

CS143 Homework #4

1. a. Total capacity can be found by multiplying the units out.

$$\begin{aligned} & 6 \text{ surfaces} * 10000 \text{ cylinders (or tracks/surface)} * 500 \text{ sectors/track} * \\ & 1024 \text{ bytes/sector} = 30000000 \text{ KB} \\ & = 30000 \text{ MB} \\ & = 30 \text{ GB} \end{aligned}$$

- b. Access Time = Seek Time + Rotational Delay + Transfer Time
= 10 ms + 10/2 ms [since it's average] + 0.02 ms
= 15.02 ms

We need to calculate Transfer Time given:
1/500 track/sector

$$10/500 \text{ ms} = 1/50 \text{ ms} = 0.02 \text{ ms}$$

- c. Each tuple uses $2 + 4 + 4 + 4 + 4 + 4 + 30 + 20 = 72$ bytes
One disk sector or block holds 1024 bytes
Therefore, $1024/72$ (floor) = 14 means a block can hold 14 tuples

We have 1000 tuples to hold.
Therefore, $1000/14$ (ceiling) = 72 means we need 72 disk blocks

- d. In order to run this query for sequential blocks, we need to set disk head, then go through all 72 blocks.

$$\begin{aligned} \text{Time} &= \text{Seek Time} + \text{Rotational Delay} + \text{Transfer Time [all blocks]} \\ &= 10 \text{ ms} + 5 \text{ ms} + 72(0.02 \text{ ms}) \\ &= 16.44 \text{ ms} \end{aligned}$$

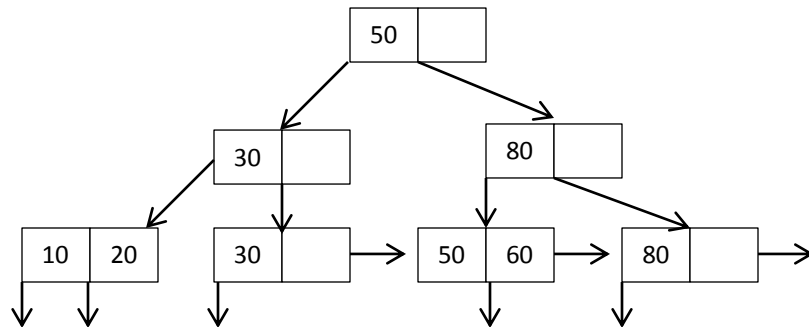
- e. We have to re-seek and rotate through the front of each sequential block for a total of 24 times, then transfer for each of the 3 sequential blocks.

$$\begin{aligned} \text{Time} &= \text{Seek Time} + \text{Rotational Time} + 24 \text{ Transfer Time} + \dots \\ &= 24(10 \text{ ms}) + 24(5 \text{ ms}) + 72(0.02 \text{ ms}) \\ &= 361.44 \text{ ms} \end{aligned}$$

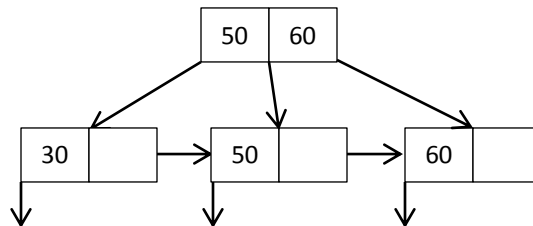
- f. We know the query will return 10 classes. But the B+ tree does not group up our class tuples in the memory, so we are looking at 10 random I/Os rather than the previous sequential I/Os. Therefore, there is no benefit to making a B+ in this case.

$$\begin{aligned} & 10(10 \text{ ms} + 5 \text{ ms} + 0.02 \text{ ms}) \\ & = 150.2 \text{ ms} \end{aligned}$$

2. a. After we insert 60, 20, and 80:



b. After we delete 20, 10, and 70:



3. B+ tree with 300 records and $n=5$; find min/max heights:

Minimum:

Level 1: 4 records

Level 2: $5(4) = 20$ records

Level 3: $5(4)(4) = 80$ records

Level 4: $5(4)(4)(4) = 320$ records

We need a minimum of 4 levels in order to fit 300 records.

Maximum: [both leaf/non-leaf need 3 pointers to prevent underflow]

Level 1: 2 records

Level 2: 6 records

Level 3: 12 records

Level 4: 24

Level 5: 48

Level 6: 96

Level 7: 192

Level 8: 384

We can reach a maximum of 7 levels by having 2 records and 3 pointers in each leaf at the very bottom.

4. We did not cover extendible hash tables in class.