

QPM Model

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1:      % -----
2:      % ----- Quarterly Projection Model (QPM) -----
3:      %
4:
5:      %
6:      !transition_variables
7:      'Real GDP (100*log)'                                L_GDP
8:      'Trend in Real GDP (100*log)'                      L_GDP_BAR
9:      'Output Gap (in %)'                                L_GDP_GAP
10:     'Quarterly Growth in Real GDP annualized (in % pa)' DLA_GDP
11:     'Real GDP Growth YoY (in % pa)'                   D4L_GDP
12:     'Real GDP Trend Growth QoQ annualized (in % pa)'  DLA_GDP_BAR
13:
14:     'Real Monetary Condition Index (in % pa)'          MCI
15:
16:     'CPI (level, 100*log)'                             L_CPI
17:     'CPI Inflation QoQ annualized (in % pa)'          DLA_CPI
18:     'Expected CPI Inflation QoQ annualized (in % pa)' E_DLA_CPI
19:     'CPI Inflation YoY (in % pa)'                     D4L_CPI
20:     'Inflation Target (in % pa)'                      D4L_CPI_TAR
21:
22:     'Real Marginal Cost (in %)'                        RMC
23:
24:     'Nominal Exchange Rate (LCY/FCY, 100*log)'        L_S
25:     'Nominal Exch. Rate Depreciation QoQ annualized (in % pa)' DLA_S
26:     'Nominal Exch. Rate Depreciation YoY (in % pa)'   D4L_S
27:     'Country Risk Premium (in % pa)'                  PREM
28:
29:     'Nominal Policy Interest Rate (in % pa)'          RS
30:     'Real Interest Rate (in % pa)'                   RR
31:     'Trend Real Interest Rate (in % pa)'             RR_BAR
32:     'Real Interest Rate Gap (in %)'                 RR_GAP
33:     'Nominal Policy Neutral Interest Rate (in % pa)' RSNEUTRAL
34:
35:     'Real Exchange Rate (level, 100*log)'            L_Z
36:     'Trend Real Exchange Rate (level, 100*log)'      L_Z_BAR
37:     'Real Exchange Rate Gap (in %)'                  L_Z_GAP
38:     'Real Exchange Rate Depreciation QoQ annualized (in % pa)' DLA_Z
39:     'Trend Real Exchange Rate Depreciation QoQ annualized (in % pa)' DLA_Z_BAR
40:
41:     'Foreign Output Gap (in %)'                      L_GDP_RW_GAP
42:     'Foreign Nominal Interest Rate (in % pa)'        RS_RW
43:     'Foreign Real Interest Rate (in % pa)'           RR_RW
44:     'Foreign Real Interest Rate Trend (in % pa)'    RR_RW_BAR
45:     'Foreign Real Interest Rate Gap (in %)'         RR_RW_GAP
46:     'Foreign CPI (level, 100*log)'                   L_CPI_RW
47:     'Foreign Inflation QoQ annualized (in % pa)'    DLA_CPI_RW
48:
49:     %
50:     !transition_shocks
51:     'Shock: Output gap (demand)'                    SHK_L_GDP_GAP ( $\sigma=1$ )
52:     'Shock: CPI inflation (cost-push)'              SHK_DLA_CPI ( $\sigma=0.75$ )
53:     'Shock: Exchange rate (UIP)'                   SHK_L_S ( $\sigma=3$ )
54:     'Shock: Interest rate (monetary policy)'       SHK_RS ( $\sigma=1$ )
55:     'Shock: Inflation target'                      SHK_D4L_CPI_TAR ( $\sigma=2$ )
56:

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57:   'Shock: Real interest rate'           SHK_RR_BAR ( $\sigma=0.5$ )
58:   'Shock: Real exchange rate depreciation' SHK_DLA_Z_BAR ( $\sigma=0.5$ )
59:   'Shock: Potential GDP growth'        SHK_DLA_GDP_BAR ( $\sigma=0.5$ )
60:
61:   'Shock: Foreign output gap'          SHK_L_GDP_RW_GAP ( $\sigma=1$ )
62:   'Shock: Foreign nominal interest rate' SHK_RS_RW ( $\sigma=1$ )
63:   'Shock: Foreign inflation'          SHK_DLA_CPI_RW ( $\sigma=2$ )
64:   'Shock: Foreign real interest rate' SHK_RR_RW_BAR ( $\sigma=0.5$ )
65:
66:   % -----
67: !parameters
68: % --- Structural coefficients ---
69: b1(0.8) b2(0.3) b3(0.5) b4(0.7)
70: a1(0.7) a2(0.2) a3(0.7)
71: e1(0.4)
72: g1(0.7) g2(0.5) g3(0.5)
73:
74: % --- AR Processes ---
75: rho_D4L_CPI_TAR(0.5)
76: rho_DLA_Z_BAR(0.8)
77: rho_RR_BAR(0.8)
78: rho_DLA_GDP_BAR(0.8)
79:
80: rho_L_GDP_RW_GAP(0.8)
81: rho_RS_RW(0.8)
82: rho_DLA_CPI_RW(0.8)
83: rho_RR_RW_BAR(0.8)
84:
85: % --- Steady State Parameters ---
86: ss_D4L_CPI_TAR(2)
87: ss_DLA_Z_BAR(-1.5)
88: ss_RR_BAR(0.5)
89: ss_DLA_GDP_BAR(2.5)
90: ss_DLA_CPI_RW(2)
91: ss_RR_RW_BAR(0.75)
92:
93:   % -----
94: !transition_equations
95: %% === IS Curve ===
96: L_GDP_GAP = b1(0.8)*L_GDP_GAP{-1} - b2(0.3)*MCI + b3(0.5)*L_GDP_RW_GAP + SHK_L_GDP_GAP ( $\sigma=1$ );
97: MCI      = b4(0.7)*RR_GAP + (1-b4(0.7))*(-L_Z_GAP);
98:
99: %% === Phillips Curve ===
100: DLA_CPI    = a1(0.7)*DLA_CPI{-1} + (1-a1(0.7))*DLA_CPI{+1} + a2(0.2)*RMC + SHK_DLA_CPI ( $\sigma=0.75$ );
101: RMC       = a3(0.7)*L_GDP_GAP + (1-a3(0.7))*L_Z_GAP;
102: E_DLA_CPI = DLA_CPI{+1};
103:
104: %% === Monetary Policy Reaction Function (a forward-looking Taylor-type Rule) ===
105: RS         = g1(0.7)*RS{-1} + (1-g1(0.7))*(RSNEUTRAL + g2(0.5)*(D4L_CPI{+4} - D4L_CPI_TAR{+4}) + g3(0.5)*L_GDP_GAP) +
SHK_RS ( $\sigma=1$ );
106: RSNEUTRAL = RR_BAR + D4L_CPI{+1};
107:
108: %% === Modified UIP condition ===
109: L_S = (1-e1(0.4))*L_S{+1} + e1(0.4)*(L_S{-1} + 2/4*(D4L_CPI_TAR - ss_DLA_CPI_RW(2) + DLA_Z_BAR)) + (-RS + RS_RW + PREM)/4 +
SHK_L_S ( $\sigma=3$ );
110:
111: %% === Definitions ===
112: % Fisher equation (RIR)

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113:     RR           = RS - D4L_CPI{+1};
114:     L_Z          = L_S + L_CPI_RW - L_CPI;
115: % Long-term version of UIP (consistency of trends)
116: DLA_Z_BAR{+1} = RR_BAR - RR_RW_BAR - PREM;
117:
118: %% === Identities ===
119: DLA_GDP_BAR = 4*(L_GDP_BAR - L_GDP_BAR{-1});
120: DLA_Z_BAR   = 4*(L_Z_BAR - L_Z_BAR{-1});
121: DLA_Z       = 4*(L_Z - L_Z{-1});
122: DLA_GDP     = 4*(L_GDP - L_GDP{-1});
123: DLA_CPI     = 4*(L_CPI - L_CPI{-1});
124: DLA_S        = 4*(L_S - L_S{-1});
125: D4L_GDP     = L_GDP - L_GDP{-4};
126: D4L_CPI     = L_CPI - L_CPI{-4};
127: D4L_S        = L_S - L_S{-4};
128:
129: %% === Gaps ===
130: RR_GAP      = RR - RR_BAR;
131: L_Z_GAP     = L_Z - L_Z_BAR;
132: L_GDP_GAP   = L_GDP - L_GDP_BAR;
133:
134: %% === Trends ===
135: D4L_CPI_TAR = rho_D4L_CPI_TAR(0.5)*D4L_CPI_TAR{-1} + (1-rho_D4L_CPI_TAR(0.5))*ss_D4L_CPI_TAR(2) + SHK_D4L_CPI_TAR( $\sigma=2$ );
136: DLA_Z_BAR   = rho_DLA_Z_BAR(0.8)*DLA_Z_BAR{-1} + (1-rho_DLA_Z_BAR(0.8))*ss_DLA_Z_BAR(-1.5) + SHK_DLA_Z_BAR( $\sigma=0.5$ );
137: RR_BAR       = rho_RR_BAR(0.8)*RR_BAR{-1} + (1-rho_RR_BAR(0.8))*ss_RR_BAR(0.5) + SHK_RR_BAR( $\sigma=0.5$ );
138: DLA_GDP_BAR = rho_DLA_GDP_BAR(0.8)*DLA_GDP_BAR{-1} + (1-rho_DLA_GDP_BAR(0.8))*ss_DLA_GDP_BAR(2.5) + SHK_DLA_GDP_BAR( $\sigma=0.5$ );
139:
140: %% === Foreign Sector Equations ===
141: L_GDP_RW_GAP = rho_L_GDP_RW_GAP(0.8)*L_GDP_RW_GAP{-1} + SHK_L_GDP_RW_GAP( $\sigma=1$ );
142: DLA_CPI_RW   = rho_DLA_CPI_RW(0.8)*DLA_CPI_RW{-1} + (1-rho_DLA_CPI_RW(0.8))*ss_DLA_CPI_RW(2) + SHK_DLA_CPI_RW( $\sigma=2$ );
143: RS_RW        = rho_RS_RW(0.8)*RS_RW{-1} + (1-rho_RS_RW(0.8))*(RR_RW_BAR + DLA_CPI_RW) + SHK_RS_RW( $\sigma=1$ );
144: RR_RW_BAR    = rho_RR_RW_BAR(0.8)*RR_RW_BAR{-1} + (1-rho_RR_RW_BAR(0.8))*ss_RR_RW_BAR(0.75) + SHK_RR_RW_BAR( $\sigma=0.5$ );
145: RR_RW        = RS_RW - DLA_CPI_RW;
146: RR_RW_GAP    = RR_RW - RR_RW_BAR;
147: DLA_CPI_RW   = 4*(L_CPI_RW - L_CPI_RW{-1});
148:
149: %% -----
150: !measurement_variables
151: OBS_L_GDP
152: OBS_L_CPI
153: OBS_RS
154: OBS_L_S
155: OBS_D4L_CPI_TAR
156:
157: OBS_L_GDP_RW_GAP
158: OBS_DLA_CPI_RW
159: OBS_RS_RW
160:
161: %% -----
162: !measurement_equations
163: OBS_L_GDP = L_GDP;
164: OBS_L_CPI = L_CPI;
165: OBS_RS   = RS;
166: OBS_L_S  = L_S;
167: OBS_D4L_CPI_TAR = D4L_CPI_TAR;
168:
169: OBS_L_GDP_RW_GAP = L_GDP_RW_GAP;
170: OBS_DLA_CPI_RW  = DLA_CPI_RW;

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171:     OBS_RS_RW      = RS_RW;
172:
173:     %% -----
174: Legend
175:     _GAP      cyclical deviation from a trend
176:     _BAR      trend (equilibrium)
177:     ss_       steady-state value
178:     DLA_     q-o-q change
179:     D4L_     y-o-y change
180:     _RW      foreign variable
181:     SHK_     equation residual
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Steady state

Variable	Description	Value
L_GDP_GAP	Output Gap (in %)	0
DLA_GDP	Quarterly Growth in Real GDP annualized (in % pa)	2.5
D4L_GDP	Real GDP Growth YoY (in % pa)	2.5
DLA_GDP_BAR	Real GDP Trend Growth QoQ annualized (in % pa)	2.5
MCI	Real Monetary Condition Index (in % pa)	0
DLA_CPI	CPI Inflation QoQ annualized (in % pa)	2
E_DLA_CPI	Expected CPI Inflation QoQ annualized (in % pa)	2
D4L_CPI	CPI Inflation YoY (in % pa)	2
D4L_CPI_TAR	Inflation Target (in % pa)	2
RMC	Real Marginal Cost (in %)	0
DLA_S	Nominal Exch. Rate Depreciation QoQ annualized (in % pa)	-1.5
D4L_S	Nominal Exch. Rate Depreciation YoY (in % pa)	-1.5
PREM	Country Risk Premium (in % pa)	1.25
RS	Nominal Policy Interest Rate (in % pa)	2.5
RR	Real Interest Rate (in % pa)	0.5
RR_BAR	Trend Real Interest Rate (in % pa)	0.5
RR_GAP	Real Interest Rate Gap (in %)	0
RSNEUTRAL	Nominal Policy Neutral Interest Rate (in % pa)	2.5
L_Z_GAP	Real Exchange Rate Gap (in %)	0
DLA_Z	Real Exchange Rate Depreciation QoQ annualized (in % pa)	-1.5
DLA_Z_BAR	Trend Real Exchange Rate Depreciation QoQ annualized (in % pa)	-1.5
L_GDP_RW_GAP	Foreign Output Gap (in %)	0
RS_RW	Foreign Nominal Interest Rate (in % pa)	2.75
RR_RW	Foreign Real Interest Rate (in % pa)	0.75
RR_RW_BAR	Foreign Real Interest Rate Trend (in % pa)	0.75
RR_RW_GAP	Foreign Real Interest Rate Gap (in %)	0
DLA_CPI_RW	Foreign Inflation QoQ annualized (in % pa)	2