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Gate Assignment 4

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Download latex code from

https://github.com/ArunSiddardha/EE900/tree/main/ Gate assignment/Gate Assignment.tex Zero is at (a,0) and there are no poles. The ROC for this plot for the above function is given by

$$\Re\{s\} > \Re\{a\}$$
 (0.0.8)

GATE-EC 1997 Q.1.5

The Laplace Transform of $e^{at}cos(at)$

1)
$$\frac{s-a}{(s-a)^2+a^2}$$

2)
$$\frac{s+a}{(s-a)^2+a^2}$$

3)
$$\frac{1}{(s-a)^2}$$

4) None of these

SOLUTION

 $let h(t) = e^{at}cos(at)$

$$h(t) = e^{at} cos(at) (0.0.1)$$

$$=e^{at}\left(\frac{e^{iat}+e^{-iat}}{2}\right) \tag{0.0.2}$$

$$=\frac{e^{(i+1)at} + e^{(1-i)at}}{2} \tag{0.0.3}$$

Taking one-sided Laplace transform for h(t)

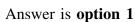
$$\mathcal{L}\left\{h(t)\right\}(s) = \frac{1}{2}\left(\mathcal{L}\left(e^{(i+1)at}\right)(s) + \mathcal{L}\left(e^{(i+1)at}\right)(s)\right)$$

(0.0.4)

We know that,
$$\mathcal{L}\{e^{at}\}(s) = \int_0^\infty e^{at} e^{st} dt = \frac{1}{s-a}$$
 (0.0.5)

$$= \frac{1}{2} \left(\frac{1}{s - (i+1)a} + \frac{1}{s - (1-i)a} \right)$$
(0.0.6)

$$= \frac{(s-a)}{(s-a)^2 + a^2}$$
(0.0.7)



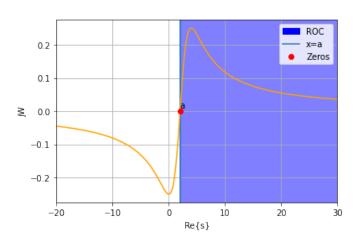


Fig. 1: ROC plot