

9. Unsupervised Techniques III: Topic Models

DS-GA 1015, Text as Data
Arthur Spirling

April 6, 2021

Goal

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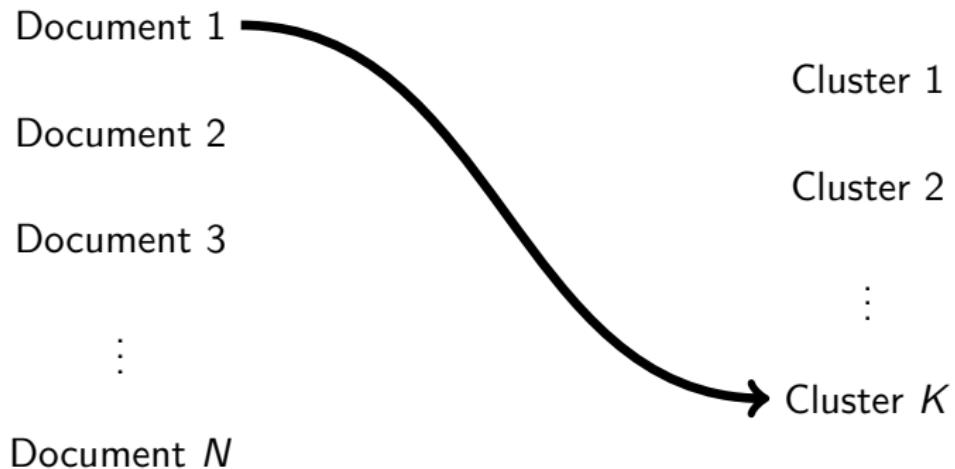
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“who pays more attention to education policy, conservatives or liberals?”

Recall: Clustering

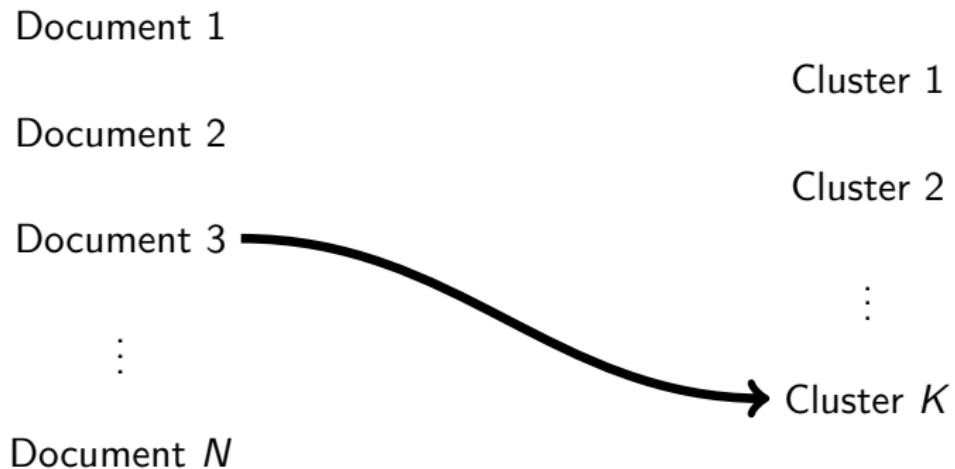
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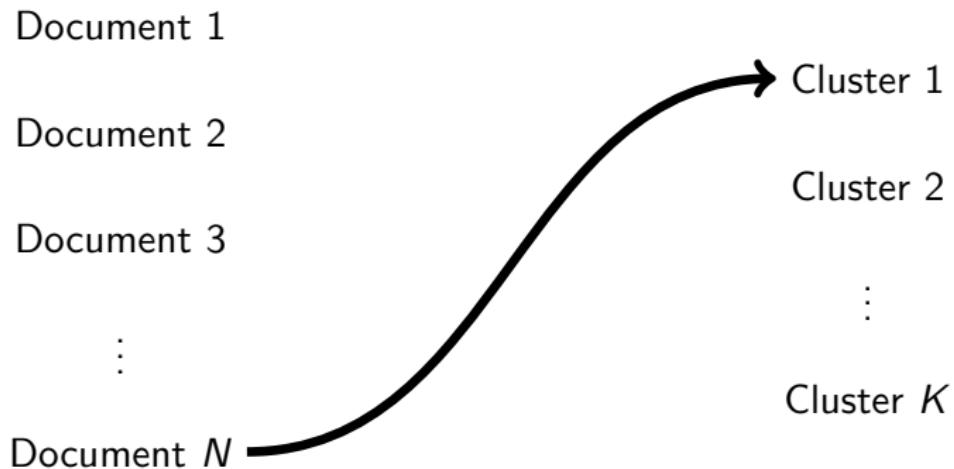
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Document 1

Cluster 1

Document 2

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Document 3

⋮

⋮

Cluster K

Document N

Topic Modeling

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Document 1

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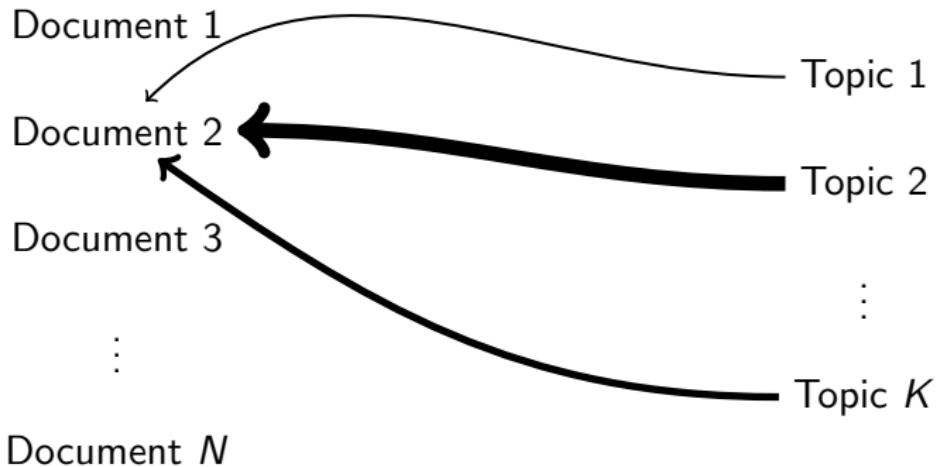
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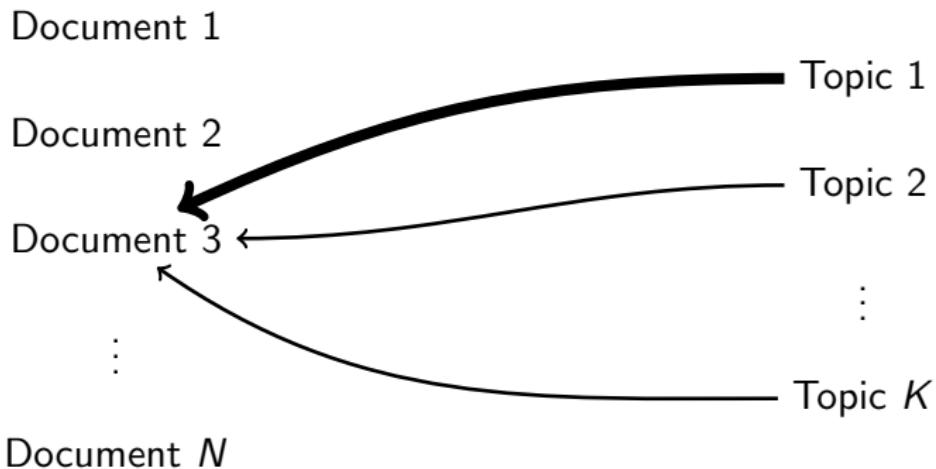
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Topic Modeling



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Now, where do the **words** in the documents come from?

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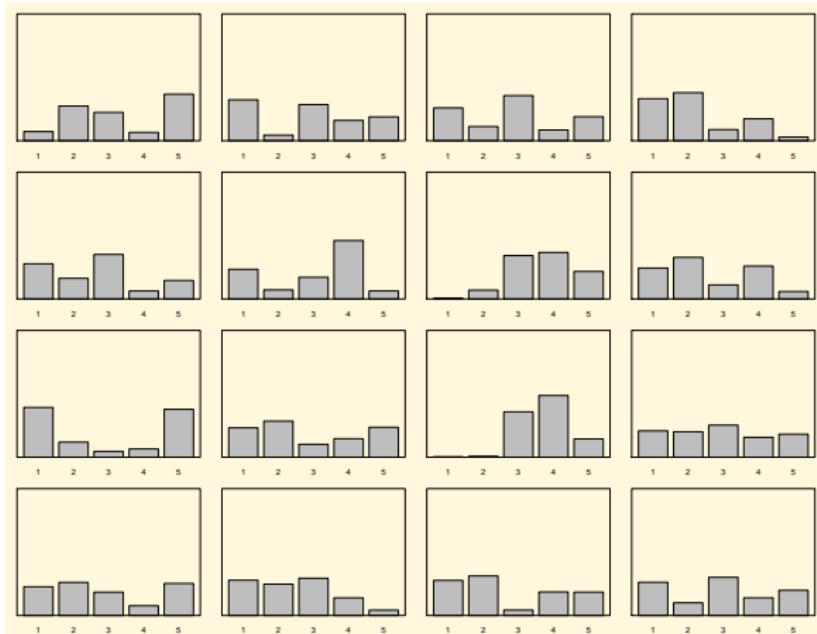
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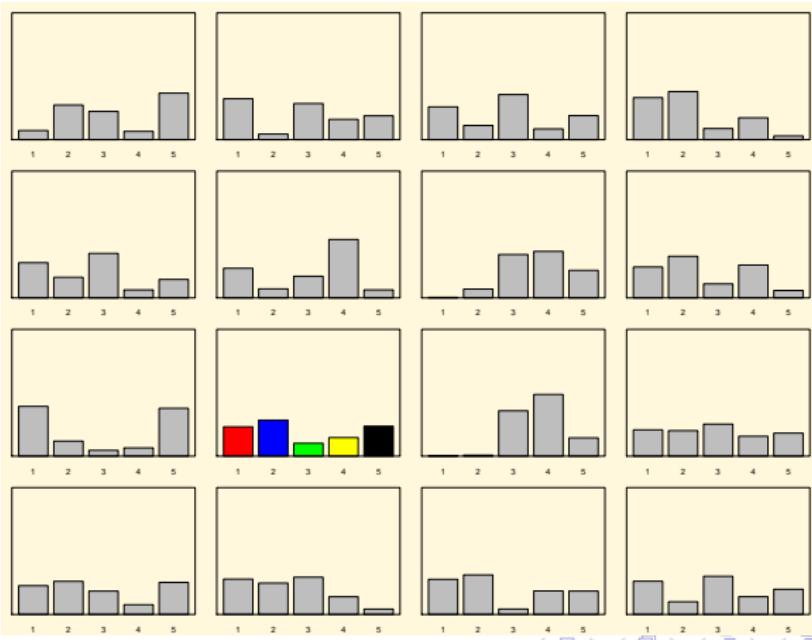
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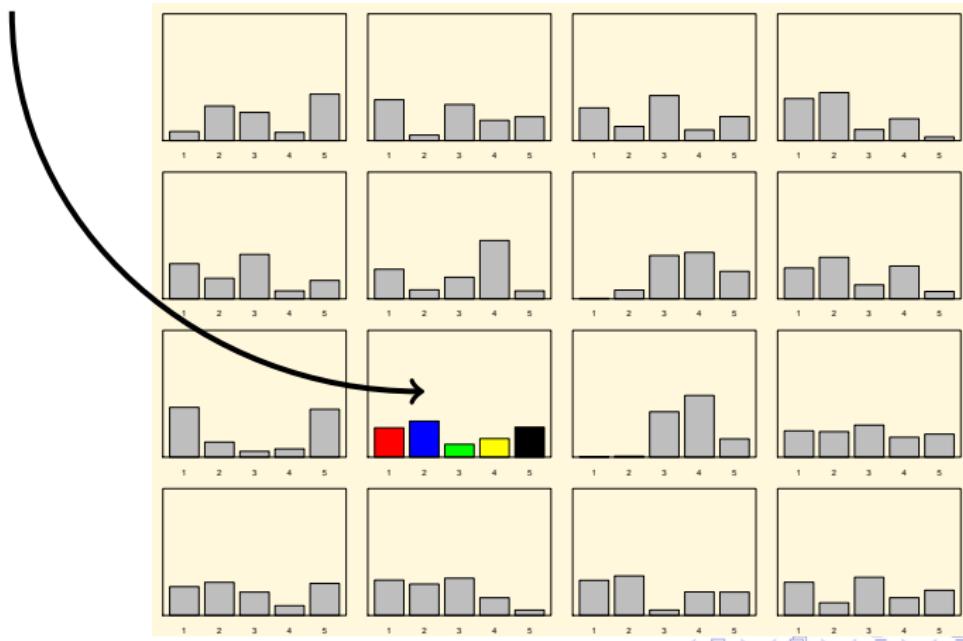
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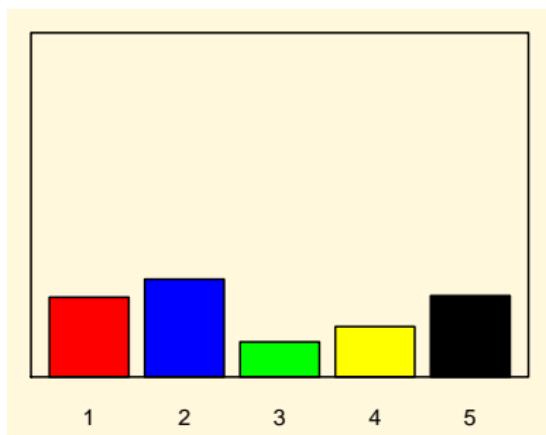
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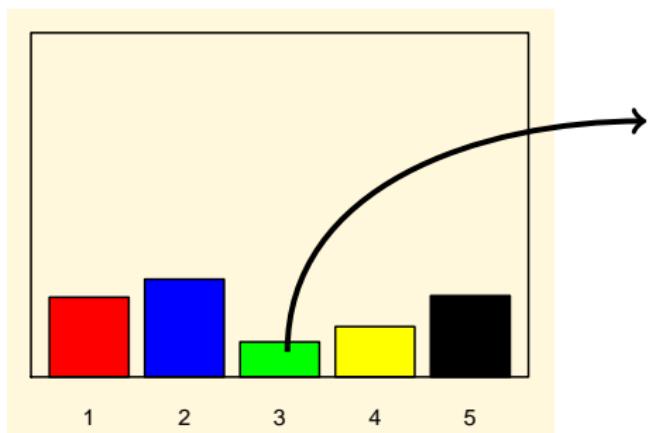
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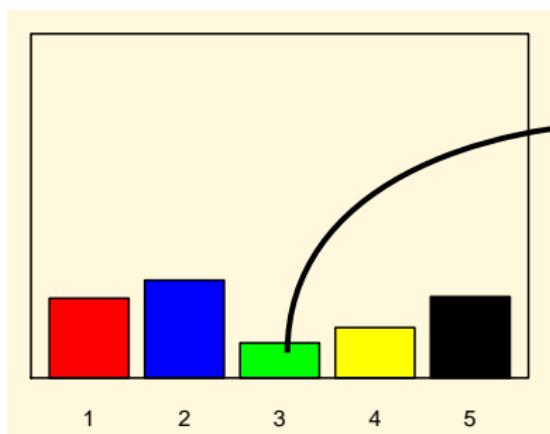
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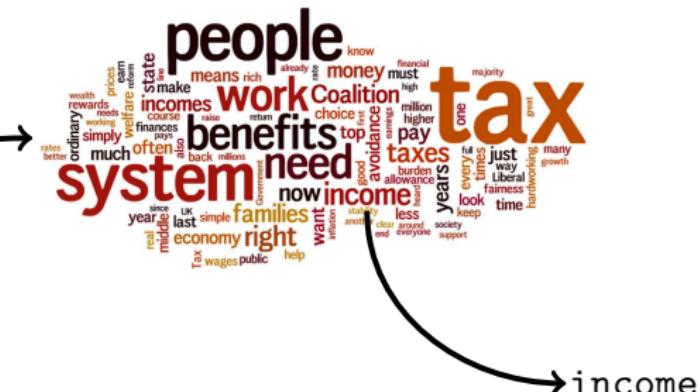
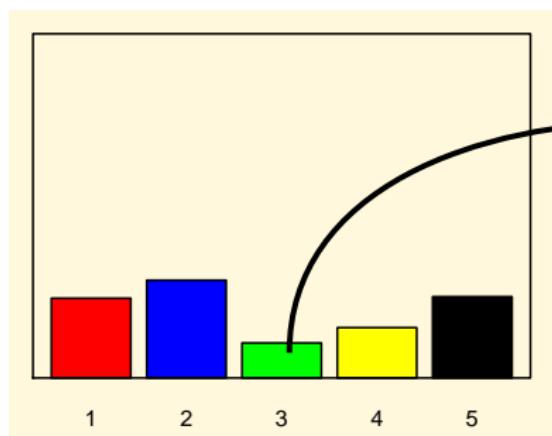
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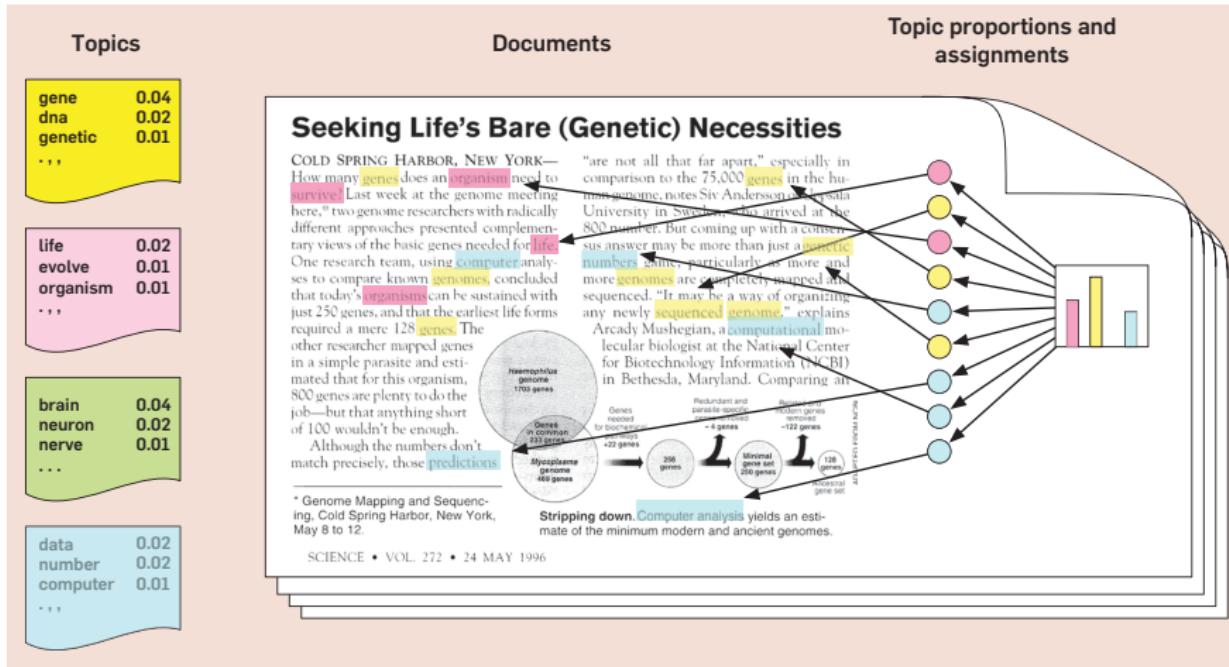
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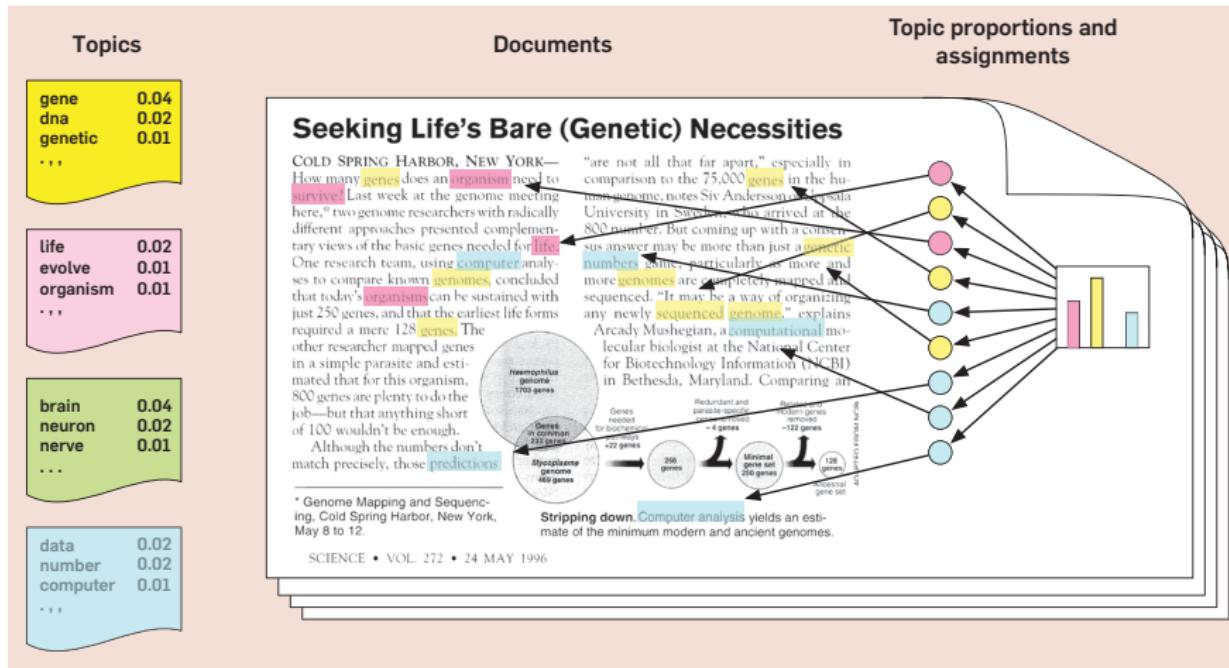


Topic Modeling a Document (Blei, 2012)

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Note that all documents share same set of topics: but some (e.g. **neuro**) may be (basically) absent in a given document.

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→ Latent Dirichlet Allocation. **LDA**.

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The multinomial distribution for the i th topic is denoted β_i , and $|\beta_i| = V$, meaning that the 'size' of this multinomial is equal to the number of different words in the corpus.

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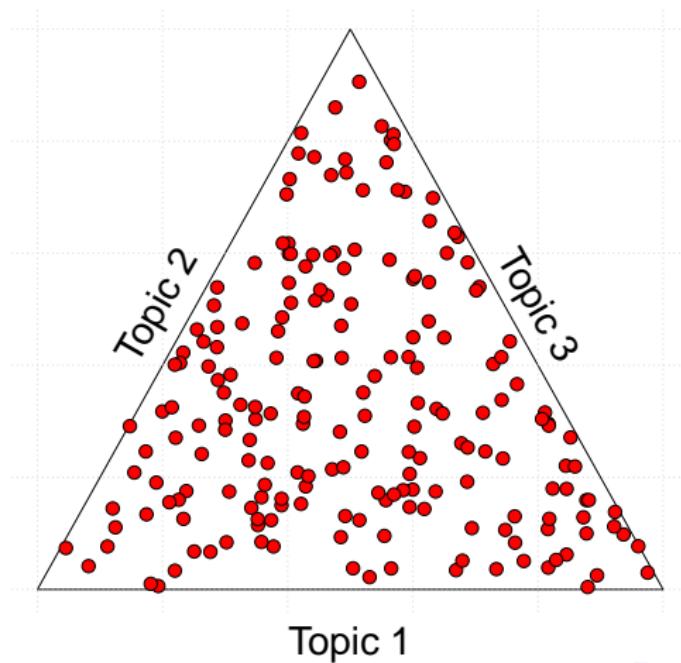
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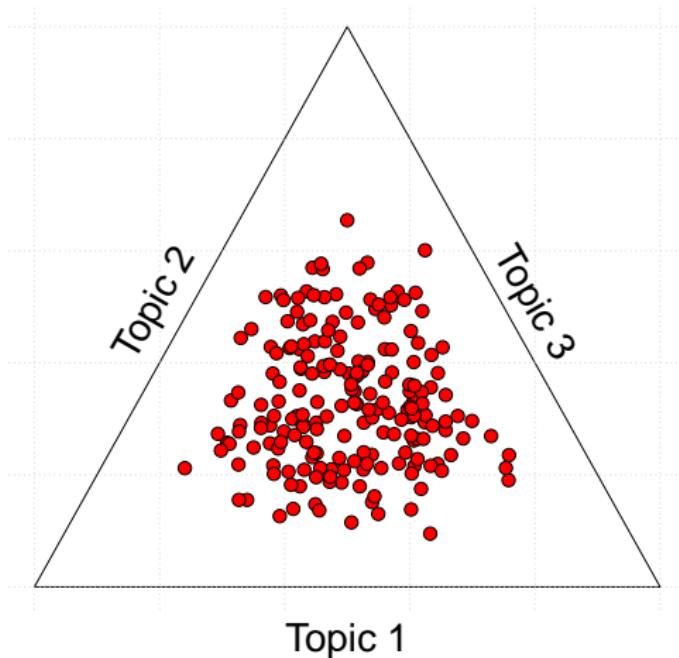
Example of Dirichlet

200 documents, 3 topics, $\alpha = 1$
(uniform)



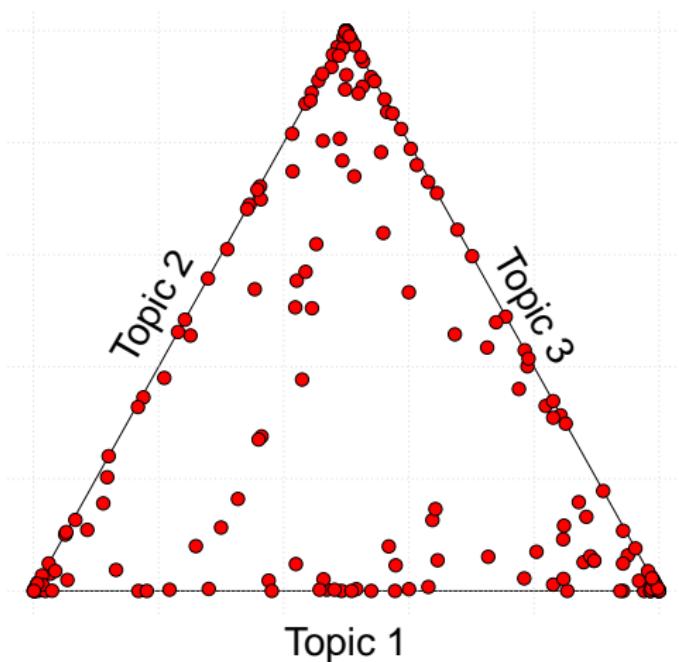
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200 documents, 3 topics, $\alpha = 5$



Example of Dirichlet

200 documents, 3 topics, $\alpha = 0.2$



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The θ_d depends on our prior for the relevant Dirichlet, α .

And we know that the actual value that $w_{d,n}$ takes depends on the distribution over words that the relevant topic entails, the β ("the word from topic 4 is "income" in this case")

While the β depends on the prior for the relevant Dirichlet, η

Plate Diagram for LDA

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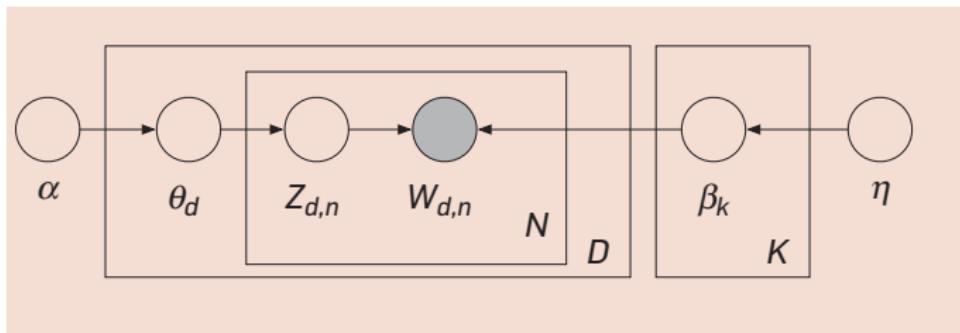
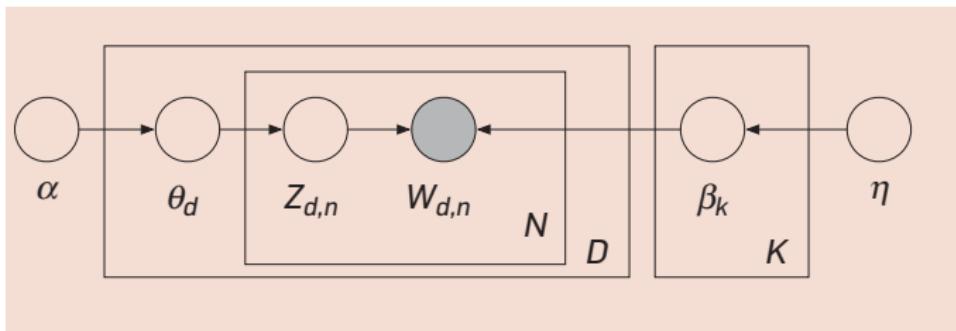
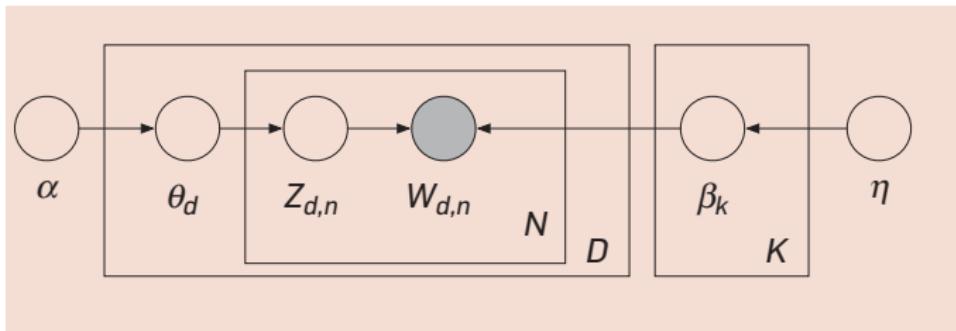


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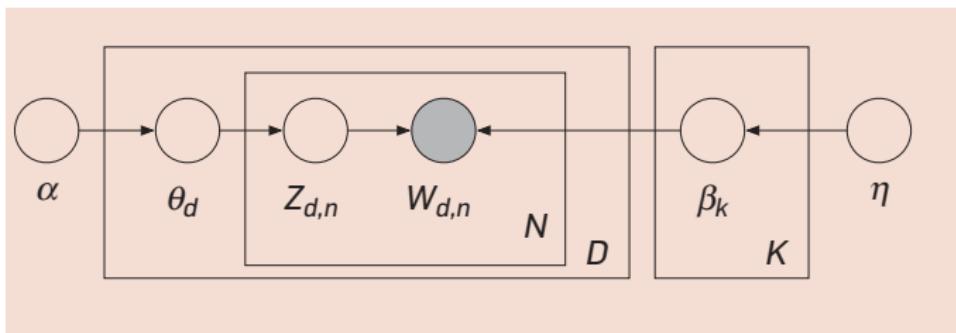
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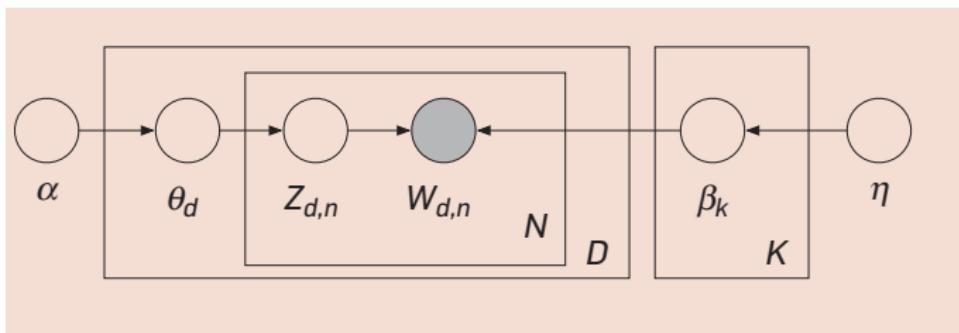
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Plates imply replication.

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Note that $w_{d,n}$ depends on $z_{d,n}$ (the mix of topics for that document) and $\beta_{1:K}$ (all the topics in terms of their distributions over the words).

Bayesian Inference: Crash Course/Reminder

Recall that...

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So,

$$\Pr(A|B) = \frac{\Pr(A, B)}{\Pr(B)}$$

And, Bayes Theorem tell us that

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NB: sometimes called the evidence in the Bayesian context, and is integral of numerator over support of θ (weighted by how plausible each value is)

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- 2 **Practicality:** for many problems, MLE doesn't work well. Perhaps because there are lots of parameters, but not much data: **priors** can help here. Or perhaps because the model, like multinomial probit, involves evaluating something complicated, analytically: Bayesian methods can **arbitrarily approximate** the integral.

Crash course complete: back to
LDA

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Posterior

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Results

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A Manifesto Example

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69 UK manifestos.

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69 UK manifestos. Some preprocessing.

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| | Topic 1 | Topic 2 | Topic 3 | Topic 4 | Topic 5 |
|--------------|---------|---------|---------|---------|---------|
| conservative | 0.00188 | 0.00088 | 0.00185 | 0.00221 | 0.00168 |
| party | 0.00145 | 0.00067 | 0.00066 | 0.00577 | 0.00093 |
| general | 0.00073 | 0.00033 | 0.00018 | 0.00192 | 0.00040 |
| election | 0.00079 | 0.00053 | 0.00022 | 0.00235 | 0.00076 |
| manifesto | 0.00059 | 0.00078 | 0.00032 | 0.00099 | 0.00048 |
| : | : | : | : | : | : |

Continued...

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'Top' 6 most frequent words in each topic:

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| 5 | tax | can | [markup] | shall | can |
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Meaningless 'junk' topics not unusual: debate as to whether one has to interpret **every** topic.

Continued

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| | Topic 1 | Topic 2 | Topic 3 | Topic 4 | Topic 5 |
|-------|---------|---------|---------|---------|---------|
| doc 1 | 0.00009 | 0.00009 | 0.00009 | 0.00009 | 0.99965 |
| doc 2 | 0.00011 | 0.00011 | 0.00011 | 0.00011 | 0.99954 |
| doc 3 | 0.00010 | 0.00010 | 0.00010 | 0.00010 | 0.99959 |
| doc 4 | 0.00006 | 0.00006 | 0.00006 | 0.00006 | 0.99978 |
| doc 5 | 0.00002 | 0.00002 | 0.00002 | 0.00002 | 0.99991 |
| doc 6 | 0.00019 | 0.00019 | 0.00019 | 0.00019 | 0.99924 |
| : | : | : | : | : | : |

Continued

The topic distribution for each document...

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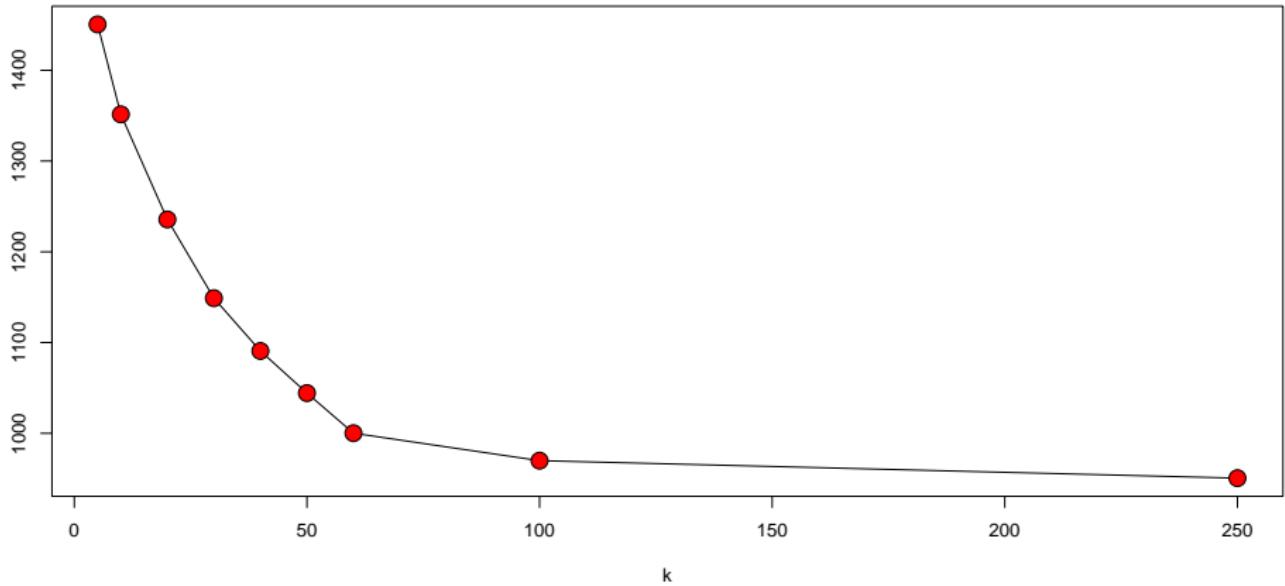
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But: the topic models that hold-out calculations suggest are optimal and not much liked by humans! “Reading Tea Leaves: How Humans Interpret Topic Models” by Chang et al.

Perplexity Likes a Lot of Topics (manifestos)



Pork to Policy (Catalinac, 2016)

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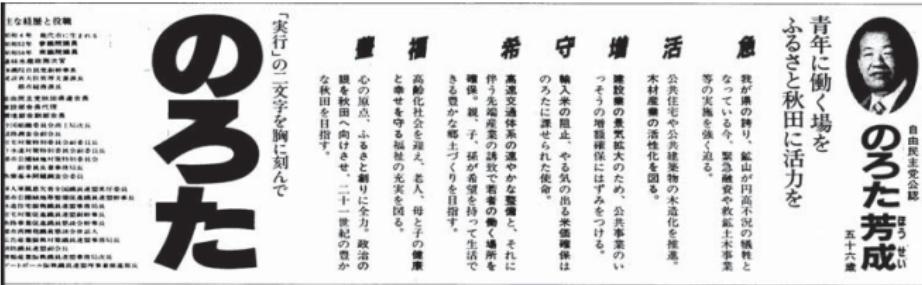


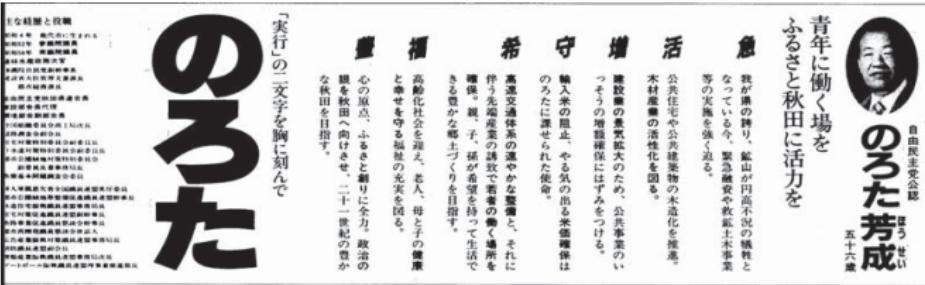
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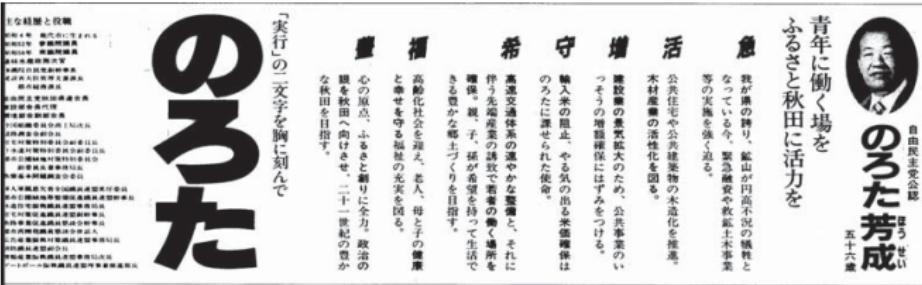
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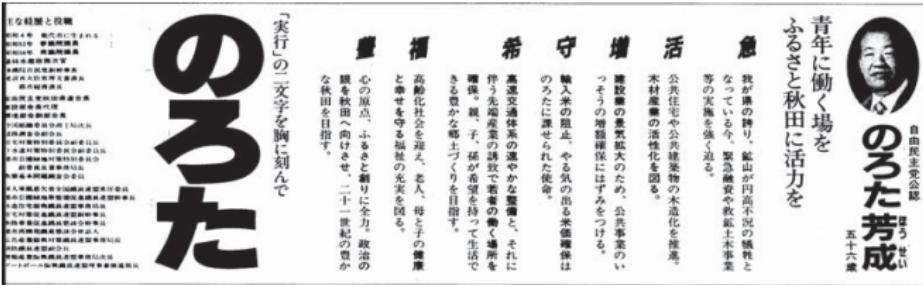
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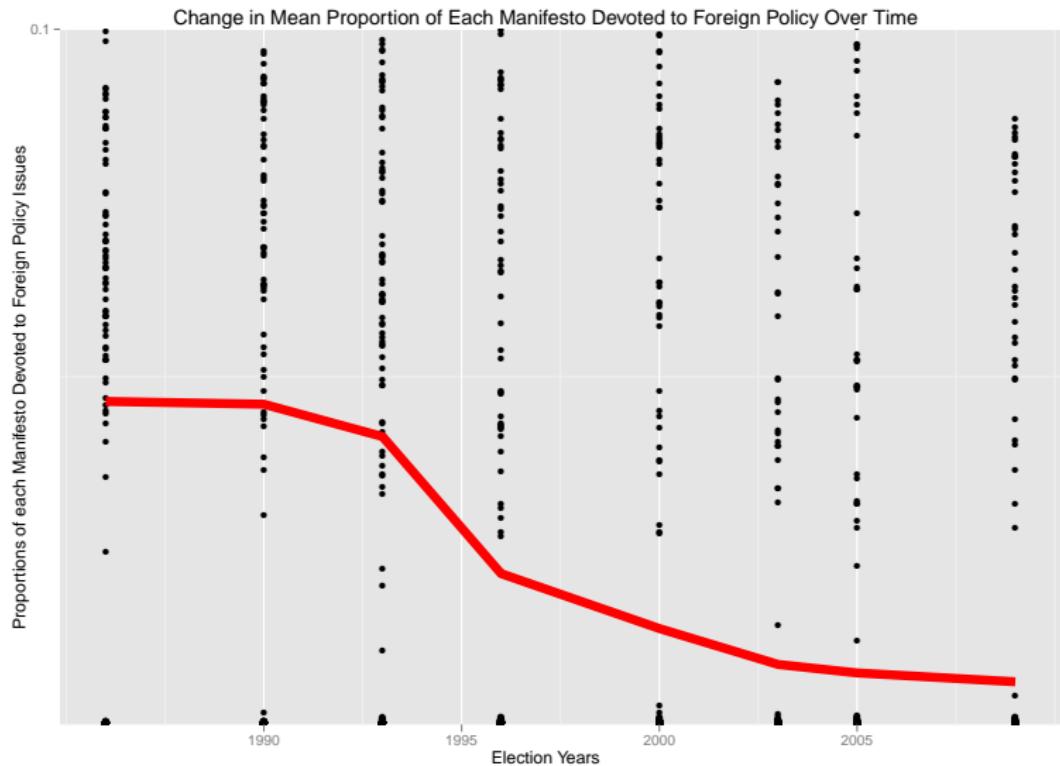
Topic Distribution over Words

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| Topic 1 | Topic 2 | Topic 3 | Topic 4 | Topic 5 | Topic 6 |
|---------|---------|---------|---------|---------|---------|
| 1 改革 | 年金 | 推進 | 区 | 政治 | 日本 |
| 2 郵政 | 円 | 整備 | 政策 | 改革 | 国 |
| 3 民営 | 廃止 | 図る | 地域 | 国民 | 外交 |
| 4 小泉 | 改革 | つとめる | まち | 企業 | 国家 |
| 5 構造 | 兆 | 社会 | 鹿児島 | 自民党 | 社会 |
| 6 政府 | 実現 | 対策 | 全力 | 日本 | 国民 |
| 7 官 | 無駄 | 振興 | 選挙 | 共産党 | 保障 |
| 8 推進 | 日本 | 充実 | 国政 | 献金 | 安全 |
| 9 民 | 増税 | 促進 | 作り | 金権 | 地域 |
| 10 自民党 | 削減 | 安定 | 横浜 | 党 | 拉致 |
| 11 日本 | 一元化 | 確立 | 対策 | 選挙 | 経済 |
| 12 制度 | 政権 | 企業 | 中小 | 禁止 | 守る |
| 13 民間 | 子供 | 実現 | 発電 | 憲法 | 問題 |
| 14 年金 | 地域 | 中小 | 推進 | 腐敗 | 北朝鮮 |
| 15 実現 | ひと | 育成 | エネルギー | 団体 | 教育 |
| 16 進める | サラリーマン | 制度 | 企業 | 区 | 責任 |
| 17 斷行 | 制度 | 政治 | 声 | ソ連 | 力 |
| 18 地方 | 議員 | 地域 | 実現 | 守る | 創る |
| 19 止める | 金 | 福祉 | 活性 | 平和 | 安心 |
| 20 保障 | 民主党 | 事業 | 自民党 | 円 | 目指す |
| 21 財政 | 年間 | 改革 | 地方 | 反対 | 誇り |
| 22 作る | 一掃 | 確保 | 尽くす | 真 | 憲法 |
| 23 賛成 | 郵政 | 強化 | 商店 | 是正 | 可能 |
| 24 社会 | 道路 | 教育 | いかす | 一掃 | 道 |
| 25 国民 | 交代 | 施設 | 全国 | 悪政 | 未来 |
| 26 公務員 | 社会保険庁 | 生活 | 政党 | 抜本 | ひと |
| 27 力 | 月額 | 支援 | ひと | 定数 | 再生 |
| 28 経済 | 手当 | 環境 | 支援 | 政党 | 将来 |
| 29 国 | 談合 | 発展 | 経済 | 金丸 | 解決 |
| 30 安心 | 吉澤 | 協議 | 福祉 | 改革 | 其本 |

Change in proportion of 'Pork' Topic

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