

Q1

- a. for computing sum of n numbers
- i) the natural size metric for inputs is n
 - ii) adding every number up to n or add every 2 number
 - iii) it cannot be different from the input size
- b) computing $n!$
- i) the natural size metric is n for input
 - ii) multiply every number until its n input or multiply 2 number
 - iii) it can't be different
- c) Finding the largest element in a list of n numbers
- i) the natural size metric is n for inputs
 - ii) comparing 2 numbers
 - iii) it cannot be different for inputs

Q2

a) $n(n+1)$ is the same order of growth as $2000n^2$
 $n^2 = n^2$

b) $100n^2$ has a smaller order of growth than $0.01n^3$
 $n^2 < n^3$

c) $\log_2 n$ has the same order of growth than $\ln n$
 $\log_2 \log n$ $\log_e \log n$

d) $(\log_2 n)^2$ has larger order of growth than $2\log_2 n$

e) 2^{n+1} has the same order of growth as 2^n

f) $\frac{(n-1)!}{n!}$ has a smaller order of growth

Q3

from lowest to highest

1. $\lg(n+1000)$

2. $\ln^2 n$

3. $\sqrt[3]{n}$

4. $0.001n^4 + 3n^3 + 1$

5. 3^n

6. 2^{2n} or 4^n

7. $(n-2)!$

Q4

a) This algorithm computes the range of a given set of numbers. It takes the largest number and subtracts it with the smaller number

b) The basic operation for this algorithm is the comparison of numbers.

c) At least you have 2 numbers, at n you have $2(n-1)$ comparisons

d) Since this algorithm does comparison, its efficiency is $O(n)$.

e) You can do
if $A[i] < \text{minval}$
 $\text{minval} \leftarrow A[i]$
else $A[i] > \text{maxval}$
 $\text{maxval} \leftarrow A[i]$

this algorithm works fine however it has $O(n^2)$.