

> #Лабораторная работа 4(Вариант 4)
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> #Задание 1

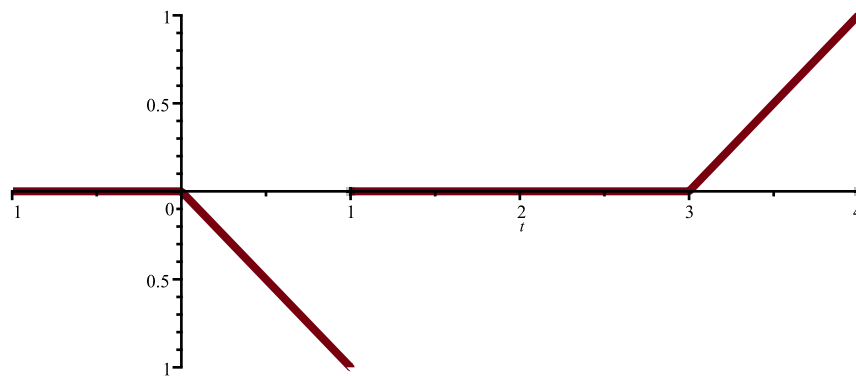
> with(inttrans) :

> $f := \text{piecewise}\left(t < 0, 0, 0 \leq t < a, -\frac{t}{a}, a \leq t < 3 \cdot a, 0, 3 \cdot a \leq t < 4 \cdot a, \frac{1}{a} \cdot t - 3\right)$

$$f := \begin{cases} 0 & t < 0 \\ -\frac{t}{a} & 0 \leq t < a \\ 0 & a \leq t < 3a \\ \frac{t}{a} - 3 & 3a \leq t < 4a \end{cases}$$

(1)

> plot(subs(a=1, f), t=-1..4, discontinuity=true, thickness=3, legend=f)
 # График функции при a=1



	0	$t < 0$
	$-\frac{t}{a}$	$0 \leq t \text{ and } t < a$
	0	$a \leq t \text{ and } t < 3a$
	$\frac{t}{a} - 3$	$3a \leq t \text{ and } t < 4a$

>

> $fp := (t) \cdot \text{Heaviside}(t) - (t-1) \cdot \text{Heaviside}(t-1) + (t-3) \cdot \text{Heaviside}(t-3)$
 $fp := t \text{Heaviside}(t) - t \text{Heaviside}(t-1) + (t-3) \text{Heaviside}(t-3)$

(2)

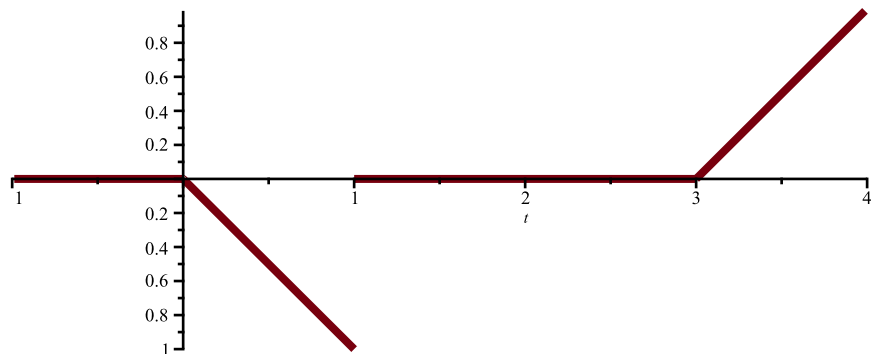
> laplace(fp, t, p) assuming a > 0 ;
 expand(%)

$$\frac{1 + e^{3p} + e^p (p + 1)}{p^2}$$

$$\frac{1}{p^2} + \frac{1}{p^2 (e^p)^3} + \frac{1}{p e^p} + \frac{1}{p^2 e^p}$$

(3)

> plot(fp, t=-1..4, scaling=constrained, thickness=3, legend=fp)



$$t\text{Heaviside}(t) + t\text{Heaviside}(t - 1) + (t - 3)\text{Heaviside}(t - 3)$$

> restart :

> #Задание 2

> with(inttrans) :

$$f := \frac{(p + 5)}{(p + 1) \cdot (p^2 - 2 \cdot p + 5)}$$

$$f := \frac{p + 5}{(p + 1) (p^2 - 2p + 5)} \quad (4)$$

> invlaplace(f, p, t);

$$\frac{e^{-t}}{2} + \frac{(-\cos(2t) + 2\sin(2t))e^t}{2} \quad (5)$$

> restart :

> #Задание 3

$$f := \frac{d^2}{dt^2}y(t) - 2 \frac{d}{dt}y(t) + y(t) = \frac{\exp(t)}{t + 1};$$

$$f := \frac{d^2}{dt^2}y(t) - 2 \frac{d}{dt}y(t) + y(t) = \frac{e^t}{t + 1} \quad (6)$$

> dsolve({f, y(0) = 0, y'(0) = 0});

$$y(t) = e^t (t \ln(t + 1) + \ln(t + 1) - t) \quad (7)$$

> restart :

> #Задание 4

> with(inttrans) :

$$\begin{aligned} &> f := \frac{d^2}{dt^2} y(t) - 2 \cdot \frac{d}{dt} y(t) - 3 \cdot y(t) = \exp(t); \\ &f := \frac{d^2}{dt^2} y(t) - 2 \frac{d}{dt} y(t) - 3 y(t) = e^t \end{aligned} \quad (8)$$

$$\begin{aligned} &> \text{expand}(\text{dsolve}(\{f, y(0) = 1, y'(0) = 1\})); \\ &y(t) = \frac{5 (e^t)^3}{8} + \frac{5}{8 e^t} - \frac{e^t}{4} \end{aligned} \quad (9)$$

> restart :

> #Задание 5

> with(inttrans) :

$$\begin{aligned} &> \text{sys_diff} := \left\{ \frac{d}{dt} x(t) = x(t) + 2 \cdot y(t) + 1, \frac{d}{dt} y(t) = 4 \cdot x(t) - y(t) \right\}; \\ &\text{sys_diff} := \left\{ \frac{d}{dt} x(t) = x(t) + 2 y(t) + 1, \frac{d}{dt} y(t) = 4 x(t) - y(t) \right\} \end{aligned} \quad (10)$$

$$\begin{aligned} &> \text{dsolve}(\{\text{sys_diff}[1], \text{sys_diff}[2], x(0) = 0, y(0) = 1\}); \\ &\left\{ x(t) = \frac{5 e^{3t}}{9} - \frac{4 e^{-3t}}{9} - \frac{1}{9}, y(t) = \frac{5 e^{3t}}{9} + \frac{8 e^{-3t}}{9} - \frac{4}{9} \right\} \end{aligned} \quad (11)$$

> restart :

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