д/з АиЛОВТ Полховский А.Ф. – 950503 Минимизация булевых функций при помощи алгоритма рота

<u>A)</u>

 $L = \{01100, 01110, 10001, 11000, 11011, 01110\}$ $N = \{01000, 10011, 11001, 11010, 10111\}$

Поиск простых импликант.

| C0*C0 | 01100 | 01110 | 10001 | 11000 | 11011 | 01000 | 10011 | 11001 | 11010 | 10111 |
|-------|----------------|-------|----------------|-------|-------------------------|-------|-------|-------|-------|-------|
| 01100 | - | | | | | | | | | |
| 01110 | 011y0 | - | | | | | | | | |
| 10001 | yyy0y | ууууу | 1 | | | | | | | |
| 11000 | y1y00 | y1yy0 | 1y00y | - | | | | | | |
| 11011 | y1yyy | y1y1y | 1y0y1 | 110yy | - | | | | | |
| 01000 | 01y00 | 01yy0 | yy00y | y1000 | y10yy | - | | | | |
| 10011 | ууууу | yyy1y | 100y1 | 1y0yy | 1y011 | yy0yy | - | | | |
| 11001 | y1y0y | y1yyy | 1y001 | 1100y | 110y1 | y100y | 1y0y1 | 1 | | |
| 11010 | y1yy0 | y1y10 | 1y0yy | 110y0 | 1101y | y10y0 | 1y01y | 110yy | - | |
| 10111 | yy1yy | yy11y | 10yy1 | 1yyyy | 1yy11 | ууууу | 10y11 | 1yyy1 | 1yy1y | - |
| A1 | 011x0 01x00 | 1 (/) | 100x1 1x001 | 1100x | 1x011 110x1 1101x | | 10x11 | Ø | Ø | Ø |

 $A1 = \{ 011x0; 01x00; 100x1; 1x001; x1000; 1100x; 110x0; 1x011; 110x1; 1101x; 10x11 \}$ $Z0 = \{ \emptyset \}$ $B1 = \{ 01100; 01110; 10001; 11000; 11011; 01000; 10011; 11001; 11010; 10111 \}$ $C1 = \{ 011x0; 01x00; 100x1; 1x001; x1000; 1100x; 110x0; 1x011; 110x1; 1101x; 10x11 \}$

| C1*C1 | 011x0 | 01x00 | 100x1 | 1x001 | x1000 | 1100x | 110x0 | 1x011 | 110x1 | 1101x | 10x11 |
|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 011x0 | - | | | | | | | | | | |
| 01x00 | 01100 | - | | | | | | | | | |
| 100x1 | уууху | yy00y | - | | | | | | | | |
| 1x001 | | | | | | | | | | | |
| x1000 | • | | | • | | | | | | | |
| 1100x | | | | | | | | | | | |
| 110x0 | - | | | | | | | | | | |
| 1x011 | | | | | | | | | | | |
| 110x1 | | | _ | | | | | | | | |
| 1101x | , | , | • | | • | • | | | | - | |
| 10x11 | yy11y | уухуу | 10011 | 100y1 | 1y0yy | 1y0y1 | 1y01y | 10011 | 1y011 | 1y011 | _ |

| A2 | Ø | Ø | 1x0x1 | 1x0x1 | Ø | 110xx | 110xx | Ø | Ø | Ø | Ø |
|----|---|---|-------|-------|---|-------|-------|---|---|---|---|
| | | | | | | | | | | | |

 $A2 = \{ 1x0x1; 110xx \}$

 $Z1 = \{ 011x0; 01x00; x1000; 10x11 \}$

 $B2 = \{ 100x1; 1x001; 1100x; 110x0; 1x011; 110x1; 1101x \}$

 $C2 = \{ 1x0x1; 110xx \}$

| C2*C2 | 1x0x1 | 110xx |
|-------|-------|-------|
| 1x0x1 | - | |
| 110xx | 110x1 | - |
| A3 | Ø | Ø |

$$A3 = \{ \emptyset \}$$

Конечное множество простых импликант $Z = \{011x0; 01x00; x1000; 10x11; 1x0x1; 110xx\}$

Поиск L-экстремалей.

| z#(Z-z) | 011 | x0 | 01x00 | x100 | 00 | | 10x11 | 1x0x1 | 110xx |
|-------------|-------|-------|-------|-------|-------|----|-------|----------------|----------------|
| 011x0 | - | | 01000 | x100 | 00 | - | 10x11 | 1x0x1 | 110xx |
| 01x00 | 011 | 10 | - | 1100 | 00 | - | 10x11 | 1x0x1 | 110xx |
| x1000 | 011 | 10 | Ø | - | | | 10x11 | 1x0x1 | 1101x 110x1 |
| 10x11 | 011 | 10 | Ø | 1100 | 00 | | - | 110x1 1x001 | 1101x 110x1 |
| 1x0x1 | 011 | 10 | Ø | 1100 | 11000 | | 10111 | - | 11010 |
| 110xx | 011 | 10 | Ø | Ø | Ø | | 10111 | 10001 | - |
| Остаток | 011 | 10 | Ø | Ø | | , | 10111 | 10001 | 11010 |
| z#(Z-z) n L | 01100 | 01110 | 10001 | 11000 | 110 | 11 | 01110 | | |
| 01110 | Ø | 01110 | Ø | Ø | Q |) | 01110 | | |
| 10111 | Ø | Ø | Ø | Ø | Q |) | Ø | | |
| 10001 | Ø | Ø | 10001 | Ø | Q |) | Ø | | |
| 11010 | Ø | Ø | Ø | Ø | Q |) | Ø | | |

Множество L-экстремалей $E = \{ 011x0; 1x0x1 \}$

$$Z' = Z - E = \{ 01x00; x1000; 10x11; 110xx \}$$

| L#E | 01100 | 01110 | 10001 | 11000 | 11011 | 01110 |
|---------|-------|-------|-------|-------|-------|-------|
| 011x0 | Ø | Ø | 10001 | 11000 | 11011 | Ø |
| 1x0x1 | Ø | Ø | Ø | 11000 | Ø | Ø |
| Остаток | Ø | Ø | Ø | 11000 | Ø | Ø |

Множество кубов, непокрытых L-экстремалями, $L' = \{ 11000 \}$

| Z'i n L' | 11000 |
|----------|-------|
| 01x00 | Ø |
| x1000 | 11000 |
| 10x11 | Ø |
| 110xx | 11000 |

Тупиковые формы:

<u>Б)</u>

$$L = \{\ 0000,\ 0010,\ 0110,\ 1101,\ 1011,\ 1001)$$

$$N = \{\ \varnothing\ \}$$

Поиск простых импликант.

| C0*C0 | 0000 | 0010 | 0110 | 1101 | 1011 | 1001 |
|-------|------|------|------|------|------|------|
| 0000 | - | | | | | |
| 0010 | 00y0 | - | | | | |
| 0110 | 0yy0 | 0y10 | - | | | |
| 1101 | yy0y | уууу | y1yy | - | | |
| 1011 | y0yy | y01y | yy1y | 1yy1 | - | |
| 1001 | y00y | y0yy | уууу | 1y01 | 10y1 | - |
| A1 | 00x0 | 0x10 | Ø | 1x01 | 10x1 | Ø |

```
A1 = { 00x0; 0x10; 1x01; 10x1 }
Z0 = { \emptyset }
B1 = { 0000; 0010; 0110; 1101; 1011; 1001 }
C1 = { <math>00x0; 0x10; 1x01; 10x1 }
```

| C1*C1 | 00x0 | 0x10 | 1x01 | 10x1 |
|-------|------|------|------|------|
| 00x0 | - | | | |
| 0x10 | 0010 | - | | |
| 1x01 | y00y | ухуу | - | |
| 10x1 | y0xy | y01y | 1001 | - |

| 4.0 | α | α | α | α |
|-----|----------|----------|----------|----------|
| AZ | Ø | Ø | Ø | Ø |
| | | | | |

$$A2 = \{ \emptyset \}$$

Конечное множество простых импликант $Z = \{00x0; 0x10; 1x01; 10x1\}$

Поиск L-экстремалей.

| z#(Z-z) | | 00x0 | | 0x10 | 1: | x01 | 10x1 |
|---------------------|------|------|-----------|-------------|-----------|-----------|------|
| 00x0 | | | | 0110 | 1: | x01 | 10x1 |
| 0x10 | | 0000 | | - | 1: | x01 | 10x1 |
| 1x01 | | 0000 | | 0110 | | - | 1011 |
| 10x1 | | 0000 | | 0110 | 1: | x01 | - |
| Остаток | | 0000 | | 0110 | 1: | x01 | 1011 |
| | | | | | | | |
| z#(Z-z) n L | 0000 | 0010 | 0110 | 0 1101 | 1011 | 1001 | |
| z#(Z-z) n L 0000 | 0000 | | 0110 Ø | 0 1101 Ø | 1011 Ø | 1001 Ø | |
| | | | | Ø | | | |
| 0000 | 0000 | Ø | Ø | Ø | Ø | Ø | |

Множество L-экстремалей $E = \{00x0; 0x10; 1x01; 10x1\}$

$$Z' = Z - E = \{ \emptyset \}$$

Минимальное покрытие - множество L-экстремалей $E = \{00x0; 0x10; 1x01; 10x1\}$

Тупиковые формы:

Fmin = $\{00x0, 0x10, 1x01, 10x1\}$

<u>B)</u>

$$L = \{110x, 0x01, 0010, 1010\}$$

$$N = \{0x11, 1000, x111\}$$

Поиск простых импликант.

| C0*C0 | 110x | 0x01 | 0010 | 1010 | 0x11 | 1000 | x111 |
|-------|------|------|------|------|------|------|------|
| 110x | - | | | | | | |
| 0x01 | y101 | - | | | | | |
| 0010 | yyy0 | ООуу | - | | | | |
| 1010 | 1yy0 | y0yy | y010 | - | | | |
| 0x11 | y1y1 | 0xy1 | 001y | y01y | - | | |

| 1000 | 1y00 | y00y | y0y0 | 10y0 | y0yy | - | |
|------|----------------------|--------------|--------------|------|------|------|---|
| x111 | 11y1 | 01y1 | 0y1y | 1y1y | 0111 | 1yyy | - |
| A1 | x101 1x00 11x1 | 0xx1 01x1 | x010 001x | 10x0 | Ø | Ø | Ø |

 $A1 = \{ x101; 1x00; 11x1; 0xx1; x010; 001x; 10x0 \}$

 $Z0 = \{ \emptyset \}$

 $B1 = \{ 110x; 0x01; 0010; 1010; 0x11; 1000; x111 \}$

 $C1 = \{ \ x101; \ 1x00; \ 11x1; \ 0xx1; \ x010; \ 001x; \ 10x0; \ 110x; \ x111 \ \}$

| C1*C1 | x101 | 1x00 | 11x1 | 0xx1 | x010 | 001x | 10x0 |
|-------|------|------|------|------|------|------|------|
| x101 | - | | | | | | |
| 1x00 | 110y | - | | | | | |
| 11x1 | 1101 | 110y | - | | | | |
| 0xx1 | 0101 | yx0y | y1x1 | - | | | |
| x010 | xyyy | 10y0 | 1y1y | 001y | - | | |
| 001x | 0yy1 | y0y0 | yy11 | 0011 | 0010 | - | |
| 10x0 | 1y0y | 1000 | 1yxy | y0xy | 1010 | y010 | - |
| 110x | 1101 | 1100 | 1101 | y101 | 1yy0 | ууух | 1y00 |
| x111 | x1y1 | 11yy | 1111 | 0111 | xy1y | 0y11 | 1y1y |
| A2 | x1x1 | Ø | x1x1 | Ø | Ø | Ø | Ø |

 $A2 = \{ x1x1 \}$

 $Z1 = \{ 1x00; x010; 001x; 10x0; 110x \}$

 $B2 = \{ x101; 11x1; 0xx1; x111 \}$

 $C2 = \{ x1x1; 0xx1 \}$

| C2*C2 | x1x1 |
|-------|------|
| x1x1 | - |
| 0xx1 | 01x1 |
| A3 | Ø |

$$A3 = \{ \emptyset \}$$

Конечное множество простых импликант $Z = \{1x00; x010; 001x; 10x0; 110x; x1x1; 0xx1\}$

Поиск L-экстремалей.

| z#(Z-z) | 1x00 | x010 | 001x | 10x0 | 110x | x1x1 | 0xx1 |
|-------------|------|--------|------|------|------|--------------|--------------|
| 1x00 | - | x010 | 001x | 1010 | 1101 | x1x1 | 0xx1 |
| x010 | 1x00 | - | 0011 | Ø | 1101 | x1x1 | 0xx1 |
| 001x | 1x00 | 1010 | - | Ø | 1101 | x1x1 | 01x1 0x01 |
| 10x0 | 1100 | Ø | 0011 | 1 | 1101 | x1x1 | 01x1 0x01 |
| 110x | Ø | Ø | 0011 | Ø | - | 01x1 x111 | 01x1 0x01 |
| x1x1 | Ø | Ø | 0011 | Ø | Ø | - | 0001 |
| 0xx1 | Ø | Ø | Ø | Ø | Ø | 1111 | - |
| Остаток | Ø | Ø | Ø | Ø | Ø | 1111 | 0001 |
| z#(Z-z) n L | 110 | x 0x01 | 0010 | 1010 | | | |
| 1111 | Ø | Ø | Ø | Ø | | | |
| 0001 | Ø | 0001 | Ø | Ø | | | |

Множество L-экстремалей $E = \{ 0xx1 \}$

 $Z' = Z - E = \{ 1x00; x010; 001x; 10x0; 110x; x1x1 \}$

| L#E | 110x | 0x01 | 0010 | 1010 |
|---------|------|------|------|------|
| 0xx1 | 110x | Ø | 0010 | 1010 |
| Остаток | 110x | Ø | 0010 | 1010 |

Множество кубов, не покрываемых L-экстремалями, $L' = L \# E = \{ 110x; 0010; 1010 \}$

| Z'i n L' | 110x | 0010 | 1010 |
|----------|------|------|------|
| 1x00 | 1100 | Ø | Ø |
| x010 | Ø | 0010 | 1010 |
| 001x | Ø | 0010 | Ø |
| 10x0 | Ø | Ø | 1010 |
| 110x | 110x | Ø | Ø |
| x1x1 | 1101 | Ø | Ø |

Тупиковые формы:

 $Fmin1 = \{ x010; 110x; 0xx1 \}$

```
L = \{ 0001, 0100, 1100, 1101, 1010, 0010 \} N = \{ 0101, 0111, 0110 \}
```

Поиск простых импликант.

| C0*C0 | 0001 | 0100 | 1100 | 1101 | 1010 | 0010 | 0101 | 0111 | 0110 |
|-------|------|----------------------|------|------|------|------|------|------|------|
| 0001 | - | | | | | | | | |
| 0100 | 0y0y | - | | | | | | | |
| 1100 | yy0y | y100 | - | | | | | | |
| 1101 | yy01 | y10y | 110y | - | | | | | |
| 1010 | y0yy | yyy0 | 1yy0 | 1yyy | _ | | | | |
| 0010 | 00yy | 0yy0 | yyy0 | уууу | y010 | - | | | |
| 0101 | 0y01 | 010y | y10y | y101 | уууу | Оууу | - | | |
| 0111 | 0yy1 | 01yy | y1yy | y1y1 | yy1y | 0y1y | 01y1 | - | |
| 0110 | Оууу | 01y0 | y1y0 | y1yy | yy10 | 0y10 | 01yy | 011y | - |
| A1 | 0x01 | x100 010x 01x0 | 110x | x101 | x010 | 0x10 | 01x1 | 011x | Ø |

```
A1 = \{ 0x01; x100; 010x; 01x0; 110x; x101; x010; 0x10; 01x1; 011x \} Z0 = \{ \emptyset \} B1 = \{ 0001; 0100; 1100; 1101; 1010; 0010; 0101; 0111; 0110 \} C1 = \{ 0x01; x100; 010x; 01x0; 110x; x101; x010; 0x10; 01x1; 011x \}
```

| C1*C1 | 0x01 | x100 | 010x | 01x0 | 110x | x101 | x010 | 0x10 | 01x1 | 011x |
|-------|------|------|--------------|------|------|------|------|------|------|------|
| 0x01 | - | | | | | | | | | |
| x100 | 010y | - | | | | | | | | |
| 010x | 0101 | 0100 | _ | | | | | | | |
| 01x0 | 010y | 0100 | 0100 | 1 | | | | | | |
| 110x | y101 | 1100 | y10x | y100 | 1 | | | | | |
| x101 | 0101 | x10y | 0101 | 010y | 1101 | - | | | | |
| x010 | 00yy | xyy0 | 0yy0 | 0y10 | 1yy0 | xyyy | - | | | |
| 0x10 | 0xyy | 01y0 | 01y0 | 0110 | y1y0 | 01yy | 0010 | _ | | |
| 01x1 | 0101 | 010y | 0101 | 01xy | y101 | 0101 | 0y1y | 011y | _ | |
| 011x | 01y1 | 01y0 | 01yx | 0110 | y1yx | 01y1 | 0y10 | 0110 | 0111 | - |
| A2 | Ø | x10x | x10x 01xx | 01xx | Ø | Ø | Ø | Ø | Ø | Ø |

```
A2 = \{ x10x; 01xx \}
Z1 = \{ 0x01; x010; 0x10 \}
```

 $B2 = \{ x100; 010x; 01x0; 110x; x101; 01x1; 011x \}$ $C2 = \{ x10x; 01xx \}$

| C2*C2 | x10x | 01xx |
|-------|------|------|
| x10x | - | |
| 01xx | 010x | - |
| A3 | Ø | Ø |

$$A3 = \{ \emptyset \}$$

Конечное множество простых импликант $Z = \{0x01; x010; 0x10; x10x; 01xx\}$

Поиск L-экстремалей.

| z#(Z-z) | 0x0 | 01 | x010 | 0x1 | .0 | x10x | 01xx |
|-------------|------|------|--------|------|------|--------------|--------------|
| 0x01 | - | | x010 | 0x1 | .0 | 110x x100 | 011x 01x0 |
| x010 | 0x | 01 | 1 - | | .0 | 110x x100 | 011x 01x0 |
| 0x10 | 0x0 | 01 | 1010 - | | | 110x x100 | 0111 0100 |
| x10x | 00 | 01 | 1010 | 011 | .0 | - | 0111 |
| 01xx | 000 | 01 | 1010 | Ø | | 110x 1100 | - |
| Остаток | 000 | 01 | 1010 | Ø | | 110x 1100 | 0111 |
| z#(Z-z) n L | 0001 | 0100 | 0 1100 | 1101 | 1010 | 0010 | |
| 0001 | 0001 | Ø | Ø | Ø | Ø | Ø |] |
| 1010 | Ø | Ø | Ø | Ø | 1010 |) Ø | |
| 110x | Ø | Ø | 1100 | 1101 | Ø | Ø | |
| 1100 | Ø | Ø | 1100 | Ø | Ø | Ø | |
| 0111 | Ø | Ø | Ø | Ø | Ø | Ø | |

Множество L-экстремалей $E = \{ 0x01; x010; x10x \}$

$$Z' = Z - E = \{ 0x10; 01xx \}$$

| L#E | 0001 | 0100 | 1100 | 1101 | 1010 | 0010 |
|---------|------|------|------|------|------|------|
| 0x01 | Ø | 0100 | 1100 | 1101 | 1010 | 0010 |
| x010 | Ø | 0100 | 1100 | 1101 | Ø | Ø |
| x10x | Ø | Ø | Ø | Ø | Ø | Ø |
| Остаток | Ø | Ø | Ø | Ø | Ø | Ø |

Минимальное покрытие - множество L-экстремалей $E = \{ 0x01; x010; x10x \}$

Тупиковые формы:

 $Fmin1 = \{ 0x01, x010, x10x \}$