Notes of Modern Quantum Chemistry, Szabo & Ostlund

hebrewsnabla

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0

spatial mol orb – ψ – i,j,k,...spatial basis fxn – ϕ – $\mu,\nu,\lambda,...$ spin orb – χ occ mol orb – a,b,c,...vir mol orb – r,s,t,...exact many-elec wfn – Φ approx many-elec wfn – Ψ exact energy – $\mathscr E$ approx energy – E

1

- 1.1
- 1.2
- 1.3

1.4 N-D Complex Vector Spaces

Suppose

$$\mathcal{O}|a\rangle = |b\rangle \tag{1.1}$$

$$\langle i \mid \mathcal{O} \mid j \rangle = O_{ij} \tag{1.2}$$

def the **adjoint** of \mathcal{O} as \mathcal{O}^{\dagger}

$$\langle a|\,\mathcal{O}^{\dagger} = \langle b| \tag{1.3}$$

$$\langle i \mid \mathcal{O}^{\dagger} \mid j \rangle = O_{ji}^*$$
 (1.4)

1.4.1 Change of Basis

$$|\alpha\rangle = \sum_{i} |i\rangle \langle i|\alpha\rangle = \sum_{i} |i\rangle U_{i\alpha}$$
 (1.5)

$$|i\rangle = \sum_{\alpha} |\alpha\rangle \langle i|\alpha\rangle = \sum_{\alpha} |\alpha\rangle U_{i\alpha}^*$$
 (1.6)

If i, α are all orthonormal, **U** must be unitary.

$$\Omega_{\alpha\beta} = \langle \alpha \, | \, \mathcal{O} \, | \, \beta \rangle = \dots \sum_{ij} U_{\alpha i}^* O_{ij} U_{j\beta} \tag{1.7}$$

or

$$\mathbf{\Omega} = \mathbf{U}^{\dagger} \mathbf{O} \mathbf{U} \tag{1.8}$$

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def

$$|\chi_{i}(\mathbf{x}_{1})\chi_{j}(\mathbf{x}_{2})\cdots\chi_{k}(\mathbf{x}_{N})\rangle \equiv \frac{1}{\sqrt{N!}}\begin{vmatrix} \chi_{i}(\mathbf{x}_{1}) & \chi_{j}(\mathbf{x}_{1}) & \cdots & \chi_{k}(\mathbf{x}_{1}) \\ \chi_{i}(\mathbf{x}_{2}) & \chi_{j}(\mathbf{x}_{2}) & \cdots & \chi_{k}(\mathbf{x}_{2}) \\ \vdots & \vdots & & \vdots \\ \chi_{i}(\mathbf{x}_{N}) & \chi_{j}(\mathbf{x}_{N}) & \cdots & \chi_{k}(\mathbf{x}_{N}) \end{vmatrix}$$
(2.1)

It can be further shortened to

$$|\chi_i \chi_j \cdots \chi_k\rangle$$
 (2.2)

- 2.2.4 The Hartree-Fock Approximation
- 2.2.5 The Minimal Basis H_2 Model
- 2.2.6 Excited Determinants

Suppose the ground state det

$$||psi_0\rangle = |\chi_1 \cdots \chi_a \cdots \chi_b \cdots \chi_N\rangle \tag{2.3}$$

thus, singly excited det

$$||psi_a^r\rangle = |\chi_1 \cdots \chi_r \cdots \chi_b \cdots \chi_N\rangle$$
 (2.4)

$$||psi_{ab}^{rs}\rangle = |\chi_1 \cdots \chi_r \cdots \chi_s \cdots \chi_N\rangle$$
 (2.5)