

## Session 3. Reading Documentation and Debugging

### 1. Reading Documentation

**Method 1:** Using `help` and `dir` within Python.

```
[1]: help(print)
```

Help on built-in function `print` in module `builtins`:

```
print(...)  
    print(value, ..., sep=' ', end='\n', file=sys.stdout, flush=False)  
  
    Prints the values to a stream, or to sys.stdout by default.  
    Optional keyword arguments:  
    file: a file-like object (stream); defaults to the current sys.stdout.  
    sep:  string inserted between values, default a space.  
    end:  string appended after the last value, default a newline.  
    flush: whether to forcibly flush the stream.
```

```
[2]: import math  
     help(math.ceil)
```

Help on built-in function `ceil` in module `math`:

```
ceil(...)  
    ceil(x)  
  
    Return the ceiling of x as an Integral.  
    This is the smallest integer >= x.
```

```
[3]: dir(math)
```

```
['__doc__', '__loader__', '__name__', '__package__', '__spec__', 'acos', 'acosh', 'asin',  
'asinh', 'atan', 'atan2', 'atanh', 'ceil', 'copysign', 'cos', 'cosh', 'degrees', 'e', 'erf',  
'erfc', 'exp', 'expm1', 'fabs', 'factorial', 'floor', 'fmod', 'frexp', 'fsum', 'gamma',  
'gcd', 'hypot', 'inf', 'isclose', 'isfinite', 'isinf', 'isnan', 'ldexp', 'lgamma', 'log',  
'log10', 'log1p', 'log2', 'modf', 'nan', 'pi', 'pow', 'radians', 'sin', 'sinh', 'sqrt',  
'tan', 'tanh', 'tau', 'trunc']
```

```
[ ]: dir(__builtin__)
```

**Method 2:** Search on Google.

Examples of what to search:

- How to round up in Python?
- f-string formatting in Python 3
- Tutorial on functions in Python 3.
- "[Copy/Paste the error message and enclose with quotes]"

## Q1. Mortgage Calculator I

Write a function `numberMonths` that calculates how many months it would take to pay off a mortgage given the monthly payment. The function has four input arguments: `total`, `monthly`, `annualInterest`, and `downpay`. Let the default values for interest be 0.0425 and for downpay be 0. Label the four arguments  $T$ ,  $M$ ,  $I$ ,  $D$  respectively. The number of months needed  $N$  is given by the formula

$$N = \text{ceil} \left( \frac{-\log(1 - \frac{i(T-D)}{M})}{\log(1 + i)} \right),$$

where  $i = I/12$  is the monthly interest rate and `ceil` is the `math.ceil` function.

```
[5]: print('Number of years needed to pay off mortgage:', numberMonths(500000,4000)/12)
```

Number of years needed to pay off mortgage: 13.833333333333334

```
[6]: print('Updated number of years:', numberMonths(500000,4000,interest=0.05)/12)
```

Updated number of years: 14.75

## 2. Debugging

The following cells illustrate an efficient method of debugging based on isolating the problem and reproducing it in the simplest manner.

```
[7]: import math
def numberMonths(total,monthly,interest=0.0425,downpay=0):
    T=total
    M=monthly
    I=interest
    D=downpay
    return math.ceil(-math.log(1-I(T-D)/M)/math.log(1+I))
numberMonths(500000,4000)/12
```

```
-----
TypeError                                Traceback (most recent call last)

<ipython-input-7-41abbd54549f> in <module>()
      6     D=downpay
      7     return math.ceil(-math.log(1-I(T-D)/M)/math.log(1+I))
----> 8 numberMonths(500000,4000)/12

<ipython-input-7-41abbd54549f> in numberMonths(total, monthly, interest, downpay)
      5     I=interest
      6     D=downpay
----> 7     return math.ceil(-math.log(1-I(T-D)/M)/math.log(1+I))
      8 numberMonths(500000,4000)/12

TypeError: 'float' object is not callable
```

### A. Recreating the error outside of the function

```
[ ]: T=500000
      M=4000
      I=0.0425
      D=0
      math.ceil(-math.log(1-(I/12)*(T-D)/M)/math.log(1+(I/12)))
```

### B. Dissecting the line containing the error

```
[ ]: T-D

[ ]: I*(T-D)

[ ]: I*(T-D)/M

[ ]: 1-I*(T-D)/M

[ ]: math.log(-4.3125)
```

### C. Correcting the logic (this time building up one component at a time)

```
[ ]: T=500000
      M=4000
      I=0.0425
      D=0
      math.ceil(-math.log(1-(I/12)*(T-D)/M)/math.log(1+(I/12)))
```

### D. Putting correct logic back into function

```
[ ]: import math
      def numberMonths(total,monthly,interest=0.0425,downpay=0):
          T=total
          M=monthly
          I=interest
          D=downpay
          return math.ceil(-math.log(1-(I/12)*(T-D)/M)/math.log(1+(I/12)))
      print('Number of years needed to pay off mortgage:', numberMonths(500000,4000)/12)
```

### (Optional: Shortening the code to work with original named variables directly.)

```
[ ]: import math
      def numberMonths(total,monthly,interest=0.0425,downpay=0):
          i=interest/12
          A=i*(total-downpay)/monthly
          top=-math.log(1-A)
          bottom=math.log(1+i)
          return math.ceil(top/bottom)
      print('Number of years needed to pay off mortgage:', numberMonths(500000,4000)/12)
```

## Q2. Mortgage Calculator II

Write a function `monthlyPayment` that calculates the monthly payment needed to pay off a mortgage in a given number of months. The function has four input arguments: `total`, `months`, `interest`, and `downpay`. Let the default values for `interest` be 0.0425 and for `downpay` be 0. Label the four arguments  $T$ ,  $N$ ,  $I$ ,  $D$  respectively. The monthly payment  $M$  is given by the formula

$$M = \frac{(1+i)^N}{(1+i)^N - 1} i(T - D),$$

where  $i = I/12$  is the monthly interest rate. Round the answer to two decimal places using the `round` function.

```
[30]: monthlyPayment(500000,12*30)
```

2459.7

```
[31]: monthlyPayment(500000,12*30,interest=0.05)
```

2684.11