



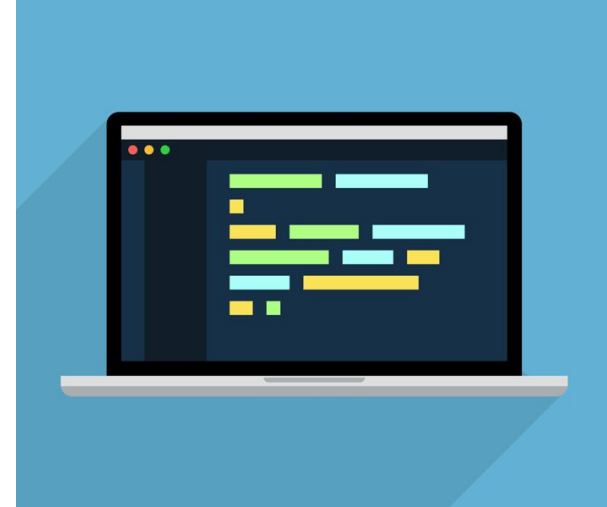
20

Stacks

by Gladden Rumao
CSA 221 : DSA

Quick Recap :

- **Linked List**
 - **Singly**
 - **Doubly**
- **Insert and delete**
 - **At beginning**
 - **At end**



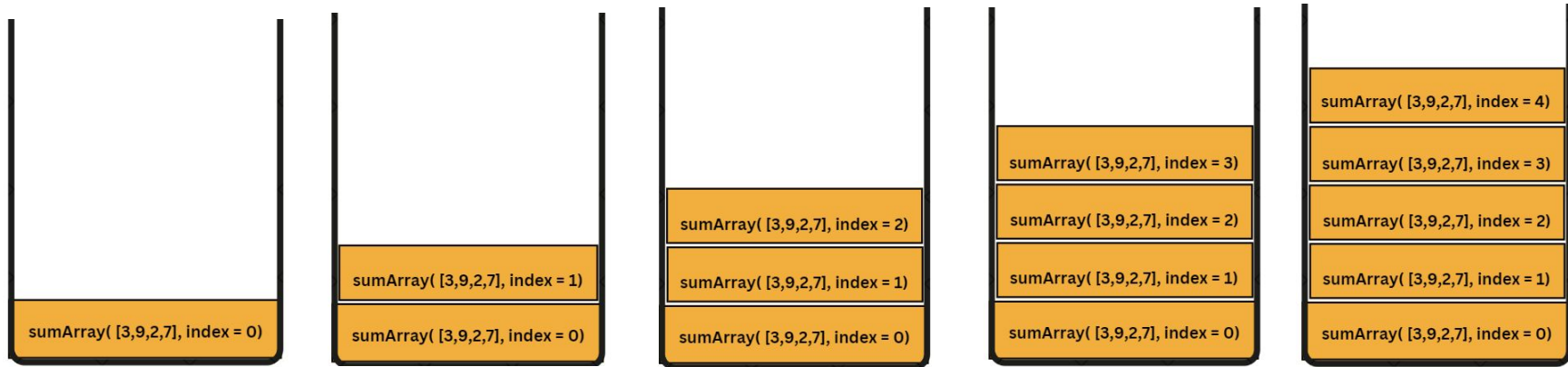
Pre-read Quiz Time!

Introduction to Stack



Can you tell ?

One use-case of it you have already seen and used

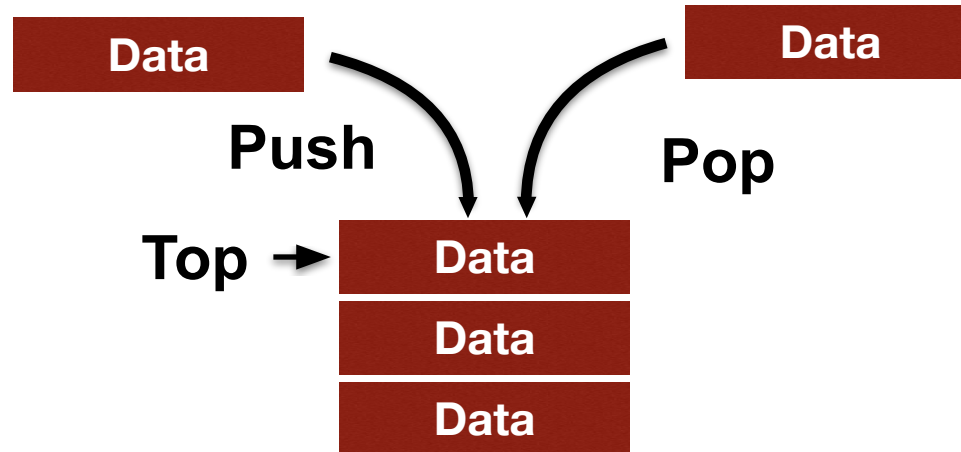


Recursive Stack

What is a stack?

What is a Stack ?

- A stack is a one-ended linear data structure which models a real world stack by having two primary operations, namely push and pop.
- A stack follows the **Last In, First Out (LIFO) principle**, where the last element pushed is the first to be popped.



What is a Stack ?

Instructions

```
pop()  
push('Onion')  
push('Celery')  
push('Watermelon')  
pop()  
pop()  
push('Lettuce')
```

Apple

Potato

Cabbage

Garlic

What is a Stack ?

Instructions

→ pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')

Apple

Potato

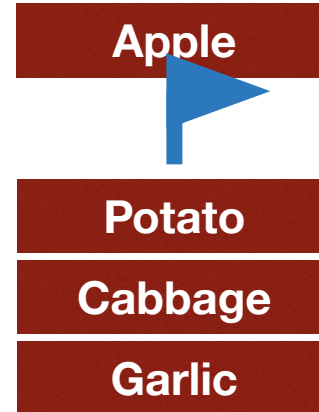
Cabbage

Garlic

What is a Stack ?

Instructions

→ pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')



What is a Stack ?

Instructions

→ pop()
push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')

Potato

Cabbage

Garlic

What is a Stack ?

Instructions

pop()
→ push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')

Potato

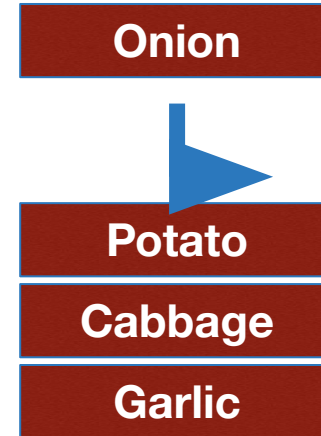
Cabbage

Garlic

What is a Stack ?

Instructions

pop()
→ push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')



What is a Stack ?

Instructions

pop()
→ push('Onion')
push('Celery')
push('Watermelon')
pop()
pop()
push('Lettuce')

Onion

Potato

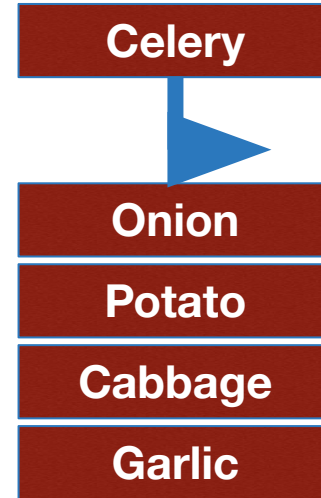
Cabbage

Garlic

What is a Stack ?

Instructions

```
pop()  
push('Onion')  
→ push('Celery')  
push('Watermelon')  
pop()  
pop()  
push('Lettuce')
```



What is a Stack ?

Instructions

```
pop()  
push('Onion')  
→ push('Celery')  
push('Watermelon')  
pop()  
pop()  
push('Lettuce')
```

Celery

Onion

Potato

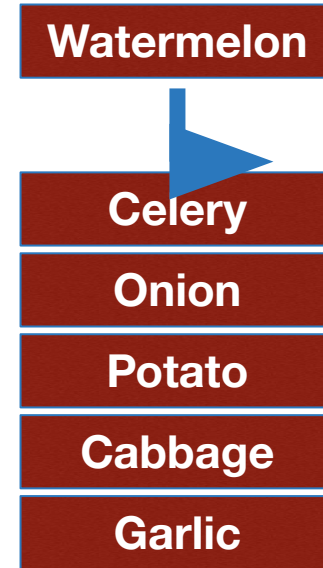
Cabbage

Garlic

What is a Stack ?


Instructions

```
pop()  
push('Onion')  
push('Celery')  
→ push('Watermelon')  
pop()  
pop()  
push('Lettuce')
```



What is a Stack ?

Instructions

pop()
push('Onion')
push('Celery')
 push('Watermelon')
pop()
pop()
push('Lettuce')

Watermelon

Celery

Onion

Potato

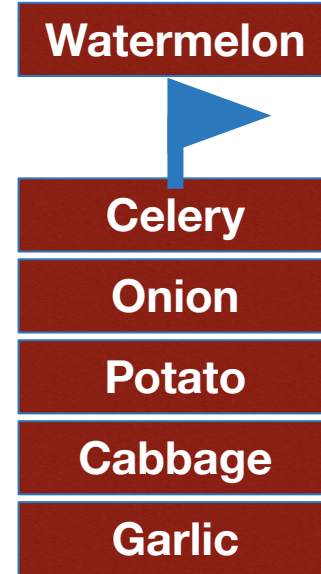
Cabbage

Garlic

What is a Stack ?

Instructions

```
pop()  
push('Onion')  
push('Celery')  
push('Watermelon')  
→ pop()  
pop()  
push('Lettuce')
```



What is a Stack ?

Instructions

```
pop()  
push('Onion')  
push('Celery')  
push('Watermelon')  
→ pop()  
pop()  
push('Lettuce')
```

| |
|---------|
| Celery |
| Onion |
| Potato |
| Cabbage |
| Garlic |

What is a Stack ?

Instructions

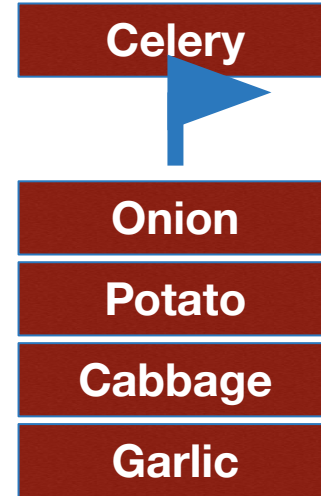
```
pop()  
push('Onion')  
push('Celery')  
push('Watermelon')  
pop()  
→ pop()  
push('Lettuce')
```

| |
|---------|
| Celery |
| Onion |
| Potato |
| Cabbage |
| Garlic |

What is a Stack ?

Instructions

```
pop()  
push('Onion')  
push('Celery')  
push('Watermelon')  
pop()  
→ pop()  
push('Lettuce')
```



What is a Stack ?

Instructions

```
pop()  
push('Onion')  
push('Celery')  
push('Watermelon')  
pop()  
→ pop()  
push('Lettuce')
```

Onion

Potato

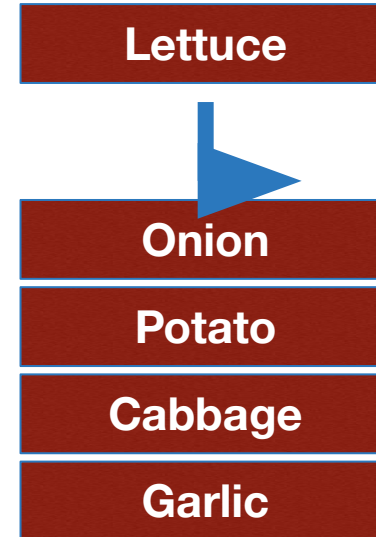
Cabbage

Garlic

What is a Stack ?

Instructions

```
pop()  
push('Onion')  
push('Celery')  
push('Watermelon')  
pop()  
pop()  
→ push('Lettuce')
```



What is a Stack ?

Instructions

```
pop()  
push('Onion')  
push('Celery')  
push('Watermelon')  
pop()  
pop()  
→ push('Lettuce')
```

| |
|---------|
| Lettuce |
| Onion |
| Potato |
| Cabbage |
| Garlic |

When and where stack is used?

- **Used by undo mechanisms in text editors.**
- **Used in compiler syntax checking for matching brackets and braces.**
- **Can be used to model a pile of books or plates.**
- **Used behind the scenes to support recursion by keeping track of previous function calls.**

How stack?

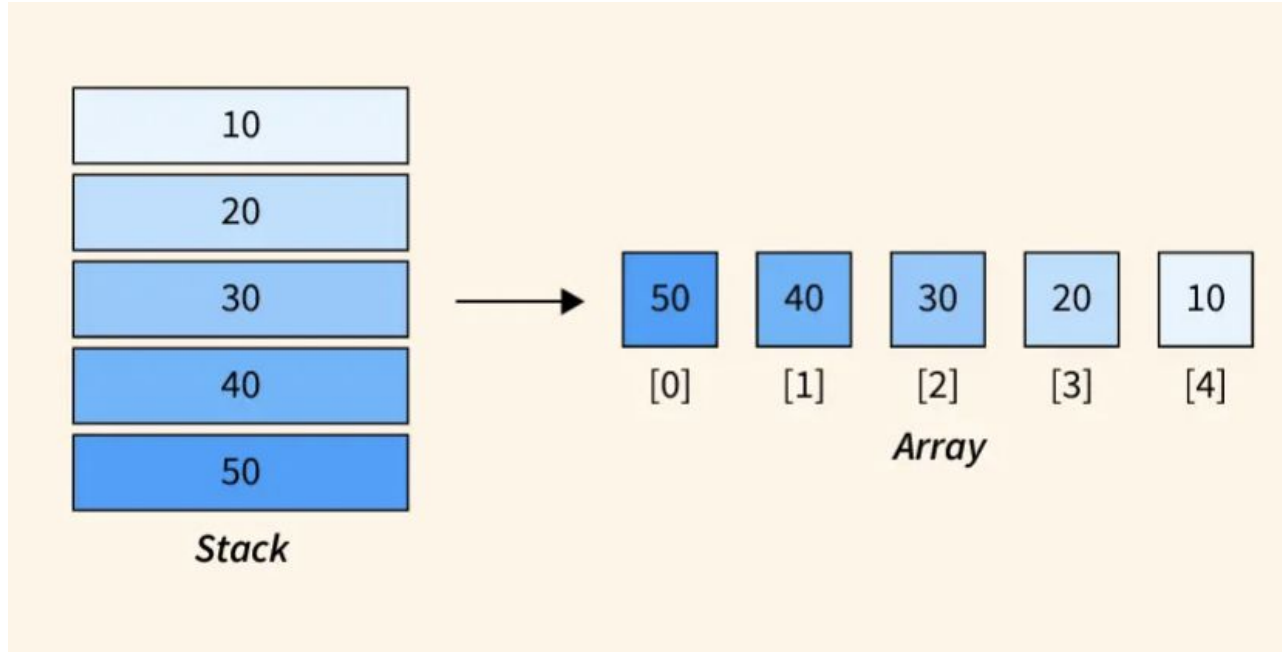
Stack Using Linked List

When and where stack is used?

- **Used by undo mechanisms in text editors.**
- **Used in compiler syntax checking for matching brackets and braces.**
- **Can be used to model a pile of books or plates.**
- **Used behind the scenes to support recursion by keeping track of previous function calls.**

Stack Using Array

Stack Using Array



Stack Using Array

| Stack operation | Operation on Array |
|------------------------|--|
| Push | Append at the end of an array |
| Pop | Delete the last element of an array |
| Peek / Top | Return the element at the last index. |
| Size | Return len of the list. |

Implementation: push and pop

```
class Stack:
    def __init__(self):
        self.stack = []

    # Add an item to the top of the stack.
    def push(self, item):
        self.stack.append(item)

    def pop(self):
        # Remove and return the top item of the stack.
        if not self.is_empty():
            return self.stack.pop()
        return None # Returns None if stack is empty.
```

Implementation: peek and size

```
def peek(self):  
    # Return the top item without removing it.  
    if not self.is_empty():  
        return self.stack[-1]  
    return None # Returns None if stack is empty.  
  
# Return the number of elements in the stack.  
def size(self):  
    return len(self.stack)
```

Stack Using Linked List

Stack Using Linked List

| Stack operation | Operation on Linked List |
|-----------------|--|
| Push | Insert at beginning of the linked list. |
| Pop | Delete at beginning of the linked list. |
| Peek / Top | Return the value at the head of the linked list. |
| Size | Return len of the array |

Implementation: Node & stack class

```
class Node:
    def __init__(self, data):
        self.data = data
        self.next = None

class Stack:
    def __init__(self):
        self.top = None
        self.count = 0 # Counter to track stack size
```

Implementation: push and peek

```
# Add an item to the top of the stack.
def push(self, item):
    new_node = Node(item)
    # Point new node to the previous top
    new_node.next = self.top
    self.top = new_node # Update top to the new node
    self.count += 1 # Increment counter

# Return the top item without removing it.
# Returns None if stack is empty.
def peek(self):
    return self.top.data if self.top else None
```

Implementation: pop and size

```
# Remove and return the top item of the stack.  
# Returns None if stack is empty.  
def pop(self):  
    if self.is_empty():  
        return None  
    popped_item = self.top.data  
    # Move top to the next node  
    self.top = self.top.next  
    self.count -= 1 # Decrement counter  
    return popped_item  
  
def size(self):  
    # Return the number of elements in the stack in O(1).  
    return self.count
```


Complexity Analysis

Time Complexity

| | |
|-----------|--------|
| Pushing | $O(1)$ |
| Popping | $O(1)$ |
| Peeking | $O(1)$ |
| Searching | $O(n)$ |
| Size | $O(1)$ |

Summary Quiz

END