

## QPM Model

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1:  % ----- %
2:  % ----- Quarterly Projection Model (QPM) ----- %
3:  % ----- %
4:
5:  % ----- %
6:  !transition_variables
7:  'Real GDP (100*log)'          L_GDP
8:  'Trend in Real GDP (100*log)' L_GDP_BAR
9:  'Output Gap (in %)'          L_GDP_GAP
10:  'Quarterly Growth in Real GDP annualized (in % pa)' DLA_GDP
11:  'Real GDP Growth YoY (in % pa)' D4L_GDP
12:  'Real GDP Trend Growth QoQ annualized (in % pa)' DLA_GDP_BAR
13:
14:  'Real Monetary Condition Index (in % pa)' MCI
15:
16:  'CPI (level, 100*log)'        L_CPI
17:  'CPI Inflation QoQ annualized (in % pa)' DLA_CPI
18:  'Expected CPI Inflation QoQ annualized (in % pa)' E_DLA_CPI
19:  'CPI Inflation YoY (in % pa)' D4L_CPI
20:  'Inflation Target (in % pa)' D4L_CPI_TAR
21:
22:  'Real Marginal Cost (in %)'    RMC
23:
24:  'Nominal Exchange Rate (LCY/FCY, 100*log)' L_S
25:  'Nominal Exch. Rate Depreciation QoQ annualized (in % pa)' DLA_S
26:  'Nominal Exch. Rate Depreciation YoY (in % pa)' D4L_S
27:  'Country Risk Premium (in % pa)' PREM
28:
29:  'Nominal Policy Interest Rate (in % pa)' RS
30:  'Real Interest Rate (in % pa)' RR
31:  'Trend Real Interest Rate (in % pa)' RR_BAR
32:  'Real Interest Rate Gap (in %)' RR_GAP
33:  'Nominal Policy Neutral Interest Rate (in % pa)' RSNEUTRAL
34:
35:  'Real Exchange Rate (level, 100*log)' L_Z
36:  'Trend Real Exchange Rate (level, 100*log)' L_Z_BAR
37:  'Real Exchange Rate Gap (in %)' L_Z_GAP
38:  'Real Exchange Rate Depreciation QoQ annualized (in % pa)' DLA_Z
39:  'Trend Real Exchange Rate Depreciation QoQ annualized(in % pa)' DLA_Z_BAR
40:
41:  'Foreign Output Gap (in %)' L_GDP_RW_GAP
42:  'Foreign Nominal Interest Rate (in % pa)' RS_RW
43:  'Foreign Real Interest Rate (in % pa)' RR_RW
44:  'Foreign Real Interest Rate Trend (in % pa)' RR_RW_BAR
45:  'Foreign Real Interest Rate Gap (in %)' RR_RW_GAP
46:  'Foreign CPI (level, 100*log)' L_CPI_RW
47:  'Foreign Inflation QoQ annualized (in % pa)' DLA_CPI_RW
48:
49:  % ----- %
50:  !transition_shocks
51:  'Shock: Output gap (demand)' SHK_L_GDP_GAP( $\sigma=1$ )
52:  'Shock: CPI inflation (cost-push)' SHK_DLA_CPI( $\sigma=0.75$ )
53:  'Shock: Exchange rate (UIP)' SHK_L_S( $\sigma=3$ )
54:  'Shock: Interest rate (monetary policy)' SHK_RS( $\sigma=1$ )
55:  'Shock: Inflation target' SHK_D4L_CPI_TAR( $\sigma=2$ )
56:

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57:      'Shock: Real interest rate'                                SHK_RR_BAR( $\sigma=0.5$ )
58:      'Shock: Real exchange rate depreciation'                  SHK_DLA_Z_BAR( $\sigma=0.5$ )
59:      'Shock: Potential GDP growth'                             SHK_DLA_GDP_BAR( $\sigma=0.5$ )
60:
61:      'Shock: Foreign output gap'                                SHK_L_GDP_RW_GAP( $\sigma=1$ )
62:      'Shock: Foreign nominal interest rate'                    SHK_RS_RW( $\sigma=1$ )
63:      'Shock: Foreign inflation'                                 SHK_DLA_CPI_RW( $\sigma=2$ )
64:      'Shock: Foreign real interest rate'                       SHK_RR_RW_BAR( $\sigma=0.5$ )
65:
66:      % ----- %
67:      !parameters
68:      % --- Structural coefficients ---
69:      b1(0.8) b2(0.3) b3(0.5) b4(0.7)
70:      a1(0.7) a2(0.2) a3(0.7)
71:      e1(0.4)
72:      g1(0.7) g2(0.5) g3(0.5)
73:
74:      % --- AR Processes ---
75:      rho_D4L_CPI_TAR(0.5)
76:      rho_DLA_Z_BAR(0.8)
77:      rho_RR_BAR(0.8)
78:      rho_DLA_GDP_BAR(0.8)
79:
80:      rho_L_GDP_RW_GAP(0.8)
81:      rho_RS_RW(0.8)
82:      rho_DLA_CPI_RW(0.8)
83:      rho_RR_RW_BAR(0.8)
84:
85:      % --- Steady State Parameters ---
86:      ss_D4L_CPI_TAR(2)
87:      ss_DLA_Z_BAR(-1.5)
88:      ss_RR_BAR(0.5)
89:      ss_DLA_GDP_BAR(2.5)
90:      ss_DLA_CPI_RW(2)
91:      ss_RR_RW_BAR(0.75)
92:
93:      % ----- %
94:      !transition equations
95:      %% === IS Curve ===
96:      L_GDP_GAP = b1(0.8)*L_GDP_GAP{-1} - b2(0.3)*MCI + b3(0.5)*L_GDP_RW_GAP + SHK_L_GDP_GAP( $\sigma=1$ );
97:      MCI       = b4(0.7)*RR_GAP + (1-b4(0.7))*(- L_Z_GAP);
98:
99:      %% === Phillips Curve ===
100:      DLA_CPI   = a1(0.7)*DLA_CPI{-1} + (1-a1(0.7))*DLA_CPI{+1} + a2(0.2)*RMC + SHK_DLA_CPI( $\sigma=0.75$ );
101:      RMC       = a3(0.7)*L_GDP_GAP + (1-a3(0.7))*L_Z_GAP;
102:      E_DLA_CPI = DLA_CPI{+1};
103:
104:      %% === Monetary Policy Reaction Function (a forward-looking Taylor-type Rule) ===
105:      RS        = g1(0.7)*RS{-1} + (1-g1(0.7))*(RSNEUTRAL + g2(0.5)*(D4L_CPI{+4} - D4L_CPI_TAR{+4})) + g3(0.5)*L_GDP_GAP +
SHK_RS( $\sigma=1$ );
106:      RSNEUTRAL = RR_BAR + D4L_CPI{+1};
107:
108:      %% === Modified UIP condition ===
109:      L_S       = (1-e1(0.4))*L_S{+1} + e1(0.4)*(L_S{-1} + 2/4*(D4L_CPI_TAR - ss_DLA_CPI_RW(2) + DLA_Z_BAR)) + (- RS + RS_RW + PREM)/4 +
SHK_L_S( $\sigma=3$ );
110:
111:      %% === Definitions ===
112:      % Fisher equation (RIR)

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113:      RR          = RS - D4L_CPI{+1};
114:      L_Z          = L_S + L_CPI_RW - L_CPI;
115:      % Long-term version of UIP (consistency of trends)
116:      DLA_Z_BAR{+1} = RR_BAR - RR_RW_BAR - PREM;
117:
118:      %% === Identities ===
119:      DLA_GDP_BAR = 4*(L_GDP_BAR - L_GDP_BAR{-1});
120:      DLA_Z_BAR   = 4*(L_Z_BAR - L_Z_BAR{-1});
121:      DLA_Z       = 4*(L_Z - L_Z{-1});
122:      DLA_GDP     = 4*(L_GDP - L_GDP{-1});
123:      DLA_CPI     = 4*(L_CPI - L_CPI{-1});
124:      DLA_S       = 4*(L_S - L_S{-1});
125:      D4L_GDP     = L_GDP - L_GDP{-4};
126:      D4L_CPI     = L_CPI - L_CPI{-4};
127:      D4L_S       = L_S - L_S{-4};
128:
129:      %% === Gaps ===
130:      RR_GAP      = RR - RR_BAR;
131:      L_Z_GAP     = L_Z - L_Z_BAR;
132:      L_GDP_GAP   = L_GDP - L_GDP_BAR;
133:
134:      %% === Trends ===
135:      D4L_CPI_TAR = rho_D4L_CPI_TAR(0.5)*D4L_CPI_TAR{-1} + (1-rho_D4L_CPI_TAR(0.5))*ss_D4L_CPI_TAR(2) + SHK_D4L_CPI_TAR(sigma=2);
136:      DLA_Z_BAR   = rho_DLA_Z_BAR(0.8)*DLA_Z_BAR{-1} + (1-rho_DLA_Z_BAR(0.8))*ss_DLA_Z_BAR(-1.5) + SHK_DLA_Z_BAR(sigma=0.5);
137:      RR_BAR      = rho_RR_BAR(0.8)*RR_BAR{-1} + (1-rho_RR_BAR(0.8))*ss_RR_BAR(0.5) + SHK_RR_BAR(sigma=0.5);
138:      DLA_GDP_BAR = rho_DLA_GDP_BAR(0.8)*DLA_GDP_BAR{-1} + (1-rho_DLA_GDP_BAR(0.8))*ss_DLA_GDP_BAR(2.5) + SHK_DLA_GDP_BAR(sigma=0.5);
139:
140:      %% === Foreign Sector Equations ===
141:      L_GDP_RW_GAP = rho_L_GDP_RW_GAP(0.8)*L_GDP_RW_GAP{-1} + SHK_L_GDP_RW_GAP(sigma=1);
142:      DLA_CPI_RW   = rho_DLA_CPI_RW(0.8)*DLA_CPI_RW{-1} + (1-rho_DLA_CPI_RW(0.8))*ss_DLA_CPI_RW(2) + SHK_DLA_CPI_RW(sigma=2);
143:      RS_RW        = rho_RS_RW(0.8)*RS_RW{-1} + (1-rho_RS_RW(0.8))*(RR_RW_BAR + DLA_CPI_RW) + SHK_RS_RW(sigma=1);
144:      RR_RW_BAR    = rho_RR_RW_BAR(0.8)*RR_RW_BAR{-1} + (1-rho_RR_RW_BAR(0.8))*ss_RR_RW_BAR(0.75) + SHK_RR_RW_BAR(sigma=0.5);
145:      RR_RW        = RS_RW - DLA_CPI_RW;
146:      RR_RW_GAP    = RR_RW - RR_RW_BAR;
147:      DLA_CPI_RW   = 4*(L_CPI_RW - L_CPI_RW{-1});
148:
149:      %% ----- %
150:      !measurement_variables
151:      OBS_L_GDP
152:      OBS_L_CPI
153:      OBS_RS
154:      OBS_L_S
155:      OBS_D4L_CPI_TAR
156:
157:      OBS_L_GDP_RW_GAP
158:      OBS_DLA_CPI_RW
159:      OBS_RS_RW
160:
161:      %% ----- %
162:      !measurement_equations
163:      OBS_L_GDP = L_GDP;
164:      OBS_L_CPI = L_CPI;
165:      OBS_RS    = RS;
166:      OBS_L_S   = L_S;
167:      OBS_D4L_CPI_TAR = D4L_CPI_TAR;
168:
169:      OBS_L_GDP_RW_GAP = L_GDP_RW_GAP;
170:      OBS_DLA_CPI_RW   = DLA_CPI_RW;

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171:     OBS_RS_RW      = RS_RW;
172:
173:     %% ----- %
174:     Legend
175:     _GAP      cyclical deviation from a trend
176:     _BAR      trend (equilibrium)
177:     ss_       steady-state value
178:     DLA_      q-o-q change
179:     D4L_      y-o-y change
180:     _RW       foreign variable
181:     SHK_      equation residual
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## Steady state

Variable	Description	Value
L_GDP_GAP	Output Gap (in %)	0
DLA_GDP	Quarterly Growth in Real GDP annualized (in % pa)	2.5
D4L_GDP	Real GDP Growth YoY (in % pa)	2.5
DLA_GDP_BAR	Real GDP Trend Growth QoQ annualized (in % pa)	2.5
MCI	Real Monetary Condition Index (in % pa)	0
DLA_CPI	CPI Inflation QoQ annualized (in % pa)	2
E_DLA_CPI	Expected CPI Inflation QoQ annualized (in % pa)	2
D4L_CPI	CPI Inflation YoY (in % pa)	2
D4L_CPI_TAR	Inflation Target (in % pa)	2
RMC	Real Marginal Cost (in %)	0
DLA_S	Nominal Exch. Rate Depreciation QoQ annualized (in % pa)	-1.5
D4L_S	Nominal Exch. Rate Depreciation YoY (in % pa)	-1.5
PREM	Country Risk Premium (in % pa)	1.25
RS	Nominal Policy Interest Rate (in % pa)	2.5
RR	Real Interest Rate (in % pa)	0.5
RR_BAR	Trend Real Interest Rate (in % pa)	0.5
RR_GAP	Real Interest Rate Gap (in %)	0
RSNEUTRAL	Nominal Policy Neutral Interest Rate (in % pa)	2.5
L_Z_GAP	Real Exchange Rate Gap (in %)	0
DLA_Z	Real Exchange Rate Depreciation QoQ annualized (in % pa)	-1.5
DLA_Z_BAR	Trend Real Exchange Rate Depreciation QoQ annualized(in % pa)	-1.5
L_GDP_RW_GAP	Foreign Output Gap (in %)	0
RS_RW	Foreign Nominal Interest Rate (in % pa)	2.75
RR_RW	Foreign Real Interest Rate (in % pa)	0.75
RR_RW_BAR	Foreign Real Interest Rate Trend (in % pa)	0.75
RR_RW_GAP	Foreign Real Interest Rate Gap (in %)	0
DLA_CPI_RW	Foreign Inflation QoQ annualized (in % pa)	2