

Time Series Labb 1

Time Series Analysis, Umeå University

Artem Shiryayev Group 8

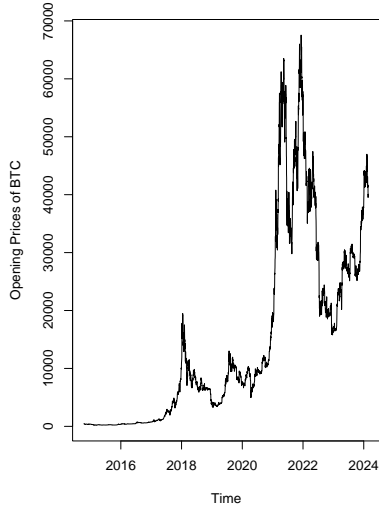
2024-03-15

Problem Formulation

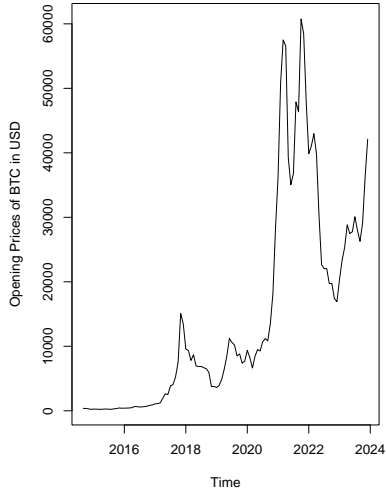
- ▶ Time Series Forecasting
- ▶ Investment Decision based on Accuracy of Models
- ▶ Exploration of data
- ▶ Model evaluation

Data Presentation

Original data

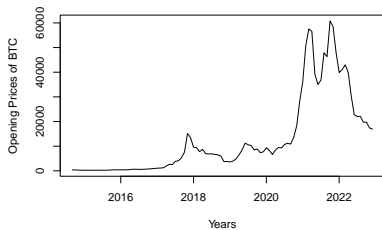


Smoothed Monthly data

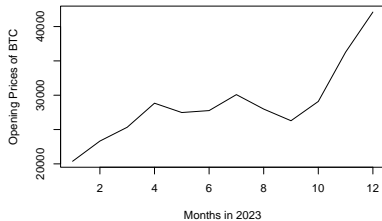


Data Presentation

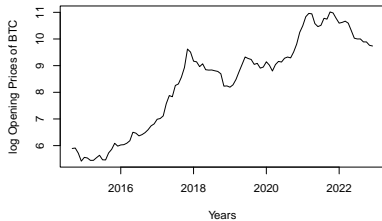
Split Training data



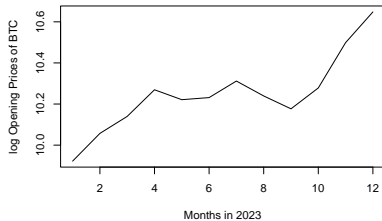
Split test data



Log train data

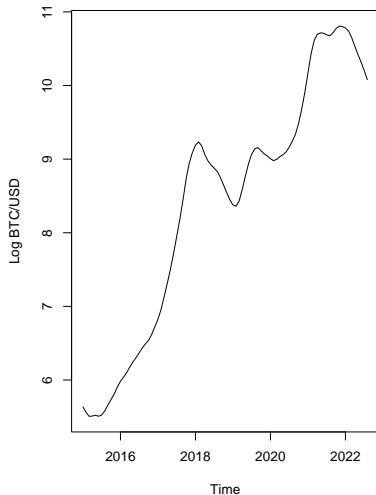


Log test data

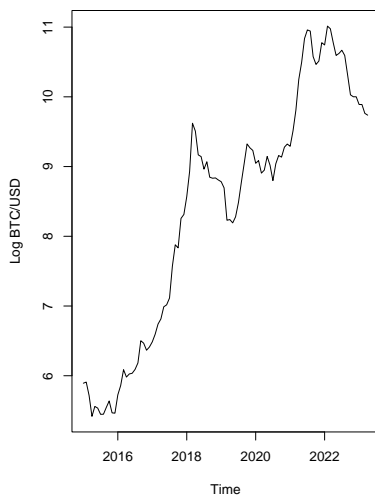


Statistical Methods Results: S1

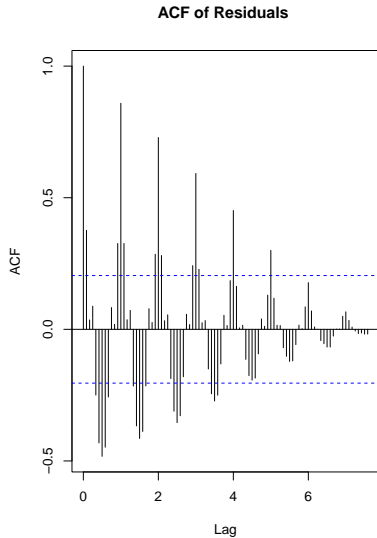
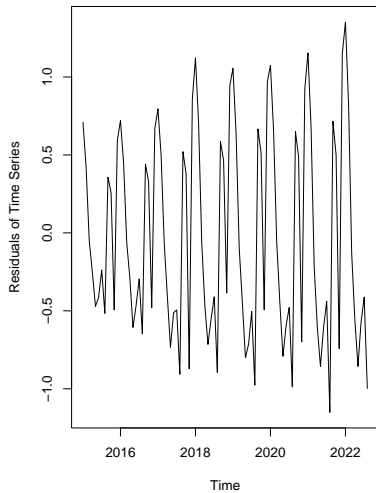
S1 Filtered Time Series



Unfiltered Time Series



Statistical Methods Results: S1



Statistical Methods Results: S2

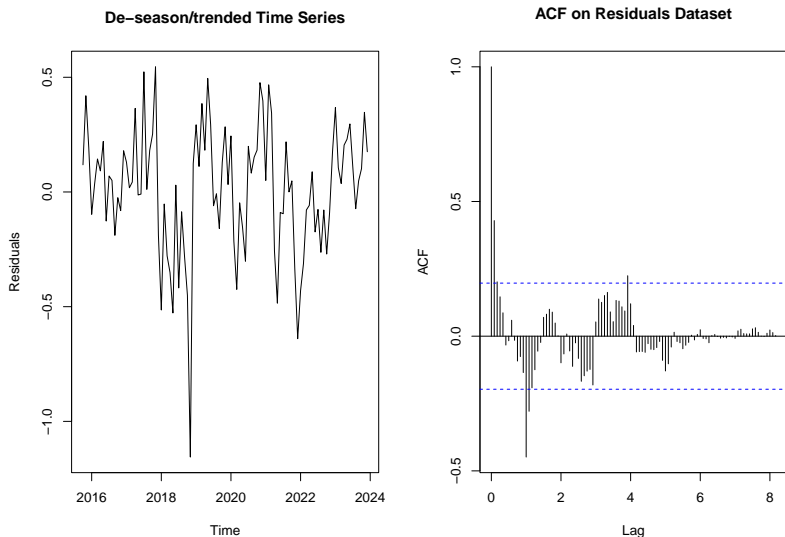


Figure 1: Differenced Method for de-seasonalized and de-trending Time

Checking Assumptions

- ▶ Visually checking the sample autocorrelation function

H_0 = The Time Series is iid Noise

H_1 = The Time Series is NOT iid Noise

- ▶ Protmanteau test
- ▶ Turning point test
- ▶ Difference-sign test
- ▶ Mann-Kendall Rank test
- ▶ Augmented Dicker-Fuller test
- ▶ Checking for normality
 - ▶ Histogram
 - ▶ qq plot
 - ▶ Normality test
 - ▶ Shapiro-Wilks test
 - ▶ Shapiro-Francia test

Checking Assumptions

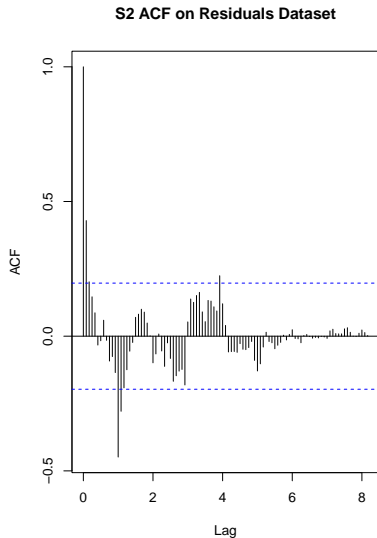
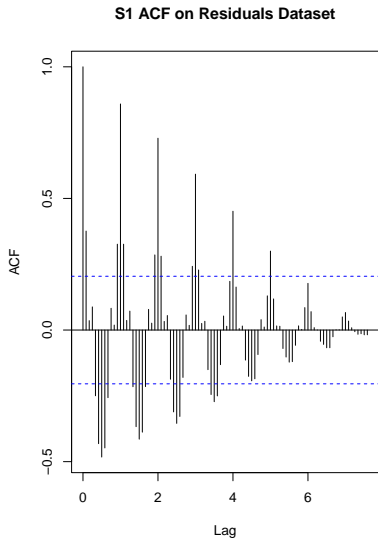


Figure 2: ACF for S1 and S2 methods on time series

Checking Assumptions

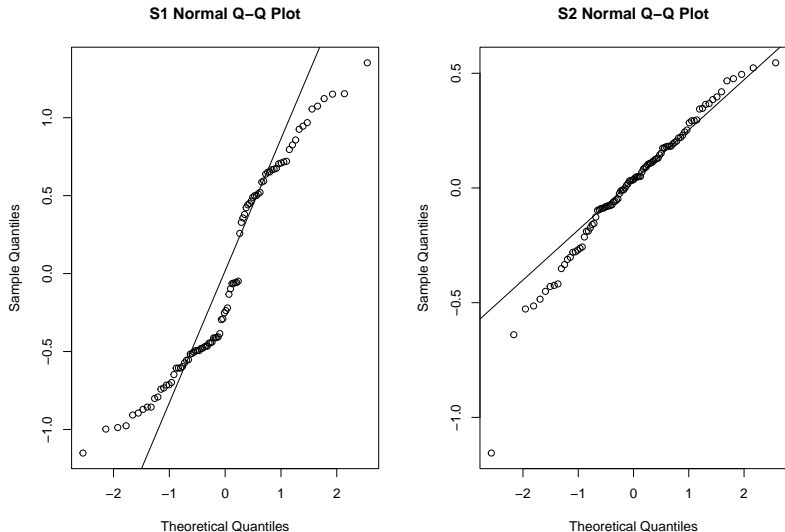


Figure 3: Q-Q plots for Normality of Residuals of S1 and S2 Method

Spectral Analysis

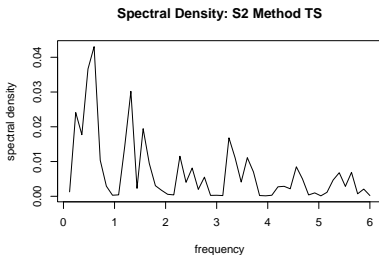
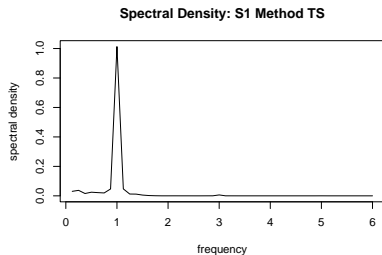
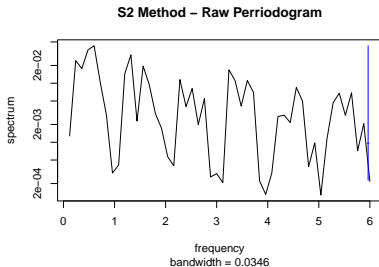
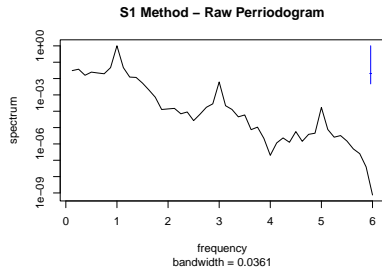


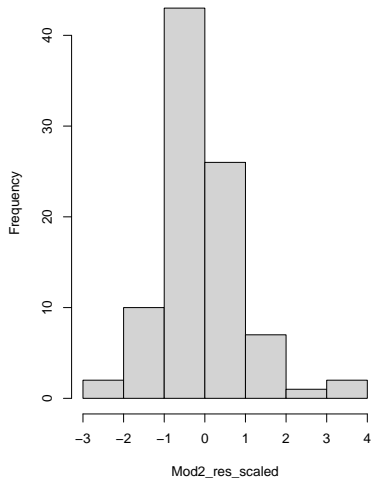
Figure 4: Spectral Analysis on S1 and S2 data

Fitting ARMA models

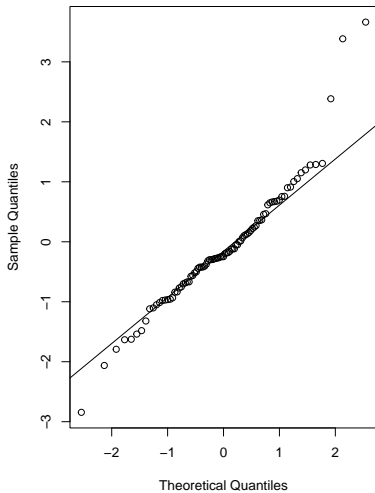
- ▶ Check ACF for $AR(p)$, PACF for $MA(q)$
- ▶ Evaluate using AIC
- ▶ Fit model
- ▶ Residual Diagnostics

Fitting ARMA models

Histogram of Rescaled residuals



Normal Q-Q Plot



Fitting ARMA models

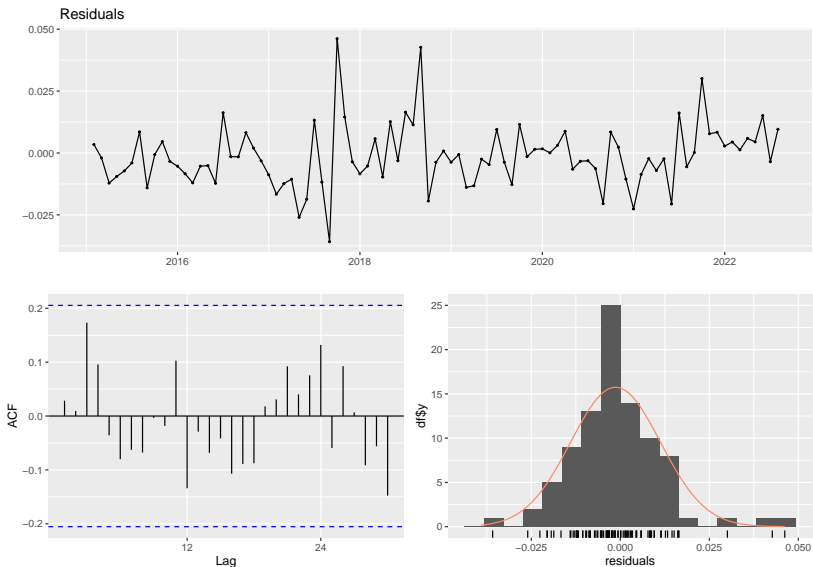


Figure 5: Residual checks

Forecast of 2023

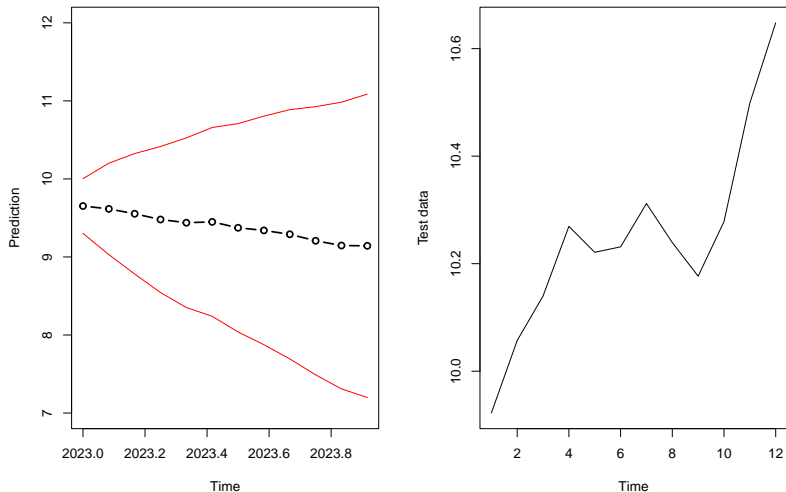


Figure 6: Forecast with SARIMA(9,0,1) Model with 95 CI

Forecast of 2023

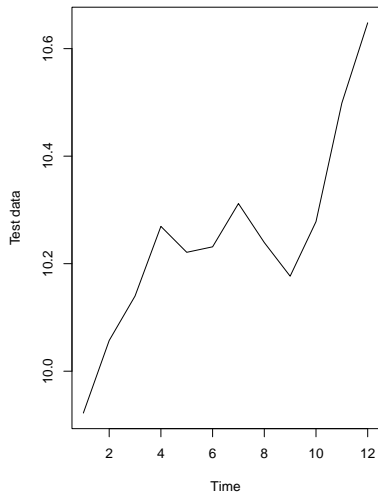
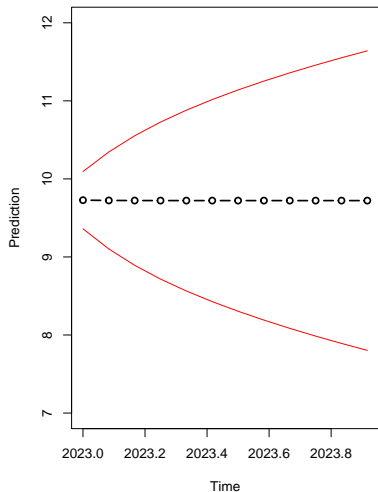


Figure 7: Forecast with auto.arima AR(1) Model with 95 CI

Summary

| Model | ARMA(1,1) | ARMA(9,1) | SARMA(9,0,1) | |
|-------|-----------|-----------|------------------|-------|
| | | | $\times (1,0,1)$ | AR(1) |
| MSE | 1261 | 1258 | 10.1 | 3.72 |

Conclusion

- ▶ Poor performance, linear time series model is insufficient or poorly specified for using on this kind of data set
- ▶ Stationary assumption and normality assumption violated
- ▶ Intuitively the assumption of the model that $s_t = s_{t+d}$ may be too strong
- ▶ Poor data handling and processing from my side
- ▶ Challenging to fit a suitable model

Questions?

Thank you for listening.