Haskell's type classes

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A type-class primer

A standard type class

Formal type parameter for instantiating type

class Eq a where
(==) :: a -> a -> Bool

Let's define equality for expressions.

A type-class instance

instance Eq Expr where

The (==) function is defined by pattern matching.

The full Eq class

```
class Eq a
where
  (==), (/=) :: a -> a -> Bool
  x/=y = not (x==y)
  x==y = not (x/=y)
```

Either of (==) or (/=) is sufficient for a complete defintion.

Another type class

```
class Show a
  where
    show :: a -> String
    ...

instance Show Expr
  where
    show (Const i) = "Const " ++ show i
    show (Add x y) = "Add" ++ f x ++ f y
    where
    f x = " (" ++ show x ++ ")"
```

Types with constraints

```
> :t id No constraint = parametric polymorphism
```

Constraint on actual type parameter = type-class polymorphism

Types with constraints

```
> :t filter
(a -> Bool) -> [a] -> [a]
> :t \a -> filter (a/=)
(Eq a) => a -> [a] -> [a]
```

Type classes vs. interfaces

C#/Java concept	Haskell concept
Class	
Interface	Type class
Interface member	Type-class member
Interface implementation	Type-class instance

Specifics of type classes when compared to C#/Java-like interfaces

- Retroactive implementation
- Explicit reference to implementing type
 - Multiple references ("binary methods")
 - Reference in result position ("static methods")
- Default implementations of members
- Multiple type parameters

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Different kinds of "methods"

```
> :t show
                            instance
(Show a) => a -> String
> :t read
                             static
(Read a) => String -> a
> :t (==)
                             binary
(Eq a) => a -> a -> Bool
```

Let's solve the expression problem with open datatypes and open functions.

Point of reference: the closed datatype

Note that there are two constructors; one of them of them involves recursive references.

Point of reference: the closed function

```
evaluate :: Expr -> Int
evaluate (Const i) = i
evaluate (Add l r) =
   evaluate l + evaluate r
```

Note that there is one equation per datatype constructor, and there are recursive function applications.

The open datatype

One datatype per original constructor

```
data Const = Const Int
data Add l r = Add l r

Class Expr x
instance Expr Const
instance (Expr l, Expr r) =>
Expr (Add l r)
```

A type class for the original datatype

The **open function** (type-class declaration)

A super-class constraint

class (Expr x =>) Evaluate x

where

evaluate :: x -> Int

The open function (type-class instances)

```
Constraints
instance Evaluate Const
                            for recursive
where
                                calls
  evaluate (Const i) = i
instance (Evaluate 1, Evaluate r) =>
     Evaluate (Add 1 r)
 where
  evaluate (Add 1 r) =
     evaluate 1 + evaluate r
```

A data extension

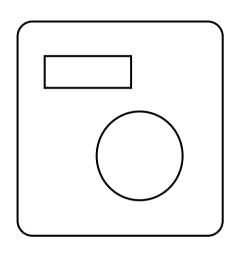
```
data Expr x => Neg x = Neg x
instance Expr x => Expr (Neg x)
instance Evaluate x => Evaluate (Neg x)
where
evaluate (Neg x) = 0 - evaluate x
```

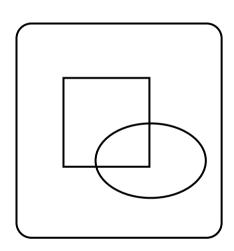
3 steps:

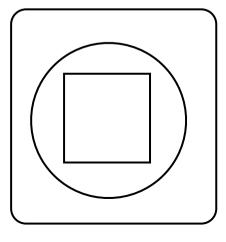
- Declare a designated datatype for the data variant.
- Instantiate the type class for the open datatype.
- Instantiate all type classes for existing operations.

Multi-parameter type classes: from sets of types (with common operations) to relations on types

A programming scenario: shapes and intersection







Point of reference: the closed datatype

```
data Shape =
   Square { x,y :: Int, length :: Int }
   | Rectangle { x,y :: Int, height, width :: Int }
   | Circle { x,y :: Int, radius :: Float }
   | Ellipse { x,y :: Int, major, minor :: Float }
```

Suppose we want to be extensible with regard to shapes.

Point of reference: the closed function

There are as many equations as there are combinations of forms of shape.

The open datatype

```
data Square = Square Int Int Int
data Rectangle = Rectangle Int Int Int Int
data Circle = Circle Int Int Float
data Ellipse = Ellipse Int Int Float Float

class Shape x
instance Shape Square
instance Shape Rectangle
instance Shape Circle
instance Shape Ellipse
```

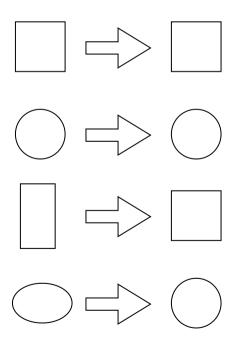
The open function

Wow! Type classes may have multiple type parameters. class (Shape x, Shape y) => {Intersect x y} where intersect :: x -> y -> Bool instance Intersect Square Square where intersect s s' = ...instance Intersect Rectangle Rectangle where intersect r r' = ...Exercise: Fill in the "..."!

Functional dependencies: from *relations* on types (with common operations) to *functions* on types

What if the result type depends on the argument type(s)?

Consider an operation normalize.



Preserve area and origin!

Point of reference: the closed function

```
normalize :: Shape -> Shape
normalize s@(Square _ _ _ ) = s
normalize (Rectangle x y h w) = Square ...
normalize c@(Circle _ _ _ ) = c
normalize (Ellipse x y a i) = Circle ...
```

The **open datatype** for normal shapes

class Shape s => NormalShape s
instance NormalShape Square
instance NormalShape Circle

"A normal shape is a shape."

The **open function** for normalization

```
class (Shape s1, NormalShape s2)
                  => Normalize s1 s2
where
 normalize :: s1 -> s2
instance Normalize Square Square
where
 normalize = id
instance Normalize Circle Circle
where
 normalize = id
instance Normalize Rectangle Square where ...
instance Normalize Ellipse Circle where ...
```

A weird type error

> normalize (Square 1 2 3)

Type error!

> normalize (Square 1 2 3) :: Square

Square 1 2 3

Why do we need to specify the result type? There is only one instance with argument type Square!

A hypothetical program

Instances at compile time of the expression

```
instance Normalize Square Square where ...
instance Normalize Circle Circle where ...
instance Normalize Rectangle Square where ...
instance Normalize Ellipse Circle where ...
```

An instance in a module that is compiled later

Type classes with functional dependencies

```
class (Shape s1, NormalShape s2)
=> Normalize s1 s2
There cannot be two
instances with the same
s1 (but different s2).

normalize :: s1 -> s2
```

> normalize (Square 1 2 3) Square 1 2 3

Further reading

- JavaGI (Wehr et al., ECOOP 2007; see also Wehr's PhD thesis)
- Haskell's type classes (Lämmel, Ostermann, GPCE 2006)
- Open data types and functions (Löh and Hinze, PPDP 2006)
- Fun with Type Functions (Kiselyov et al., May 2010)
- Language support for generic programming (Garcia et al., JFP 2007)
- Multiple dispatch in MultiJava (Clifton et al., ACM TOPLAS 2006)
- Multimethods à la Clojure

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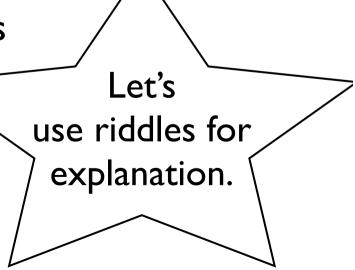
Nifty issues

- Scrap your boilerplate code
- Equality on open data
- Construct open data

Over-precise open types

Heterogenous lists

• ...



A riddle on instance derivation ("scrap your boilerplate" code)

Derive such instances automatically.

How to implement other **generic** operations once and for all?

A riddle on open equality

```
class Eq a where
  (==) :: a -> a -> Bool
```

This type class cannot work for open datatypes since, in general, values of an open datatype can be of different Haskell types. How do we recover?

A riddle on open data construction

read :: (Read a) => String -> a

Now suppose you instantiate the Read type class for the different data variants of the open datatype Expr. How would you read an arbitrary expression?

A riddle on type overprecision

```
> let n1 = Const 1
> let n40 = Const 40
> let n42 = Add (Add n1 n1) n40
> :t n42
n42 :: Add (Add Const Const) Const
```

Isn't the type a bit too precise? The type resembles the structure of the value!

A riddle on heterogenous lists: intersection for a list of shapes

How to do such an operation with an open datatype? More specifically, what's the type of intersect?

Thanks! Questions and comments welcome.