

## Session 3 Handout

### 1. Defining and Calling your Own Functions

```
[1]: def calculateWage(hours,base=10,bonus=.5):  
    ''' Calculates weekly wage '''  
    if hours<=40:  
        pay=hours*base  
    else:  
        pay=hours*base+(hours-40)*base*bonus  
    return pay  
  
help(calculateWage)  
print('Pay for 42 hours with default base and bonus:',calculateWage(42))  
print('Pay for 42 hours with base 12/hour and default bonus:',calculateWage(42,12))  
print('Pay for 42 hours with base 12/hour and bonus 60%:', calculateWage(42,12,.6))  
print('Pay for 42 hours with default base and bonus 50%:',calculateWage(42,bonus=0.6))
```

Help on function calculateWage in module \_\_main\_\_:

```
calculateWage(hours, base=10, bonus=0.5)  
    Calculates weekly wage
```

```
Pay for 42 hours with default base and bonus: 430.0  
Pay for 42 hours with base 12/hour and default bonus: 516.0  
Pay for 42 hours with base 12/hour and bonus 60%: 518.4  
Pay for 42 hours with default base and bonus 50%: 432.0
```

**Q1:** (Modification of case 2 from last session) Write a function named orderQuantity that takes two input arguments, inventory and basestock. If inventory is at least equal to basestock, then return 0. Otherwise, return the difference between basestock and inventory. Set the default value for inventory to be 0 and for basestock to be 100. Include an appropriate docstring to explain what the function does.

```
[2]: def orderQuantity(inventory=0,basestock=100):  
    ''' Calculates order quantity given inventory level and basestock level'''  
    if inventory>=basestock:  
        return 0  
    else:  
        return basestock-inventory  
  
[3]: # Code to test your function  
help(orderQuantity)  
print(orderQuantity())  
print(orderQuantity(25))  
print(orderQuantity(51,50))  
print(orderQuantity(basestock=200))  
print(orderQuantity(inventory=80))
```

Help on function orderQuantity in module \_\_main\_\_:

```
orderQuantity(inventory=0, basestock=100)
```

```
    Calculates order quantity given inventory level and basestock level

100
75
0
200
20
```

**Q2:** Walk through the code to explain each line of the above output.

### Packaging functions within a module

Open Spyder and create a new Python script, and copy paste the two functions `calculateWage` and `orderQuantity` into the script. Save the script into the same folder as this notebook, as `session3.py`. If everything is correct, you should be able to run the following.

```
[4]: import session3
      print(session3.calculateWage(40))
      print(session3.orderQuantity(30))
      help(session3.orderQuantity)
```

```
400
70
Help on function orderQuantity in module session3:
```

```
orderQuantity(inventory, basestock=100)
    Calculates order quantity given inventory level and basestock level
```

```
[5]: print('Module contains the following variables and functions:', dir(session3))
```

```
Module contains the following variables and functions: ['__builtins__', '__cached__', '__doc__'
```

```
[6]: help(session3)
```

```
Help on module session3:
```

NAME

```
    session3 - Created on Fri Jan 11 14:52:23 2019
```

DESCRIPTION

```
    @author: pengshi
```

FUNCTIONS

```
    calculateWage(hours, base=10, bonus=0.5)
        Calculates weekly wage
```

```
    monthlyPayment(total, months, interest=0.0425, downpay=0)
```

```
    numberMonths(total, monthly, interest=0.0425, downpay=0)
```

```

obtainNumeric(prompt='')
    Elicits user to input a number, and continues to ask if input is invalid.

orderQuantity(inventory, basestock=100)
    Calculates order quantity given inventory level and basestock level

```

FILE

```
c:\users\pengshi\dropbox\teaching\2019-spring-dso599\course material\handouts and notes\s
```

## 2. Exploring Existing Functions

```
[7]: help(print)
```

Help on built-in function print in module builtins:

```

print(...)
    print(value, ..., sep=' ', end='\n', file=sys.stdout, flush=False)

    Prints the values to a stream, or to sys.stdout by default.
    Optional keyword arguments:
    file: a file-like object (stream); defaults to the current sys.stdout.
    sep: string inserted between values, default a space.
    end: string appended after the last value, default a newline.
    flush: whether to forcibly flush the stream.

```

```
[8]: print(dir(__builtins__))
```

```
['ArithmeticError', 'AssertionError', 'AttributeError', 'BaseException', 'BlockingIOError', 'B
```

**Q3:** Run the above line and out of the items in all lowercase, choose five that look interesting to you, and use type and help and trial and error to find out what each of these built-in objects are and what you can do with them. Explain to your neighbor.

```
[9]: help(abs)
```

Help on built-in function abs in module builtins:

```

abs(x, /)
    Return the absolute value of the argument.

```

```
[10]: help(max)
```

Help on built-in function max in module builtins:

```
max(...)
    max(iterable, *[, default=obj, key=func]) -> value
    max(arg1, arg2, *args, *[, key=func]) -> value
```

With a single iterable argument, return its biggest item. The default keyword-only argument specifies an object to return if the provided iterable is empty.  
With two or more arguments, return the largest argument.

```
[11]: help(min)
```

Help on built-in function min in module builtins:

```
min(...)
    min(iterable, *[, default=obj, key=func]) -> value
    min(arg1, arg2, *args, *[, key=func]) -> value
```

With a single iterable argument, return its smallest item. The default keyword-only argument specifies an object to return if the provided iterable is empty.  
With two or more arguments, return the smallest argument.

```
[12]: help(sum)
```

Help on built-in function sum in module builtins:

```
sum(iterable, start=0, /)
    Return the sum of a 'start' value (default: 0) plus an iterable of numbers

    When the iterable is empty, return the start value.
    This function is intended specifically for use with numeric values and may
    reject non-numeric types.
```

**Q4:** Import the math module and print the list of variables and functions within this module using dir. Choose five functions from this list and use help and trial and error to figure out how to use them. Explain to your neighbor.

```
[13]: import math
      print(dir(math))
```

```
['__doc__', '__loader__', '__name__', '__package__', '__spec__', 'acos', 'acosh', 'asin', 'asinh', 'atan2', 'atanh', 'ceil', 'copysign', 'cos', 'cosh', 'dgamma', 'digamma', 'erf', 'erfc', 'erfi', 'exp', 'exp2', 'expm1', 'fabs', 'factorial', 'floor', 'fmod', 'frexp', 'fsum', 'gamma', 'hypot', 'isfinite', 'isinf', 'isnan', 'ldexp', 'lgamma', 'log', 'log10', 'log2', 'logp1', 'logspace', 'modf', 'nan', 'perm', 'pi', 'pow', 'radians', 'reciprocal', 'remainder', 'sin', 'sinh', 'sqrt', 'tan', 'tanh', 'trunc', 'zeta']
```

```
[14]: help(math.cos)
```

Help on built-in function cos in module math:

```
cos(...)
    cos(x)

    Return the cosine of x (measured in radians).
```

```
[15]: help(math.log)
```

Help on built-in function log in module math:

```
log(...)
    log(x[, base])

    Return the logarithm of x to the given base.
    If the base not specified, returns the natural logarithm (base e) of x.
```

**Q5:** Use `dir` on the string object "Hi". Choose five functions from this list and use `help` and trial and error to figure out how to use these functions built in to every string object. Explain to your neighbor.

```
[16]: print(dir('Hi'))
```

```
['__add__', '__class__', '__contains__', '__delattr__', '__dir__', '__doc__', '__eq__', '__fo
```

```
[17]: help('Hi'.lower)
```

Help on built-in function lower:

```
lower(...) method of builtins.str instance
    S.lower() -> str

    Return a copy of the string S converted to lowercase.
```

```
[18]: help(str.lower)
```

Help on method\_descriptor:

```
lower(...)
    S.lower() -> str

    Return a copy of the string S converted to lowercase.
```

```
[19]: help(str.find)
```

Help on method\_descriptor:

```
find(...)
    S.find(sub[, start[, end]]) -> int
```

Return the lowest index in S where substring sub is found, such that sub is contained within S[start:end]. Optional arguments start and end are interpreted as in slice notation.

Return -1 on failure.

### Case 6a. Mortgage Calculator I

Write a function `numberMonths` in module `session3` that calculates how many months it would take to pay off a mortgage given the monthly payment. The function has four input arguments: `total`, `monthly`, `interest`, and `downpay`. Let the default values for `interest` be 0.0425 and for `downpay` be 0. Label the four arguments  $T$ ,  $M$ ,  $I$ ,  $D$  respectively. The number of months needed  $N$  is given by the formula

$$N = \text{ceil} \left( \frac{-\log(1 - \frac{i(T-D)}{M})}{\log(1 + i)} \right),$$

where  $i = I/12$  is the monthly interest rate and `ceil` is the `math.ceil` function. (Note, after modifying the `session3.py`, you will have to restart the kernel using the toolbar above to reload the latest version.)

```
[20]: import session3 as s3
      s3.numberMonths(500000,4000)/12
```

13.833333333333334

```
[21]: s3.numberMonths(500000,4000,interest=0.05)/12
```

14.75

### Case 6b. Mortgage Calculator II

Write a function `monthlyPayment` in module `session3` that calculates the monthly payment needed to pay off a mortgage in a given number of months. The function has four input arguments: `total`, `months`, `interest`, and `downpay`. Let the default values for `interest` be 0.0425 and for `downpay` be 0. Label the four arguments  $T$ ,  $N$ ,  $I$ ,  $D$  respectively. The monthly payment  $M$  is given by the formula

$$M = \frac{(1+i)^N}{(1+i)^N - 1} i(T - D),$$

where  $i = I/12$  is the monthly interest rate. Round the answer to two decimal places using the `round` function.

```
[22]: s3.monthlyPayment(500000,12*30)
```

2459.7

```
[23]: s3.monthlyPayment(500000,12*30,interest=0.05)
```

2684.11

The two functions are below.

```
[ ]: import math
def numberMonths(total,monthly,interest=0.0425,downpay=0):
    i=interest/12
    return math.ceil(-math.log(1-i*(total-downpay)/monthly)/math.log(1+i))

def monthlyPayment(total,months,interest=0.0425,downpay=0):
    i=interest/12
    return round((1+i)**months*(total-downpay)*i/((1+i)**months-1),2)
```

Note that it is easier to debug if you dissected the formula into small chunks, as below

```
[ ]: import math
def numberMonths(total,monthly,interest=0.0425,downpay=0):
    i=interest/12
    A=i*(total-downpay)/monthly
    top=-math.log(1-A)
    bottom=math.log(1+i)
    return math.ceil(top/bottom)

def monthlyPayment(total,months,interest=0.0425,downpay=0):
    i=interest/12
    top=(1+i)**months*i*(total-downpay)
    bottom=(1+i)**months-1
    return round(top/bottom,2)
```