# X-formers

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#### **Need for Transformer variants**

- Vanilla transformers are inefficient at processing long sequences
  - Computation and memory complexity of self-attention is high
- Doesn't use structural/inductive bias of input data
  - Variants: Introduce structural bias, regularization, pre-training on large-scale unlabeled data
- To handle specialized downstream tasks/applications

### **Taxonomy for X-former variants**

- Many variants address multiple needs
  - Example: Sparse Transformers addresses computational requirements and adds structural prior
- Taxonomy should be based on the ways in which they improve vanilla x-former
  - Architecture modification
  - Pre-training
  - Applications

#### **Vanilla Transformer**

- Seq2Seq model
  - Encoder usually multiple stacked on top of each other
  - Decoder - usually multiple stacked on top of each other

#### Encoder

- Multi-head self-attention
- Position-wise feed-forward network(FFN)
- Residual connection
- Layer Norm

#### Decoder

- Multi-head self-attention (autoregressive in nature)
- Cross attention with encoder state
- o FFN

### **Vanilla Transformer**

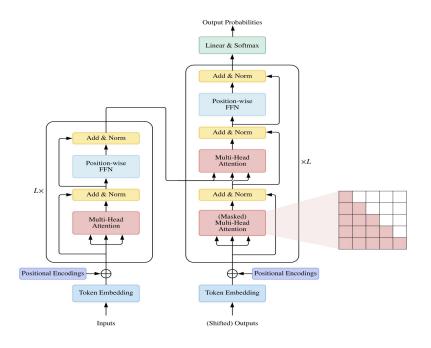


Fig. 1. Overview of vanilla Transformer architecture

#### **Attention Module**

Attention(Q, K, V) = softmax 
$$\left(\frac{QK^{\top}}{\sqrt{D_k}}\right)$$
 V = AV,

MultiHeadAttn(
$$\mathbf{Q}, \mathbf{K}, \mathbf{V}$$
) = Concat(head<sub>1</sub>, · · · , head<sub>H</sub>) $\mathbf{W}^{O}$ , where head<sub>i</sub> = Attention( $\mathbf{Q}\mathbf{W}_{i}^{Q}, \mathbf{K}\mathbf{W}_{i}^{K}, \mathbf{V}\mathbf{W}_{i}^{V}$ ).

#### **Self vs Masked vs Cross Attention**

- Self: Q = K = V = X
- Masked: Restrict attention to certain parts of input. Ex: Decoder restricting attention to previous positions
- Cross-Attention:
  - Queries are projected from the previous layer.
  - Keys and values are projected from the encoder output

### **Position wise FFN**

$$FFN(\mathbf{H'}) = ReLU(\mathbf{H'W}^1 + \mathbf{b}^1)\mathbf{W}^2 + \mathbf{b}^2,$$

Provides rich representation to the attention outputs

### **Residual connection + Layer Norm**

$$H' = LayerNorm(SelfAttention(X) + X)$$
  
 $H = LayerNorm(FFN(H') + H'),$ 

- Residual connections
  - helps with vanishing gradient problem
  - o retain information about the original input

# **Transformer - model usage**

- Encoder-Decoder
  - Full transformer architecture
  - Seq2seq modeling like Neural machine translation
- Encoder
  - classification / sequence labeling
- Decoder
  - Sequence generation

### **Model Analysis**

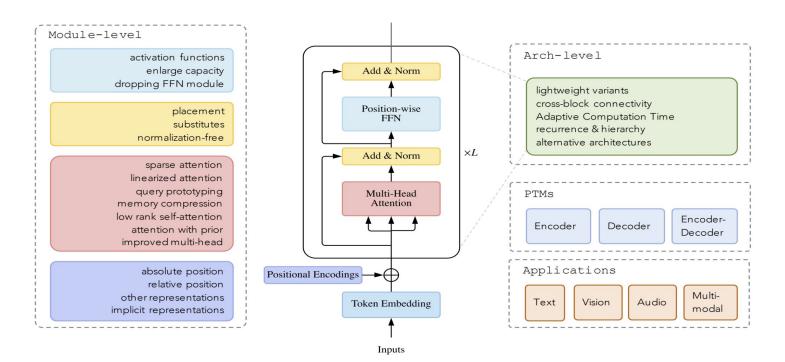
Module	Complexity	#Parameters
self-attention	$O(T^2 \cdot D)$	$4D^2$
position-wise FFN	$O(T \cdot D^2)$	$8D^2$

- T Sequence length; D Hidden dimension
- Short-sequence: Bottleneck is FFN
- Long-sequence: Bottleneck Self-Attention; In computation and space
  - Pixel level image generation, long text document modeling are infeasible

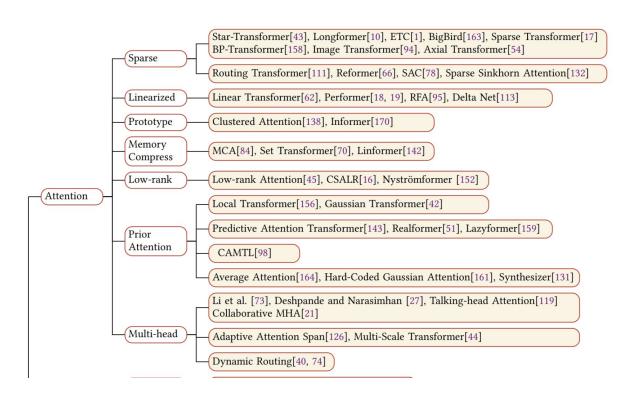
#### **Self-Attention vs Conv vs FC vs Recurrent**

- Conv vs SA: Convolutional network need to stack conv layers deep to get global receptive field. SA can get global receptive field with constant number of layers.
- FC vs SA: SA is flexible in handling variable-length inputs
- Recurrent vs SA: Constant sequential operations make SA more parallelizable and better at long-range modeling
- Inductive bias:
  - Conv layers impose translation invariance and locality with shared local kernel functions.
  - Recurrent layers impose temporal invariance and locality
  - TF make very little use of structural info and is prone to overfitting on small-scale data

# **Taxonomy of Transformers**



#### **Attention level variants**



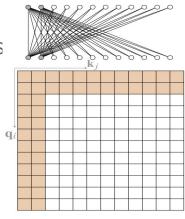
# **Sparse Attention**

- Learned Attention matrix is often sparse across most data points
- Incorporate this information to reduce the number of query-key pairs computed

$$\hat{\mathbf{A}}_{ij} = \begin{cases} \mathbf{q}_i \mathbf{k}_j^\top & \text{if token } i \text{ attends to token } j, \\ -\infty & \text{if token } i \text{ does not attend to token } j, \end{cases}$$

### **Sparse Attention - Global Attention**

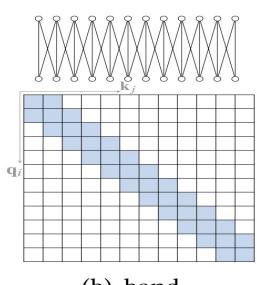
- Global nodes: Retain the ability to model long range deps
- Serve as the hub for information propagation between nodes
- Global nodes attend to all nodes in the sequence



(a) global

### **Sparse Attention - Band Attention**

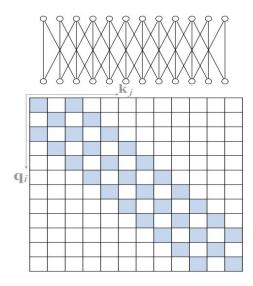
- Sliding window attention
- Aka local attention
- Restrict each query to attend to it its neighbor nodes



(b) band

### **Dilated Attention**

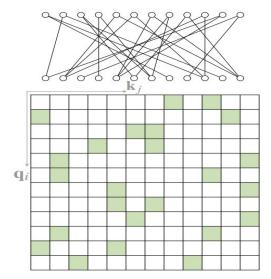
- Idea is similar to dilation in CNN
- Increased receptive field without increasing computation
- Aka strided attention



(c) dilated

#### **Random Attention**

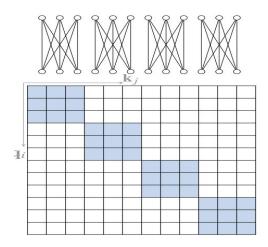
- Randomly sampled nodes for each query
- Random graphs can have similar spectral properties with complete graphs that leads to fast mixing time for random walking on graphs



(d) random

#### **Block Local Attention**

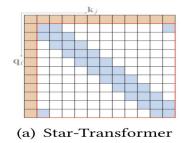
- Segments input sequence into several non-overlapping query blocks
- Queries in a query block attend to only the keys in the corresponding block

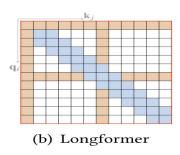


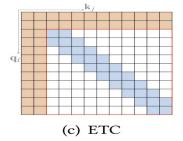
(e) block local

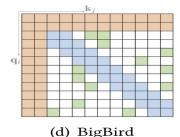
### **Compound Sparse Attention**

- Combination of multiple attention patterns
- Star-Transformer: Band Attention + Global Attention
- Longformer: Band Attention + Internal global-node attention + dilated window attention in upper layers
- Extended Transformer Construction(ETC): Band + External-node global attention
- BigBird: Band + Global + Random Attention to approximate full attention







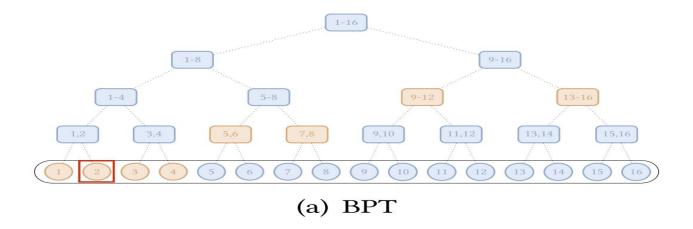


### **Compound Sparse Attention**

- Sparse Transformer: Different sparse patterns for different types of data
- Data with periodic structure(Images):
  - Composition of band attention and strided attention
- Data without periodic structure(text):
  - Block local attention + global attention

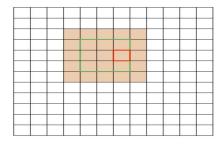
### **Extended Sparse Attention**

- For text: BP transformer
  - Binary tree with tokens as leaf nodes and internal nodes as span nodes containing many tokens

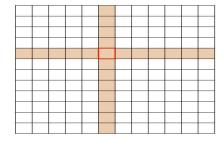


### **Extended Sparse Attention**

- Image Transformer:
  - flattens image pixels in raster-scan order and applies block local sparse attention
  - 2D block local attention with query and memory blocks arranged in 2D
- Axial Transformer:
  - Applies independent attention modules over each axis of the image
  - Mixes information along one axis while keeping information from the other axis independent



(b) block local (2D)



(c) axial (2D)

# **Content-based Sparse Attention**

- Sparse graph is created based on the input content
- Idea: Select those keys that are likely to have large similarity scores with the given query
- Routing Transformer:
  - K-means clustering to cluster both queries and keys to the same set of centroid vectors
  - Each query attends only to the keys that belong to the same cluster
- Reformer
  - Locality sensitive hashing to select key-value pairs for each query
  - Each query attends only to the keys within the same hashing bucket
  - LSH function to hash queries and keys into several buckets with similar items fall in the same bucket with high probability

### **Content-based Sparse Attention**

#### Sparse Adaptive Connection(SAC)

- Input sequence as a graph and learns to construct attention edges to improve task specific performances
- Uses adaptive sparse connection using LSTM edge predictor to construct edges between tokens
- Uses reinforcement learning to predict edges

#### Sparse Sinkhorn Attention

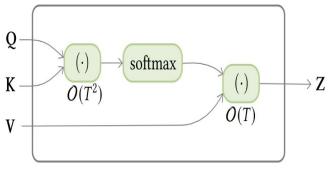
- Splits queries and keys into several blocks and assigns a key block to each query block
- The assignment of key block to query block is done via sorting network which uses Sinkhorn normalization
- Permutation matrix representing the assignment

- Attention computation is quadratic in sequence length T.
- O(T^2 D)
- How to get linear computation complexity?

Attention(Q, K, V) = softmax 
$$\left(\frac{QK^{\top}}{\sqrt{D_k}}\right)V = AV$$
,

- N, M sequence lengths of queries and keys/values
- Dk; Dv dimensions of queries/keys and values
- Q N x Dk; K M x Dk; V M x Dv;
- Q.K^T N x M; (Q.K^T)V = N x Dv => O(T^2.D) => O(T^2) when T >> D
- Q(K^T.V) O(T.D^2) => O(T) when T >> D

- Unnormalized attention A\_hat = exp(Q.K^T)
- Replace this unnormalized attention with a torch.matmul(phi(Q), phi(K)^T)
- Phi feature map applied in row-wise manner
- Standard Self-Attention  $Z = D^{-1}\hat{A}V$ , where  $D = diag(\hat{A}1_T^T)$ ;
- Because  $A_{hat} = \exp(Q.K^T) = phi(Q).phi(K)^T$
- And, Dot product is associative
- phi(Q).(phi(K)^T . V)



(a) standard self-attention (b) linearized self-attention

Q

K

V

 $(\cdot)$ 

O(T)

O(T)

ightarrow Z

- Feature map used in Linear Transformer: phi(x) = elu(x) + 1
- The feature map doesn't approximate dot product attention
- Empirically performs on par with standard transformer
- Performer
  - Uses random feature maps that approximate the scoring function of Transformer

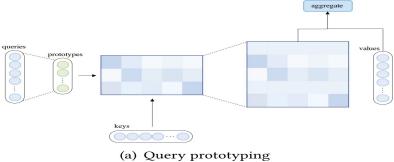
$$\phi(\mathbf{x}) = \frac{h(\mathbf{x})}{\sqrt{m}} [f_1(\omega_1^\top \mathbf{x}), \cdots, f_m(\omega_m^\top \mathbf{x}), \cdots, f_l(\omega_1^\top \mathbf{x}), \cdots, f_l(\omega_m^\top \mathbf{x})],$$
  
$$f_1, \cdots, f_l : \mathbb{R} \to \mathbb{R} \text{ and } h : \mathbb{R}^D \to \mathbb{R}.$$

#### **Performer variants**

- They vary in the number of functions the feature maps take and h(x)
- Some variants
  - L = 2; f1 = sin; f2 = cos; h(x) = exp( I2norm(x))/2
  - $\circ$  L=1; f1 = exp; h(x) = exp(-l2norm(x))/2
  - $\circ$  L=1; f1 = RELU; h(x)=1 (Protein sequence modeling and NMT find this effective)

# **Query Prototyping and Memory Compression**

- Idea: Reduce the number of queries or key-value pairs
- Prototype queries:
  - Several prototype queries serve as the main source to compute attention matrix
  - Clustered Attention: groups queries into clusters and compute attention distribution for cluster centroids. All queries in the cluster share the attention distribution of the centroid
  - o Informer selects prototype queries using sparsity measurement
    - KL divergence between query's attention distribution and discrete uniform distribution
    - Select Top-u queries as prototype



### **Memory Compressed Attention**

- Idea: Reduce the number of key-value pairs before applying attention
- MCA:
  - Uses strided convolution with local attention
  - Can capture global context
  - Reduces number of keys and values by a factor of kernel size k
- Set Transformer
  - External trainable global nodes
    - Summarizes information from inputs
    - Summarized representations serve as a compressed memory that the inputs attend to
    - Shown to perform with linear computational complexity in sequence length

# **Other Compressed variants**

- Linformer
  - Linear projections to project keys and values from length n to smaller length k
  - Assumes an input sequence length
  - Cannot be used autoregressively
- Poolingformer
  - Two-level attention
    - Sliding window
    - Compressed memory attention
  - Compression achieved by max pooling, pooling with dynamic convolution

### **Low rank Self-Attention**

- Idea: Self-Attention matrix is often low-rank
- Low-rank parameterization:
  - Model the low-rank property as inductive bias by limiting the dimension of query/keys Dk
  - Self-attention matrix decomposed into low-rank attention module with small Dk to capture long-range non-local interactions and a bank attention module to capture local dependencies
- Low-rank Approximation:
  - Performer variants were inspired from kernel approximation with feature maps
  - Decompose attention matrix A into C.G.C where feature maps are used to approximate G

# Nyström based Attention approximation

- Another form of low rank approximation
- Idea:
  - Select m landmark nodes from T inputs with down-sampling(strided average pooling)

$$\tilde{\mathbf{A}} = \operatorname{softmax} \left( \mathbf{Q} \tilde{\mathbf{K}}^{\top} \right) \left( \operatorname{softmax} \left( \tilde{\mathbf{Q}} \tilde{\mathbf{K}}^{\top} \right) \right)^{-1} \operatorname{softmax} \left( \tilde{\mathbf{Q}} \mathbf{K}^{\top} \right)$$

- Inverse doesn't always exist
- Identity matrix could be added to make sure that the inverse always exists
- Nyström-former used Moore-Penrose pseudoinverse in place of inverse

## **Attention with Prior**

- Attention matrix = softmax(QK^T)
  - Generated using input sequences
- Prior: Attention distribution stemming from source other than input, referred as prior
- Fusion of two attention distribution matrices can be done by computing a weighted sum of the scores corresponding to the prior and generated attention before applying softmax

## **Priors that model locality**

- Text data usually exhibits preference for locality
- This can be modelled as a prior attention
- Multiply the generated attention distribution with some Gaussian density
  - o Gaussian density Gij indicates higher probability that the i-th input attend to j-th input
  - Pi predicts a central position for each query Qi using a FFN

$$G_{ij} = -\frac{(j - p_i)^2}{2\sigma^2},$$

- Gaussian Transfomer
  - $G_{ij} = -|w(i-j)^2 + b|$

## **Priors from lower modules**

- Observation: Attention distributions are similar in adjacent layers
- Idea: Use attention distribution from previous layer as a prior

$$\hat{\mathbf{A}}^{(l)} = w_1 \cdot \mathbf{A}^{(l)} + w_2 \cdot g(\mathbf{A}^{(l-1)})$$

- Predictive Attention Transformer
  - Apply a 2D convolution to previous attention scores
  - Final attention = convex combination of generated attention score and convoluted scores
- Realformer
  - Directly adds previous attention scores resembling a residual skip connection
- Lazyformer
  - Shares attention maps between a number of adjacent layers
  - Attention maps computed once but reused several times as prior

# **Multi-task adapters**

- Adapters: Task-dependent modules attached in specific locations of a pre-trained network for cross-task efficient parameter sharing
- Idea: Use trainable attention priors that depends on task encoding

$$M(\mathbf{z}_i) = \bigoplus_{j=1}^m A'_j(\mathbf{z}_i), \quad A'_j(\mathbf{z}_i) = A_j \gamma_i(\mathbf{z}_i) + \beta_i(\mathbf{z}_i)$$

- Zi depends on task specific encoding
- Gamma and Beta are Feature wise linear modulation functions
- This trainable prior is added to attention scores of upper layers in pre-trained transformers

# **Attention with only prior**

- Idea: No generated attention. Only prior attention distribution
- Average Attention network:
  - Discrete uniform distribution as the only source of attention distribution
  - A FFN gating layer on top of the average attention module
  - Used in decoder side
  - Decoder like RNN and avoids O(T^2) complexity
- Gaussian distribution as prior
  - Achieves comparable performance to baseline machine translation
- Synthesizer
  - Replace generated attention with learnable, randomly initialized attention scores
  - Replace attention score with a FFN that is conditioned on the querying input

## **Multi-head Attention variants**

- Multi-heads: Allows to attend to information from different representation subspaces at different positions
- Do the attention heads capture distinct features?
- Attention heads don't interact with each other
- Variants
  - Encourage distinction learned features between attention heads
  - Add mechanisms to guide attention head behaviors
- Regularization terms to loss function to encourage diversity among attention heads
- Observation: Multiple attention heads pay attention to CLS and SEP tokens
  - Auxillary loss: Frobenius norm between attention distribution maps and predefined attention patterns

## **Multi-head Attention variants**

- Talking-head Attention
  - Linearly projects the generated attention scores from hk to h heads
  - Applies softmax
  - Projects output to hv heads for value aggregation
    - This moves information between attention heads in a learnable fashion
- Collaborative Multi-head Attention
  - Shared query and key projection
  - o In the normal attention shown below, Wq and Wk are different for each head

MultiHeadAttn(
$$\mathbf{Q}, \mathbf{K}, \mathbf{V}$$
) = Concat(head<sub>1</sub>, · · · , head<sub>H</sub>) $\mathbf{W}^{O}$ , where head<sub>i</sub> = Attention( $\mathbf{Q}\mathbf{W}_{i}^{Q}, \mathbf{K}\mathbf{W}_{i}^{K}, \mathbf{V}\mathbf{W}_{i}^{V}$ ).

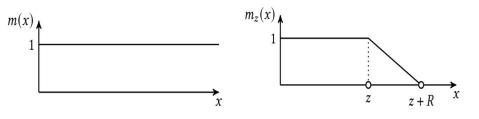
# **Multi-head with Restricted spans**

- Full attention span: A query can attend to all key-value pairs
- Observation: Some heads focus on local context and some heads attend to broader contexts
- Restricting attention spans on some heads can save memory footprint and computational time while allowing to extend to long sequences
- Learnable attention span
  - Restricted attention span are implemented via attention masks
  - Learnable scalar z represents a distance/span value
  - Character-level language modeling show adaptive-span models outperform baseline models

# **Multi-head with Restricted span**

#### Multi-scale Transformer

- Fixed attention span with different heads in different layers using a different max span
- Scales are designed from an intuitive linguistic perspective and empirical observation
- Higher layers have more scale/span length
- Lower layers are confined to smaller scale



 $m_z(x)$ 

(a) mask function for vanilla attention (b) mask function for adaptive span

(c) mask function for fixed span

# **Multi-head with Refined Aggregation**

 Multi-head attention usually concatenates attention head outputs and projects them to final output representation

$$\text{MultiHeadAttn}(Q, K, V) = \sum_{i=1}^{H} \text{Attention}(Q\mathbf{W}_{i}^{Q}, K\mathbf{W}_{i}^{K}, V\mathbf{W}_{i}^{V}\mathbf{W}_{i}^{O}).$$

- Idea: This aggregation doesn't fully exploit the expressiveness of multi-head attention
- Alternate aggregation:
  - Dynamic routing
  - EM routing
- Computational overhead is alleviated by applying complex aggregation to lower layers

## **Multi-head variants**

- Multi-query attention
  - Key-value pairs are shared among attention heads
  - Faster decode operations with minimal quality loss
- Usual Head size: Key dimension / H
  - Variant: Attention head size to be same as input sequence length

## **Module-level variant - Position**

- Self-Attention and position-wise FFN are permutation equivariant
  - Same set of inputs regardless of permutation will product same set of outputs with permutation matching the input permutation
- Position information has to be added
- Variants:
  - Absolute position representations
    - Position encoding for index t of size Dm is generated
    - Position encoding is added to token embeddings and fed to transformer

$$PE(t)_i = \begin{cases} \sin(\omega_i t) & \text{if } i \text{ is even,} \\ \cos(\omega_i t) & \text{if } i \text{ is odd,} \end{cases}$$

# **Position Encoding variants**

- Learned position embeddings for each position
  - Number of embeddings is limited to a maximum sequence length
  - Loses inductive bias
- Sinusoidal position representation with each frequency learned from data
  - More robust compared to hand-crafted position representation
- FLOATER
  - Positional representation as continuous dynamical system and adopts Neural ODE to enable end-to-end training
  - Inductive and flexible with a fully learnable approach
- Add positional encodings to each layer input and not just the first layer since positional information gets lost after first few layers

# **Relative Position Representation**

- Represent positional relationships between tokens as opposed to position of tokens
- Pairwise positional relationships between input elements could be more beneficial than position of elements
- Music Transformer uses relative position representation
- Transformer-XL use a sinusoidal encoding to represent positional relationship but fuses contents and position information
- DeBERTa utilizes position embeddings similar to Transformer-XL

# **Other Representations**

- TUPE Transformers with Untied Position Encoding
  - absolute position-to-position term
  - Relative content-to-content term
  - Bias term representing relative positional relationships

### Roformer

- Rotary Position Embedding to represent the position of a token by multiplying the affine transformed embedding of the input by a rotatory matrix
- Combines absolute and relative information

## Implicit encoding of position

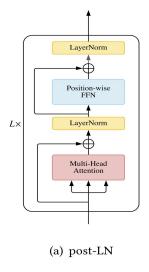
- Encode positional information in word embeddings
- Embedding function generalized to continuous function over positions
- R-Transformer
  - Model locality of sequential data with a local RNN
  - Inputs fed to local RNN and then to MHSA
- Conditional Positional Encoding:
  - Generate conditional position encodings with a 2-D convolution with zero-padding at each layer input
  - Convolution implicitly encodes position information

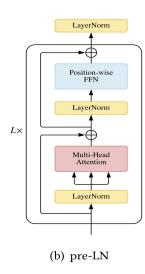
# **Position Representation on Decoder**

- Decoders use cross attention and masks (to limit attention to previous inputs)
- Masked self-attention is not permutation equivariant
- A model that only uses the decoder is capable of sensing position information without explicit position representation
- Removing explicit position information on decoders improve performance

# **Layer Norm**

- Layer Norm + Residual connection stabilize training of deep networks
- Where to apply Layer Norm?
  - Vanilla Transformer used Post-LN
  - Later transformers used Pre-LN





## **Layer Norm based variants**

- Empirical results show post-LN without learning warm-up lead to unstable training
  - Because of large gradients near output layer at initialization
  - Pre-LN doesn't suffer from this problem
- Post-LN outperforms pre-LN variants after convergence
- post-LN variants don't suffer from gradient imbalance
  - Amplification effect is the cause
    - Heavier dependency on residual branch leads to larger output shift in post-LN transformers
    - Remedy: Initialize parameters based on activation variations of sample data

# **Layer Norm substitutes**

- Layer Norm has learnable parameters which aren't very useful and increase risk of overfitting
- AdaNorm a normalization technique without learnable parameters
- Scaled L2 normalization
- PowerNorm
  - Modifies BatchNorm
    - Relaxes zero-mean normalization
    - Uses quadratic mean of the signal instead of variance
    - Uses running statistics of quadratic mean instead of using per-batch statistics

## **Normalization-free Transformers**

### ReZero

- Replaces LN module with a learnable residual connection
- $\circ$  H' = H + alpha \* F(H)
- o alpha is a learnable parameter with zero-initialization
- Better dynamic isometry for input signals and leads to faster convergence

## **Position-wise FFN**

- Simply stacking self-attention modules causes a rank-collapse
  - o Token-uniformity inductive bias
- FFN mitigates this issue
- Variants:
  - Replace ReLU with Swish function f(x) = x \* sigmoid(beta \* x)
  - GPT replaces ReLU with GELU
  - Mini-dalle replaces ReLU with GLU

# **Replacing FFN**

- Idea: Replace FFN with similar structures with more parameters thereby improving model capacity
- Product-Key memory layers
  - A query network
  - A key selection module containing two sets of sub-keys
  - Value lookup table
  - Project input to a latency space using query network
  - Compare generated query to keys that are cartesian product of two sub-keys
  - Get K-nearest neighbors; Aggregate them to produce final output
  - Experiments on large-scale language modeling improved performance with negligible overhead

# **Replacing FFN**

- Mixture-of-Experts(MoE)
  - Sparsely-gated MoE instead of FFN
    - Experts are several FFNs
    - Outputs: weighted sum of FFN outputs using gate values computed by routing function
    - Routing function is learnable. Assigns tokens to experts
    - Only the experts with top-k gate values are activated in forward pass
- Switch Transformer
  - Routes using only a single expert with the largest gate value
  - Auxillary loss function to load balance between experts
- Top-k routing with expert prototyping
  - Top-k prototype groups and top-1 routing within group
- Instead of learnable routing function, hash function can be used
  - Tokens are hashed to fixed number of buckets(experts)

# **Dropping FFN**

- Observation: Replacing ReLU activation in FFN with softmax and dropping bias term turns FFN into an attention module where position-wise inputs attend to a global key-value memory
- Idea: Drop FFN by adding a set of learnable global key-value pairs
- In the decoder of a transformer, FFNs contribute very little with their large number of parameters.
  - Empirical results show improvement in inference and training with little loss of performance

## **Architecture-level variants**

- Lite-Transformer
  - Replaces attention module with a two-branch structure
    - Attention to capture long-range contexts
    - Depth-wise convolution and linear layers to capture local dependencies
- Funnel Transformer
  - Length of the hidden sequence is gradually reduced using pooling along the sequence dimension and recovered using up-sampling
  - Reduces FLOPs and memory
- DeLighT Transformer
  - Replaces transformer block with three sub-modules
    - Expand-and-reduce to learn wider representations with low computation requirements
    - Single-head self-attention to learn pairwise interaction
    - Reduce-and-expand FFN
  - Leads to a deeper network with fewer parameters and FLOPs

## **Cross-Block connectivity**

- In a deep encoder-decoder transformer
  - Cross-attention module in the decoder only utilize the final outputs of the encoder
  - The error/feedback signal has to traverse along the depth of the encoder
  - Transformers are more susceptible to optimization issues like vanishing gradients

### Transparent Attention:

- Weighted sum of encoder representations at all encoder layers
- Use that as input in the cross attention module
- This shortens the path for the error signal to the encoders and eases the optimization of deeper
   Transformers

### Feedback Transformer

- Vanilla Transformer: Decoders were attending history representations of lower layers
- Feedback mechanism where each position in the decoder can attend to history representation from all layers

## **Adaptive Computation Time**

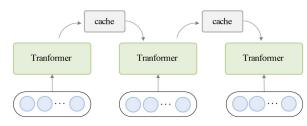
- Idea: Computation time conditioned on the inputs
- More computation for harder data and less computation for easy data
  - Efficiency for easy examples
  - Feature refinement for hard examples
- Universal Transformer
  - Recurrence-over-depth mechanism that iteratively refines representations for all symbols using a module that is shared over depth
  - Per-position dynamic halting mechanism that calculates a halting probability for each symbol at every time step
  - If halting prob > threshold, representation for subsequent time steps is unchanged
  - Recurrence is stopped when all symbols halt or max number of steps is reached

## **Adaptive Computation Time**

- Conditional Computation Transformer
  - Adds a gating module to each self-attention and FFN to decide whether to skip the current layer
  - Auxillary loss that encourages the model to adjust the gating modules to match the practical computation cost to the available computation budget
- Adapt the number of layers to each input in order to achieve good speed-accuracy trade-off
  - Choosing to exit early
  - Add an internal classifier at each layer and jointly train all classifiers
  - Classifier output says yes or no to the exit question
  - o Criteria:
    - Entropy of output probability distribution of current layer
    - Number of times predictions remain unchanged to decide to whether to exit
    - Window-based uncertainty criterion to achieve token-level partial exiting in sequence labeling tasks
    - Voting-based exit strategy that considers each layer predictions of all past internal classifiers to infer the correct label and to decide whether to exit

# **Divide and Conquer**

- Decompose input sequence into finer segments
- Transformers are reused for different input segments
- Recurrent Transformers
  - A cache memory is maintained to incorporate history information
  - Cache is an additional input to the network
  - Network writes hidden state to cache
  - Example: Transformer-XL
- Compressive Transformer
  - Extends the cache with two levels of memory
    - Activations from previous segment
    - Compressed activations from older segments
- Memformer
  - Introduces cross attention to encoder
    - Allows encoder to attend to the memory
    - Memory slot attention on top of the encoder output to write the memory for next segment



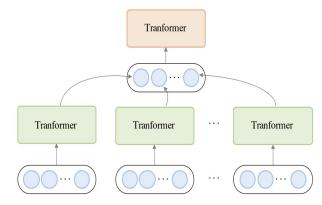
(a) Recurrent Transformer

### **Recurrent Transformer**

- Extended context:
  - Transformer-XL: L x Nmem; Nmem is the length of cached memory sequence
  - Compressive Transformer: L x (Nmem + c Ncm); c is compression rate; Ncm is length of compressed memory
- Notes to avoid expensive BPTT:
  - Local loss functions where original memories are constructed from compressed memories
  - Memformer uses: Memory Replay Back-Propagation algorithm which replays the memory at each timestep to accomplish back propagation over long unrolls
- Alternate ways to add recurrence to transformers
  - ERNIE-Doc
  - Compressed single vector representation of divided segments

## **Hierarchical Transformer**

- Decompose inputs hierarchically into elements of finer granularity
- Low-level features are first fed to a Transformer encoder
  - Outputs are aggregated to form a high level feature -> High-level transformer
- Allows modeling of long inputs with limited resources
- Potential to generate richer representations that are beneficial to tasks



(b) Hierarchical Transformer

## **Hierarchical Transformers**

#### Document translation

- Previous sentences from both source and target are used in translating a new sentence
- Attention is used to summarize low-level information

#### HIBERT

- Encodes a document of text by first learning sentence representations
- Then uses sentence representations to encode document-level representations

### Hi-Transformer

- Sentence Transformer
- Document Transformer
- Learns hierarchically document context aware sentence representations
- Document context-aware sentence representations are fed to another sentence transformer to improve sentence context modeling

# **Hierarchical TF for richer representation**

- Task specific rich representations
- TENER
  - Low-level TF encoder to encoder character features which is concatenated to word embeddings as input to high-level TF encoder
- Vision Transformer
  - Divide input image into several patches that serve as basic input elements to TF
  - Loses pixel information within patches
  - TNT: Fixes this issue by using inner TF block that transforms pixel representations and an outer
     TF block that takes fused vectors of patch representations and pixel representations as input

## **Alternate Architectures**

- Macaron Transformer
  - Replaces each transformer block with FFN-attention-FFN variant
- Sandwich Transformer
  - Reorganizes attention modules and FFN modules such that attention modules are mainly located in lower layers and FFN modules in upper layers
  - Improves perplexity on multiple language models without increasing parameters
- Mask Attention Network
  - Prepends a dynamic mask attention module to self-attention module in each TF block
  - Mask is conditioned on token representations
  - Effectively models model locality in text data
- Evolved Transformer
  - Uses Evolution based architecture search to come up with a TF architecture
  - Shows consistent improved performance on language tasks
- DARTSformer
  - Uses Differentiable architecture search for searching architecture and outperforms ET

## **Pre-trained Transformer Variants**

- Transformers are suitable for learning universal representations
- Transformers are used for producing pre-trained that can be later fine-tuned for downstream tasks
- Pre-training is usually combined with self-supervised tasks
- Encoder only
  - o BERT with Masked Language Modeling and Next Sentence Prediction as self-supervision
  - RoBERTa: Removed NSP from BERT
- Decoder only
  - O GPT, GPT-2, GPT-3
  - Impressive few shot performance
- Encoder-Decoder
  - o BART model is able to perform both natural language understanding and generation

## References

Survey of Transformers - https://arxiv.org/pdf/2106.04554.pdf