

# Euribor (January 1994 - October 2024) Univariate DL TSA

November 19, 2024

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[1]: #Long Short-Term Memory Model

import os
import random
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import statsmodels.api as sm
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
from sklearn.preprocessing import MinMaxScaler
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import LSTM, Dense, Input
from tensorflow.keras.callbacks import EarlyStopping
from sklearn.metrics import mean_squared_error

random.seed(42)

new_directory = 'C:/Users/artem/Desktop'

os.chdir(new_directory)

euribor_data = pd.read_csv('ECB Data Portal_20241114135109.csv')

euribor_data.rename(columns={'Euribor 1-year - Historical close, average of_
↳ observations through period (FM.M.U2.EUR.RT.MM.EURIBOR1YD_.HSTA)':_
↳ 'Euribor'}, inplace=True)

columns_to_remove = ['DATE', 'TIME PERIOD']

euribor_data = euribor_data.drop(columns=columns_to_remove)

dates = pd.date_range(start='1994', periods=len(euribor_data), freq='M')

euribor_data.index = dates

def acf_pacf_fig(series, both=True, lag=30):
    fig, axes = plt.subplots(1, 2 if both else 1, figsize=(15, 5))
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if both:
    plot_acf(series, lags=lag, ax=axes[0])
    plot_pacf(series, lags=lag, ax=axes[1])
    axes[0].set_title('ACF Plot')
    axes[1].set_title('PACF Plot')
else:
    plot_acf(series, lags=lag, ax=axes[0])
    axes[0].set_title('ACF Plot')

plt.tight_layout()
plt.show()

acf_pacf_fig(euribor_data['Euribor'], both=True, lag=30)

train = euribor_data.iloc[:300]
valid_start = euribor_data.index[300]
test_start = euribor_data.index[324]

valid = euribor_data[(euribor_data.index >= valid_start) & (euribor_data.index_
    ↪ < test_start)]
test = euribor_data[test_start:]

scaler = MinMaxScaler()
train.loc[:, 'Euribor'] = scaler.fit_transform(train[['Euribor']])
valid.loc[:, 'Euribor'] = scaler.transform(valid[['Euribor']])
test.loc[:, 'Euribor'] = scaler.transform(test[['Euribor']])

T = 12
HORIZON = 3

def prepare_shifted_data(data, T, horizon):
    data_shifted = data.copy()

    y_columns = []
    for h in range(1, horizon + 1):
        data_shifted[f'y_t+{h}'] = data_shifted['Euribor'].shift(-h)
        y_columns.append(f'y_t+{h}')

    for t in range(1, T + 1):
        data_shifted[f'Euribor_t-{t}'] = data_shifted['Euribor'].shift(t)

    data_shifted.dropna(inplace=True)

    y = np.array(data_shifted[y_columns])
    X = np.array(data_shifted[[f'Euribor_t-{t}' for t in range(1, T + 1)]])

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    return X.reshape(X.shape[0], T, 1), y

X_train, y_train = prepare_shifted_data(train, T, HORIZON)
X_valid, y_valid = prepare_shifted_data(valid, T, HORIZON)
X_test, y_test = prepare_shifted_data(test, T, HORIZON)

print(f"X_train shape: {X_train.shape}, y_train shape: {y_train.shape}")

latent_dim = 6
batch_size = 16
epochs = 50

model = Sequential()

model.add(Input(shape=(X_train.shape[1], X_train.shape[2])))

model.add(LSTM(latent_dim, return_sequences=True))

model.add(LSTM(units=64, return_sequences=False))

model.add(Dense(HORIZON))

model.compile(optimizer='adam', loss='mean_squared_error')

LSTM_earlystop = EarlyStopping(monitor='val_loss', patience=5)

model_fit = model.fit(
    X_train, y_train,
    batch_size=batch_size,
    epochs=epochs,
    validation_data=(X_valid, y_valid),
    callbacks=[LSTM_earlystop],
    verbose=1
)

preds = model.predict(X_test)

evdta = pd.DataFrame(preds, columns=[f't+{t}' for t in range(1, 4)])

predicted_values = evdta[['t+1', 't+2', 't+3']].values
scaled_predicted_values = scaler.inverse_transform(predicted_values)

evdta[['t+1', 't+2', 't+3']] = scaled_predicted_values

evdta['Average Prediction'] = evdta[['t+1', 't+2', 't+3']].mean(axis=1)

evdta.columns = [f'November 2024' if col == 't+1' else

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        f'December 2024' if col == 't+2' else
        f'January 2025' if col == 't+3' else
        'Average Prediction' if col == 'Average Prediction' else col
    for col in evdta.columns]

evdta = evdta.drop(columns=['actual'], errors='ignore')

print(evdta[['November 2024', 'December 2024', 'January 2025', 'Average_
    ↪Prediction']])

y_test_flattened = y_test.reshape(-1, 1)

avg_nov_2024 = evdta['November 2024'].mean()
avg_dec_2024 = evdta['December 2024'].mean()
avg_jan_2025 = evdta['January 2025'].mean()

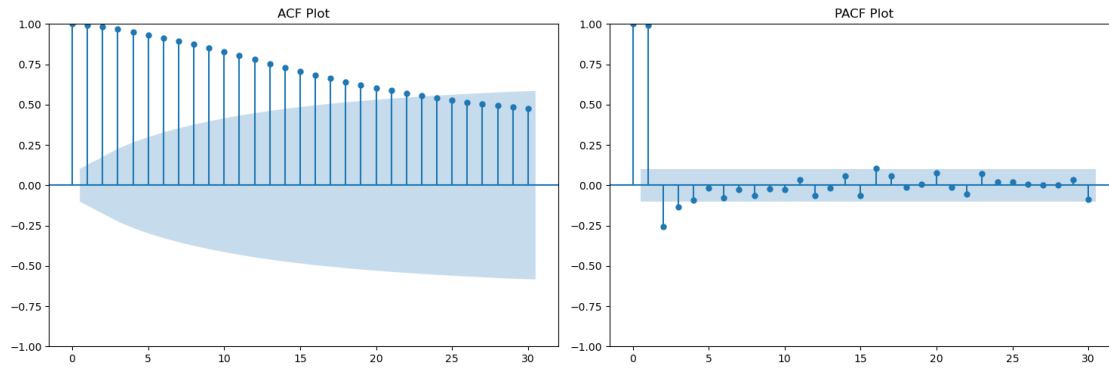
print(f"Average Prediction for November 2024 (t+1): {avg_nov_2024}")
print(f"Average Prediction for December 2024 (t+2): {avg_dec_2024}")
print(f"Average Prediction for January 2025 (t+3): {avg_jan_2025}")

mse_avg = mean_squared_error(y_test_flattened[:len(evdta)], evdta['Average_
    ↪Prediction'])
mse_t1 = mean_squared_error(y_test_flattened[:len(evdta)], evdta['November_
    ↪2024'])
mse_t2 = mean_squared_error(y_test_flattened[:len(evdta)], evdta['December_
    ↪2024'])
mse_t3 = mean_squared_error(y_test_flattened[:len(evdta)], evdta['January_
    ↪2025'])

rmse_avg = np.sqrt(mse_avg)
rmse_t1 = np.sqrt(mse_t1)
rmse_t2 = np.sqrt(mse_t2)
rmse_t3 = np.sqrt(mse_t3)

print(f"Root Mean Squared Error for November 2024 (t+1): {rmse_t1}")
print(f"Root Mean Squared Error for December 2024 (t+2): {rmse_t2}")
print(f"Root Mean Squared Error for January 2025 (t+3): {rmse_t3}")
print(f"Root Mean Squared Error for Average Prediction: {rmse_avg}")

```



X\_train shape: (285, 12, 1), y\_train shape: (285, 3)

Epoch 1/50

18/18 4s 27ms/step -

loss: 0.1423 - val\_loss: 0.0461

Epoch 2/50

18/18 0s 6ms/step - loss:

0.0229 - val\_loss: 0.0151

Epoch 3/50

18/18 0s 6ms/step - loss:

0.0144 - val\_loss: 0.0059

Epoch 4/50

18/18 0s 6ms/step - loss:

0.0091 - val\_loss: 0.0013

Epoch 5/50

18/18 0s 6ms/step - loss:

0.0092 - val\_loss: 0.0013

Epoch 6/50

18/18 0s 7ms/step - loss:

0.0065 - val\_loss: 9.3834e-04

Epoch 7/50

18/18 0s 6ms/step - loss:

0.0058 - val\_loss: 8.6217e-04

Epoch 8/50

18/18 0s 6ms/step - loss:

0.0083 - val\_loss: 5.7020e-04

Epoch 9/50

18/18 0s 6ms/step - loss:

0.0056 - val\_loss: 6.3694e-04

Epoch 10/50

18/18 0s 6ms/step - loss:

0.0056 - val\_loss: 4.2841e-04

Epoch 11/50

18/18 0s 6ms/step - loss:

0.0053 - val\_loss: 3.8109e-04

Epoch 12/50  
 18/18 0s 6ms/step - loss:  
 0.0065 - val\_loss: 4.0378e-04  
 Epoch 13/50  
 18/18 0s 6ms/step - loss:  
 0.0060 - val\_loss: 4.3089e-04  
 Epoch 14/50  
 18/18 0s 7ms/step - loss:  
 0.0069 - val\_loss: 4.0723e-04  
 Epoch 15/50  
 18/18 0s 6ms/step - loss:  
 0.0059 - val\_loss: 4.3359e-04  
 Epoch 16/50  
 18/18 0s 7ms/step - loss:  
 0.0071 - val\_loss: 5.3090e-04  
 1/1 0s 292ms/step

|    | November 2024 | December 2024 | January 2025 | Average Prediction |
|----|---------------|---------------|--------------|--------------------|
| 0  | -0.513842     | -0.596957     | -0.657899    | -0.589566          |
| 1  | -0.512376     | -0.595330     | -0.656155    | -0.587954          |
| 2  | -0.494421     | -0.576701     | -0.634231    | -0.568451          |
| 3  | -0.465938     | -0.547148     | -0.599549    | -0.537545          |
| 4  | -0.409225     | -0.488305     | -0.530839    | -0.476123          |
| 5  | -0.322665     | -0.398485     | -0.426898    | -0.382682          |
| 6  | -0.170665     | -0.241576     | -0.246739    | -0.219660          |
| 7  | -0.009449     | -0.075035     | -0.059288    | -0.047924          |
| 8  | 0.174426      | 0.114567      | 0.150393     | 0.146462           |
| 9  | 0.478820      | 0.423541      | 0.490288     | 0.464216           |
| 10 | 0.819592      | 0.766778      | 0.859006     | 0.815126           |
| 11 | 1.161768      | 1.109935      | 1.217030     | 1.162911           |
| 12 | 1.496709      | 1.444765      | 1.556278     | 1.499251           |
| 13 | 1.837602      | 1.783501      | 1.891763     | 1.837622           |
| 14 | 2.159513      | 2.102251      | 2.199465     | 2.153743           |
| 15 | 2.445696      | 2.385621      | 2.465174     | 2.432163           |
| 16 | 2.692814      | 2.630453      | 2.688586     | 2.670618           |
| 17 | 2.906277      | 2.841924      | 2.877263     | 2.875154           |
| 18 | 3.093936      | 3.027268      | 3.040529     | 3.053911           |
| 19 | 3.259900      | 3.190957      | 3.182710     | 3.211189           |
| 20 | 3.374998      | 3.305911      | 3.277369     | 3.319426           |
| 21 | 3.470929      | 3.400422      | 3.357051     | 3.409467           |
| 22 | 3.545433      | 3.474257      | 3.417847     | 3.479179           |
| 23 | 3.580452      | 3.511541      | 3.442323     | 3.511439           |
| 24 | 3.548896      | 3.487685      | 3.405252     | 3.480611           |
| 25 | 3.502805      | 3.449220      | 3.356881     | 3.436302           |
| 26 | 3.464830      | 3.416858      | 3.318235     | 3.399974           |
| 27 | 3.434076      | 3.389976      | 3.287984     | 3.370679           |
| 28 | 3.402551      | 3.361372      | 3.258308     | 3.340744           |
| 29 | 3.370859      | 3.331589      | 3.229773     | 3.310740           |
| 30 | 3.338750      | 3.300547      | 3.202035     | 3.280444           |

Average Prediction for November 2024 (t+1): 1.8600982427597046  
 Average Prediction for December 2024 (t+2): 1.7977873086929321  
 Average Prediction for January 2025 (t+3): 1.7858045101165771  
 Root Mean Squared Error for November 2024 (t+1): 2.219490154865728  
 Root Mean Squared Error for December 2024 (t+2): 2.1779990854982882  
 Root Mean Squared Error for January 2025 (t+3): 2.1589742859434256  
 Root Mean Squared Error for Average Prediction: 2.185119397986958

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[2]: #Gated Recurrent Units Model

import os
import random
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import statsmodels.api as sm
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
from sklearn.preprocessing import MinMaxScaler
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import GRU, Dense, Input
from tensorflow.keras.callbacks import EarlyStopping
from sklearn.metrics import mean_squared_error

random.seed(42)

new_directory = 'C:/Users/artem/Desktop'

os.chdir(new_directory)

euribor_data = pd.read_csv('ECB Data Portal_20241114135109.csv')

euribor_data.rename(columns={'Euribor 1-year - Historical close, average of
    ↳ observations through period (FM.M.U2.EUR.RT.MM.EURIBOR1YD_.HSTA)':
    ↳ 'Euribor'}, inplace=True)

columns_to_remove = ['DATE', 'TIME PERIOD']

euribor_data = euribor_data.drop(columns=columns_to_remove)

dates = pd.date_range(start='1994', periods=len(euribor_data), freq='M')

euribor_data.index = dates

def acf_pacf_fig(series, both=True, lag=30):
    fig, axes = plt.subplots(1, 2 if both else 1, figsize=(15, 5))

    if both:

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        plot_acf(series, lags=lag, ax=axes[0])
        plot_pacf(series, lags=lag, ax=axes[1])
        axes[0].set_title('ACF Plot')
        axes[1].set_title('PACF Plot')
    else:
        plot_acf(series, lags=lag, ax=axes[0])
        axes[0].set_title('ACF Plot')

plt.tight_layout()
plt.show()

acf_pacf_fig(euribor_data['Euribor'], both=True, lag=30)

train = euribor_data.iloc[:300]
valid_start = euribor_data.index[300]
test_start = euribor_data.index[324]

valid = euribor_data[(euribor_data.index >= valid_start) & (euribor_data.index_
    ↪ < test_start)]
test = euribor_data[test_start:]

scaler = MinMaxScaler()
train.loc[:, 'Euribor'] = scaler.fit_transform(train[['Euribor']])
valid.loc[:, 'Euribor'] = scaler.transform(valid[['Euribor']])
test.loc[:, 'Euribor'] = scaler.transform(test[['Euribor']])

T = 12
HORIZON = 3

def prepare_shifted_data(data, T, horizon):
    data_shifted = data.copy()

    y_columns = []
    for h in range(1, horizon + 1):
        data_shifted[f'y_t+{h}'] = data_shifted['Euribor'].shift(-h)
        y_columns.append(f'y_t+{h}')

    for t in range(1, T + 1):
        data_shifted[f'Euribor_t-{t}'] = data_shifted['Euribor'].shift(t)

    data_shifted.dropna(inplace=True)

    y = np.array(data_shifted[y_columns])
    X = np.array(data_shifted[[f'Euribor_t-{t}' for t in range(1, T + 1)]])

    return X.reshape(X.shape[0], T, 1), y

```



```

X_train, y_train = prepare_shifted_data(train, T, HORIZON)
X_valid, y_valid = prepare_shifted_data(valid, T, HORIZON)
X_test, y_test = prepare_shifted_data(test, T, HORIZON)

print(f"X_train shape: {X_train.shape}, y_train shape: {y_train.shape}")

latent_dim = 6
batch_size = 16
epochs = 50

model = Sequential()

model.add(Input(shape=(X_train.shape[1], X_train.shape[2])))

model.add(GRU(latent_dim, return_sequences=True))

model.add(GRU(units=64, return_sequences=False))

model.add(Dense(HORIZON))

model.compile(optimizer='adam', loss='mean_squared_error')

GRU_earlystop = EarlyStopping(monitor='val_loss', patience=5)

model_fit = model.fit(
    X_train, y_train,
    batch_size=batch_size,
    epochs=epochs,
    validation_data=(X_valid, y_valid),
    callbacks=[GRU_earlystop],
    verbose=1
)

preds = model.predict(X_test)

evdta = pd.DataFrame(preds, columns=[f't+{t}' for t in range(1, 4)])

predicted_values = evdta[['t+1', 't+2', 't+3']].values
scaled_predicted_values = scaler.inverse_transform(predicted_values)

evdta[['t+1', 't+2', 't+3']] = scaled_predicted_values

evdta['Average Prediction'] = evdta[['t+1', 't+2', 't+3']].mean(axis=1)

evdta.columns = [f'November 2024' if col == 't+1' else
                  f'December 2024' if col == 't+2' else
                  f'January 2025' if col == 't+3' else

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        'Average Prediction' if col == 'Average Prediction' else col
    for col in evdta.columns]

evdta = evdta.drop(columns=['actual'], errors='ignore')

print(evdta[['November 2024', 'December 2024', 'January 2025', 'Average_
    ↪Prediction']]))

y_test_flattened = y_test.reshape(-1, 1)

avg_nov_2024 = evdta['November 2024'].mean()
avg_dec_2024 = evdta['December 2024'].mean()
avg_jan_2025 = evdta['January 2025'].mean()

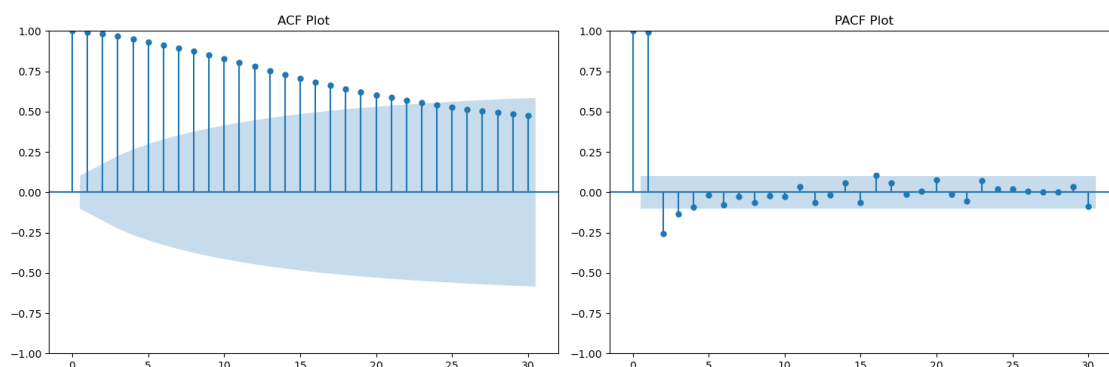
print(f"Average Prediction for November 2024 (t+1): {avg_nov_2024}")
print(f"Average Prediction for December 2024 (t+2): {avg_dec_2024}")
print(f"Average Prediction for January 2025 (t+3): {avg_jan_2025}")

mse_avg = mean_squared_error(y_test_flattened[:len(evdta)], evdta['Average_
    ↪Prediction'])
mse_t1 = mean_squared_error(y_test_flattened[:len(evdta)], evdta['November_
    ↪2024'])
mse_t2 = mean_squared_error(y_test_flattened[:len(evdta)], evdta['December_
    ↪2024'])
mse_t3 = mean_squared_error(y_test_flattened[:len(evdta)], evdta['January_
    ↪2025'])

rmse_avg = np.sqrt(mse_avg)
rmse_t1 = np.sqrt(mse_t1)
rmse_t2 = np.sqrt(mse_t2)
rmse_t3 = np.sqrt(mse_t3)

print(f"Root Mean Squared Error for November 2024 (t+1): {rmse_t1}")
print(f"Root Mean Squared Error for December 2024 (t+2): {rmse_t2}")
print(f"Root Mean Squared Error for January 2025 (t+3): {rmse_t3}")
print(f"Root Mean Squared Error for Average Prediction: {rmse_avg}")

```



X\_train shape: (285, 12, 1), y\_train shape: (285, 3)

Epoch 1/50

18/18 4s 30ms/step -

loss: 0.1394 - val\_loss: 0.0382

Epoch 2/50

18/18 0s 6ms/step - loss:

0.0229 - val\_loss: 0.0187

Epoch 3/50

18/18 0s 6ms/step - loss:

0.0146 - val\_loss: 0.0078

Epoch 4/50

18/18 0s 6ms/step - loss:

0.0124 - val\_loss: 0.0013

Epoch 5/50

18/18 0s 6ms/step - loss:

0.0092 - val\_loss: 3.6294e-04

Epoch 6/50

18/18 0s 6ms/step - loss:

0.0087 - val\_loss: 3.0588e-04

Epoch 7/50

18/18 0s 6ms/step - loss:

0.0109 - val\_loss: 6.6394e-04

Epoch 8/50

18/18 0s 8ms/step - loss:

0.0096 - val\_loss: 4.2341e-04

Epoch 9/50

18/18 0s 7ms/step - loss:

0.0089 - val\_loss: 3.3639e-04

Epoch 10/50

18/18 0s 6ms/step - loss:

0.0073 - val\_loss: 8.0440e-04

Epoch 11/50

18/18 0s 7ms/step - loss:

0.0085 - val\_loss: 4.6750e-04

1/1 0s 333ms/step

|   | November 2024 | December 2024 | January 2025 | Average Prediction |
|---|---------------|---------------|--------------|--------------------|
| 0 | -0.648621     | -0.635227     | -0.630596    | -0.638148          |
| 1 | -0.647411     | -0.633726     | -0.628999    | -0.636712          |
| 2 | -0.638996     | -0.625769     | -0.619968    | -0.628244          |
| 3 | -0.624120     | -0.612127     | -0.604648    | -0.613632          |
| 4 | -0.592462     | -0.583064     | -0.572357    | -0.582628          |
| 5 | -0.539480     | -0.534185     | -0.518635    | -0.530767          |
| 6 | -0.444075     | -0.445588     | -0.421973    | -0.437212          |
| 7 | -0.324724     | -0.333861     | -0.301648    | -0.320078          |
| 8 | -0.172195     | -0.189908     | -0.148590    | -0.170231          |

|    |          |          |          |          |
|----|----------|----------|----------|----------|
| 9  | 0.063333 | 0.033595 | 0.087044 | 0.061324 |
| 10 | 0.353824 | 0.312231 | 0.376074 | 0.347376 |
| 11 | 0.683871 | 0.633360 | 0.703954 | 0.673728 |
| 12 | 1.042277 | 0.987171 | 1.060531 | 1.029993 |
| 13 | 1.424056 | 1.368472 | 1.440997 | 1.411175 |
| 14 | 1.806793 | 1.754894 | 1.822512 | 1.794733 |
| 15 | 2.169140 | 2.125386 | 2.186223 | 2.160250 |
| 16 | 2.497047 | 2.464001 | 2.517128 | 2.492725 |
| 17 | 2.784491 | 2.763579 | 2.809592 | 2.785887 |
| 18 | 3.032425 | 3.023797 | 3.062415 | 3.039546 |
| 19 | 3.236872 | 3.241931 | 3.279630 | 3.252811 |
| 20 | 3.385033 | 3.401459 | 3.443518 | 3.410004 |
| 21 | 3.505092 | 3.526976 | 3.568779 | 3.533615 |
| 22 | 3.602897 | 3.629452 | 3.670153 | 3.634167 |
| 23 | 3.670188 | 3.701962 | 3.742972 | 3.705041 |
| 24 | 3.693460 | 3.731358 | 3.773673 | 3.732830 |
| 25 | 3.694934 | 3.738529 | 3.781076 | 3.738180 |
| 26 | 3.685333 | 3.734404 | 3.777510 | 3.732416 |
| 27 | 3.665533 | 3.719832 | 3.765172 | 3.716846 |
| 28 | 3.634139 | 3.692933 | 3.742435 | 3.689836 |
| 29 | 3.594673 | 3.656388 | 3.711120 | 3.654060 |
| 30 | 3.551725 | 3.614386 | 3.673718 | 3.613276 |

Average Prediction for November 2024 (t+1): 1.746614694595337

Average Prediction for December 2024 (t+2): 1.7504078149795532

Average Prediction for January 2025 (t+3): 1.7918970584869385

Root Mean Squared Error for November 2024 (t+1): 2.2464573938800116

Root Mean Squared Error for December 2024 (t+2): 2.261140885208698

Root Mean Squared Error for January 2025 (t+3): 2.2964614155436798

Root Mean Squared Error for Average Prediction: 2.267953548481707

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