

1 Distributions

| Distribution | Moments | Bernoulli | Binomial | Geometric | Poisson | Exponential | Uniform | Normal |
|--------------|---|------------------|------------------------------|-------------------|-------------------------------------|--|----------------------|--|
| PDF | | $p^x(1-p)^{1-x}$ | $\binom{n}{x}p^x(1-p)^{n-x}$ | $(1-p)^{x-1}p$ | $e^{-\lambda} \frac{\lambda^x}{x!}$ | $\frac{1}{\lambda} e^{-\frac{x}{\lambda}}$ | $\frac{1}{b-a}$ | $\frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$ |
| E[X] | $\bar{X} = \frac{1}{n} \sum_{i=1}^n X_i$ | p | np | $\frac{1}{p}$ | λ | λ | $\frac{a+b}{2}$ | μ |
| Var[X] | $E[X^2] = \frac{1}{n} \sum_{i=1}^n (X_i - \bar{X})^2$ | $p(1-p)$ | $np(1-p)$ | $\frac{1-p}{p^2}$ | λ | λ^2 | $\frac{(b-a)^2}{12}$ | σ^2 |

2 Hypothesis Testing

| H ₀ | H _A | Conditions | Test Statistic | Rejection Region | Degrees of freedom |
|-----------------|--|---|--|--|----------------------|
| $\mu_1 = \mu_2$ | $\mu_1 < \mu_2$ $\mu_1 > \mu_2$ $\mu_1 \neq \mu_2$ | Known σ | $Z = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$ | $Z < -z_\alpha$ $Z > z_\alpha$ $ Z > z_{\alpha/2} $ | |
| $\mu_1 = \mu_2$ | $\mu_1 < \mu_2$ $\mu_1 > \mu_2$ $\mu_1 \neq \mu_2$ | Unknown but equal σ $s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2$ $s_p^2 = \frac{(n_1-1)s_1^2 + (n_2-1)s_2^2}{n_1+n_2-2}$ | $t = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{s_p^2 (\frac{1}{n_1} + \frac{1}{n_2})}}$ | $t < -t_{df,\alpha}$ $t > t_{df,\alpha}$ $ t > t_{df,\alpha/2} $ | df = $n_1 + n_2 - 2$ |
| $\pi_1 = \pi_2$ | $\pi_1 < \pi_2$ $\pi_1 > \pi_2$ $\pi_1 \neq \pi_2$ | Z-test for proportions | $Z = \frac{(\hat{\pi}_1 - \hat{\pi}_2) - (\pi_1 - \pi_2)}{\sqrt{\frac{\hat{\pi}_1(1-\hat{\pi}_1)}{n_1} + \frac{\hat{\pi}_2(1-\hat{\pi}_2)}{n_2}}}$ | $Z < -z_\alpha$ $Z > z_\alpha$ $ Z > z_{\alpha/2} $ | |
| $\beta_1 = 0$ | $\beta_1 \neq 0$ | Test for linear relationship | $t = \frac{\hat{\beta}_1 - \beta_1}{\sqrt{\frac{s^2}{S_{xx}}}}$ | $t > t_{df,\alpha/2} $ | df = $n - 2$ |

3 Linear Regression Formulas

$$\hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x} \quad (1)$$

$$\hat{\beta}_1 = \frac{S_{xy}}{S_{xx}} \quad (2)$$

$$S_{xx} = \sum_{i=1}^n (x_i - \bar{x})^2 \quad (3)$$

$$S_{xy} = \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y}) \quad (4)$$

$$SS_{RESID} = \sum_{i=1}^n (y_i - \hat{y})^2 \quad (5)$$

$$RegressionVariance : s^2 = \frac{SS_{RESID}}{n-2} \quad (6)$$

$$NormalEquations : \begin{cases} \sum_{i=1}^n (y_i - \beta_0 - \beta_1 x_i) = 0 \\ \sum_{i=1}^n x_i (y_i - \beta_0 - \beta_1 x_i) = 0 \end{cases} \quad (7)$$