Linear Modeling in R

Cheat Sheet

| Model type | Probability distribution | Dependent variable | Variable types | Independent variable(s) | R |
|------------------------------|-----------------------------|-------------------------------------|---|-----------------------------------|--|
| linear models | Normal | continuous | fixed effects (main effects, interactions, polynomials) random effects | nominal, continuous nominal | $\label{eq:local_problem} \begin{split} & nominal \ IV \\ & \ lm \ (y \ \sim \ factor \ (x) \) \\ & \ continuous \ IV \\ & \ lm \ (y \ \sim \ x) \\ & \ interaction \\ & \ lm \ (y \ \sim \ x \ + \ (1 \ \ \tau) \) \\ & \ lmer \ (y \ \sim \ x \ + \ (1 \ \ \tau) \) \end{split}$ |
| generalized linear models | Poisson | count | fixed effects (main effects, interactions, polynomials) | nominal, continuous | $\begin{split} &\text{glm}\left(y\sim x, \text{ family=poisson}\right) \\ &\text{model rates with offset} \\ &\text{glm}\left(y\sim x, \text{ offset=log}\left(t\right), \text{ family=poisson}\right) \\ &\text{model overdispersion with negative binomial} \\ &\text{glm.nb}\left(y\sim x\right) \end{split}$ |
| | binomial | binary | | | glm(y ~ x, family=binomial) |
| | | count (y successes, n trials) | | | <pre>glm(cbind(y, n-y) ~ x, family=binomial)</pre> |
| | | , | random effects | nominal | glmer(y \sim x + (1 τ), family=family) |

Parameter interpretation & model comparison

parameter interpretation

✓ possible fixes to failure to meet assumptions

LM with nominal IV's (ANOVA)

- extract ANOVA table to view sum-of-squares: aov ()
- ✓ overall model test, *F*-test: anova ()
- ✓ post-hoc tests to test for differences in factor levels: tukeyHSD()

LM with nominal and continuous IV's

- partial regression plots: avPlots()
- ✓ compare nested models with partial F-test, e.g., anova ()
- \checkmark compare non-nested models with AIC or adjusted R², e.g. AIC ()

GLM with Poisson distribution (Poisson regression)

- · uses log link, coefficients are outputted on log scale
- exponentiate coefficients to interpret them as ratios, e.g., exp(coef())
- ✓ compare nested models with likelihood ratio test: lrtest(), anova(..., test="Chisq")
- ✓ compare non-nested models with AIC, e.g. AIC ()

GLM binary logistic regression

- · uses logit link, coefficients are outputted as log-odds
- exponentiate coefficients to interpret them as odds, e.g., exp(coef (mod))
- take inverse logit to predict as probability, e.g., inv.logit()
- √ same model comparison as Poisson regression

GLM binomial count logistic regression

- same coefficient interpretation as binary logistic regression
- √ same model comparison as Poisson regression

G/LM assumptions and testing

- assumptions
- possible fixes to failure to meet assumptions

DV is Independently & Identically Distributed

- each sample must have the same distribution and all samples must be mutually independent
- assess study design: are observations correlated?
- plot data in order they were collected/measured: do not want patterns
- ✓ include random effects to account for nested design, spatial or temporal autocorrelation

DV & IV are linearly related

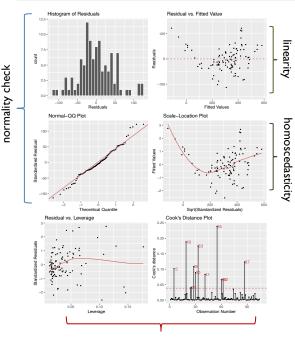
- evaluate graphically, e.g. ggpairs ()
- residuals must be ~ normally distributed with a mean of 0; examine residuals, e.g., plot (model), qqnorm(), qqline()
- ✓ transform DV, e.g. log()
- √ add interaction or polynomial to IV to account for non-linearity

No strong multicollinearity

- are IV's strongly correlated (r ≥ 0.70)?
- · assess graphically or check correlations among IV's
- test variance inflation factor after running model, e.g. vif(); VIF should be < 5
- ✓ remove I of the highly correlated IV's often IV
 with lowest correlation with DV
- √ combine correlated IV's into a single variable

Constant variance or homoscedasticity - LM's

- evaluate graphically: does spread of DV increase over continuous IV's?
 test equality of variance of DV for nominal IV's
- test equality of variance of DV for nominal IV's, e.g. var.test()
- assess with residual plot: do standardized residuals look like a cloud of points without pattern?
- ✓ transform DV with log or other transform, e.g.
 log()
- √ use a different model



outlier & influential points

Link function correctly specified - GLM's

- evaluate relationship between mean and variance; for Poisson and binomial count models no overdispersion, \$\phi > 2\$, e.g. dispersiontest(), check overdispersion()?
- check model goodness of fit, e.g. pchisq()
- check relative fit of model, e.g. pr2(),
 r.squaredGLMM()
- ✓ use quasipoisson or quasibinomial models to scale standard errors of coefficients
- employ negative binomial model for counts, e.g. glm.nb()
- √ add an observation-level random effect to account for extra variance

No highly influential observations

- assess graphically with leverage plot; plot (model)
- calculate Cook's distance, e.g.,
 cooks.distance(), observations with cook's
 distance > 4 times the mean may be influential
- check with outlierTest()
- ✓ check for data entry or transcription errors
- ✓ remove extreme or highly influential datapoints (must have a reason to do so!)
- present results with and without highly influential datapoints