

# List of NP-complete problems

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Here are some of the more commonly known problems that are NP-complete when expressed as decision problems. This list is in no way comprehensive (there are more than 3000 known NP-complete problems). Most of the problems in this list are taken from Garey and Johnson's seminal book *Computers and Intractability: A Guide to the Theory of NP-Completeness*, and are here presented in the same order and organization.

## Contents

- 1 Graph theory
  - 1.1 Covering and partitioning
  - 1.2 Subgraphs and supergraphs
  - 1.3 Vertex ordering
  - 1.4 Iso- and other morphisms
  - 1.5 Miscellaneous
- 2 Network design
  - 2.1 Spanning trees
  - 2.2 Cuts and connectivity
  - 2.3 Routing problems
  - 2.4 Flow problems
  - 2.5 Miscellaneous
  - 2.6 Graph Drawing
- 3 Sets and partitions
  - 3.1 Covering, hitting, and splitting
  - 3.2 Weighted set problems
  - 3.3 Set partitions
- 4 Storage and retrieval
  - 4.1 Data storage
  - 4.2 Compression and representation
  - 4.3 Database problems
- 5 Sequencing and scheduling
  - 5.1 Sequencing on one processor
  - 5.2 Multiprocessor scheduling
  - 5.3 Shop scheduling
  - 5.4 Miscellaneous
- 6 Mathematical programming
- 7 Algebra and number theory
  - 7.1 Divisibility problems
  - 7.2 Solvability of equations
  - 7.3 Miscellaneous
- 8 Games and puzzles
- 9 Logic
  - 9.1 Propositional logic
  - 9.2 Miscellaneous
- 10 Automata and language theory
  - 10.1 Automata theory

- 10.2 Formal languages
- 11 Computational geometry
- 12 Program optimization
  - 12.1 Code generation
  - 12.2 Programs and schemes
- 13 Miscellaneous
- 14 See also
- 15 Notes
- 16 References

## Graph theory

### Covering and partitioning

- Vertex cover<sup>[1][2]</sup>
- Dominating set, a.k.a. domination number<sup>[3]</sup>

NP-complete special cases include the edge dominating set problem, i.e., the dominating set problem in line graphs. NP-complete variants include the connected dominating set problem.

- Domatic partition, a.k.a. domatic number<sup>[4]</sup>
- Graph coloring, a.k.a. chromatic number<sup>[1][5]</sup>
- Partition into cliques

This is the same problem as coloring the complement of the given graph.<sup>[6]</sup>

- Complete coloring, a.k.a. achromatic number<sup>[7]</sup>
- Monochromatic triangle<sup>[8]</sup>
- Feedback vertex set<sup>[1][9]</sup>
- Feedback arc set<sup>[1][10]</sup>
- Partial feedback edge set<sup>[11]</sup>
- Minimum maximal independent set a.k.a. minimum independent dominating set<sup>[12]</sup>

NP-complete special cases include the minimum maximal matching problem,<sup>[13]</sup> which is essentially equal to the edge dominating set problem (see above).

- Partition into triangles<sup>[14]</sup>
- Partition into isomorphic subgraphs<sup>[15]</sup>
- Partition into Hamiltonian subgraphs<sup>[16]</sup>
- Partition into forests<sup>[17]</sup>
- Partition into perfect matchings<sup>[18]</sup>
- Two-stage maximum weight stochastic matching<sup>[citation needed]</sup>
- Clique covering problem<sup>[1][19]</sup>
- Berth allocation problem<sup>[citation needed]</sup>
- Covering by complete bipartite subgraphs<sup>[20]</sup>
- Grundy number<sup>[21]</sup>

- Rank coloring a.k.a. cycle rank
- Treewidth<sup>[22]</sup>

## Subgraphs and supergraphs

- Clique<sup>[1][23]</sup>
- Independent set<sup>[24]</sup>
- Induced subgraph with property  $\Pi$ <sup>[citation needed]</sup>
- Induced connected subgraph with property  $\Pi$ <sup>[citation needed]</sup>
- Induced path<sup>[25]</sup>
- Balanced complete bipartite subgraph<sup>[26]</sup>
- Bipartite subgraph<sup>[27]</sup>
- Degree-bounded connected subgraph<sup>[28]</sup>
- Planar subgraph<sup>[29]</sup>
- Edge-subgraph<sup>[30]</sup>
- Transitive subgraph<sup>[31]</sup>
- Unconnected subgraph<sup>[32]</sup>
- Minimum k-connected subgraph<sup>[33]</sup>
- Cubic subgraph<sup>[34]</sup>
- Minimum equivalent digraph<sup>[35]</sup>
- Hamiltonian completion<sup>[36]</sup>
- Interval graph completion<sup>[37]</sup>
- Path graph completion<sup>[38]</sup>

## Vertex ordering

- Hamiltonian circuit<sup>[1][39]</sup>
- Directed Hamiltonian circuit<sup>[1][40]</sup>
- Hamiltonian path<sup>[41]</sup>
- Bandwidth<sup>[42]</sup>
- Directed bandwidth<sup>[43]</sup>
- Optimal linear arrangement<sup>[44]</sup>
- Directed optimal linear arrangement<sup>[45]</sup>
- Minimum cut linear arrangement<sup>[46]</sup>
- Rooted tree arrangement<sup>[47]</sup>
- Directed elimination ordering<sup>[48]</sup>
- Elimination degree sequence<sup>[49]</sup>
- Pathwidth,<sup>[22]</sup> or, equivalently, interval thickness, and vertex separation number<sup>[50]</sup>

## Iso- and other morphisms

- Subgraph isomorphism<sup>[51]</sup>
- Largest common subgraph<sup>[52]</sup>
- Maximum subgraph matching<sup>[53]</sup>
- Graph contractibility<sup>[54]</sup>

- Graph homomorphism<sup>[55]</sup>
- Digraph D-morphism<sup>[56]</sup>

## Miscellaneous

- Path with forbidden pairs<sup>[57]</sup>
- Multiple choice matching<sup>[58]</sup>
- Graph Grundy numbering<sup>[21]</sup>
- Kernel<sup>[59]</sup>
- K-closure<sup>[60]</sup>
- Intersection graph basis<sup>[61]</sup>
- Path distinguishers<sup>[62]</sup>
- Metric dimension<sup>[63]</sup>
- Nešetřil–Rödl dimension<sup>[64]</sup>
- Threshold number<sup>[65]</sup>
- Oriented diameter<sup>[66]</sup>
- Weighted diameter<sup>[67]</sup>

## Network design

### Spanning trees

- Degree-constrained spanning tree
- Minimum degree spanning tree
- Maximum leaf spanning tree
- Minimum k-spanning tree
- Shortest total path length spanning tree
- Bounded diameter spanning tree
- Capacitated spanning tree
- Geometric capacitated spanning tree
- Optimum communication spanning tree
- Isomorphic spanning tree
- Kth best spanning tree
- Bounded component spanning forest
- Multiple choice branching
- Steiner tree<sup>[1]</sup>
- Geometric Steiner tree
- Cable Trench Problem
- Minimum touching tree/Minimum length corridor

### Cuts and connectivity

- Graph partitioning
- Acyclic partition
- Maximum cut<sup>[1]</sup>
- Minimum bounded cut (minimum cut into bounded sets)
- Biconnectivity augmentation

- Strong connectivity augmentation
- Network reliability
- Network survivability
- Normalized cut<sup>[68]</sup>
- Multiway cut
- Minimum k-cut
- k-vital edges

## Routing problems

- Bottleneck traveling salesman
- Chinese postman for mixed graphs
- Euclidean traveling salesman
- k-Chinese postman
- K most vital arcs
- Kth shortest path problem
- Metric traveling salesman
- Longest circuit problem
- Longest path problem
- Prize collecting traveling salesman
- Rural postman
- Shortest path in general networks
- Shortest weight-constrained path
- Stacker-crane
- Time constrained traveling salesman feasibility
- Traveling salesman problem
- Vehicle routing problem
- Capacitated arc routing problem

## Flow problems

- Minimum edge-cost flow
- Integral flow with multipliers
- Path constrained network flow
- Integral flow with homologous arcs
- Integral flow with bundles
- Undirected flow with lower bounds
- Directed two-commodity integral flow
- Undirected two-commodity integral flow
- Disjoint connecting paths
- Maximum length-bounded disjoint paths
- Maximum fixed-length disjoint paths
- Maximum flow network interdiction problem
- Unsplittable multicommodity flow

## Miscellaneous

- Quadratic assignment problem
- Minimizing dummy activities in PERT networks
- Constrained triangulation

- Intersection graph for segments on a grid
- Edge embedding on a grid
- Geometric connected dominating set
- Minimum broadcast time problem
- Min-max multicenter
- Min-sum multicenter
- Uncapacitated Facility Location
- Metric k-center

## Graph Drawing

Graphs occur frequently in everyday applications, and are used to model a lot of often huge data. Such examples include biological or social networks, which contain hundreds, thousands and even billions of nodes in some cases (see e.g. Facebook or LinkedIn). Therefore, even when all information is available in the form of a graph, it is important to have good ways of visualizing the data in order to make sense of it and extract interesting features, and this is what makes graph drawing important.

- Rectilinear planarity testing<sup>[69]</sup>
- Upward planarity testing<sup>[69]</sup>
- Upward sphericity testing
- Maximum upward planar subgraph computation for embedded digraphs

## Sets and partitions

### Covering, hitting, and splitting

- 3-dimensional matching<sup>[1][70]</sup>
- Exact cover<sup>[1][71]</sup>
- Set packing<sup>[1][72]</sup>
- Set splitting<sup>[73]</sup>
- Set cover<sup>[1][74]</sup>
- Minimum test set<sup>[75]</sup>
- Set basis<sup>[76]</sup>
- Hitting set<sup>[1][77]</sup>
- Intersection pattern<sup>[78]</sup>
- Comparative containment<sup>[79]</sup>
- 3-matroid intersection<sup>[80]</sup>

### Weighted set problems

- Partition<sup>[1]</sup>
- Subset sum
- Subset product
- 3-partition
- Numerical 3-dimensional matching
- Numerical matching with target sums
- Expected component sum

- Minimum sum of squares
- Kth largest subset
- Kth largest m-tuple

## Set partitions

- Median partition

## Storage and retrieval

### Data storage

- Bin packing<sup>[81]</sup>
- Dynamic storage allocation<sup>[82]</sup>
- Pruned trie space minimization<sup>[83]</sup>
- Expected retrieval cost<sup>[84]</sup>
- Rooted tree storage assignment<sup>[85]</sup>
- Multiple copy file allocation<sup>[86]</sup>
- Capacity assignment<sup>[87]</sup>

### Compression and representation

- Shortest common supersequence<sup>[88]</sup>
- Shortest common superstring<sup>[89]</sup>
- Longest common subsequence problem for the case of arbitrary (i.e., not *a priori* fixed) number of input sequences. (In contrast, the alphabet size is immaterial as long as it is greater than one.)<sup>[90]</sup>
- Bounded Post correspondence problem<sup>[91]</sup>
- Hitting string<sup>[92]</sup>
- Sparse matrix compression<sup>[93]</sup>
- Consecutive ones submatrix<sup>[94]</sup>
- Consecutive ones matrix partition<sup>[95]</sup>
- Consecutive ones matrix augmentation<sup>[96]</sup>
- Consecutive block minimization<sup>[97]</sup>
- Consecutive sets<sup>[98]</sup>
- 2-dimensional consecutive sets<sup>[99]</sup>
- String-to-string correction<sup>[100]</sup>
- Grouping by swapping<sup>[101]</sup>
- External macro data compression<sup>[102]</sup>
- Internal macro data compression<sup>[103]</sup>
- Regular expression substitution<sup>[104]</sup>
- Rectilinear picture compression<sup>[105]</sup>
- Optimal vector quantization codebook<sup>[citation needed]</sup>
- Minimal grammar-based compression<sup>[citation needed]</sup>
- Adaptive block-size compression<sup>[citation needed]</sup>

## Database problems

- Minimum cardinality key<sup>[106]</sup>
- Additional key<sup>[107]</sup>
- Prime attribute name<sup>[108]</sup>
- Boyce-Codd normal form violation<sup>[109]</sup>
- Conjunctive query foldability<sup>[110]</sup>
- Conjunctive Boolean query<sup>[111]</sup>
- Tableau equivalence<sup>[112]</sup>
- Serializability of database histories<sup>[113]</sup>
- Safety of database transaction systems<sup>[114]</sup>
- Consistency of database frequency tables<sup>[115]</sup>
- Safety of file protection systems<sup>[116]</sup>

## Sequencing and scheduling

### Sequencing on one processor

- Job sequencing<sup>[1]</sup>
- Sequencing with release times and deadlines
- Sequencing to minimize tardy tasks
- Sequencing to minimize tardy weight
- Sequencing to minimize weighted completion time
- Sequencing to minimize weighted tardiness
- Sequencing with deadlines and set-up times
- Sequencing to minimize maximum cumulative cost

### Multiprocessor scheduling

- Multiprocessor scheduling
- Precedence constrained scheduling
- Resource constrained scheduling
- Scheduling with individual deadlines
- Preemptive scheduling
- Scheduling to minimize weighted completion time

### Shop scheduling

- Open-shop scheduling
- Flow Shop Scheduling Problem
- No-wait Flow Shop Scheduling
- Two-processor Flow Shop with bounded buffer
- Job-shop scheduling

### Miscellaneous

- Timetable design



- Staff scheduling
- Production planning
- Deadlock avoidance

## Mathematical programming

- Integer linear programming
- 0-1 linear programming<sup>[1]</sup>
- Quadratic programming (NP-hard in some cases, P if convex)
- Cost-parametric linear programming
- Feasible basis extension
- Open hemisphere
- K-relevancy
- Traveling salesman polytope non-adjacency
- Knapsack<sup>[1]</sup>
- Integer knapsack
- Continuous multiple choice knapsack
- Partially ordered knapsack
- Generalized assignment problem
- Comparative vector inequalities
- Selecting a maximum volume submatrix – Problem of selecting the best conditioned subset of a larger  $m \times n$  matrix. This class of problem is associated with Rank revealing QR factorizations and D optimal experimental design.<sup>[117]</sup>
- Sparse approximation

## Algebra and number theory

### Divisibility problems

- Quadratic congruences
- Simultaneous incongruences
- Simultaneous divisibility of linear polynomials
- Comparative divisibility
- Exponential expression divisibility
- Non-divisibility of a product polynomial
- Non-trivial greatest common divisor

### Solvability of equations

- Quadratic Diophantine equations
- Algebraic equations over  $\text{GF}(2)$ ; or over any finite field.
- Root of modulus 1
- Number of roots for a product polynomial
- Periodic solution recurrence relation
- Non-linear univariate polynomials over  $\text{GF}[2^n]$ ,  $n$  the length of the input. Indeed over any  $\text{GF}[q^n]$ .

## Miscellaneous

- Permanent evaluation
- Cosine product integration
- Equilibrium point
- Unification with commutative operators
- Unification for finitely presented algebras
- Integer expression membership
- Minimal addition chain

## Games and puzzles

- Alternating hitting set
- Alternating maximum weighted matching
- Annihilation
- Battleship
- Bulls and Cows, marketed as Master Mind
- Clickomania (SameGame)
- Cross Sums
- Crossword puzzle construction
- Eternity II
- Fillomino<sup>[118]</sup>
- Flood-It<sup>[119]</sup>
- FreeCell<sup>[120]</sup>
- Heyawake<sup>[121]</sup>
- Instant Insanity
- Kakuro
- Lemmings<sup>[122]</sup>
- Light Up
- Masyu
- Minesweeper Consistency Problem<sup>[123]</sup>
- Nurikabe
- Paint by numbers (Nonogram)
- Rabin games
- Sift
- Slither Link
- Square-tiling
- Sudoku
- Tetris
- Variable partition truth assignment
- Verbal arithmetic

# Logic

## Propositional logic

Propositional logic problems, in particular satisfiability problems and their variants, are of particular practical interest because many practical problems can be solved by expressing them as satisfiability problems, and then using efficient SAT solvers to obtain an exact solution quickly<sup>[*citation needed*]</sup>.

- Boolean satisfiability<sup>[1][124]</sup>
- 3-satisfiability<sup>[1][125]</sup>
- Not-all-equal 3SAT<sup>[126]</sup>
- One-in-three 3SAT<sup>[127]</sup>
- Maximum 2-Satisfiability<sup>[128]</sup>
- Generalized satisfiability<sup>[129]</sup>
- Non-tautology<sup>[130]</sup>
- Minimum equivalent disjunctive normal form for a given truth table<sup>[131]</sup>
- Truth-functionally complete connectives<sup>[132]</sup>
- Planar-3SAT
- Monotone-3SAT

## Miscellaneous

- Modal logic S5-Satisfiability
- Negation-free logic
- Conjunctive satisfiability with functions and inequalities
- Minimum axiom set
- First order subsumption
- Second order instantiation

# Automata and language theory

## Automata theory

- Reduction of incompletely specified automata<sup>[133]</sup>
- Minimum inferred finite state automaton<sup>[134]</sup>

## Formal languages

- Minimum inferred regular expression<sup>[135]</sup>
- Reynolds covering for context-free grammars<sup>[136]</sup>
- Non-LR(k) context-free grammar<sup>[137]</sup>
- Context-free programmed language membership<sup>[138]</sup>
- Quasi-real-time language membership<sup>[139]</sup>

## Computational geometry

- Testing whether a tree may be represented as Euclidean minimum spanning tree
- Unit disk graph recognition (Unit disk graphs are intersection graphs of circles of unit radius in the plane)<sup>[140]</sup>
- Many motion planning among polygonal obstacles in the plane are NP-hard.
  - Planar partitioning into connected subassemblies: Given a set  $A$  of non-overlapping (but possibly touching) polygons in the plane, decide if there is a proper subset  $S$  of  $A$  that can be separated from  $A \setminus S$  by a collision-free rigid motion of  $S$ , and such that both  $S$  and  $A \setminus S$  are connected.<sup>[141]</sup>
- Art gallery problem and its variations.

## Program optimization

### Code generation

- Register sufficiency
- Feasible register assignment
- Register sufficiency for loops
- Code generation on a one-register machine
- Code generation with unlimited registers
- Code generation for parallel assignments
- Code generation with address expressions
- Code generation with unfixed variable locations
- Ensemble computation
- Microcode bit optimization

### Programs and schemes

- Inequivalence of programs with arrays
- Inequivalence of programs with assignments
- Inequivalence of finite memory programs
- Inequivalence of loop programs without nesting
- Inequivalence of simple functions
- Strong inequivalence of Ianov schemes
- Strong inequivalence for monadic recursion
- Non-containment for free B-schemes
- Non-freedom for loop-free program schemes
- Programs with formally recursive procedures

## Miscellaneous

- Sorting by Reversals
- Sorting by Transpositions
- Block Sorting (Sorting by Block Moves)
- Pancake sorting
- Cyclic ordering
- Non-liveness of free choice Petri nets

- Reachability for 1-conservative Petri nets
- Finite function generation
- Permutation generation
- Decoding of linear codes
- Shapley–Shubik power index
- Clustering
- Randomization test for matched pairs
- Maximum likelihood ranking
- Matrix domination
- Matrix cover
- Simply deviated disjunction
- Decision tree
- Minimum weight and/or graph solution
- Fault detection in logic circuits
- Fault detection in directed graphs
- Fault detection with test points
- Three-dimensional Ising model<sup>[142]</sup>

## See also

- Karp's 21 NP-complete problems
- List of PSPACE-complete problems

## Notes

1. <sup>^</sup> *abcdefghijklmnopqrstuvwxyz* Karp (1972)
2. <sup>^</sup> Garey & Johnson (1979): GT1
3. <sup>^</sup> Garey & Johnson (1979): GT2
4. <sup>^</sup> Garey & Johnson (1979): GT3
5. <sup>^</sup> Garey & Johnson (1979): GT4
6. <sup>^</sup> Garey & Johnson (1979): GT15
7. <sup>^</sup> Garey & Johnson (1979): GT5
8. <sup>^</sup> Garey & Johnson (1979): GT6
9. <sup>^</sup> Garey & Johnson (1979): GT7
10. <sup>^</sup> Garey & Johnson (1979): GT8
11. <sup>^</sup> Garey & Johnson (1979): GT9
12. <sup>^</sup> Minimum Independent Dominating Set (<http://www.csc.kth.se/~viggo/wwwcompendium/node14.html>)
13. <sup>^</sup> Garey & Johnson (1979): GT10
14. <sup>^</sup> Garey & Johnson (1979): GT11
15. <sup>^</sup> Garey & Johnson (1979): GT12
16. <sup>^</sup> Garey & Johnson (1979): GT13
17. <sup>^</sup> Garey & Johnson (1979): GT14
18. <sup>^</sup> Garey & Johnson (1979): GT16
19. <sup>^</sup> Garey & Johnson (1979): GT17
20. <sup>^</sup> Garey & Johnson (1979): GT18
21. <sup>^</sup> <sup>a b</sup> Garey & Johnson (1979): GT56
22. <sup>^</sup> <sup>a b</sup> Arnborg, Corneil & Proskurowski (1987)
23. <sup>^</sup> Garey & Johnson (1979): GT19
24. <sup>^</sup> Garey & Johnson (1979): GT20
25. <sup>^</sup> Garey & Johnson (1979): GT23
26. <sup>^</sup> Garey & Johnson (1979): GT24
27. <sup>^</sup> Garey & Johnson (1979): GT25

28. ^ Garey & Johnson (1979): GT26
29. ^ Garey & Johnson (1979): GT27
30. ^ Garey & Johnson (1979): GT28
31. ^ Garey & Johnson (1979): GT29
32. ^ Garey & Johnson (1979): GT30
33. ^ Garey & Johnson (1979): GT31
34. ^ Garey & Johnson (1979): GT32
35. ^ Garey & Johnson (1979): GT33
36. ^ Garey & Johnson (1979): GT34
37. ^ Garey & Johnson (1979): GT35
38. ^ Garey & Johnson (1979): GT36
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46. ^ Garey & Johnson (1979): GT44
47. ^ Garey & Johnson (1979): GT45
48. ^ Garey & Johnson (1979): GT46
49. ^ Garey & Johnson (1979): GT47
50. ^ Kashiwabara & Fujisawa (1979); Ohtsuki et al. (1979); Lengauer (1981).
51. ^ Garey & Johnson (1979): GT48
52. ^ Garey & Johnson (1979): GT49
53. ^ Garey & Johnson (1979): GT50
54. ^ Garey & Johnson (1979): GT51
55. ^ Garey & Johnson (1979): GT52
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67. ^ Garey & Johnson (1979): GT65
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*IEEE*. 20 October 2009. <http://www.cs.berkeley.edu/~malik/papers/SM-ncut.pdf>.
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70. ^ Garey & Johnson (1979): SP1
71. ^ Garey & Johnson (1979): SP2
72. ^ Garey & Johnson (1979): SP3
73. ^ Garey & Johnson (1979): SP4
74. ^ Garey & Johnson (1979): SP5
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76. ^ Garey & Johnson (1979): SP7
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78. ^ Garey & Johnson (1979): SP9
79. ^ Garey & Johnson (1979): SP10
80. ^ Garey & Johnson (1979): SP11
81. ^ Garey & Johnson (1979): SR1

82. ^ Garey & Johnson (1979): SR2
83. ^ Garey & Johnson (1979): SR3
84. ^ Garey & Johnson (1979): SR4
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124. ^ Garey & Johnson (1979): LO1
125. ^ Garey & Johnson (1979): LO2
126. ^ Garey & Johnson (1979): LO3
127. ^ Garey & Johnson (1979): LO4
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