g_1 $T(n) = 3T(n/2) + n^2$ $\rightarrow T(n) = aT(n/6) + f(n^2)$ a)1, b),1 On compairing a=3, b=2, \f(n)=n2 Now, C = lega = leg 3 = 1.584 ne = n' 584 x n2 $f(n) > n^{c}$ $f(n) > n^{c}$ $f(n) \ge o(n^{2})$ 92) $T(n) = 4T(n/2) + n^2$ \rightarrow all 1, 6/1a=4, b=2, $f(n)=n^2$ C= log 4 = 02 $n^{c} = n^{2} \mathcal{I}(n) = n^{2}$ · · · T(n) · · · (n² lg2n) 93) T(n)27(n/2)+2" a=1 f(n) z 2 n c-lega-legc=0 n° = 10° = 1 f(n)>n° T(n) = 0(2")

4) T(n) 22 T(n/2) + n -> a=2" b=2, f(n)=n2 C= loga = log2 ncon f(n) = n° P(n)= o(n2 legen) 95) T(n)= 16T(n/4)+n) a=16, b=4 f(n) = n $c = \log 16 = \log (4)^2 = 2 \log 4$ $= 2 \sqrt{4}$ nc > n2 f(n)< n° T(n)=0 (n²) 96) T(n)=2T(n/2)+nlegn $\rightarrow a=2, b=2$ f(n)=nlegn $C = \log 2 = 1$ $n^2 = n^2 = n$ n logn > n f(w) > nc T(a) = o (n leg n)

```
g7) T(n)= 2T(n/2) + n/lagn
 ) a=2, b=2, f(n)= n/legn
   C= lag 2 = 1
   nc = n1 = n
  lag n < n
 · . f(n) < nc
 :. T(n) = 0 (n)
98) T(n) = 2T(n/4) + n0.51
-> a = 2, b = 4, f(n) = n0.51
    C = lega = leg 2 = 0.5
   · n°5 < n°.51
    f(n)>nc
   · . T(n) = 0 (nº.51)
gg) T(n) 2 0.5 T (n/2) + 1/n
-> a=0.5, b=2
   0 1/1 but here a is 0.5
 so me cannet apply Master's
Theorem.
910) T(n)= 16T(n/4)+n!
-> a=16, b=4, f(n)=n!
 · · · C = log a z log 16 2 2
```

 $n^{c} = n^{2}$

As n/ >n²

... T(n) = 0(n!)

```
911) 4T(n/2) + lag n
-, a=4, b=e, f(n)=lagn
    C = lega . leg 4 = 2
    [(n) · lagn
      · lagn × n²
        $(n)(n°
      T(n): 0(nc)
           = 0 (n2)
Q12) T(n) 2 sqrt(n) T(n/2) + logn
_, a=\n, b=2
  C= lago a = lagon = 1 lagon
· · - legen < leg(n)
,. f(u)>uc
   T(n) = 0 (f(n))
       = 0 (leg (n))
(13) T(n)=3T(n/2)+n
\rightarrow a=3; b=2; f(n)=n
  C = log a = log 3 = 1.5849
nc = 1.5489
    n< n1.5849
> f(n) < nc
     T(n)=0(n1.5849)
Q14) T(n) = 3T(n/3) + sqrt (n)
\rightarrow \alpha=3, b=3
  C = lega = leg3 = 1
    n^{c} = n^{2} = n
 As sgut (n) < n
     f(n)(nc
     T(n) 20(n)
```

\$15)
$$T(n) : 4T(n/2) + n$$

\[
\to a = 4, b = 2
\]

 $C = lag a = lag = 2$
 $h^{c} = n^{2}$
 $n < n^{2}$ (for any constant)

 $f(n) < n^{c}$
 $f(n) = 3T(n/4) + n lag n$

\[
\to a = 3, b = 4, f(n) = n lag n
\]

 $C = lag a = lag = 0.792$
 $n^{c} = n^{c} + 1$
 $n^{c} = n^{c} = 1$
 $f(n) = n/2$
 $f(n) = n$

g19) T(n)=4T(n/2) + h/legn $\rightarrow a = 4, b = 2, f(n) = n$ C= loga = log4 = 2 logn lagn (n2 T(n) = 0 (n2) 820) T(n) = 64T(n/8) - n2 lagn -> a=64 b=8 C = log a = log 64 = log (8)2 $n^{c} = n^{2}$ $(n^2 \log n) n^2$ $T(n) = O(n^2 \log n)$ g21) T(n)= 7T (n/3)+n2 $\rightarrow a = 7; b = 3; f(n) = n^2$ C= loga = log37 = 1-7712 nc = n1.7712 n1.7712 < n2 T(n) = 0 (n2) 822) T(n)= T(n/2)+n(2-(asn) \rightarrow a=1,b=2C= lag a = lag 1 = 0 n° = n° = 1 $n(2-(con))n^{c}$ T(n) = 0 (n(2-cosn))