

## Scaling Definitions

### 1) Consensus (Old)

Define

$Z_M = 300000$  bytes ; Minimum penalty free zone.

$M_B$  = Block weight in bytes.

$M_L$  = The median over the last 100000 blocks of  $\max(\min(M_B, 1.7M_L), Z_M, M_L/1.7)$  ; recursive calculation for  $M_L$  with  $M_L$  starting at  $M_L$  of previous 100001 block (currently =  $Z_M$ );  
Long term median

$M_L$  ; Dynamic penalty free zone.

$M_S$  = the median over the last 100 blocks of  $\max(M_B, M_L)$  ;  
Effective short term median.

$M_N = \min(M_S, 50M_L)$  ; Median for Penalty calculation.

$R_{Base}$  = Block Reward.

$0 < M_B \leq 2M_N$  ; Requirement for a valid block.

$B = M_B / M_N - 1$  where  $-1 < B \leq 1$

$P_B = R_{Base}B^2$  for  $B > 0$  ; Monero applies a penalty  $P_B$ , to increase the block weight by  $B$ ;  $P_B = 0$  for  $B \leq 0$

## Scaling Definitions (Consensus 17<sup>th</sup> December 2025 MRL meeting. Wallet fee calculations January 2026)

### 1) Consensus (New)

Define

$Z_M = 625000$  bytes ; Minimum penalty free zone.

$M_B$  = Block weight in bytes.

$M_L$  = The median over the last 100000 blocks of  $\max(\min(M_B, 1.2M_L), Z_M, M_L/1.2)$  ; recursive calculation for  $M_L$  with  $M_L$  starting at  $M_L$  of previous 100001 block (currently =  $Z_M$ );  
Long term median

$M_L$  ; Dynamic penalty free zone.

$M_S$  = The median over the last 100 blocks of  $M_B$  ; Short Term Median.

$M_N = \min(\max(M_S, M_L), 8M_L)$ ; Median for Penalty Calculation.

$R_{Base}$  = Block Reward.

$0 < M_B \leq 2M_N$  ; Requirement for valid block.

$B = M_B / M_N - 1$  where  $-1 < B \leq 1$

$P_B = R_{Base}B^2$  for  $B > 0$  ; Monero applies a penalty  $P_B$ , to increase the block weight by  $B$ ;  $P_B = 0$  for  $B \leq 0$

### Changes

- 1) Maximum growth of  $M_S$  is reduced from  $50M_L$  to  $8M_L$
- 3) Rate of growth and decline of  $M_L$  is decreased from  $1.7x$  to  $1.2x$
- 4)  $Z_M$  is increased from  $300000$  bytes to  $625000$  bytes
- 5) Definition change to reflect the code. Also  $M_N$  is added to the transitional consideration and  $M_{SW}$  removed.  $M_{SW}$  is no longer relevant since the short term median is no longer used for the fee calculation.

## 2a) Minimum Fee For Node Relay (Old)

We add a, penalty attracting, transaction T with a size of  $T_T$  to a block of weight  $M_B$

Define

$T_R = 3000$  bytes ; Reference Transaction weight. Note:  $T_R$  must be greater than  $T_2$ .  $T_2$  equals the weight in bytes of a 2 input and 2 output transaction.

$$B_T = T_T / M_N$$

$P_{BT} = R_{Base}(B+B_T)^2 = R_{base}(B^2 + 2BB_T + B_T^2)$  ; The new penalty, where  $B + B_T > 0$

$P_T = P_{BT} - P_B = R_{Base}(2BB_T + B_T^2)$  ; Increase in penalty from adding transaction T

$F_T = R_{Base}(2BB_T + B_T^2)$  ; The additional fee required to overcome the increase in penalty  $P_T$

For the case  $B = 0$  this reduces to  $F_T = R_{Base}B_T^2$

$M_F = M_L$  ; Median for minimum fee calculation.  $M_L$  is used instead of  $M_N$  for fee stability (MRL issue #70), as an anti spam measure (The fee reduction is only applied when  $M_N$  has been vetted by  $M_L$ ), and to facilitate scaling during periods of fast growth in  $M_N$ .

To calculate the minimum fee we consider a transaction of weight  $T_R$  at the start of the penalty,  $B = 0$  with  $M_N = M_F$  95% of the fee required to pay the penalty incurred is the minimum fee.

$$B_{RL} = T_R / M_F;$$

$F_R = R_{Base}B_{RL}^2$  ; Fee required to pay the penalty incurred

$f_R = R_{Base}B_{RL}/M_F$  ; Fee required to pay the penalty incurred per byte for a given  $M_F$

$f_I = 0.95f_R$  ; Minimum fee per byte

## 2a) Minimum Fee For Node Relay (New)

We add a, penalty attracting, transaction T with a size of  $T_T$  to a block of weight  $M_B$

Define

$T_R = 10000$  bytes ; Reference Transaction weight. Note:  $T_R$  must be greater than  $T_2$ .  $T_2$  equals the weight in bytes of a 2 input and 2 output transaction.

$$B_T = T_T / M_N$$

$P_{BT} = R_{Base}(B+B_T)^2 = R_{base}(B^2 + 2BB_T + B_T^2)$  ; The new penalty, where  $B + B_T > 0$

$P_T = P_{BT} - P_B = R_{Base}(2BB_T + B_T^2)$  ; Increase in penalty from adding transaction T

$F_T = R_{Base}(2BB_T + B_T^2)$  ; The additional fee required to overcome the increase in penalty  $P_T$

For the case  $B = 0$  this reduces to  $F_T = R_{Base}B_T^2$

$M_F = M_L$  ; Median for minimum fee calculation.  $M_L$  is used instead of  $M_N$  for fee stability (MRL issue #70), as an anti spam measure (The fee reduction is only applied when  $M_N$  has been vetted by  $M_L$ ), and to facilitate scaling during periods of fast growth in  $M_N$ .

To calculate the minimum fee we consider a transaction of weight  $T_R$  at the start of the penalty,  $B = 0$  with  $M_N = M_F$  100% of the fee required to pay the penalty incurred is the minimum fee.

$$B_{RL} = T_R / M_F;$$

$F_{RL} = R_{Base}B_{RL}^2$  ; Fee required to pay the penalty incurred

$f_{RL} = R_{Base}B_{RL}/M_F$  ; Fee required to pay the penalty incurred per byte for a given  $M_F$

$f_{IL} = f_{RL}$  ; Minimum fee per byte

## Changes

- 1)  $T_R$  is increased from 3000 bytes to 10000 bytes. For clarity  $T_R$  is defined outside of consensus.
- 2) There is no reduction to 95% of the minimum fee. This is all now handled on the wallet side.

## 2b) Wallet Fees (Old)

For the calculation of wallet fees we assume that the next 10 blocks have no transactions, other than the coinbase transaction, the empty blocks, We then calculate  $M_{LW}$  and  $M_{SW}$  by following the calculation of  $M_L$  and  $M_S$  at this future point. We use the previous 99990 blocks and the future 10 empty blocks (100000 blocks) for  $M_L$ .

Define

$$M_{BW} = M_B \text{ for the last 99990 blocks}$$

$M_{BW} = 0$  for the future 10 blocks; A value of 0 bytes can be used for the empty blocks for the purposes of calculating  $M_{LW}$ .

$M_{LW}$  = The median over the last 99990 blocks and future 10 blocks (100000 blocks) of  $\max(\min(M_{BW}, 2M_L), Z_M, M_L/2)$ ; The current value of  $M_L$  from consensus is used; Effective long term median for wallet fees

$M_{LW}$  ; Penalty free zone for wallet fees

$M_{FW} = M_{LW}$  ; Median for wallet fee calculation

$B_{RLW} = T_R / M_{FW}$  ; Used for the low and normal fees

$B_R = T_R / Z_M$  ; Used for the medium and high fees

$F_L = R_{Base}B_{RLW}^2$  ; Low transaction fee for reference transaction

$f_L = R_{Base}B_{RLW}/M_{FW}$  ; Low transaction fee per byte for a given  $M_{FW}$

$f_N = 4f_L$  ; Normal transaction fee per byte for a given  $M_{FW}$

$f_M = 16R_{Base}B_R/M_{FW}$  ; Medium Transaction fee per byte for a given  $M_{FW}$

$f_P = 2R_{Base}/M_{NW} = f_M M_{FW}/(8B_R M_{NW})$ ; Maximum Penalty (B =1) Transaction fee per byte for a given  $M_{NW}$

$f_H = 4f_M \max(1, M_{FW}/(32B_R M_{NW}))$ ; High Transaction fee per byte

## 2b) Wallet Fees (New)

For the calculation of wallet fees we assume that the next 1000 blocks have no transactions, other than the coinbase transaction, the empty blocks, We then calculate  $M_{LW}$  by following the calculation of  $M_L$  at this future point. We use the previous 99000 blocks and the future 1000 empty blocks (100000 blocks) for  $M_L$ .

Define

$$M_{BW} = M_B \text{ for the last 99000 blocks}$$

$M_{BW} = 0$  for the future 1000 blocks; A value of 0 bytes can be used for the empty blocks for the purposes of calculating  $M_{LW}$ .

$M_{LW}$  = The median over the last 99000 blocks and future 1000 blocks (100000 blocks) of  $\max(\min(M_{BW}, 1.2M_L), Z_M, M_L/2)$ ; The current value of  $M_L$  from consensus is used; Effective long term median for wallet fees

$M_{LW}$  ; Penalty free zone for wallet fees

$M_{FW} = M_{LW}$  ; Median for wallet fee calculation

$B_{RLW} = T_R / M_{FW}$  ; Used for all fees except the maximum fee

$F_L = R_{Base}B_{RLW}^2$  ; Low (minimum scaling) transaction fee for reference transaction

$f_L = R_{Base}B_{RLW}/M_{FW}$  ; Low (minimum scaling) transaction fee per byte for a given  $M_{FW}$

$f_N = 4f_L$  ; Normal transaction fee per byte for a given  $M_{FW}$

$f_M = 16f_L$  ; Medium Transaction fee per byte for a given  $M_{FW}$

$f_H = 64f_L$  ; High Transaction fee per byte for a given  $M_{FW}$

$f_X = 2R_{Base}/M_{FW} = 2(M_{FW}/T_R)f_L$ . Maximum Transaction fee. This is greater than or equal to Maximum Penalty (B =1). For  $M_{FW} = Z_M = 625000$  bytes  $f_X = 125f_L$ . This still works to provide a high fee after two cycles of  $M_L$  (MRL issue #70) with a growth rate of  $M_L = 1.2$ .

### Changes

- 1) All fees including the high fee are now based upon  $M_{FW}$  with the ratio between fees constant for a given  $M_{FW}$ .
- 2) The grace period is increased to 1000 blocks.
- 3) 5 fee levels with a 4x factor between fees for the lower 4 fee levels,  $f_L$ ,  $f_N$ ,  $f_M$ , and  $f_H$ . Additional fee levels can be added, below  $f_X$  if needed at 256x, 1024x, 4096x etc., for larger  $M_L$ , provided these additional fee levels are below  $1.44f_X$ .

**3) Consensus Transitional considerations for Minimum penalty free zone,  $Z_M$ , and Median calculations after the fork.**

Define:

$Z_{M\text{Old}} = 300000$  bytes ( $Z_M$  before hard fork)

$M_{B\text{Old}}$  = Block Weight in bytes (before hard fork)

**3) Consensus Transitional considerations for Minimum penalty free zone,  $Z_M$ , and Median calculations after the fork.**

Calculation of  $M_L$ ,  $M_S$ ,  $M_N$  and  $M_{LW}$  where blocks from a previous Monero version are included in a calculation after the fork.  $M_B$  is modified as follows:

Define

$Z_M = 625000$  bytes

For blocks before the hard fork

$$M_B = M_{B\text{Old}} \left( Z_M / Z_{M\text{Old}} \right)$$

The medians are then calculated normally.

Note: This is only necessary if  $M_{L\text{Old}} > Z_{M\text{Old}}$ , where  $M_{L\text{Old}}$  is the long term median just before the fork.

#### 4) Wallet Fee Rounding

Wallet fees,  $f_N$ ,  $f_L$ ,  $f_M$ , and  $f_H$  are rounded up to the desired number of significant digits in the significand

##### Wallet Fee Rounding Examples

Two significant digits

27810	Rounded to : 28000
37.94	Rounded to : 38
0.5555	Rounded to : 0.56
0.002342	Rounded to : 0.0024

#### 4) Wallet Fee Rounding

Wallet fees,  $f_N$ ,  $f_L$ ,  $f_M$ ,  $f_H$ , and  $f_X$  are rounded up to 2 significant digits in the significand

##### Wallet Fee Rounding Examples

Two significant digits

27810	Rounded to : 28000
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0.002342	Rounded to : 0.0024

**Note:**

**Wallet fees are rounded up**