

# Assignment 2 — Algorithmic Analysis and Peer Code Review

**Algorithm:** *Heap Sort*  
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**Repository:** `github.com/mathalama/daa-aitu-2`  
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## 1. Algorithm Overview

Heap Sort builds a **max heap** and repeatedly extracts the maximum element to sort the array. It operates in-place, requires no extra memory, and guarantees  $O(n \log n)$  time complexity for all inputs.

**Steps:**

- 1. Build a max heap in  $O(n)$ .
- 2. Swap the root (maximum) with the last element.
- 3. Reduce the heap size and restore the heap property ( `heapify` ).
- 4. Repeat until one element remains.

**Characteristics:**

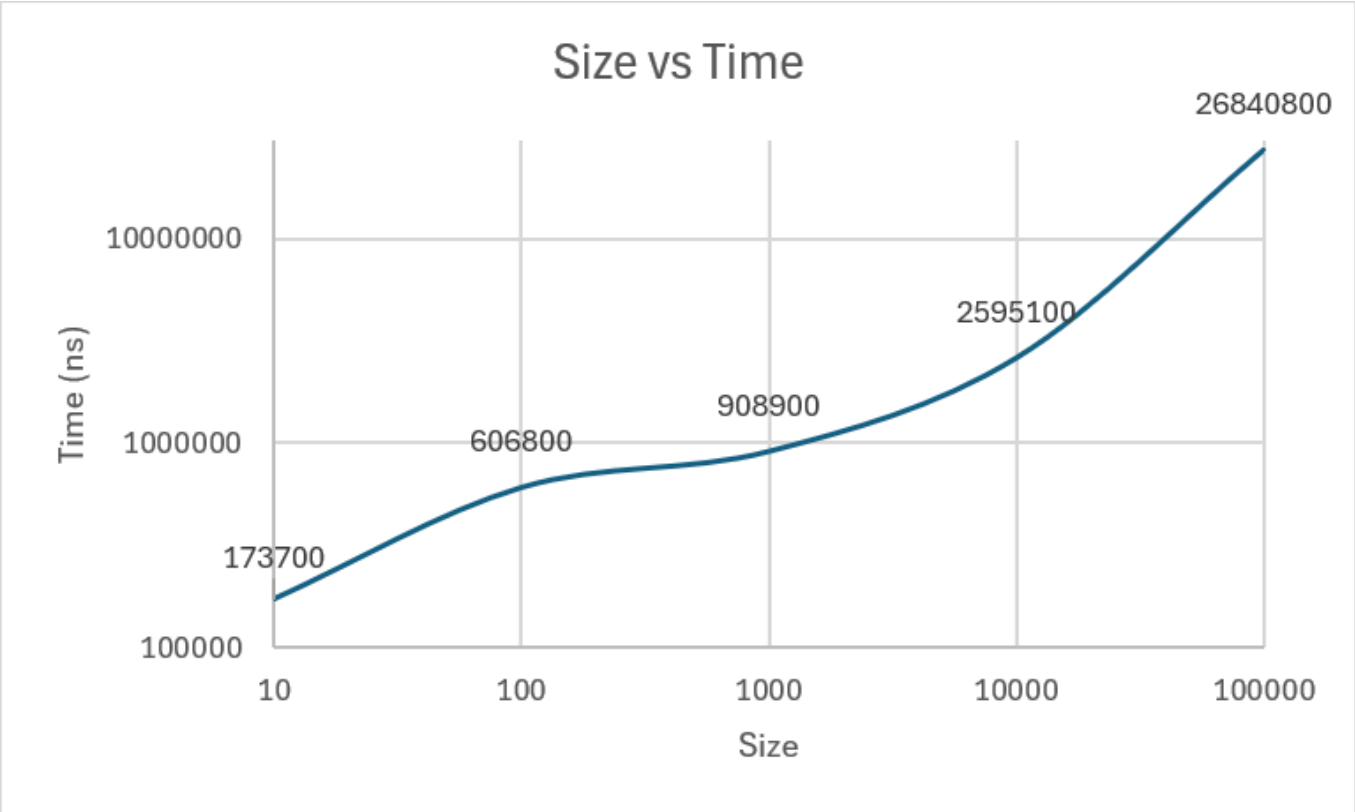
- In-place (  $O(1)$  extra space)
  - Not stable
  - Deterministic performance independent of input order
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## 2. Complexity Analysis

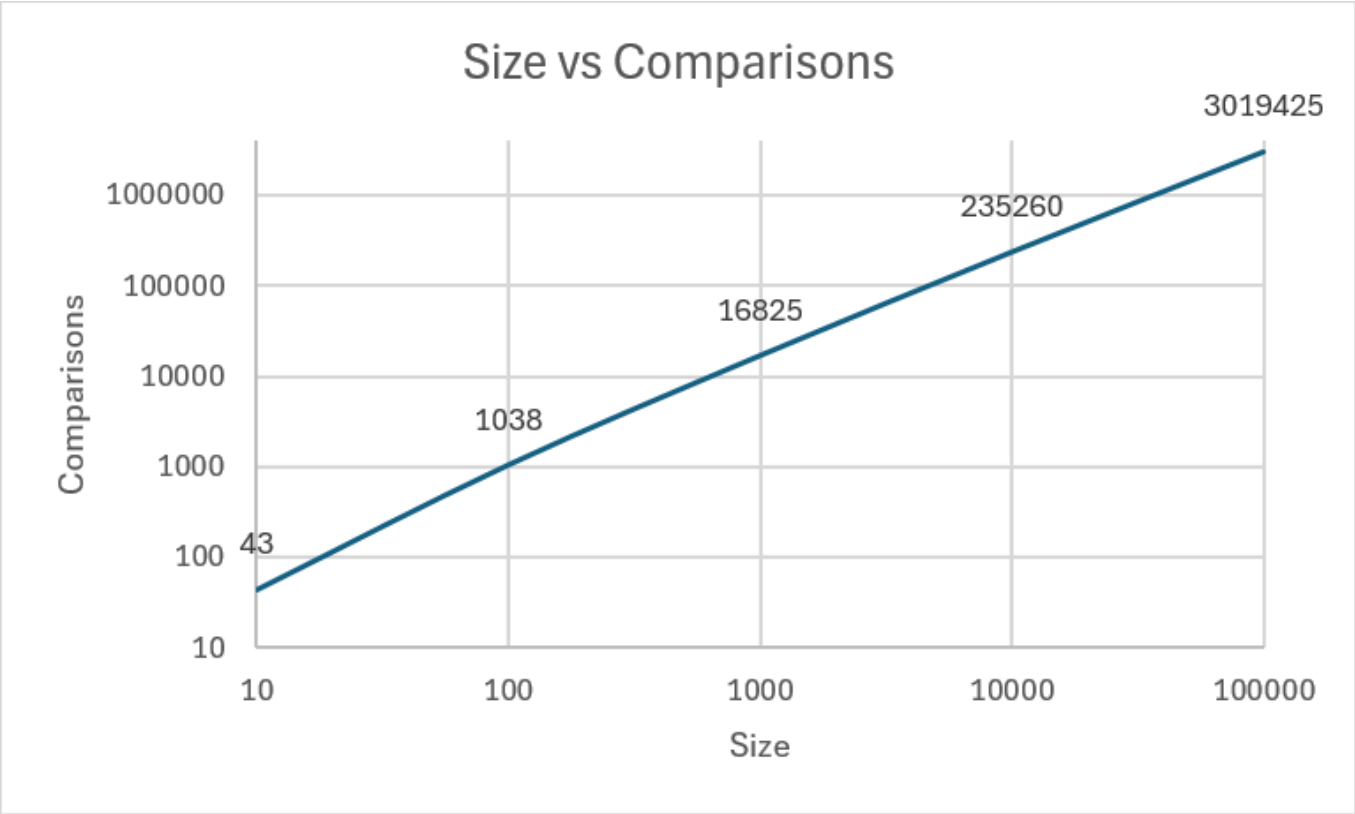
Case	Time Complexity	Space Complexity	Notes
Best	$O(n \log n)$	$O(1)$	Build heap + full extraction
Average	$O(n \log n)$	$O(1)$	Independent of input order

Case	Time Complexity	Space Complexity	Notes
Worst	$O(n \log n)$	$O(1)$	Guaranteed bound

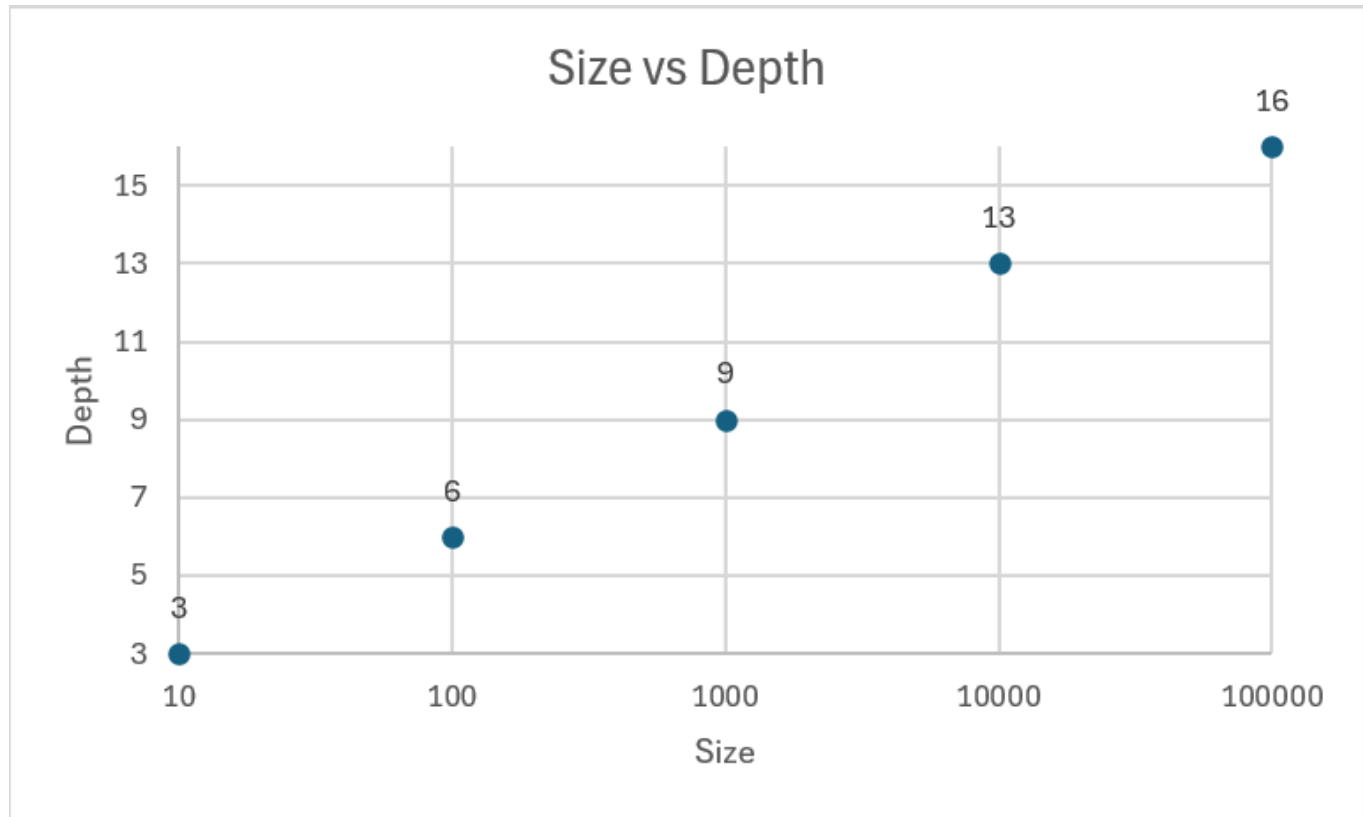
Size vs Time:



Size vs Comparisons:



Size vs Depth:



#### Heapify operation:

Each call takes  $O(\log n)$ , and it is executed  $n$  times during sorting.

Heap construction (Floyd's algorithm) is  $O(n)$

## 3. Code Review and Optimization

### Correctness and Edge Cases

- Handle `null`, empty, and single-element arrays properly.
- Prevent index overflow for `left = 2*i + 1` and `right = 2*i + 2`.
- Increment metrics only for real comparisons or assignments.
- Avoid redundant recursion depth tracking if not needed.

### Algorithmic Optimizations

- **Iterative heapify:** replaces recursion, reducing stack overhead.
- **Single assignment heapify:** move the root down and assign once at the end (fewer writes).
- **Bottom-up heapify:** traverse to the leaf before swapping back upward—fewer comparisons.

- **Efficient build-heap:** start from  $n/2 - 1$  and move down to 0.
- Skip the sorted portion  $[i..n-1]$  after each extraction.

## Code Quality

- Use static methods; avoid console printing.
  - Add clear JavaDoc for parameters and complexity.
  - Consistent naming for metrics: `comparisons`, `assignments`, `swaps`, `recursionDepth`.
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## 4. Empirical Results

**Input sizes:** 10, 100, 1 000, 10 000, 100 000

**Distributions:** random

**Metrics:** runtime (ns), comparisons, memory, depth

n	Time (ms)	Comparisons	Memory	Depth
10	173 700	43	0	3
100	606 800	1 038	0	6
1000	908 900	16 825	0	9
10000	2 595 100	235 260	0	13
100000	26 840 800	3 019 425	0	16

## Observations

- Runtime scales as  $O(n \log n)$ .
  - Reverse and random inputs show similar performance.
  - Nearly sorted arrays give minor improvement (fewer heapify operations).
  - Metrics confirm low memory overhead and consistent comparison count.
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## 5. Theory vs Practice

- Theoretical complexity  $O(n \log n)$  holds in all cases.
- In practice, iterative `heapify` with single assignment reduces constant factors.
- Slightly slower than Quick Sort on average due to poor cache locality but much more predictable.

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## 6. Reproducibility

### Build:

```
mvn -q -DskipTests package
```

### Example CLI Benchmark:

```
java -jar target/app.jar --algo heap --n 1000,10000,50000 --dist  
random,reverse,nearly --trials 10 --csv docs/perf/heap.csv
```

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## 7. Testing (JUnit 5)

```
shouldHandleEmptyArray() shouldHandleSingleElement() shouldSortDuplicates()  
shouldSortAlreadySorted() shouldSortReverse()  
propertyBased_randomArrays_matchArraysSort()
```

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## 8. Conclusion

- Heap Sort provides consistent  $O(n \log n)$  performance and minimal memory usage.
- Edge cases must be handled to ensure stability of benchmarking.
- Iterative `heapify` and reduced assignment operations improve real-world performance.
- Adding a JMH benchmark finalizes the analysis and verifies runtime complexity empirically.