



```
92 What should be time complexity of:
         for (inti-1 to u)
             i=i*2, \rightarrow o(1)
L) for i => 1, 2, 4, 6, 8 . . . . n times
       ie Stries is a GP
   So a=1, n=2/1
    Kth value of GP:
             th = ank-1
             th = 1(2)k-1
             2n=2k
          lag_2(2n) = k lag 2
            lag 2 + lag n = le
            leg 2 n+1 = h (Neglecting '1')
  So, Time Complexity T(n) > 0 (lag, n) - Ans.
```

13. T(n) = [3T(n-1) if n > 0otherwise 1 f4 is $T(n) \Rightarrow 3T(n-1) - (1)$ $T(n) \Rightarrow 1$ put $n \Rightarrow n-1$ in (1) $T(n-1) \Rightarrow 3T(n-2) - (2)$ put (2) in (1) $T(n) \Rightarrow 3x \Rightarrow T(n-2)$ $T(n) \Rightarrow 9T(n-2) \rightarrow (3)$ put $n \Rightarrow n-2$ in (1) T(n-2) = 3T(n-3)put in (3). $T(n) = 27T(n-3) \rightarrow 4$

```
Generalising series,

T(h) = 3^{k} T(n-k) - (5)

for hth terms, Let n-k=1 (Base Case)

h = n-1
put in (5)
T(n) = 3^{n-1} T(1)
T(n) = 3^{n-1} \qquad (neglecting 3')
T(n) = 0 (3^{n})
```

By
$$T(n) = \int_{0}^{\infty} 2T(n-1)-1$$
 of $n > 0$, otherwise L

$$T(n) = 2T(n-1)-1 \rightarrow (1)$$

put $n = n-1$

$$T(n-1) = 2T(n-2)-1 \rightarrow (2)$$

put in (1)

$$T(n) = 2 \times (2T(n-2)-1)-1$$

$$= 4T(n-2)-2-1 - (3)$$

put $n = n-2$ in (1)

$$T(n-2) = 2T(n-3)-1$$

Put in (1)

$$T(n) = 2^{k} T(n-k)-2^{k-1}-2^{k-2}...2^{n}$$

Furtherm

Let $n-k=1$

$$k=n-1$$

$$T(n) = 2^{k-1} T(1)-2^{k} \left(\frac{1}{2}+\frac{1}{2^{2}}+...+\frac{1}{2^{k}}\right)$$

$$= 2^{k-1}-2^{k-1} \left(\frac{1}{2}+\frac{1}{2^{2}}+...+\frac{1}{2^{k}}\right)$$

ie Svives in GP.

a=/2 , n=/2.

```
50,

T(n) = 2^{n-1} (1 - (1/2)^{n-1})

= 2^{n-1} (1 - 1 + (1/2)^{n-1})

= 2^{n-1} (1 - 1 + (1/2)^{n-1})

= 2^{n-1} - 1

= 2^{n-1} - 1

= 2^{n-1} - 1

= 2^{n-1} - 1
```

```
95 what should be time complexity of
            int i=1, s=1;
            while (s <= n)
              i i++;
               S = S + L;
             2 printf ("#");
- i=1 2 3 4 5 6 ...
   8= 1+3+6+10+15+ ....
  Sum of se 1+3+6+10+ ... + n - 1)
  Also 5 2 1+3+6+10+11. Tn-1+Tn -> 2)
   0= 1+2+3+4+ ... n-Tn
   Tk = 1+2+3+4+ ... + K
   TK = 1 K (K+1)
    for K iterations
    1+2+3+ ... k (= n
     \frac{k(k+1)}{2} < = w
      \frac{k^2+K}{2} < = n
      O(k2) <= N
         K = 0( Ju)
       T(n) = O(Jn) Que.
```

```
go Time Camplerity of
      void f (int n)

int i, count = 0;
       far(i=61; i * i <= n; ++ i)
 La As i2 en
    i=1,2,3,4,... Ju
  £ 1+2+3+4+ ... + Jn
       T(n) 2 Jn * (Jn +1)
        T(n)= n + Jn
         T(n) = o(n) \rightarrow Aus.
97. Time Complexity of
         void f (intr)
          int i, j, h, count =0;
```

for (int i = 1/2; i(=n; ++18) for (j=1; j(=n; j=j*2) for (h=1; h <= n; h= k+2)

count ++;

Is shire, for h= h2 k=1,2,4,8,... h ". Series is in GP No, a=1, n=2

> a (n-1) $=\frac{1(2^{k}-1)}{1}$ n = 2k -1 n+1=2h leg_(n)=h

```
i j h (7)

lag(n) lag(n)* lag(n)*

lag(n) * lag(n)*

n lag(n) lag(n)* lag(n)*

T.C \Rightarrow O(n * lagn * lagn)

\Rightarrow O(n lag^2(n)) \rightarrow lns

The Camplexity of
```

```
& Time Complexity of
          void function ( int n)
             of (n==1) return;
             for (i=+ ten) {
              for (j=1 to n) {
             3 printf (" * "),
       function (n-3);
  4 for (i= 1 to n)
       me get j=n times enery turn
            · · · · * j = n2
     hth, Now, T(n) = n<sup>2</sup> + T(n-3);
               T(n-3) = (n23)2 + T(n-6);
               T(n-6) = (n 6) 2 + T(n-9);
              and T(1)=1;
       Now, substitute each value in T(n)
         T(n) = n^2 + (n-3)^2 + (n-6)^2 + \dots + 1
          Let 1 - 3h = 1
               h = (n-1)/3 total terms = k+1
    T(n) = n^2 + (n-3)^2 + (n-6)^2 + \dots + 1
     T(n) = ~ 4 n2
      T(n)~(h-1)/3 # n2
      50, T(n) 20(n3) - Ans
```

```
19. Time Complexity of:-

vaid function (int n)

for (int i=1 to n) {

for (int j=1; j <= n; j=j+i) {
```

prints (" * "),

j=1+2+....(n),j+i) 4 for i = 1 j=1+3+5...(n),j+i) i = 2 j=1+4+7...(n),j+i) nth term of AP is T(n)= a+d* m T(m) = 1 + d xm (n-1)/d=n for i=1 (n-1)/1 times i=2 (n-1)/2 times me get, T(n) 2 i 2 j 2 + l 2 j 2 + ... in-1 j n-1 $2(n-1)+(n-2)+(n-3)+\cdots$ 2 n+n/2 + n/3 + .. n/n-1 - nx1 2 n [1+1/2+1/3+ ··· 1/n-1] - n+1 znxlagn-n+1 Since 1 1/x = lag x T(n) = O(nlegn) - Ans.

```
For the Function n'R & C<sup>n</sup>, what is the asymptotic Relationship b/00 these functions?

Assume that h>=1 & C>1 are constants. Find out the value of C & no. of which relationship holds.

Is given nh and c<sup>n</sup>

Relationship b/w nh & c<sup>n</sup> is

nh = 0 (c<sup>n</sup>)

nh & accn)

V n > no h constant, a>0

for no=1; c=2

no=1 & c=2 -> Ans
```