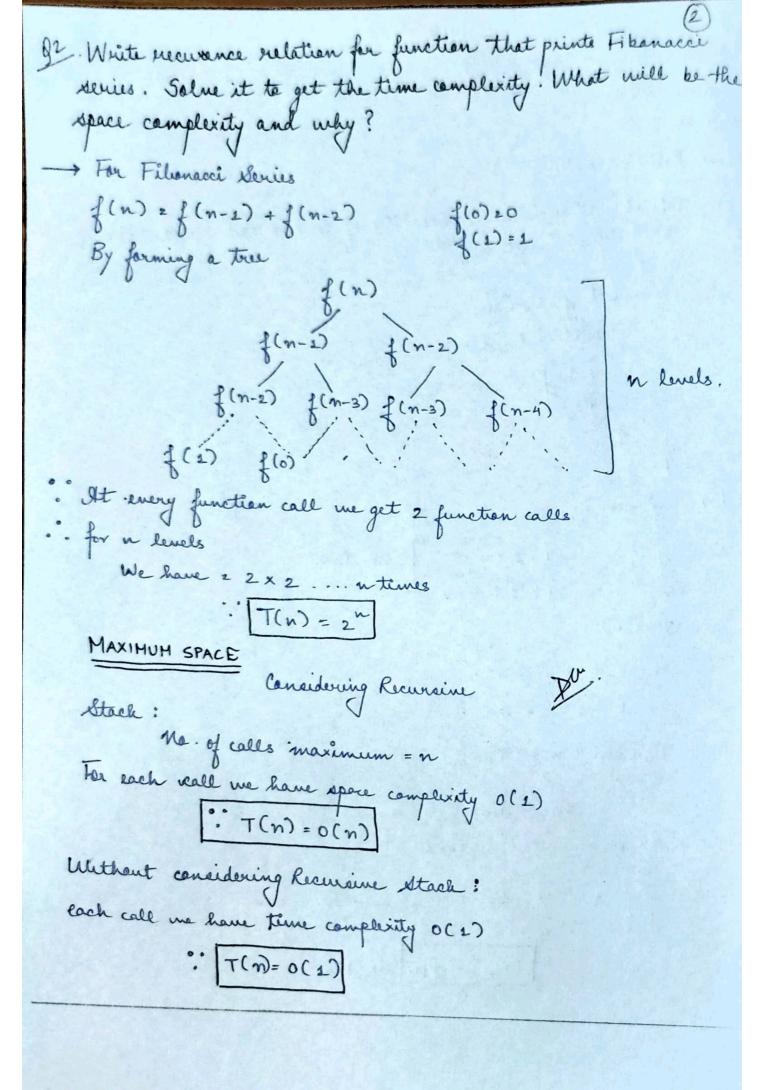
What is the time complexity of below cade and have? vaid fun (int n) int j=1, i=0; while (i(n) { i+=j;
j++; J=2 J=3 m-level i=21+2 i = 1 + 2 + 3for (i) , 1 + 2 + 3 + ... + < n 1+2+3+m < n : m(m+1) <n m & Jn By summation method $\Rightarrow \underbrace{1}_{i=1} 1 \Rightarrow 1+1+\dots+In \text{ times}$ T(n) = Jn - Ans



```
Write pragrams which have complexity:
  n (lag n), n', lag (lag n)
1) n lagn - Juick sant
       vaid quickwart (int aur (), int law, int high)
            if ( low < high)
               int pi = partition ( aur, low, high);
               quedant ( am, leve, pi-1);
              quickent ( av, pi + 1, high);
   int partition (int ave [], int law, int high)
            int pinet 2 ave [ high ];
             int i = (law - 1);
        for ( int j = lone; j <= high -1; j ++)
               if (arr(i) < pinet)
                   suap (davici), davicj);
           return (i+1); have [high]);
2) n3 -> Multiplication of 2 square matrix
       for (i=0; i < n1; i++) {
           for (j=0; j < c2; j++)
                 for ( h = 0; h < c1; h++)
                       Motilij] + = a[i][h] * b[k][j];
```

gh. Salue the following recurrence relation T(n) = T(n/4) + T(n/2) + Cn^2

$$T(n/a) \qquad T(n/2 \rightarrow 1)$$

$$T(n/a) \qquad T(n/a) \qquad T(n/a) \qquad T(n/a) \rightarrow 2.$$

At level

$$0 \to Cn^{2}$$

$$1 \to \frac{n^{2}}{4^{2}} + \frac{n^{2}}{2^{2}} = \frac{C5n^{2}}{16}$$

$$2 \to \frac{n^{2}}{8^{2}} + \frac{n^{2}}{16^{2}} + \frac{n^{2}}{4^{2}} + \frac{n^{2}}{8^{2}} = \left(\frac{5}{16}\right)^{2}n^{2}C$$

$$\vdots$$

$$\max \text{ level} = \frac{n}{2^{K}} = 1$$

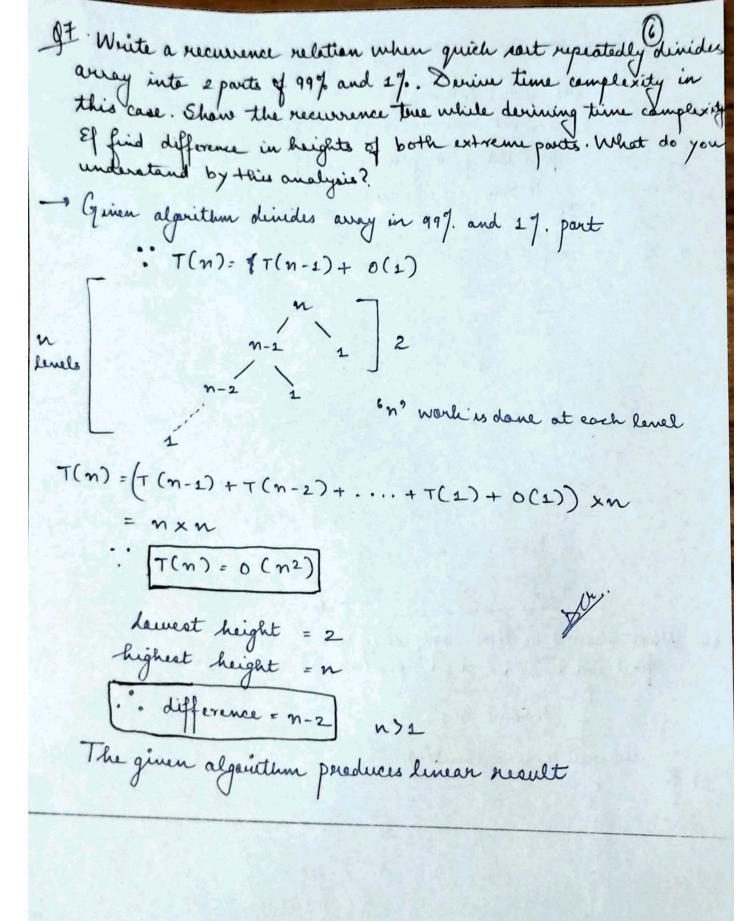
$$T(n) = c \left(n^{2} + \left(\frac{5}{16} \right) n^{2} + \left(\frac{5}{16} \right)^{2} n^{2} + \dots + \left(\frac{5}{16} \right)^{2} n^{2} \right)$$

$$T(n) = C n^{2} \left[1 + \left(\frac{5}{16} \right) + \left(\frac{5}{16} \right)^{2} + \dots + \left(\frac{5}{16} \right)^{2} n^{2} \right]$$

$$T(n) = C n^{2} \times 1 \times \left(\frac{1 - \left(\frac{5}{16} \right)^{2} n^{2}}{1 - \left(\frac{5}{16} \right)^{2}} \right)$$

```
gs. What is the time complexity of following funt??
              int fun (int n) {
               for Eint k=2; i <= n; i++) {
                for ( int j = 1; jen ; 1 + + 1) {
                  11 Some O(x) task
                                                j= (n-1)/i-times
                         1+5+9
         £ (n-1)
      : T(n) = (\frac{n-1}{1}) + (\frac{n-1}{2}) + (\frac{n-1}{3}) + \cdots + (\frac{n-1}{n})
     T(n) = n[1+1/2+1/3+...+1/n] - 1x[1+1/2+1/3+..+1/n]
             z nlagn-lagn
               T(n)=O(nlagn) -> Ons.
go. What should be time camplexity of for ( int i=2, i <= n; i = pow(i, k))
                 11 Some 0(1)
        where he is a constant
                                  2 km <= n
                                   km z legzn
                                    m = lag k lag 2 n
             : £ 1
                          1+1+1 .... in times
```

T(n) = O(log klagn) -Ans.



Annuage following in increasing order of note of growth:

a) n, n!, logn, log logn, neat (n), log(n!), n logn, log(n), 2, 2², 4, n², 100

log log logn < logn < (logn)² < Tn < n < n logn < log (n!) < n² <

b) 2ⁿ < 4ⁿ < 2²

2(2ⁿ), 4n, 2n, 1, log(n), log (log(n)), Tlog(n), log 2n, 2 log(n), n, log (n!), n!, n2, n log(n)

4 < log logn < Tlogn < logn < log 2n < 2 logn < n < n logn

c) 8²ⁿ

7 100 < log (n!), n log (n!) < n² < n! < 2ⁿ

7 100 < log (n!), n log (n!), n log (n!), n!, log (n), n log (n!), n!, log (n), n log (n!), n!, log (n), n log (n)) < n log (n!), n!, log (n), n log (n) < n log (n!) < n log

*