

## Teorema do Binômio

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①

$$\binom{6}{k} x^{6-k} y^k \mid \binom{6}{k} x^{6-k} 2x^{2k} = ? x^8$$

$$\begin{array}{|l} 2k = 8 \\ k = 4 \end{array} \quad \binom{6}{4} = \frac{6!}{4! \cdot 2}$$

$$15 \cdot 2^4 x^8 = 15 \cdot 16 x^8 = 240 x^8$$

Letra C

②

$$(14x - 13y)^{237}$$

$$\begin{array}{l} x = 1 \\ y = 1 \end{array} \quad \begin{array}{l} 14 - 13 = 1 \\ 1^{237} = 1 \end{array}$$

Letra B

③

$$(x + a)^{11}$$



$$k = 11 - 5$$

$$k = 6$$

$$\binom{11}{6} = 462$$

$$462 \times 5 \times 6 = 1386$$

$$2^6 = 1386$$

$$462$$

$$0^6 = 3$$

Setra A

$$0 = \sqrt[5]{3}$$

④

$$\left(x + \frac{1}{x^2}\right)^9$$

$$(x + x^{-2})^9$$

$$\binom{9}{k} x^{9-k} x^{-2k} = x^0$$

$$9 - k - 2k = 0$$

$$9 - 3k = 0$$

$$9 = 3k$$

$$k = 3$$

Setra B



$$5. \left(x + \frac{1}{x^2}\right)^n \quad \binom{n}{k} x^{n-k} (x^{-2})^k = x^0$$

$$n - k - 2k = 0$$

$$n - 3k = 0$$

$$n = 3k$$

Setra C

6.

$$\left(3x^3 + \frac{2}{x^2}\right)^5 = (3x^3 + 2x^{-2})^5$$

Linha 5 triângulo de Pascal

1 5 10 10 5 1

$$\begin{array}{l} 1 (3x^3)^5 \cdot (2x^{-2})^0 = 243x^{15} \\ 5 (3x^3)^4 \cdot (2x^{-2})^1 = 810x^{10} \\ 10 (3x^3)^3 \cdot (2x^{-2})^2 = 1080x^5 \\ 10 (3x^3)^2 \cdot (2x^{-2})^3 = 720 \\ 5 (3x^3)^1 \cdot (2x^{-2})^4 = \frac{240}{x^5} \\ 1 (3x^3)^0 \cdot (2x^{-2})^5 = \frac{32}{x^{10}} \end{array}$$

$$\begin{aligned} & (243x^{15} + 810x^{10} + 1080x^5 + 720 + \frac{240}{x^5} + \frac{32}{x^{10}}) - \\ & (243x^{15} + 810x^{10} + 1080x^5 + \cancel{720} + \frac{240}{x^5} + \frac{32}{x^{10}}) = \\ & 720 \end{aligned}$$

Setra E

f.

$$(2x + y)^5$$

$$x = 1$$

$$x = 1$$

$$3^5 = 243$$

Extra 6