmod 7 = 12 \bmod 7 = 5$$

There's a clash

$$\begin{aligned} \therefore H(5) &= [5 \bmod 7 + 1\{5-0\}] \bmod 7 \\ &= (5+5) \bmod 7 \\ &= 10 \bmod 7 = 3 \end{aligned}$$

$$\Rightarrow H(30) = \underline{\underline{3}}$$

0	7
1	.
2	9
3	30
4	18
5	33
6	51

resulting hash table

1) If an element occurs more than $\lceil n/2 \rceil$ times then that element would also be the median.

∴ ① Using the $\text{SELECT}(k, n, A)$ algorithm we'll get the median.

② Divide A into $n/5$ groups of 5 elements each.

③ Find the median of each group

④ Find the median of medians by calling $\text{SELECT}(n/10, n/5)$ recursively

⑤ Let median = m ,
 $k=0$

for i to $\text{length}(\text{Array})$
if ($A[i] == m$)

② Let median = m ,

$k = 0$

for i to length Array

if ($A[i] == m$)

$k = k + 1;$

if ($k > \lceil \frac{n}{2} \rceil$)

then m occurs $\lceil \frac{n}{2} \rceil$ times

else

it doesn't

Both ① & ② run in $O(n)$ time

\therefore This algorithm runs in $O(n)$.