### 3. Descriptive Inference II

DS-GA 1015, Text as Data Arthur Spirling

Feb 16, 2021



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e.g. authors with limited vocabularies will have a low lexical diversity.

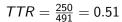
February 11, 2021





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# Other Ideas

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4 D > 4 D > 4 E > 4 E > 9 Q C

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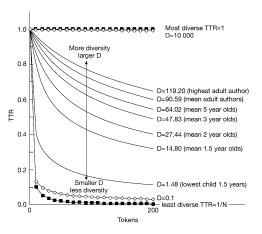


Figure 1: Model TTR plotted against samples of increasing length for different values of D

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• Kincaid et al later translate to US School grade level that would be (on average) required to comprehend text.

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## Readability Guidelines

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Score	Education	Description	Clve % US popn
0-30	college graduates	very difficult	28
31–50		difficult	72
51–60		fairly difficult	85
61–70	9th grade	standard	_
71–80		fairly easy	_
81–90		easy	_
91–100	4th grade	very easy	_

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# Aside: Syllables

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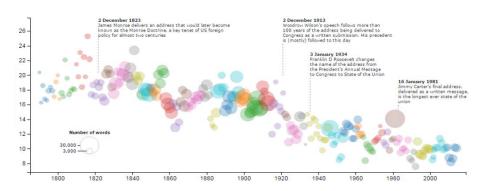
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- ± rules for special endings and use of consonents (e.g. hassle vs mule)

#### The state of our union is ... dumber:

How the linguistic standard of the presidential address has declined

Using the Flesch-Kincaid readability test the Guardian has tracked the reading level of every State of the Union



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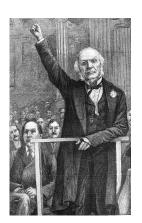
new voters tended to be poorer and less literate

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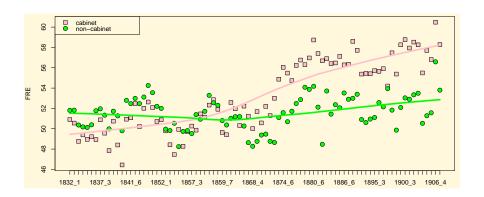


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# Flesch overtime plot



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yields grade level of text sample.

#### DC

$$0.1579 \times (\text{PDW}) + 0.0496 \times \left(\frac{\text{total words}}{\text{total sentences}}\right)$$

where PDW is percentage of difficult words,

and a 'difficult' word is one that does not appear on Dale & Chall's list of 763 (later updated to 3000) 'familiar' words.

e.g. about, back, call, etc.





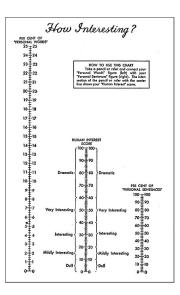
Designed for education, not politics



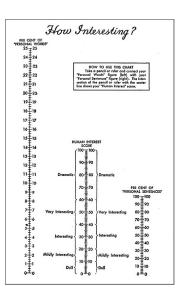
- Designed for education, not politics
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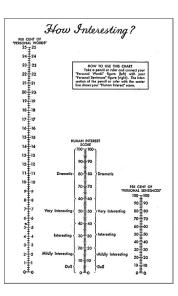
- Designed for education, not politics
- Tested/validated on children, not adults
- Designed for readers in 1940/50s, not easily updated.



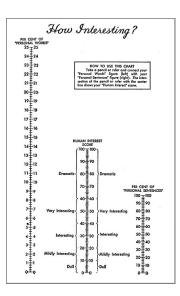
Cannot assess quality/fit of predictions for documents;



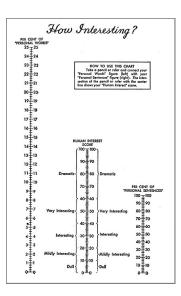
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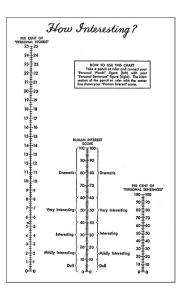
- Cannot assess quality/fit of predictions for documents; no 'ground truth' to compare to
- Cannot assess relative model fit;



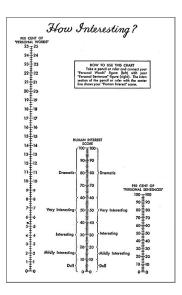
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- Rarity of terms included in static, ad hoc way.

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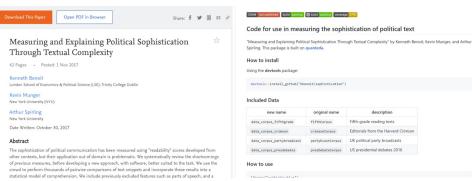
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  - ightarrow provide better measure of political sophistication

February 11, 2021









github.com/kbenoit/sophistication



The first cession was made by the State of New York, and the largest, which in area exceeded all the others, by the State of Virginia.



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I speak to you not just as a President, but as a father, when I say that responsibility for our children's education must begin at home.



The first cession was made by the State of New York, and the largest, which in area exceeded all the others, by the State of Virginia.



I speak to you not just as a President, but as a father, when I say that responsibility for our children's education must begin at home.

Cleveland wins on FRE, but Obama wins in our model (penalizing for rarity).

# Style and Stylometrics





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- then collapse on author to get word frequencies specific to the authors
- now model these author-specific rates with Poisson and negative binomial distributions
- use Bayes' theorem to determine the posterior probability that Hamilton (Madison) wrote a particular disputed essay for all such essays
- i.e. they ask "if rates of function word usage are constant within authors for these documents, which author was most likely to have written essay x given the observed function word usage of these authors on the other documents?"

a one but their have when must and things if are some every up is	been the has what more an our do who no even to into would of	had were may also or can there his any so in with now at than	its all only by then her which my down this not as such for upon
up			for upon
your on should	be that	from was	it will

# may think that sentence length distinguishes authors

been the has what more an our do who no	had were may also or can there his any so in	its all only by then her which my down this
an	can	her
our	there	which
do	his	my
who	any	down
no	so	this
even	in	not
to	with	as
into	now	such
would	at	for
of	than	upon
be	from	it
that	was	will
	the has what more an our do who no even to into would of be	the were has may what also more or an can our there do his who any no so even in to with into now would at of than be from

may think that sentence length distinguishes authors, but Hamilton and Madison "practically twins" on this.

a	been	had	its
one	the	were	all
but	has	may	only
their	what	also	by
have	more	or	then
when	an	can	her
must	our	there	which
and	do	his	my
things	who	any	down
if	no	so	this
are	even	in	not
some	to	with	as
every	into	now	such
up	would	at	for
is	of	than	upon
your	be	from	it
on	that	was	will
should			

heen had its а the all one were but has mav only their what also bν then have more or when can her an which there must OUR his and do my things who down any this nο so not even to with as some into such everv now would for up of than upon be from it your on that was will should

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use function words—conjunctions, prepositions, pronouns—

heen had its а the all one were but has mav only their what also bν then have more or when can her which there must Our his and do my things who down anv this nο so not even with as some into such everv now would for up of than upon be from it your on that was will should

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heen had its а the all one were but has mav only their what also bν have then more when can her there which must Our and do his my things who down anv nο SO this not even with as some into such everv now for would up than of upon be from it your on that was will should

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use function words—conjunctions, prepositions, pronouns—for two (related) reasons:

• authors use them unconsciously

a one but their have when must and things if are some every up is your on should	been the has what more an our do who no even to into would of be that	had were may also or can there his any so in with now at than from was	its all only by then her which my down this not as such for upon it will

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a one but their have when must and things if are some every	been the has what more an our do who no even to into	had were may also or can there his any so in with	its all only by then her which my down this not as
must	our	there	which
	do	his	my
things	who	any	down
if	no	so	this
are	even	in	not
some	to	with	as
every	into	now	such
up	would	at	for
is	of	than	upon
your	be	from	it
on	that	was	will
should			

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#### More Details

a	been	had	its
one	the	were	all
but	has	may	only
their	what	also	by
have	more	or	then
when	an	can	her
must	our	there	which
and	do	his	my
things	who	any	down
if	no	so	this
are	even	in	not
some	to	with	as
every	into	now	such
up	would	at	for
is	of	than	upon
your	be	from	it
on	that	was	will
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  - → wrong, but models relying on these assns discriminate well (see Peng & Hengartner on e.g. Austen v Shakespeare)

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and Negative Binomial (which adds a gamma distributed random effect,  $\delta$ ):

$$NB(X_w = x | \Theta_w = (\omega, \mu, \delta)) = \frac{\gamma(x+k)}{x! \gamma(k)} (\omega \delta)^x (1 + \omega \delta)^{-(x+k)}$$

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    - + confirmed by many subsequent analyses (via e.g. machine learning)





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  - → think a little more systematically about the sampling distribution of a statistic.

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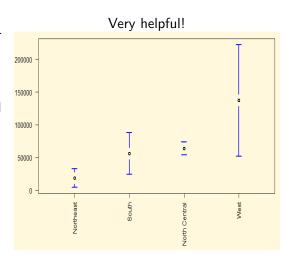
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ightarrow difficult to know how we should calculate the sampling distribution and thus the standard error.

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() February 11, 2021

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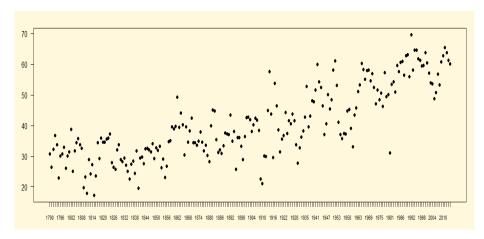
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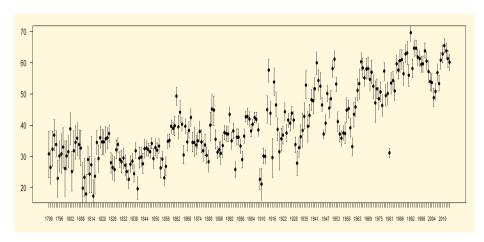
btw long texts give rise to smaller SEs than short ones, which makes sense!

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  - → SIMEX (simulation-extrapolation) or MO (multiple overimputation) might be called for.

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