FeedForward Neural Networks

Course 3, Module 3, Lesson 1



Learning Objectives

- Learn the mode of action of feedforward neural networks
- Learn the mathematical equations of the hidden layers, a building block that makes neural networks special among machine learning models

Feedforward Neural Networks

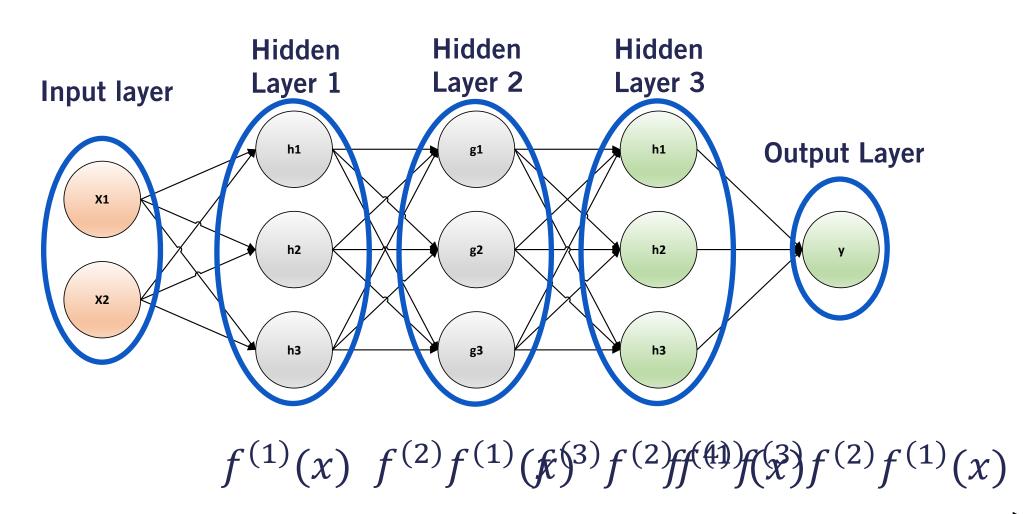
 A Feedforward Neural Network defines a mapping from input x to output y as:

$$y = f(x; \theta)$$

 An N layer FNN is represented as the function composition:

$$f(x;\theta) = f^{(N)} \left(f^{(N-1)} \left(\dots f^{(2)} \left(f^{(1)}(x) \right) \right) \right)$$

Feedforward Neural Networks: Example



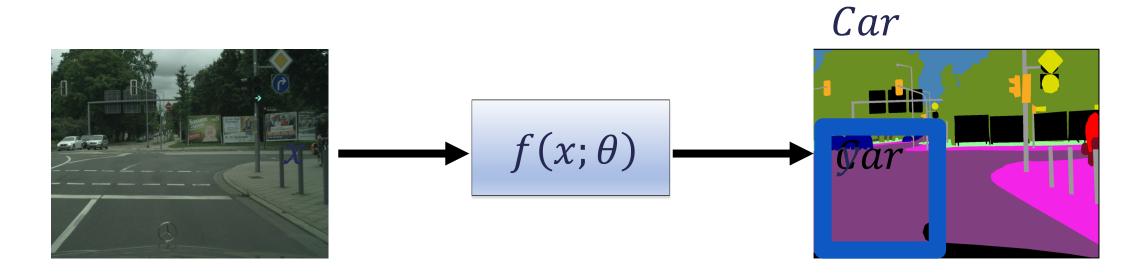
Feedforward Neural Networks

$$f(x;\theta) = f^{(N)} \left(f^{(N-1)} \left(\dots f^{(2)} \left(f^{(1)}(x) \right) \right) \right)$$

- x is called the input layer
- The final function $f^{(N)}$ is called the **output layer**
- The functions $f^{(1)}$ to $f^{(N-1)}$ are called the **hidden layers**

Feedforward Neural Networks

- Functions to estimate:
 - Object Classification: Image → Label
 - **Object Detection:** Image → Label + Location
 - Depth Estimation: Image → Depth for every pixel
 - Semantic Segmentation: Image → Label for every pixel

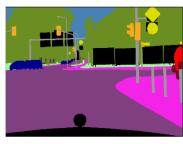


Mode Of Action Of Neural Networks

- Training: Give neural network examples of $f^*(x)$. for a wide variation of the input x. Then, optimize its parameters θ to force $f(x; \theta) \cong f^*(x)$
- Pairs of x and $f^*(x)$ are called **training data**



X



$$f^*(x)$$

 Only output is specified by training data! Network is free to do anything with its hidden layers

Hidden Units



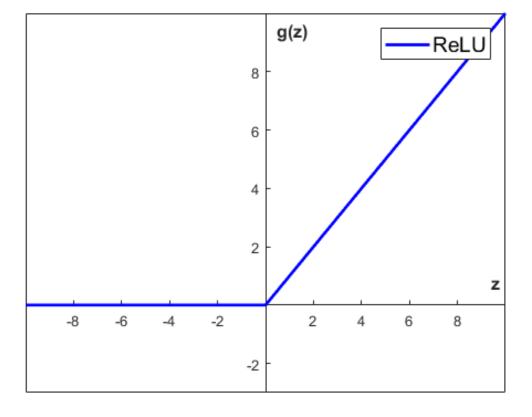
- Activation function g
- Input h_{n-1}
- Weight matrix W
- Bias **b**
- Parameters $\boldsymbol{\theta}$ are the weights and biases of all the layers of the network
- Transformed parameters passed through activation function g

The Rectified Linear Unit: ReLU

 The ReLU hidden unit is currently the default choice of activation function for Feedforward Neural

Networks

$$g(z) = \max(0, z)$$



Example: Hidden Layer With RELU Activation Function

Function
$$h_{n-1} = \begin{bmatrix} -17 & 12 & -6 \\ -14 & 2 & 7 \end{bmatrix}, \quad W = \begin{bmatrix} 9 & -2 & 9 & 10 & -3 \\ -3 & 10 & 4 & 6 & 3 \end{bmatrix}, \quad b = \begin{bmatrix} -2 & -18 & -12 \\ -6 & -3 & 2 \\ -7 & 4 & -9 \\ -6 & -12 & -10 \\ -8 & 4 & -15 \end{bmatrix}$$

$$2 \times 3$$

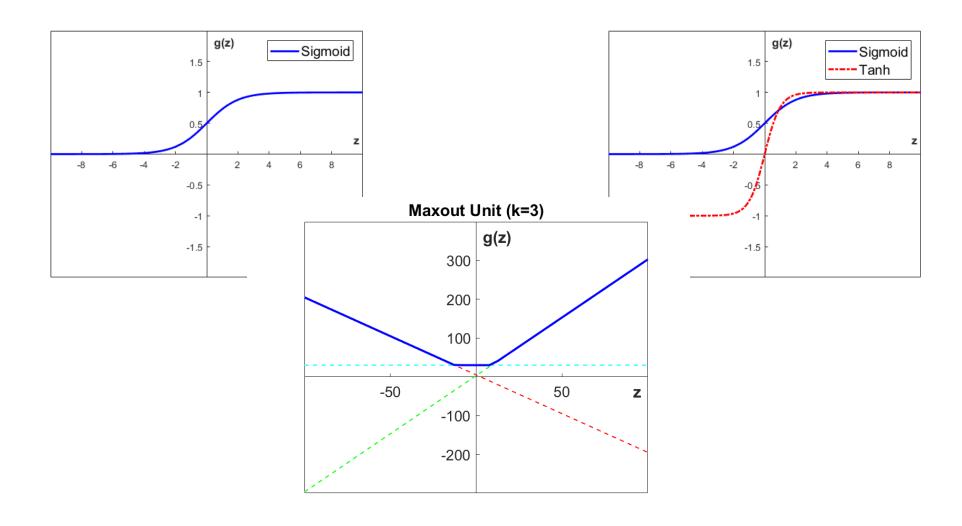
Evaluate affine transformation $W^T h_{n-1} + b$:

$$\begin{bmatrix} 9 & -3 \\ -2 & 10 \\ 9 & 4 \\ 10 & 6 \\ -3 & 3 \end{bmatrix} \begin{bmatrix} -17 & 12 & -6 \\ -14 & 2 & 7 \end{bmatrix} + \begin{bmatrix} -2 & -18 & -12 \\ -6 & -3 & 2 \\ -7 & 4 & -9 \\ -6 & -12 & -10 \\ -8 & 4 & -15 \end{bmatrix} = \begin{bmatrix} -113 & 84 & -87 \\ -112 & -7 & 84 \\ -216 & 120 & -35 \\ -260 & 120 & -28 \\ 1 & -26 & 24 \end{bmatrix}$$

$$h_n = \max(0, W^T h_{n-1} + b) = \begin{bmatrix} 0 & 84 & 0 \\ 0 & 0 & 84 \\ 0 & 120 & 0 \\ 0 & 120 & 0 \\ 1 & 0 & 24 \end{bmatrix}$$

5×3

Activation Functions



Summary

- Feedforward neural networks can be used for a variety of perception tasks related to self-driving cars
- Feedforward neural networks rely on hidden layers to implement a good approximation of a target function
- Various activation functions are available to use within hidden layers. RELU is the default baseline
- Next: Output Layers and Loss Functions