

Big O notation

Explained with a Company Party Analogy

Imagine you're planning a company party and need to invite all employees.

Let's say:



- **n = number of employees**

Different ways to handle the invitations represent different algorithms. Big O helps us describe how the **time or effort** grows as the number of employees increases.

Extremely good

$O(1)$ - Constant Time


Analogy: You announce, "Party at 6 PM!" during an all-hands meeting.

-  One action, no matter how many people are there.
-  Time does **not** increase with more employees.

Scalability: Excellent

$O(\log n)$ - Logarithmic Time

Analogy: You tell one person, who tells two others, who each tell two more, like a tree.

-  Spreads quickly, even as the company grows.
- Extremely efficient.

Scalability: Excellent - ideal for large teams.

Just good

🟡 $O(n)$ - Linear Time

Analogy: You go around and tell each person individually.

- 👤 More employees = more time.
- 10 employees = 10 minutes.
- 100 employees = 100 minutes.

Scalability: Okay, but effort grows with company size.

🟡 $O(n \log n)$ - Log-linear Time

Analogy: You break the team into small groups for some characteristic or let's say departments, e.g. managers, sales, IT, etc., then meet with each group one by one.

- 📁 Smart compromise between personal and scalable.
- Grows reasonably with size.

Scalability: Good - a balanced approach.

So so

🔴 $O(n^2)$ - Quadratic Time

Analogy: You arrange for every employee to talk to every other employee to coordinate party details.

- 💬 10 employees = 100 conversations.
- 100 employees = 10,000 conversations!
- Effort grows **explosively**.

Scalability: Very poor - avoid this pattern.

Summary Table

| Big O | Party Analogy | Scales Well? |
|---------------|------------------------------------|--------------|
| $O(1)$ | One announcement to all | ✅ Excellent |
| $O(\log n)$ | You tell one, they tell two others | ✅ Very good |
| $O(n)$ | Tell each person one by one | 🟡 Okay |
| $O(n \log n)$ | Group then talk to each | 🟡 Good |
| $O(n^2)$ | Everyone talks to everyone | ❌ Bad |

Examples

Add vs Multiply Complexity

Drop constants and non-dominant

Best, worst and expected cases

BigO / Theta / Omega

Time vs/and Space Complexity

Amortized Time

LogN Runtimes

Recursive Runtimes

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