



# Change Detection Algorithm with Hardware Constraints

Prof. Ingo Sander<sup>1</sup>, Postdoc Marcello Costa<sup>2</sup>

September 16, 2024 — <sup>1</sup>KTH Royal Institute of Technology, <sup>2</sup>Cisb-Saab



# Contents

Problem Introduction and Background

Change Detection Algorithm:  
2D-AR(1) on Synchronous MoC

VHF-UWB SAR Dataset: CARABAS-II

Extension for  $n$ -lags

Demo 2: 2D-AR(1) processing on ForSyde/Haskell

1. **Elementary bitemporal Change Detection:** → rapid data analysis, low complexity, power consumption, and memory requirements, parallelized extension<sup>1</sup>
2. **Time-series methods**<sup>3</sup> → ARIMA, PCA, SVM, Random Forest, NN, K-means, GLM, EM, SVD, XGboost, LSTM,..
3. **Synchronous MoC and Parallelism** → Distributed data processing architectures for runtime, memory and energy saving<sup>2</sup>
4. **Particular case: Ultra-wideband (UWB) SAR** → stable scatters in time, random motions of targets in the clutter as a first-order autoregressive AR(1) process

---

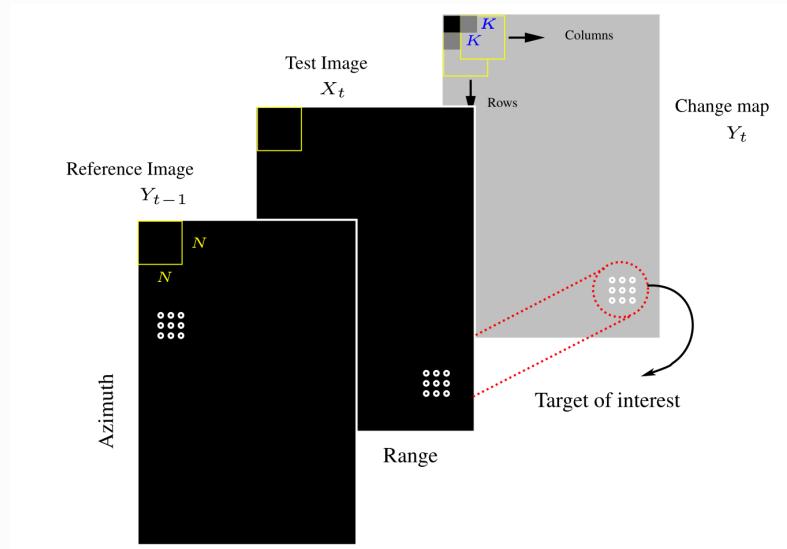
<sup>1</sup>Wu, Suya, et al. "Quickest Change Detection for Unnormalized Statistical Models," *IEEE Trans. on Inf. Theory*, v. 70, n. 2, pp. 1220-1232, 2024.

<sup>2</sup>Rabhi et al., "Patterns and skeletons for parallel and distributed computing," Springer Science & Business Media, 2003.

<sup>3</sup>Bayer, F.M., et al., "A Novel Rayleigh Dynamical Model for Remote Sensing Data Interpretation," *IEEE Trans. on Geoscience and Remote Sensing*, v. 58, n. 7, pp. 4989-4999, 2020.

# Time series Prediction Model

$$\hat{Y}_t = f(X_t, Y_{t-1}, Y_{t-2}, \dots, Y_{t-p}) + \epsilon_t, \quad (1)$$



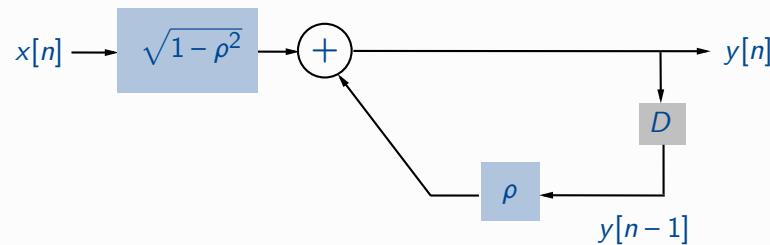
## Combinational solution

$X_t$	$Y_{t-1}$	Change
0	0	No change
0	1	No change
1	0	Change
1	1	No change

Note: Anomaly = 1, background = 0.

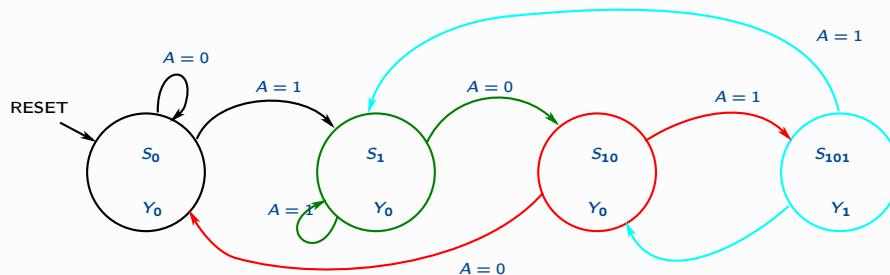
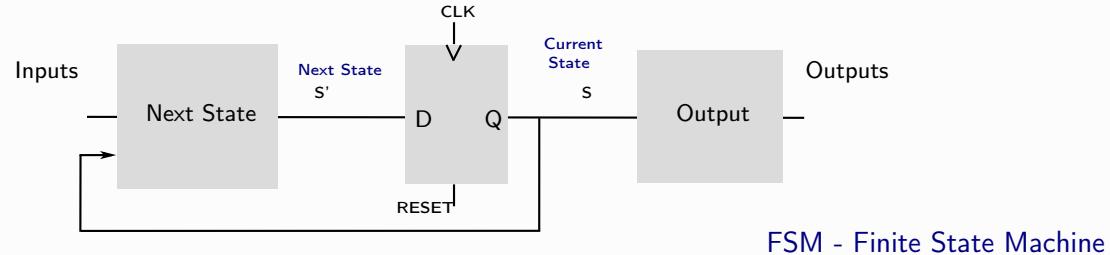
**Auto-regressive first order Model (AR(1)):** Detects uncorrelated samples between  $y_{t-1}$  and  $x_t$  as a predicted anomaly to compose the change map  $y_t$ , which describes the degree of retained memory of previous states.

$$\underbrace{\hat{y}_t}_{\text{changes}} = \underbrace{\rho}_{\text{corr. ref. signal}} \underbrace{y_{t-1}}_{\text{test signal}} + \sqrt{1 - \rho^2} \underbrace{x_t}_{\text{test signal}}, \quad (2)$$



where  $\rho \rightarrow [0, 1]$ .  
 Embedded systems

# Synchronous Model of Computation (MoC)

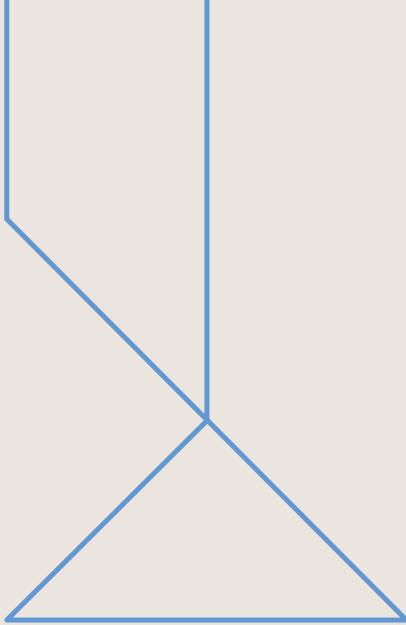


Structure for a first order IIR filter.

Embedded systems

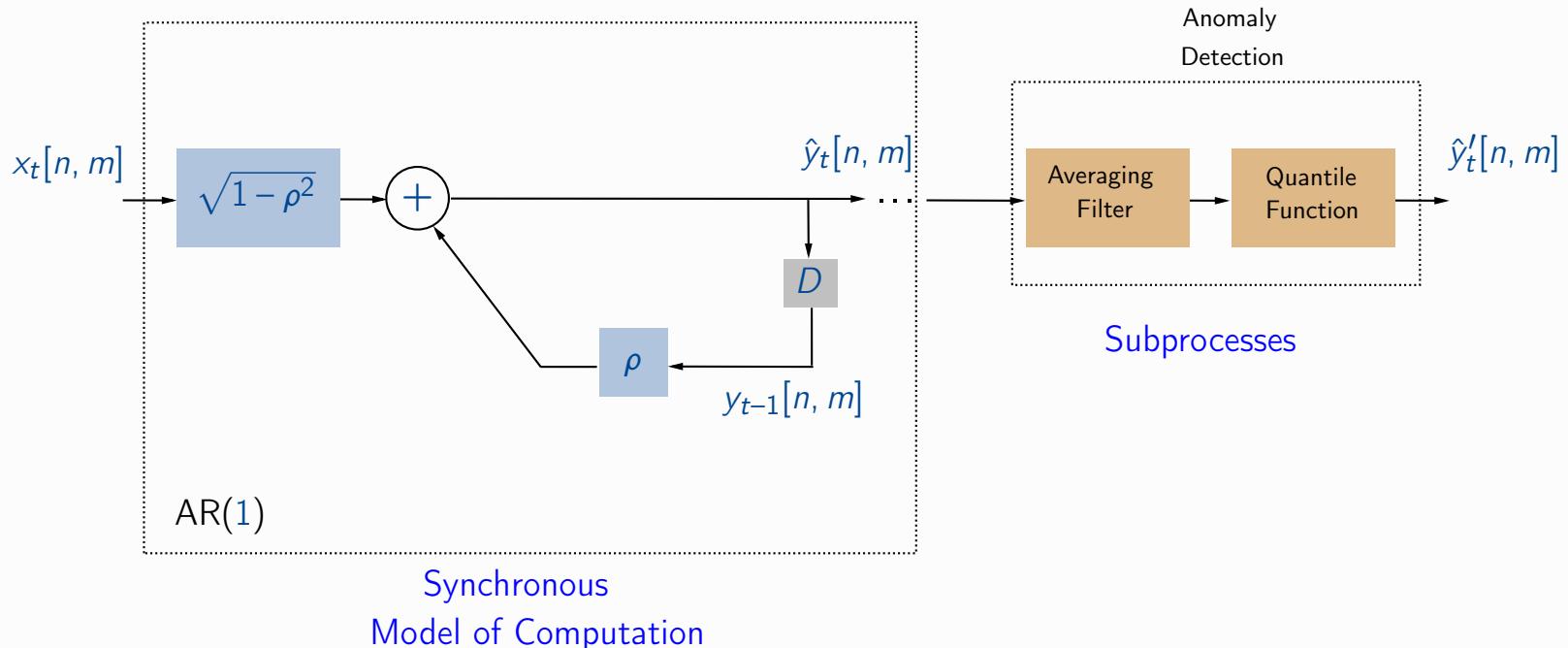
IL2232 - Project Change Detection

6/28



Change Detection Algorithm:  
2D-AR(1) on Synchronous MoC

## Time-Spatial Implementation:



## Spatial Filtering with Moving Average (FIR)

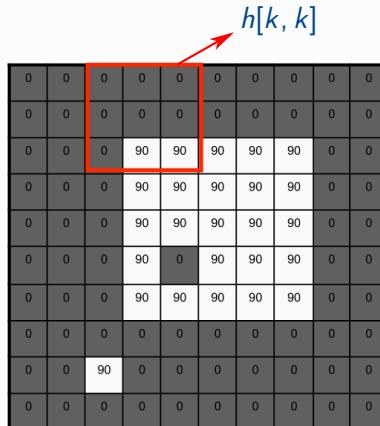
The smoothed function  $g[n, m]$  under the neighborhood influence is determined by the kernel elements  $h$  through the original signal  $f[n, m]$ , i.e.,

$$g[n, m] = (f * h)[n, m]$$

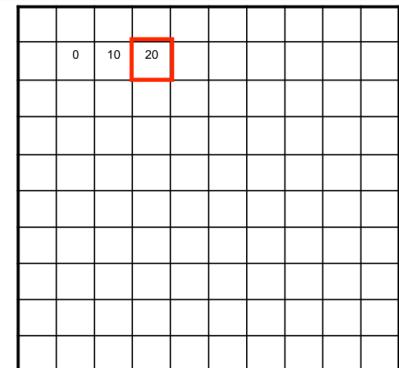
$$\sum_{k, \ell} f[k, \ell] h[n - k, m - \ell] \quad (3)$$

For a generic stencil kernel

$$h = \frac{1}{k} \begin{bmatrix} 1 & 1 & 1 & 1 \\ \vdots & \vdots & \ddots & \vdots \\ 1 & 1 & 1 & k \end{bmatrix}_{k \times k} \quad (4)$$



$$f[n, m] = \hat{y}_t[n, m]$$

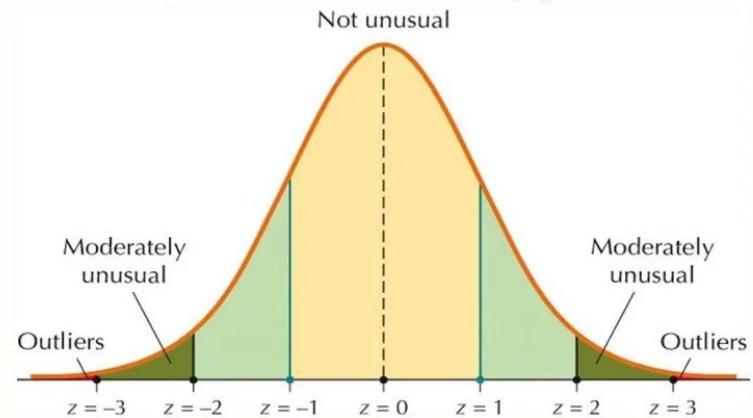


$$g[n, m] = \hat{y}'_t[n, m]$$

## Anomaly Detection

The empirical cumulative distribution function (ECDF),  $\hat{F}(\cdot)$ , is obtained from  $[\hat{y}'_1, \dots, \hat{y}'_n]$  i.i.d samples of  $\hat{y}'$ , making

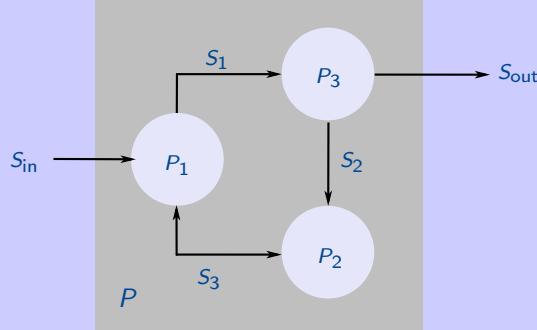
$$\begin{aligned}\hat{F}(\hat{y}') &= \frac{1}{n} \sum_{i=1}^n I(\hat{y}'_i \leq \hat{y}') \\ \hat{y}'(p) &= \hat{F}^{-1}(p),\end{aligned}\tag{5}$$



$\Rightarrow \hat{y}'(p)$  establishes the threshold on  $\hat{y}'_t[n, m]$  when  $x_t[n, m]$  has an anomaly of interest (potential target) against the lower clutter anomalies due to the state  $y_{t-1}[n, m]$

**Synchronous MoC<sup>5</sup>**: Synchronized parallel components, running in successive computation steps, where all components perform some quantum of computation.

1. Output is synchronous with input
2. Internal actions are instantaneous




---

<sup>5</sup>Albert Benveniste and Gérard Berry. "The synchronous approach to reactive and real-time systems," *Proceedings of the IEEE*, 79(9):1270–1282, September 1991.

## Change Detection Algorithm: 2D-AR(1) on Synchronous MoC

### Change Detection with AR Model

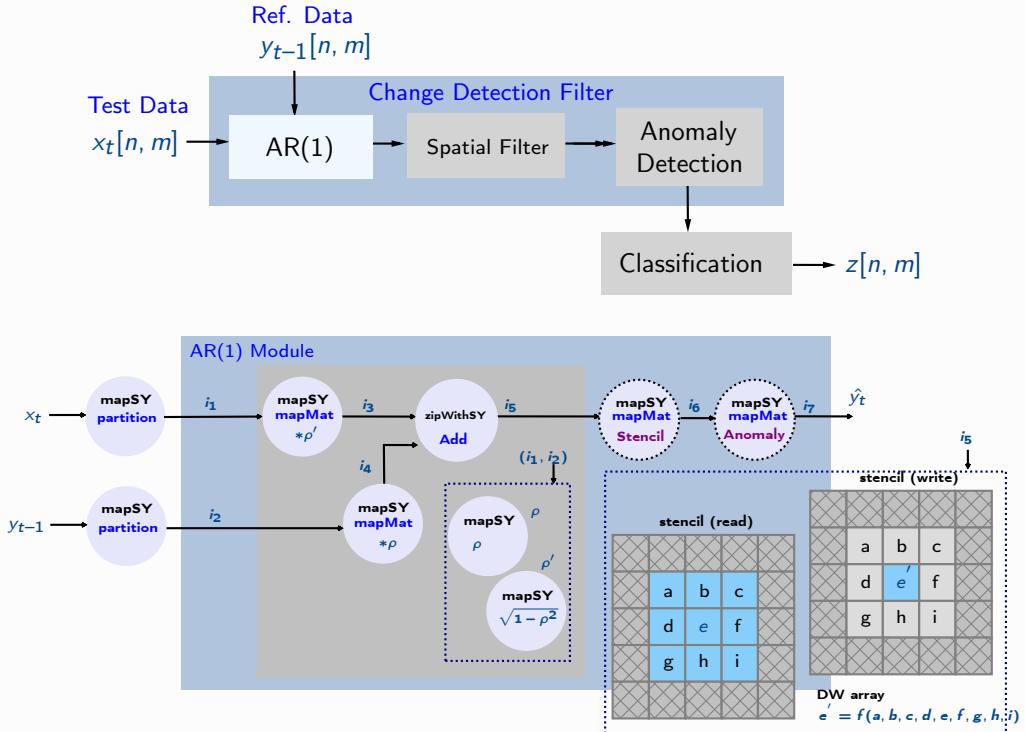
#### ► ForSyDe Framework<sup>5</sup>/Haskell

Synchronous MoC constructors:

- Combinational → `zipWithSY`, `mapSY`
- Delay → `delaySY`
- Sequential → `mooreSY`, `mealySY`

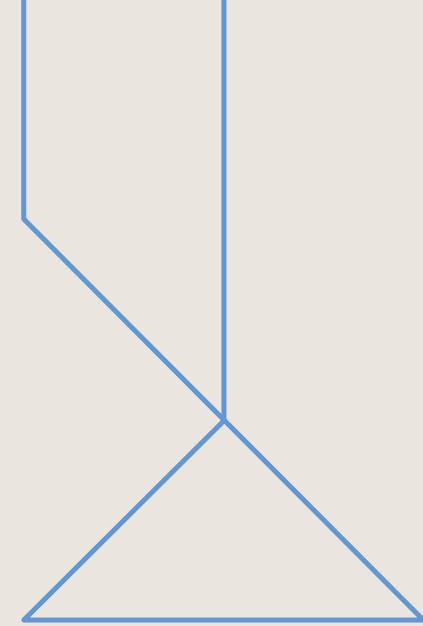
Parallel stencil computation

- `Data.Massiv.ArrayFramework`<sup>6</sup>



<sup>5</sup><https://forsyde.github.io/>

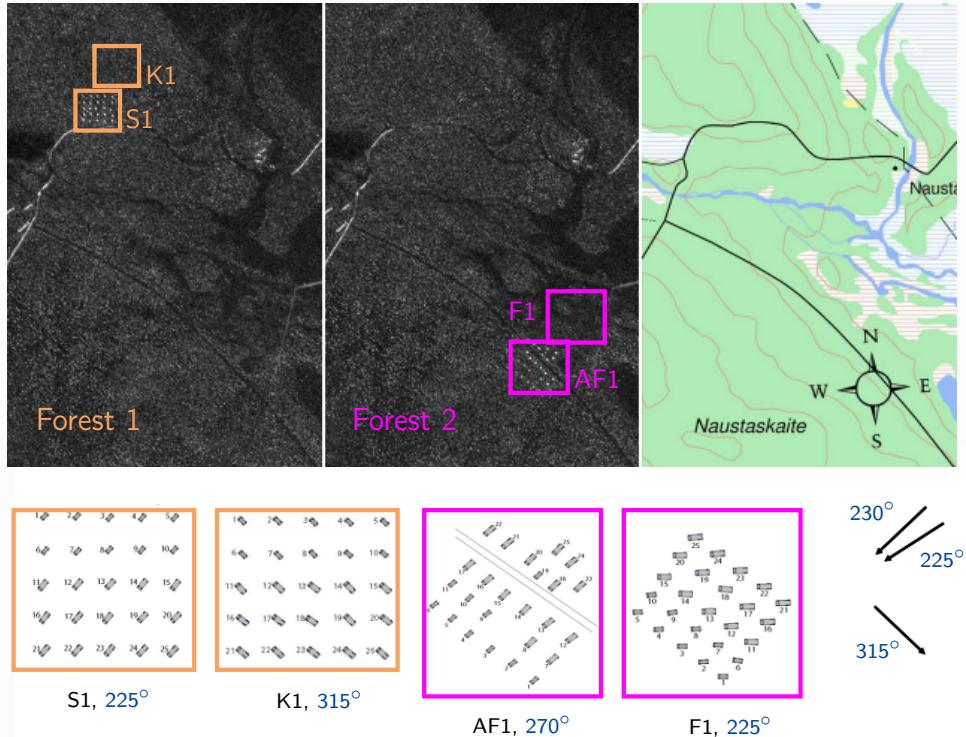
<sup>6</sup><https://hackage.haskell.org/package/massiv>



VHF-UWB SAR Dataset: CARABAS-II

## CARABAS-II dataset<sup>7</sup>:

- 24 images: magnitude VHF (20 – 90 MHz) SAR HH-polarized with 1 m resolution ( $2 \times 3 \text{ km}^2$ )
- 4 Targets position: S1, K1, F1, and AF1
- 6 passes: 3 Flight directions under ground RFI sources ON/OFF
- Application: Through-foliage detection

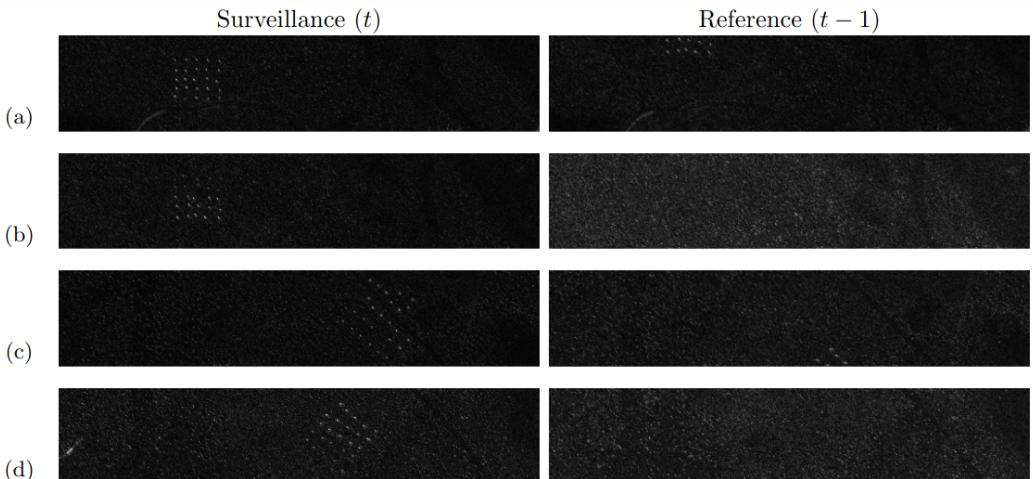


<sup>7</sup>Ulander, L.M, et al. "Change detection for low-frequency sar ground surveillance," *IEE Proceedings-Radar, Sonar and Navigation* , 152(6), pp. 413–420, 2005.

## VHF-UWB SAR Dataset: CARABAS-II

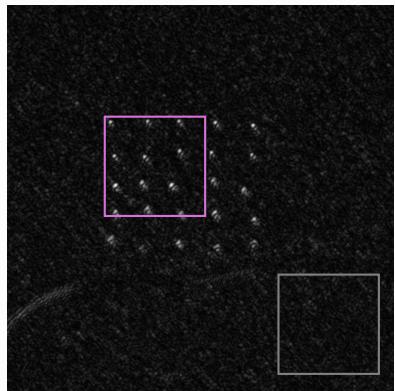
Exp. No.	Surveillance image		Reference image		Known Targets	Area [km <sup>2</sup> ]
	Mission	Pass	Mission	Pass		
(a) 1	2	1	3	1	25	6
(b) 2	3	1	4	1	25	6
(c) 3	4	1	5	1	25	6
(d) 4	5	1	2	1	25	6
5	2	2	4	2	25	6
6	3	2	5	2	25	6
7	4	2	2	2	25	6
8	5	2	3	2	25	6
9	2	3	5	3	25	6
10	3	3	2	3	25	6
11	4	3	3	3	25	6
12	5	3	4	3	25	6
13	2	4	3	4	25	6
14	3	4	4	4	25	6
15	4	4	5	4	25	6
16	5	4	2	4	25	6
17	2	5	4	5	25	6
18	3	5	5	5	25	6
19	4	5	2	5	25	6
20	5	5	3	5	25	6
21	2	6	5	6	25	6
22	3	6	2	6	25	6
23	4	6	3	6	25	6
24	5	6	4	6	25	6
Total		600	144			

Campaign sample data:  $2 \times 0.5 \text{ km}^2 (15%)$

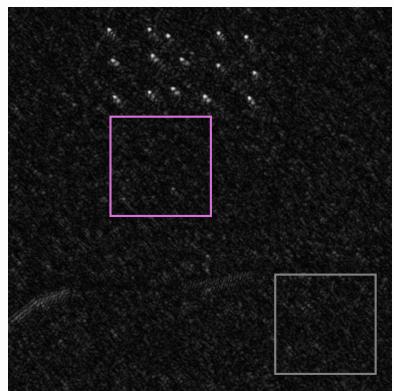


## Step 1: Block size selection

surveillance  $x_t$

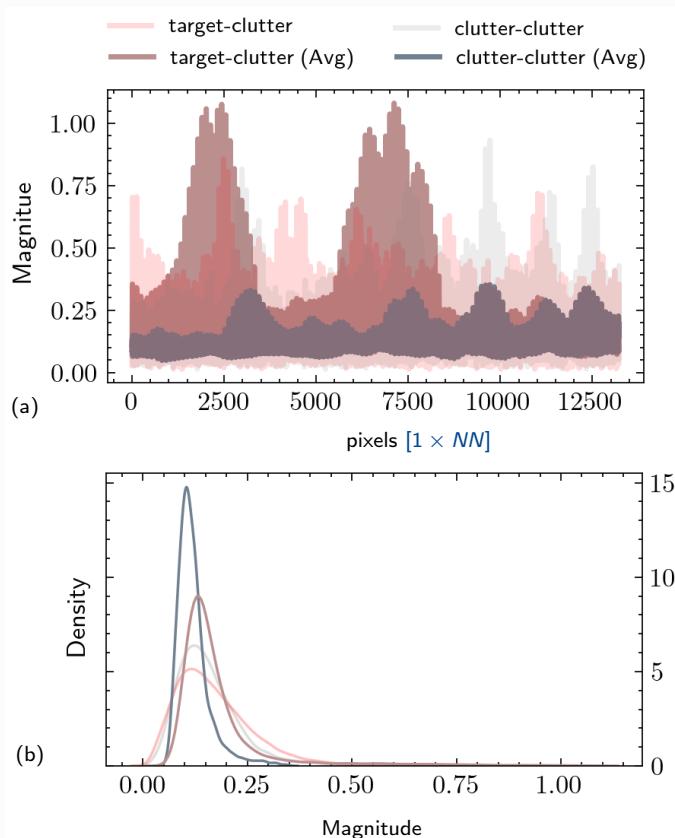


reference  $y_{t-1}$



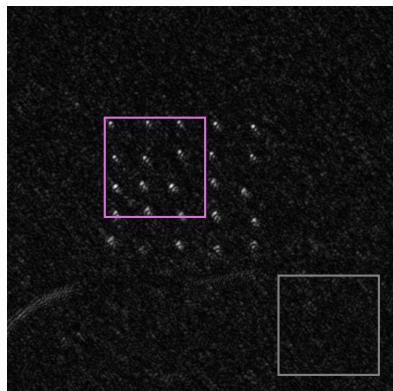
- sample  $115 \times 115$  : target-clutter
- sample  $115 \times 115$  : clutter-clutter

AR output / Estimated pdf

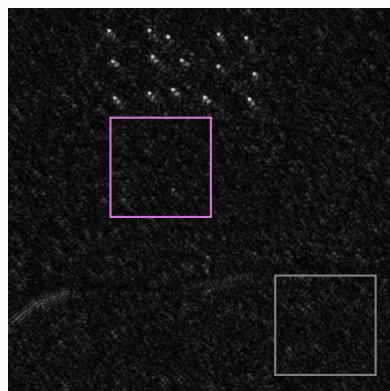


## Step 1: Block size selection

surveillance  $x_t$

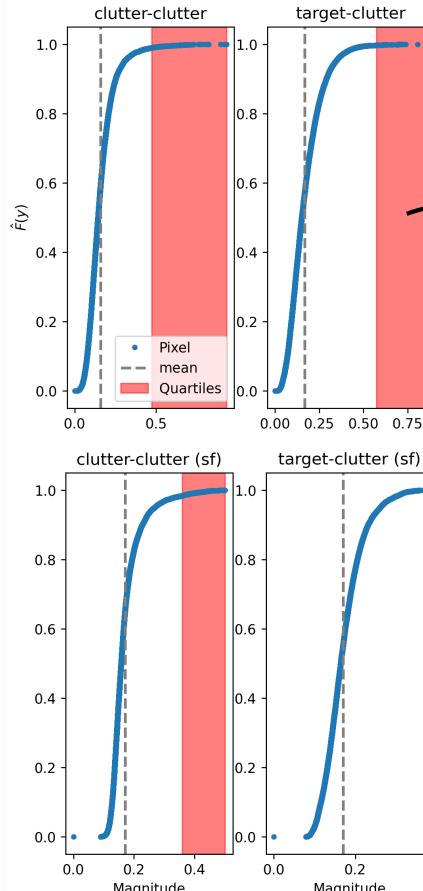


reference  $y_{t-1}$



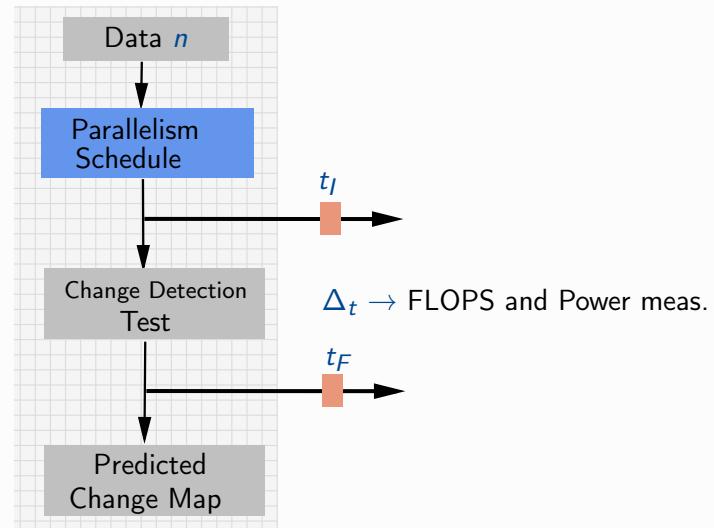
- sample  $115 \times 115$  : target-clutter
- sample  $115 \times 115$  : clutter-clutter

q-ECDF



## Step 2: HW measurements

- Scenarios: Sample dataset 15%
- Tests: [AR(1), GLRT<sup>\*</sup>]
- Analytical block  $N$ : [40,40]
- Parallelism scheduling: [4,8] cores
- Convolution block  $k$ : [9,9].
- Linux-based perfs<sup>9</sup>: htop, powerstat



\*GLRT → generalized likelihood-ratio test for Gaussian Distribution<sup>8</sup>.

---

<sup>8</sup>M. Lundberg, , et al., "A challenge problem for detection of targets in foliage," in Algorithms for Synthetic Aperture Radar Imagery XIII, p. 62370K, May 2006.

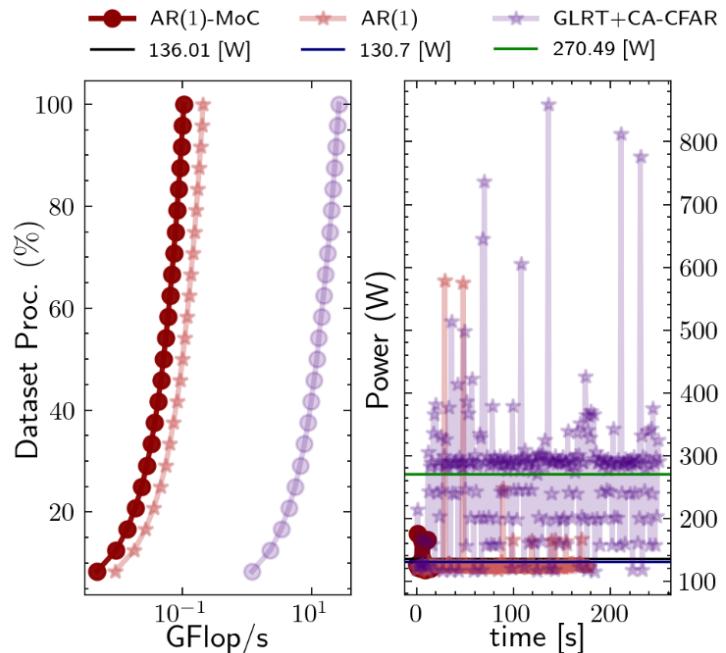
<sup>9</sup>The CPU processor Intel Core i9-12900KF, 16-Core, 24-threads, clock of 3.2 GHz and 32 GB DDR5 of memory.

## Energy-Complexity Performance

Instance	GLRT		2D-AR(1)	
	GLRT	CFAR	sf	q-ECDF
Complexity	$O(N^2)$	$O(N^2K^2)$	$O(N^2k^2)$	$O(N^2 \log N^2)$
Runtime (sec)	8.47	242.60	10.65	7.00

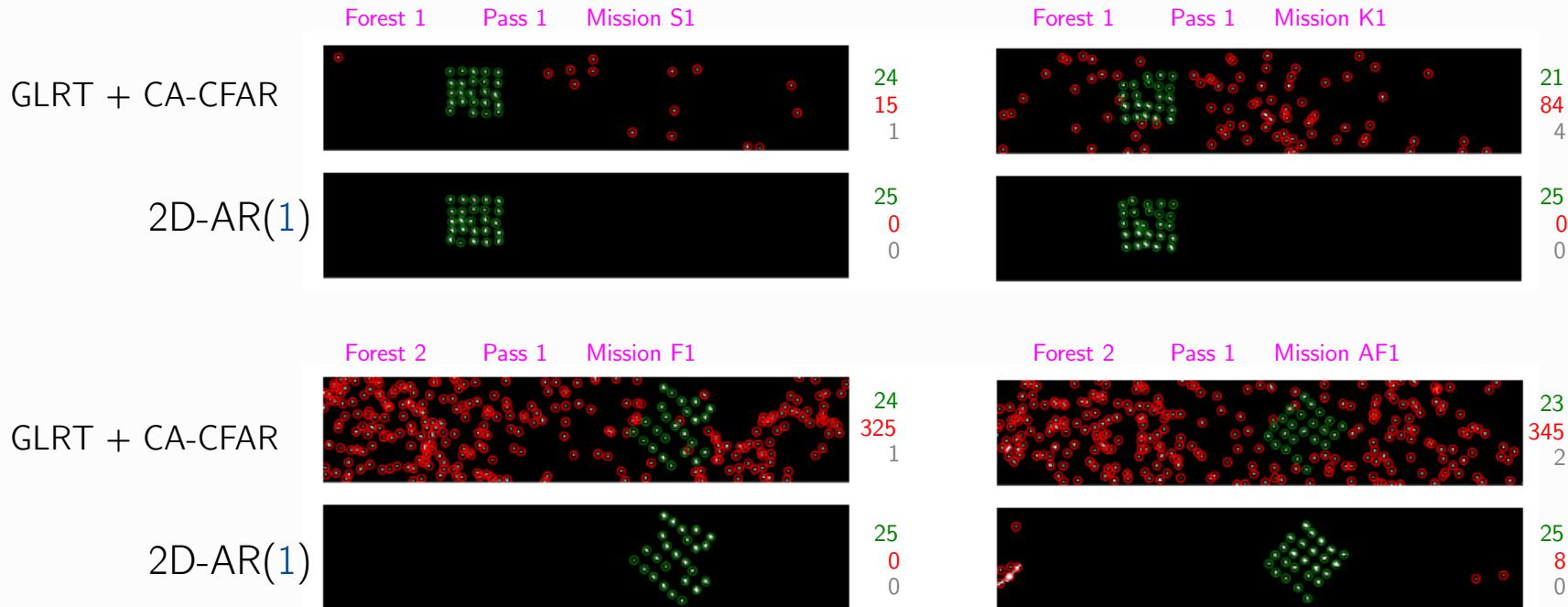
Note: sf = spatial filtering stage with averaging filter.

⇒ GLRT demands 65% additional power consumption by tested pair.

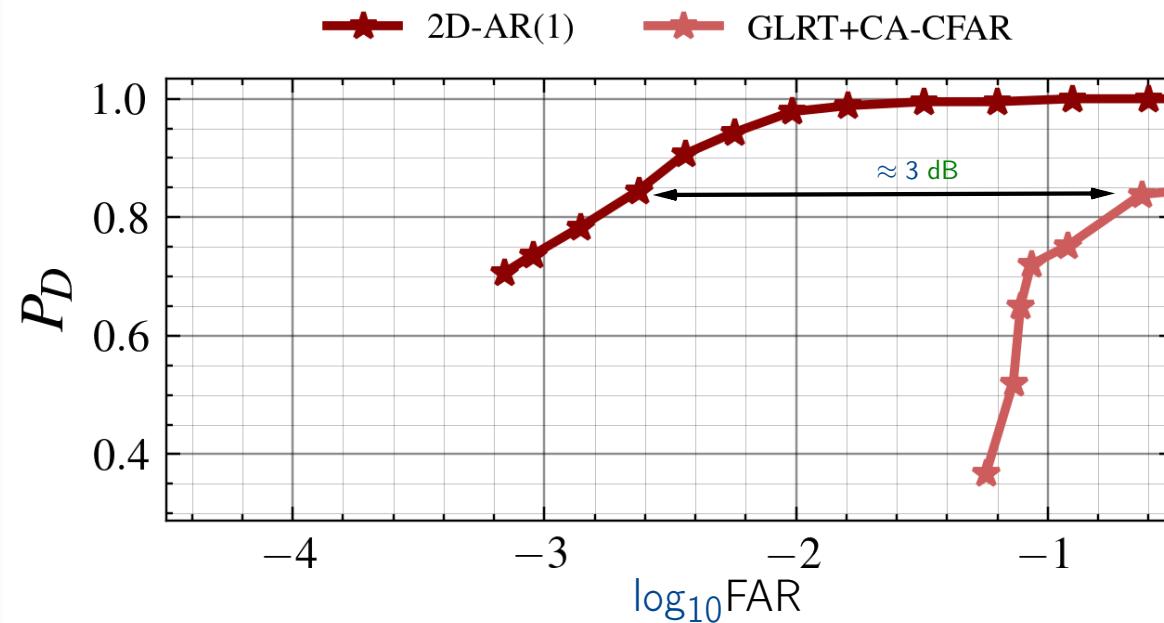


## VHF-UWB SAR Dataset: CARABAS-II

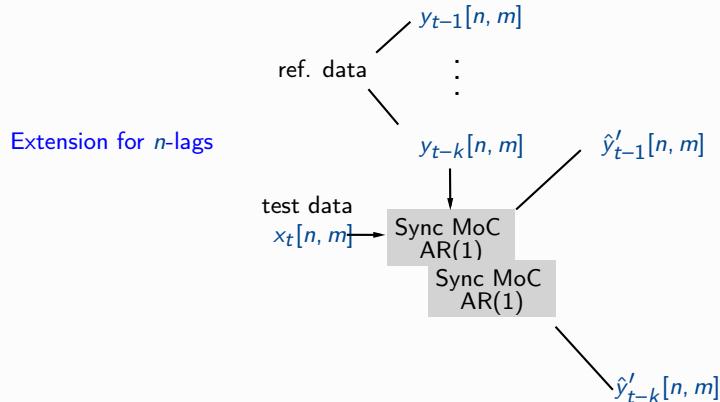
$2 \times 0.5 \text{ km}^2 (15\%)$



### Step 3 - ROC over 24[ $2 \times 3 \text{ km}^2$ (100%)]



- Hardware efforts  $\times$  detection performance are balanced over high-parallelized Sync MoC structure by  $[N, k]$  selection, enabling fast data analysis.
- Extension for a Markov chain in multitemporal ( $n$ -lags) improves the detection performance (considering relevant statistical dependencies), replicating the elementary MoC structure.



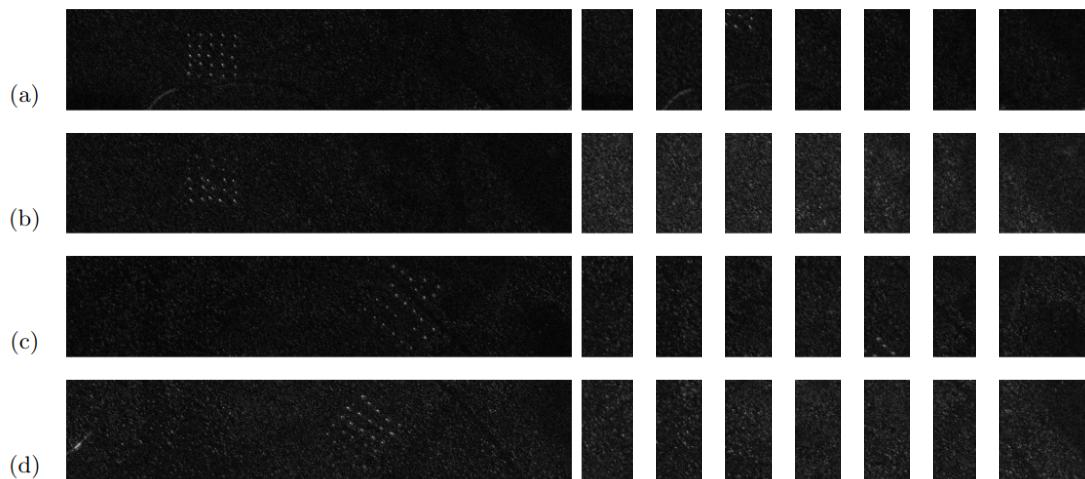
Exp. No.	Surveillance image		Reference image		Known Targets	Area [km <sup>2</sup> ]
	Mission	Pass	Mission	Pass		
1	2	1	3	1	25	6
2	3	1	4	1	25	6
3	4	1	5	1	25	6
4	5	1	2	1	25	6
5	2	2	4	2	25	6
6	3	2	5	2	25	6
7	4	2	2	2	25	6
8	5	2	3	2	25	6
9	2	3	5	3	25	6
10	3	3	2	3	25	6
11	4	3	3	3	25	6
12	5	3	4	3	25	6
13	2	4	3	4	25	6
14	3	4	4	4	25	6
15	4	4	5	4	25	6
16	5	4	2	4	25	6
17	2	5	4	5	25	6
18	3	5	5	5	25	6
19	4	5	2	5	25	6
20	5	5	3	5	25	6
21	2	6	5	6	25	6
22	3	6	2	6	25	6
23	4	6	3	6	25	6
24	5	6	4	6	25	6
Total				600	144	

Include all lags  $y(t-n)$  to improve the prediction model

Campaign sample data:  $2 \times 0.5$  km (15%)

## Surveillance ( $x_t$ )

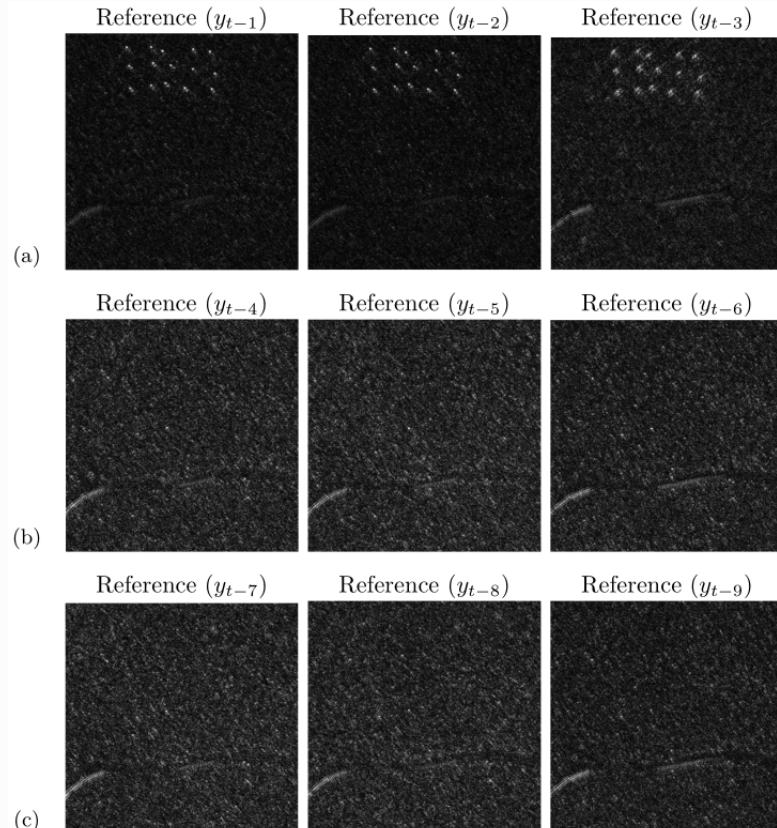
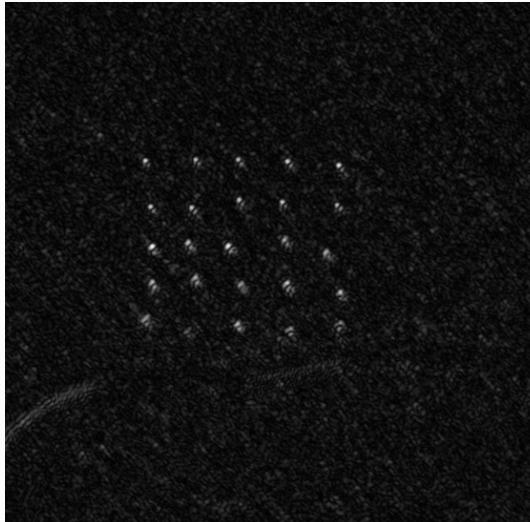
## References ([y<sub>t-n</sub>](#))

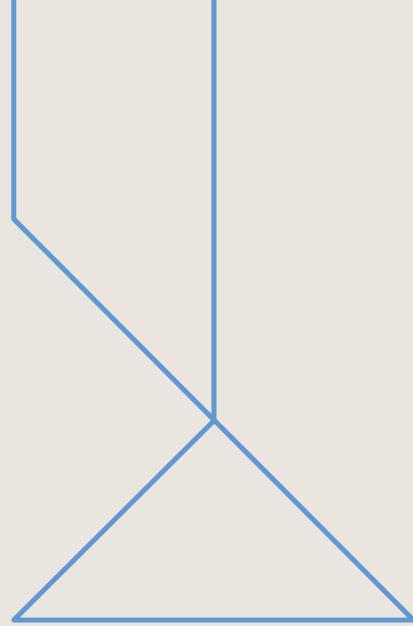


## Extension for $n$ -lags

Statistical sample data:  $0.5 \times 0.5$  km (4%)

Surveillance  $x_t$

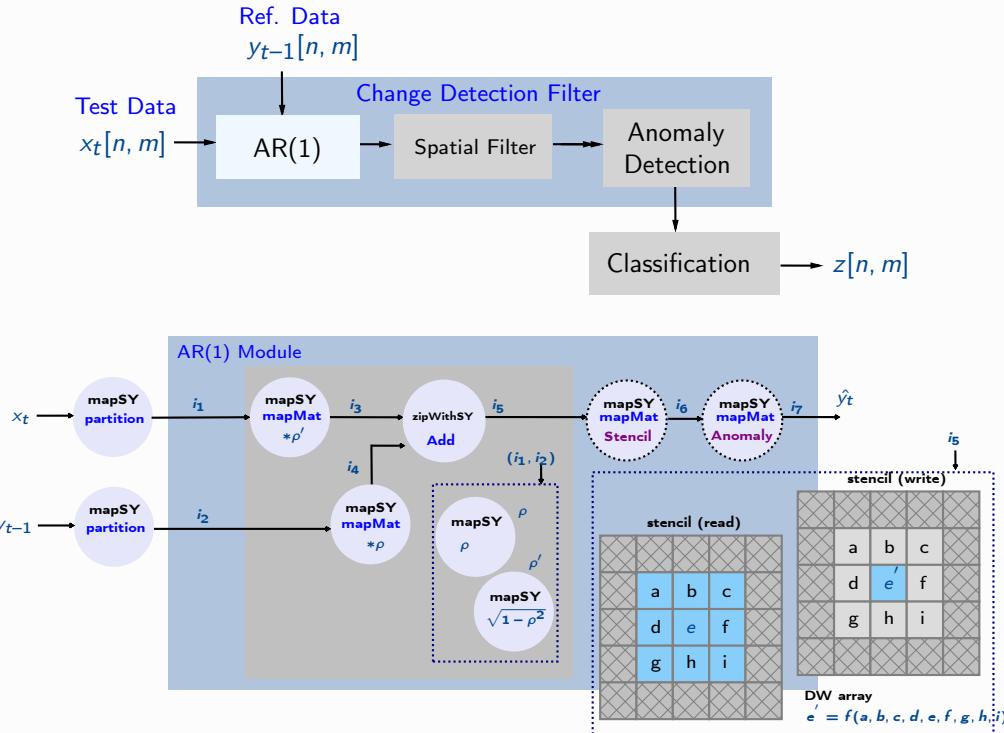




Demo 2: 2D-AR(1) processing on  
ForSyde/Haskell

## Demo 2: 2D-AR(1) processing on ForSyde/Haskell

### Change Detection with AR Model

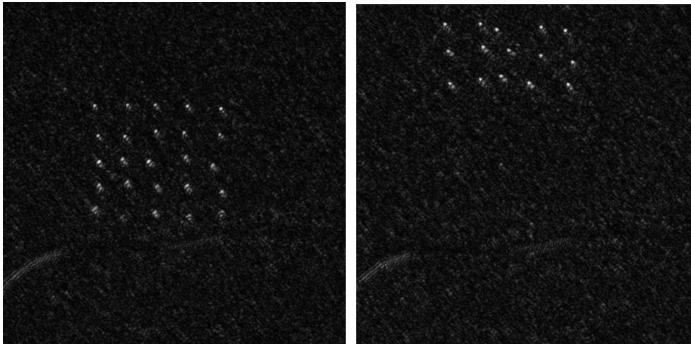


### ► Files

- changeDetection.hs
- classifier.py
- ltesti.dat ( $500 \times 500$ )  
(i=Exp.No.)
- lrefin.dat ( $500 \times 500$ ) (n=lags)
- .mat (known targets position)

## Demo 2: 2D-AR(1) processing on ForSyde/Haskell

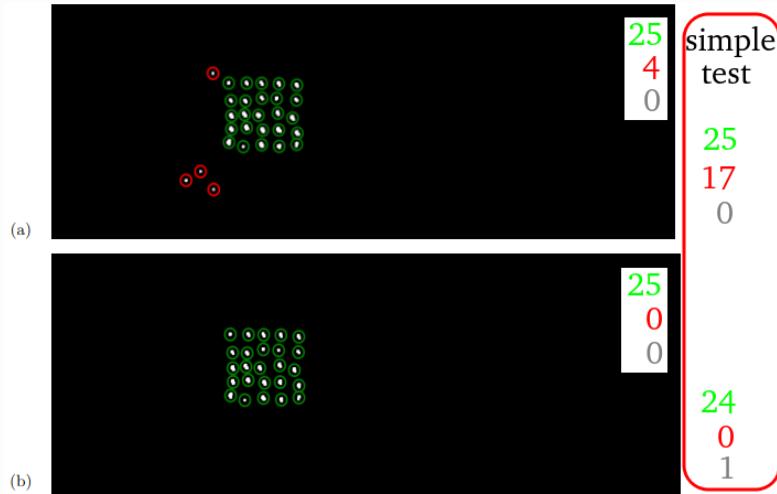
Surveillance ( $t$ ) and Reference ( $t - 1$ )



### Objectives:

- Extend to  $n$ -lags with parallelism
- HW/Detection optimization

Classification Results:



(a) threshold = 0.5, (b) threshold = 0.6

