

2. Descriptive Inference I

DS-GA 1015, Text as Data
Arthur Spirling

Feb 16, 2020

Where Are We?

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e.g. stemmed word like 'treasuri', which doesn't appear in the document itself.

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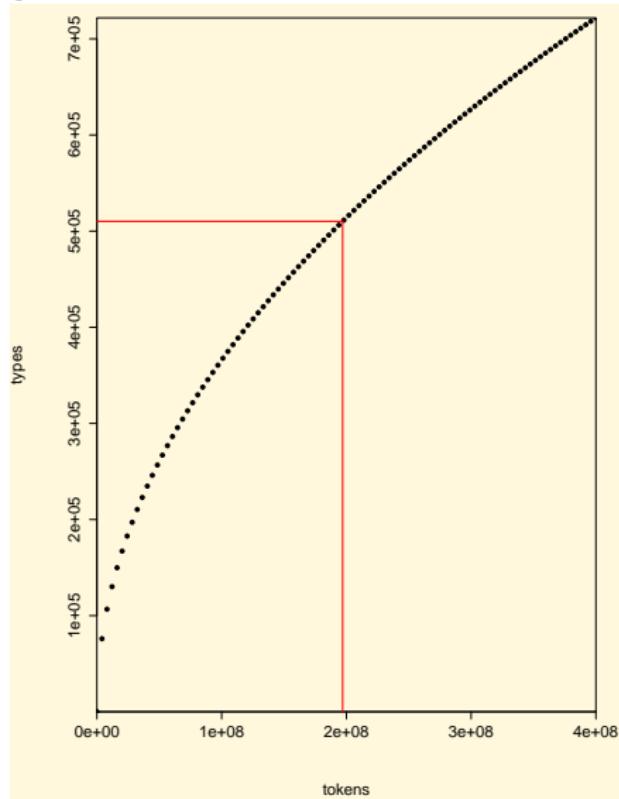
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NB number of types increases rapidly at first, then less rapidly. Need to preprocess, especially for long collections!

$k = 44, b = 0.49, T = 400,000$

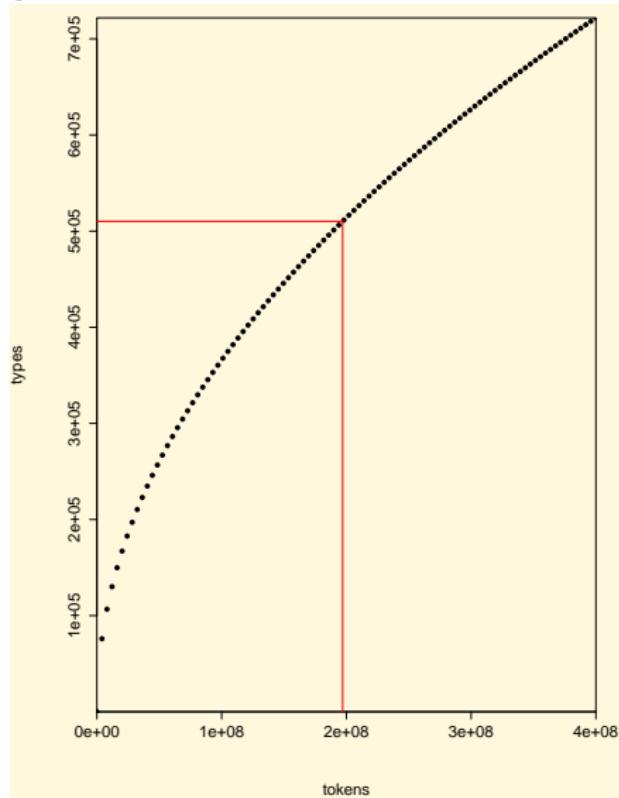
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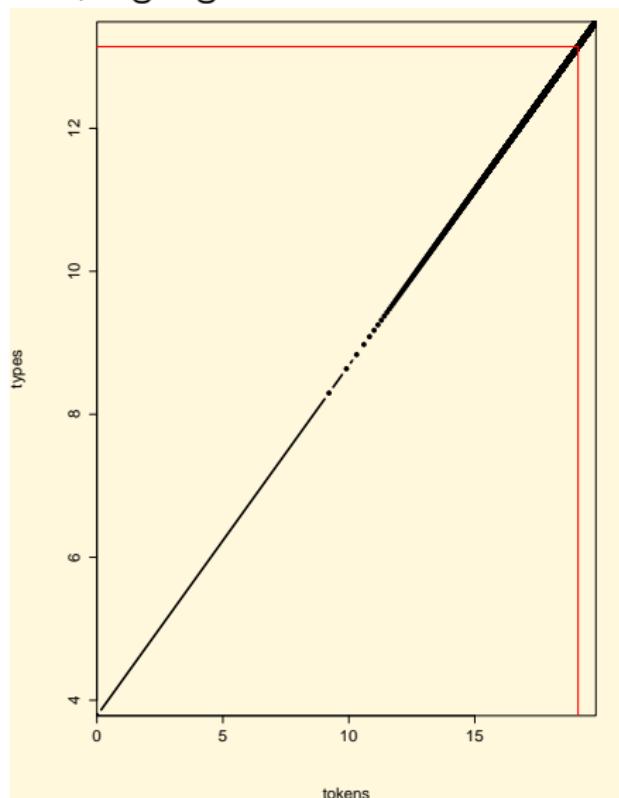
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RCV1, log-log.



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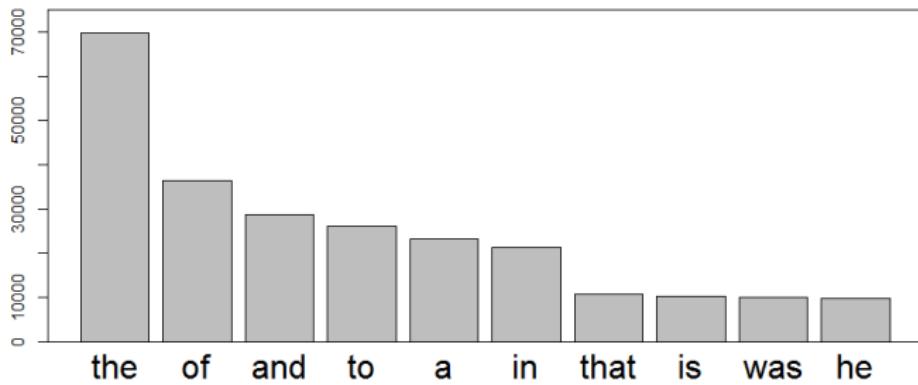
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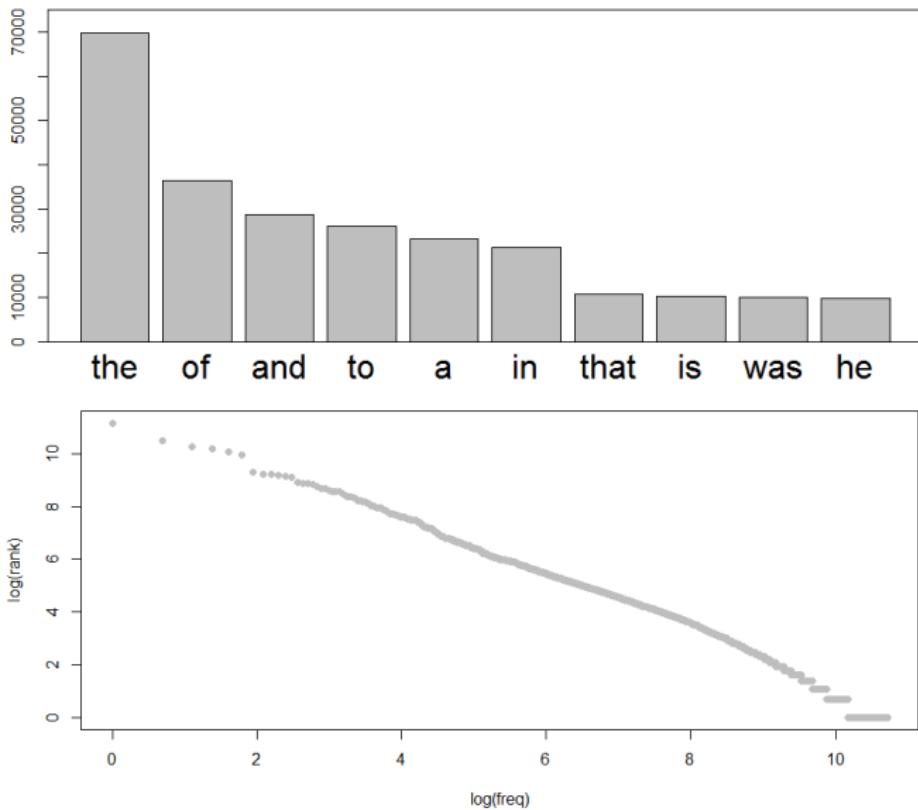
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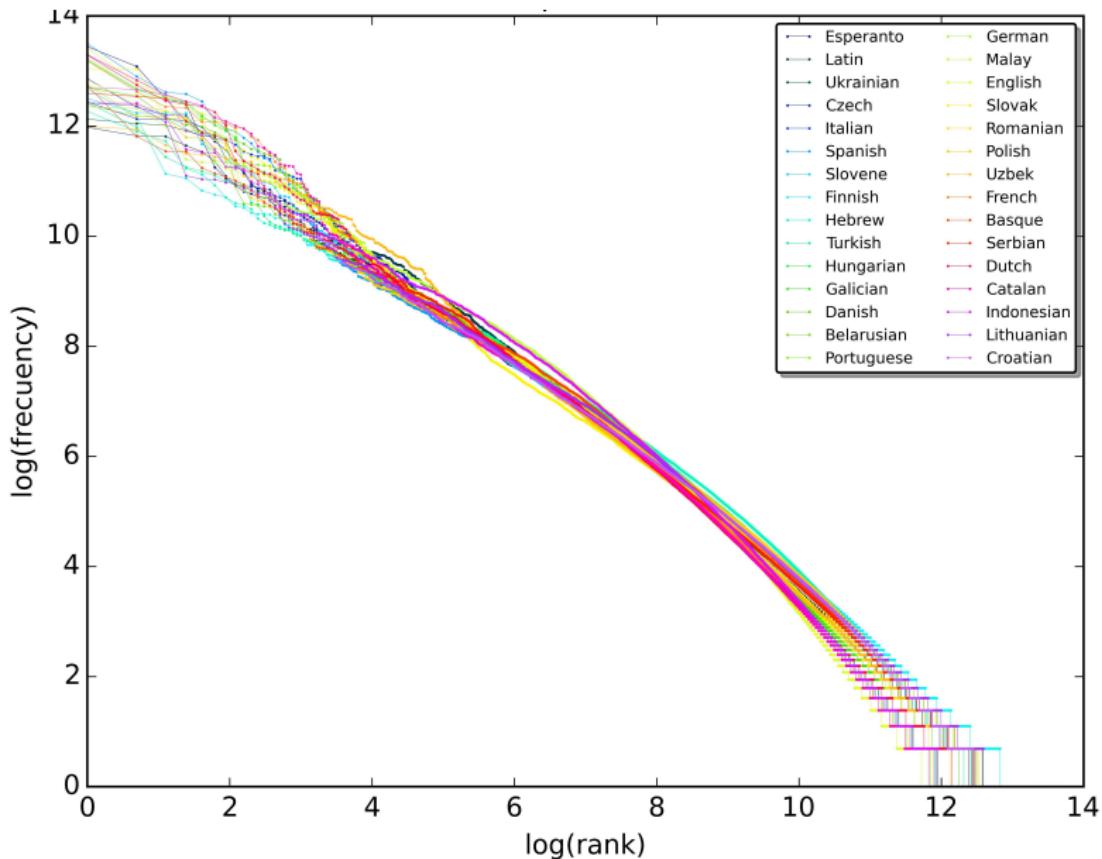
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City Populations in US (Gabaix, 1999)

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740

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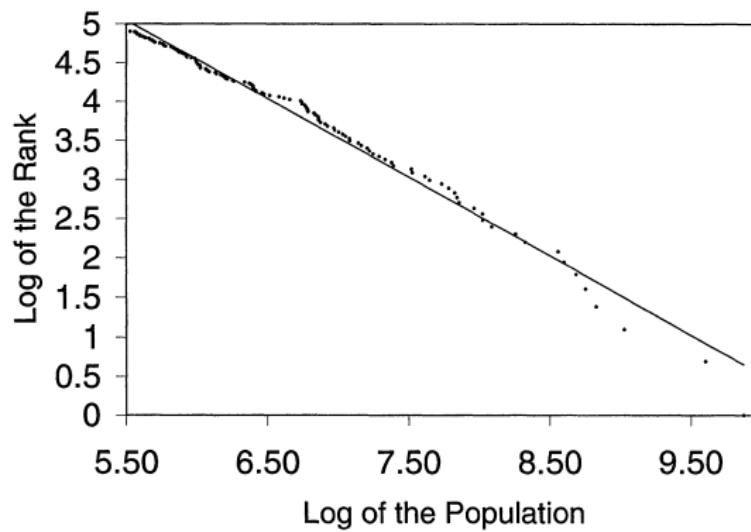


FIGURE I

Log Size versus Log Rank of the 135 largest U. S. Metropolitan Areas in 1991
Source: Statistical Abstract of the United States [1993].

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e.g. principal components analysis operates on distance matrix.

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larger distances imply lower similarity.

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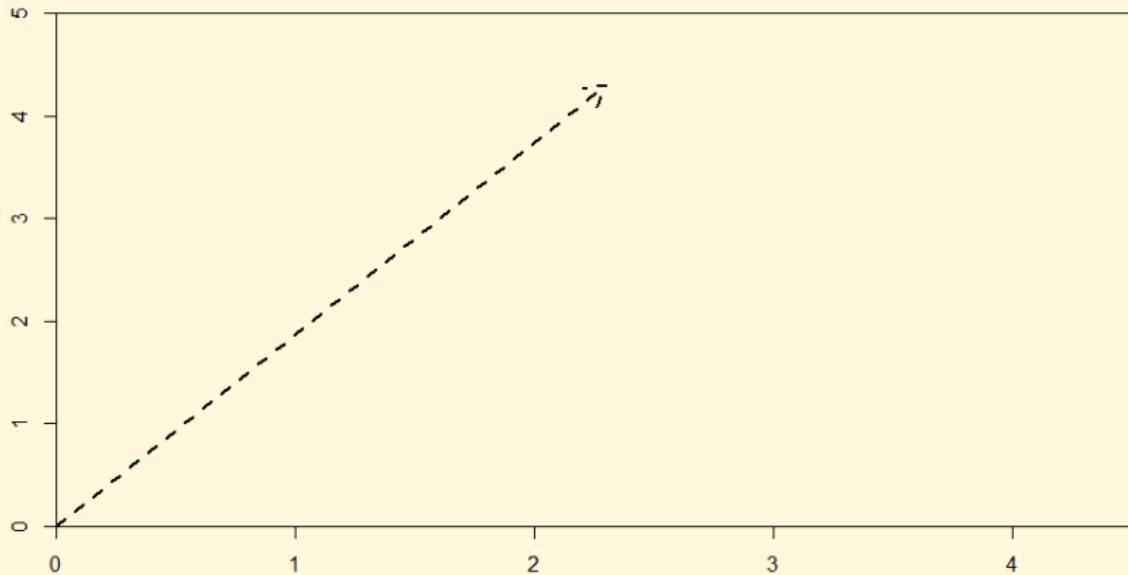
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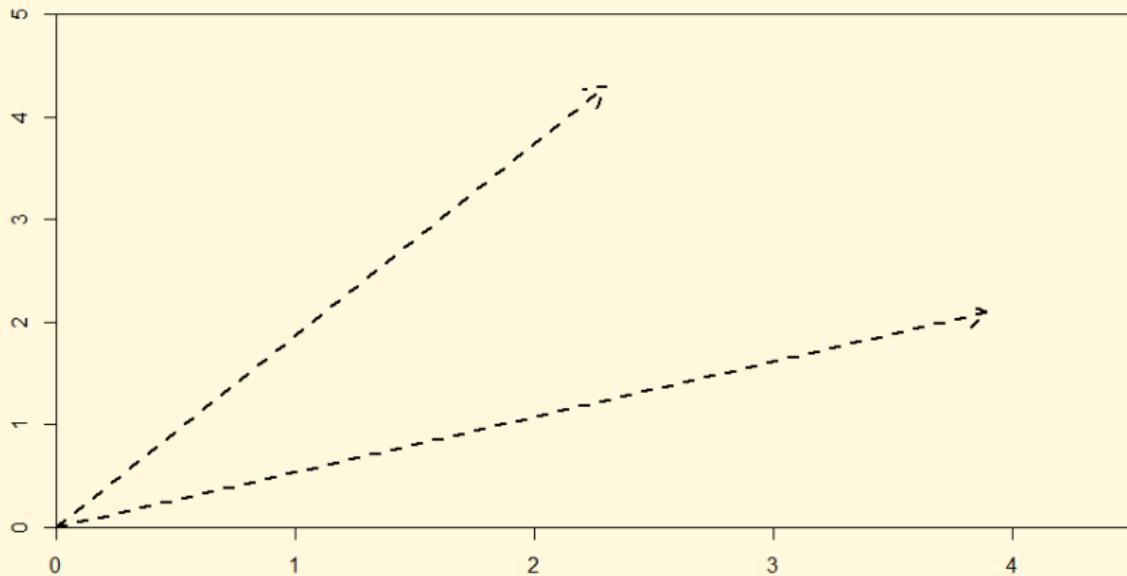
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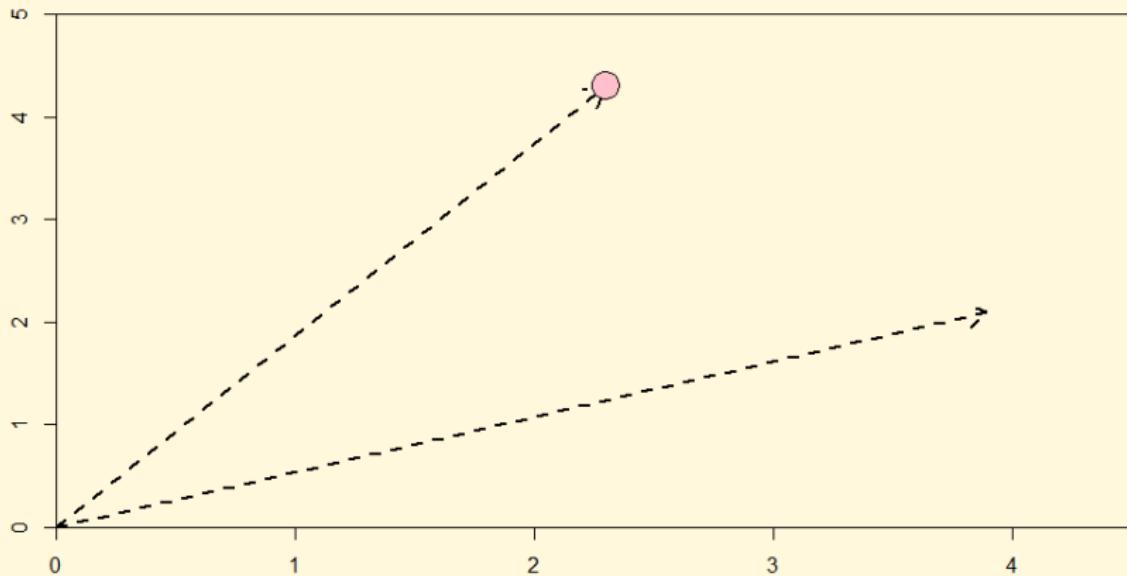
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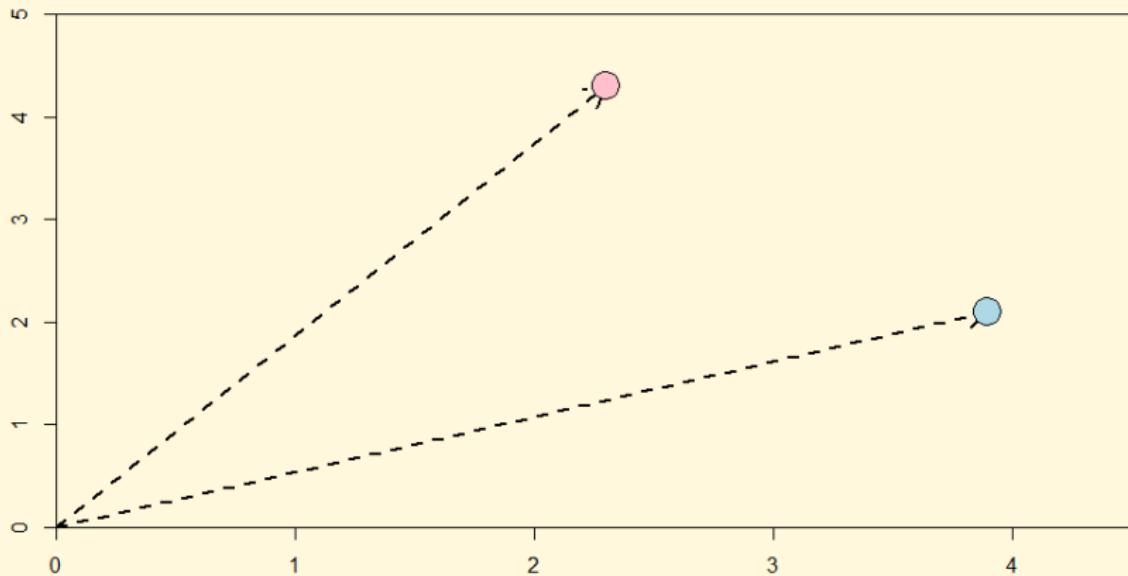
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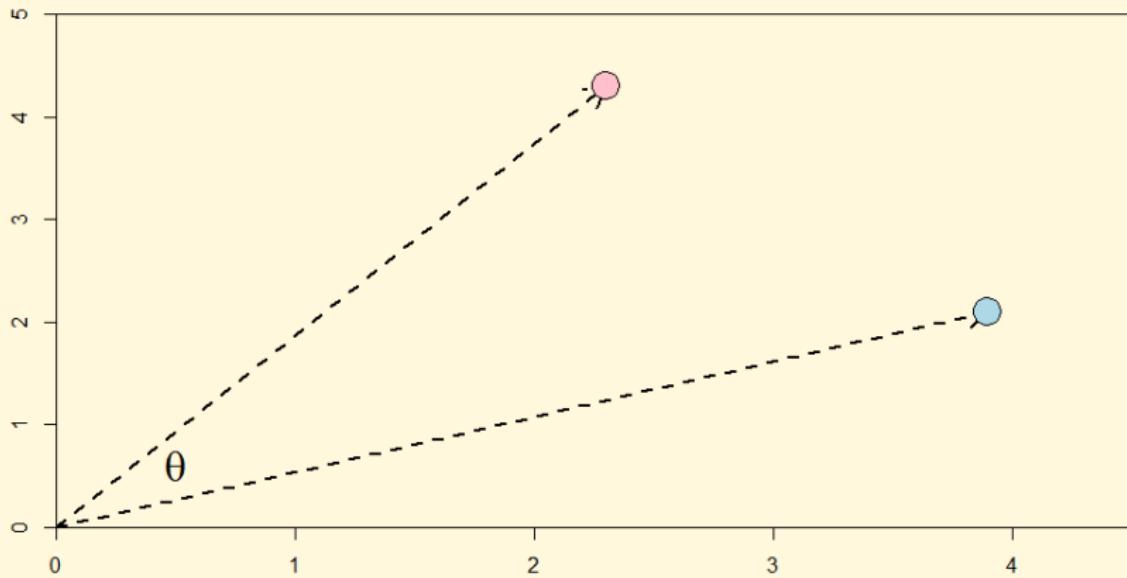
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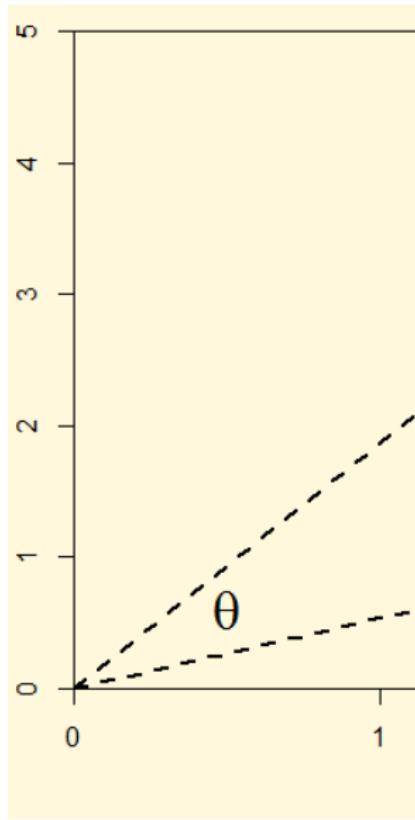
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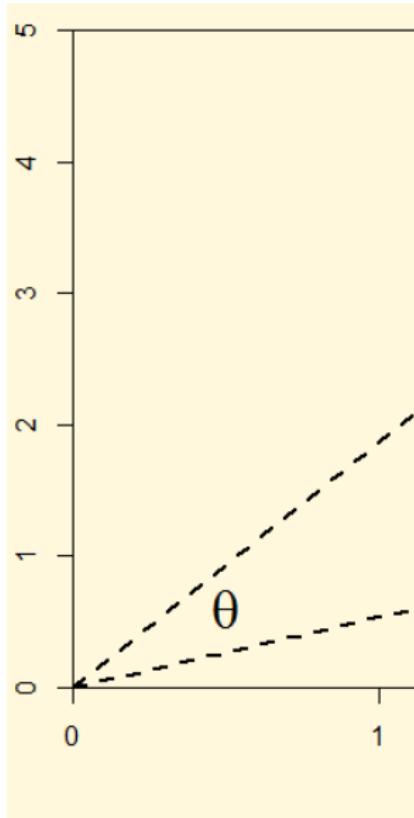


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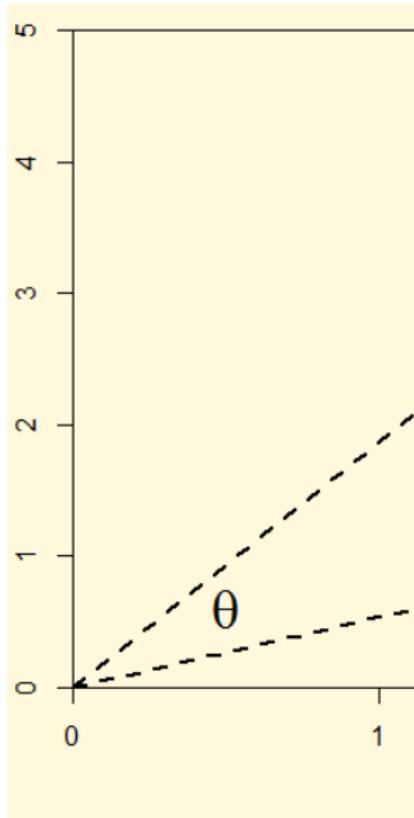


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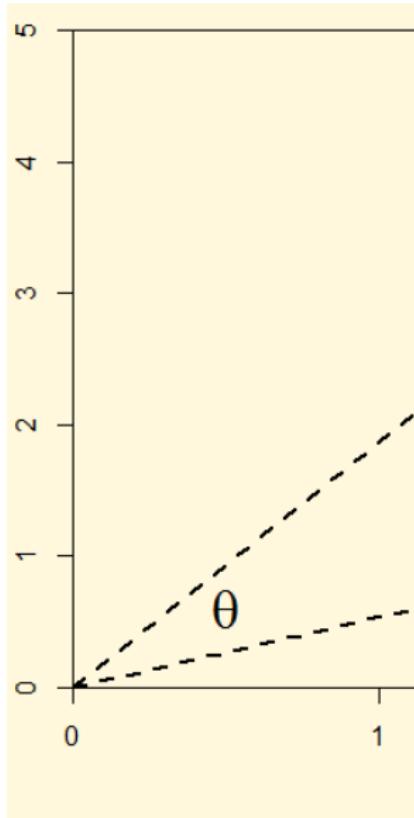
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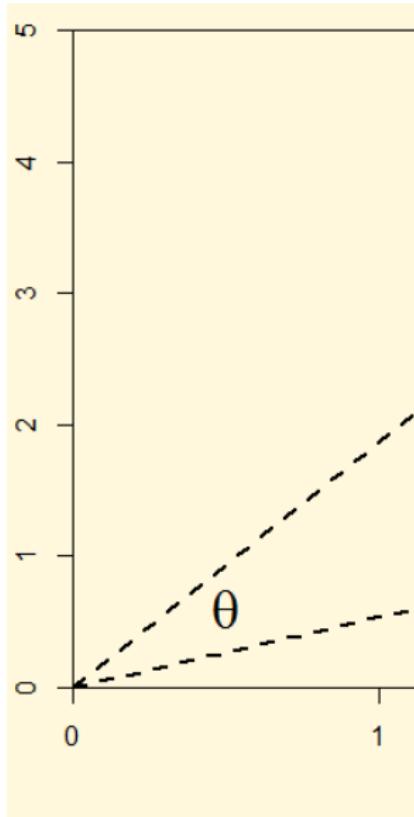
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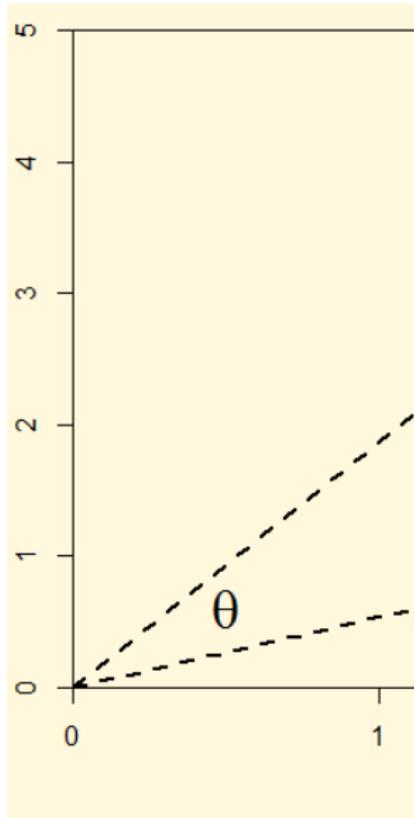
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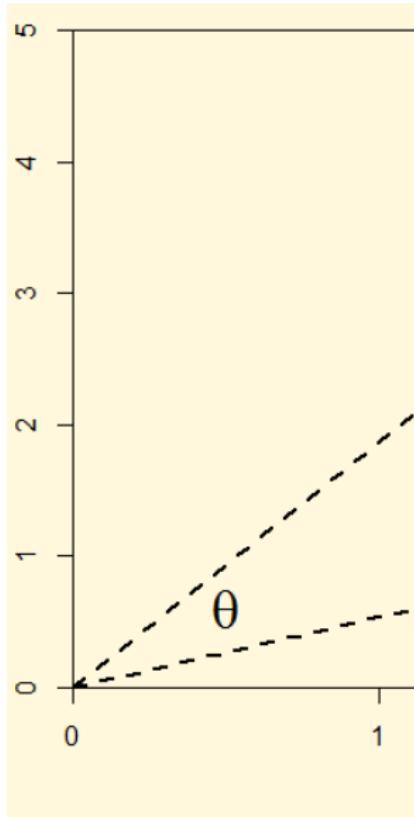
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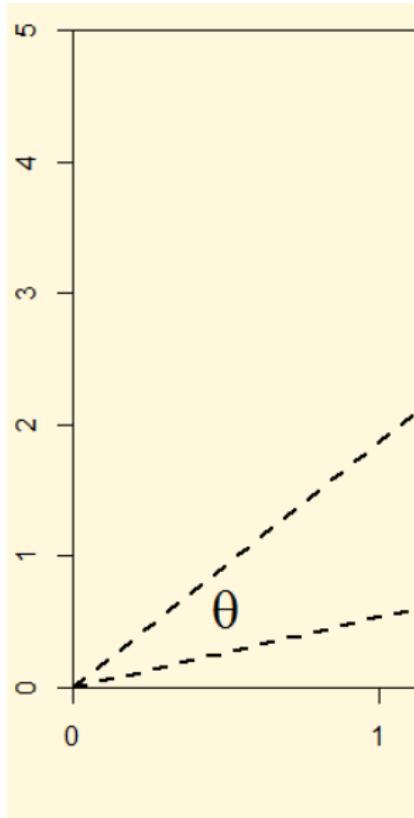
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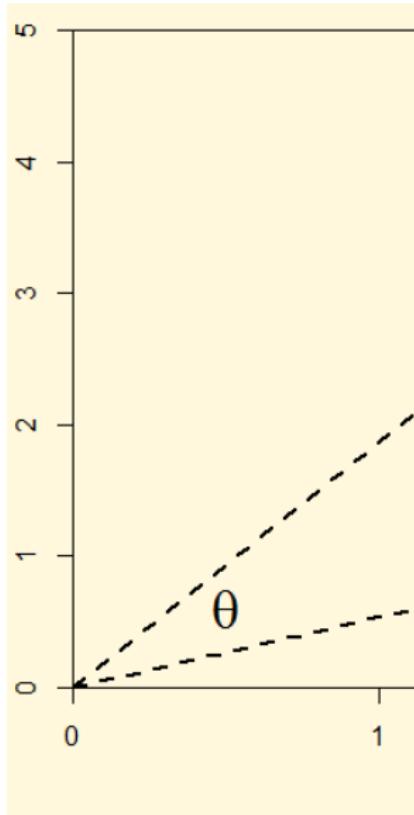
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Looks about right.

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The screenshot shows a web browser window with a black border. At the top is a blue header bar with the FDA logo and the text "U.S. FOOD & DRUG ADMINISTRATION". On the right side of the header is a search icon. Below the header, the URL bar shows the path: "Home / Regulatory Information / Dockets Management / Comment on Proposed Regulations and Submit Petitions". The main content area has a white background and features a large, bold, dark gray title: "Comment on Proposed Regulations and Submit Petitions". Below the title is a horizontal row of social media sharing icons: "f Share", "Tweet", "in Linkedin", "Email", and "Print".

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We may want to know [how much](#) different rules in different agencies at different times [change](#) in response to consultation: look at [*edit distance*](#).

see Rashin (2019) for more elaborate ideas

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The smallest number of operations taking us from s_1 to s_2 is the **Levenshtein distance** between those strings.

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How many operations? 4 + 1 + 3

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Different types of edit distances allow different types of operations.

Collocations, phrasemes and co-occurrence

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15494	to	be
13899	in	a
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[Justeson and Katz \(1995\)](#) improve performance considerably by applying **parts-of-speech** tagger,

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→ most of these are **uninteresting** pairs of function words (except 'New York')

[Justeson and Katz \(1995\)](#) improve performance considerably by applying **parts-of-speech** tagger, and only keeping those bigrams and trigrams that fulfill certain criteria...

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pattern	example
A N	Prime Minister
N N	surface area
A A N	little green men
A N N	real estate agent
N A N	home sweet home
N N N	term document matrix
N P N	Secretary of State

Reanalyzing NYT corpus: top ranked bi-grams

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frequency	$w_1 w_2$	
11487	New York	A N
7261	United States	A N
5412	Los Angeles	N N
3301	last year	A N
3191	Saudi Arabia	N N
2699	last week	A N
2514	vice president	A N
2378	Persian Gulf	A N
2161	San Francisco	N N
2106	President Bush	N N
2001	Middle East	A N
1942	Saddam Hussein	N N
1867	Soviet Union	A N
1850	White House	A N
1633	United Nations	A N
1337	York City	N N
1328	oil prices	N N
1210	next year	A N
1074	chief executive	A N
1073	real estate	A N

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can construct 2×2 table, and consider **expected** vs **observed** frequency...

2×2 table

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		Second Word		total
		w_2	$\neg w_2$	
First Word	w_1	O_{11}	O_{12}	$O_{11} + O_{12}$
	$\neg w_1$	O_{21}	O_{22}	$O_{21} + O_{22}$
total		$O_{11} + O_{21}$	$O_{12} + O_{22}$	N

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\Rightarrow reject the null hypothesis of independence: this word is a good choice as a collocation.

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Bigger the λ and z-score push up the ranking of MWEs of interest (and can be interpreted in “usual” way relative to null).

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→ small numbers here, so λ and zs small.

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- q What role did 'democratic' play in the debate?

Some KWIC from the debates: kwic() in quanteda

	preword	word	postword
:	:	:	:
[s267549.txt, 994]	evil that attends a purely	democratic	form of Government. There could be
[s267549.txt, 1015]	here, not possibly towards a	democratic	form of government, but in
[s267738.txt, 1492]	swept away in some further	democratic	change. And it is for
[s267738.txt, 1560]	throne. When you get a	democratic	basis for your institutions, you
[s267738.txt, 1952]	differences between ourselves and other	democratic	legislatures? Where is the democratic
[s267738.txt, 1957]	democratic legislatures? Where is the	democratic	legislature which enjoys the powers
[s267738.txt, 2243]	almost utterly useless against a	democratic	Chamber, and the question to
[s267738.txt, 2286]	to the violence of the	democratic	Chamber you are creating, and,
[s267738.txt, 2294]	are creating, and, as the	democratic	principle brooks no rival, this
[s267738.txt, 2374]	spirit of democracy that the	democratic	Chamber itself would become an
[s267738.txt, 2678]	power is given to the	democratic	majority, that majority does not
[s267738.txt, 2767]	job? In accordance with the	democratic	principle the army would demand
[s267744.txt, 204]	Conservative patronage, of the most	democratic	Reform Bill ever brought in.

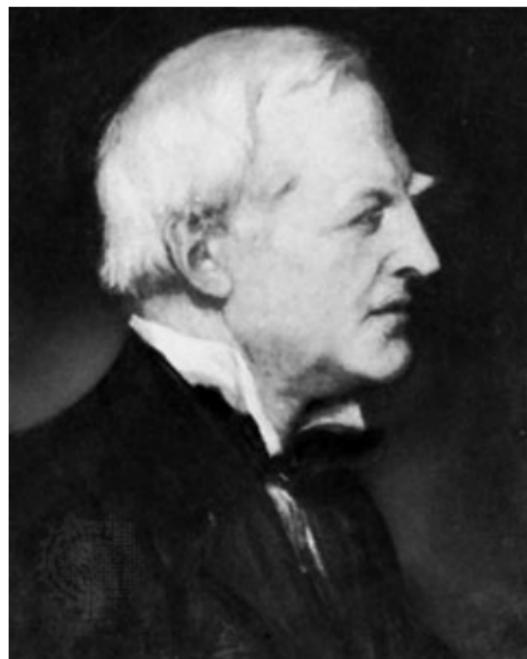
Detail: s267738.txt

Detail: s267738.txt

preword	word	postword
swept away in some further throne. When you get a differences between ourselves and other democratic legislatures? Where is the almost utterly useless against a to the violence of the are creating, and, as the spirit of democracy that the power is given to the job? In accordance with the	democratic democratic democratic democratic democratic democratic democratic democratic democratic democratic	change. And it is for basis for your institutions, you legislatures? Where is the democratic legislature which enjoys the powers Chamber, and the question to Chamber you are creating, and, principle brooks no rival, this Chamber itself would become an majority, that majority does not principle the army would demand

The Original Speaker and Speech

The Original Speaker and Speech

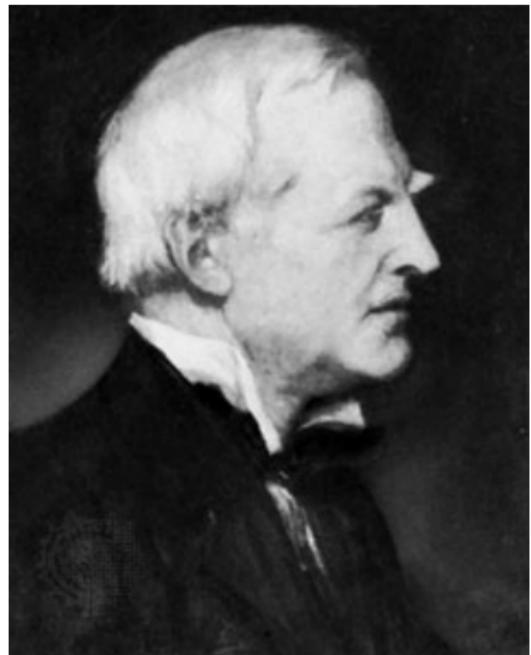


The Original Speaker and Speech



You cannot trust to a majority elected by men just above the status of paupers. The experiment has been tried; it has answered nowhere; it has failed in America, and it will not answer here.

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In accordance with the democratic principle the army would demand to elect their own officers, and there would be endless change in the Constitution arising out of the present Bill, which, so far from being an end to our evils, is only the first step to them.

Use of 'Wireless'

