

Gate Assignment

RONGALA ARUN SIDDARDHA - AI20BTECH11019

Download latex code from

https://github.com/ArunSiddardha/EE900/tree/main/Gate_assignment/Gate_Assignment.tex

The ROC for this plot for the above function is given by

$$\operatorname{Re}\{s\} > \operatorname{Re}\{a\} \quad (0.0.8)$$

GATE-EC 1997 Q.1.5

The Laplace Transform of $e^{at} \cos(at)$

1) $\frac{s-a}{(s-a)^2+a^2}$

2) $\frac{s+a}{(s-a)^2+a^2}$

3) $\frac{1}{(s-a)^2}$

4) None of these

SOLUTION

let $h(t) = e^{at} \cos(at)$

$$h(t) = e^{at} \cos(at) \quad (0.0.1)$$

$$= e^{at} \left(\frac{e^{iat} + e^{-iat}}{2} \right) \quad (0.0.2)$$

$$= \frac{e^{(i+1)at} + e^{(1-i)at}}{2} \quad (0.0.3)$$

Taking one-sided Laplace transform for $h(t)$

$$\mathcal{L}\{h(t)\}(s) = \frac{1}{2} \left(\mathcal{L}\left(e^{(i+1)at}\right)(s) + \mathcal{L}\left(e^{(1-i)at}\right)(s) \right) \quad (0.0.4)$$

We know that, $\mathcal{L}\{e^{at}\}(s) = \int_0^\infty e^{at} e^{st} dt = \frac{1}{s-a}$ (0.0.5)

$$= \frac{1}{2} \left(\frac{1}{s-(i+1)a} + \frac{1}{s-(1-i)a} \right) \quad (0.0.6)$$

$$= \frac{(s-a)}{(s-a)^2 + a^2} \quad (0.0.7)$$

Answer is **option 1**

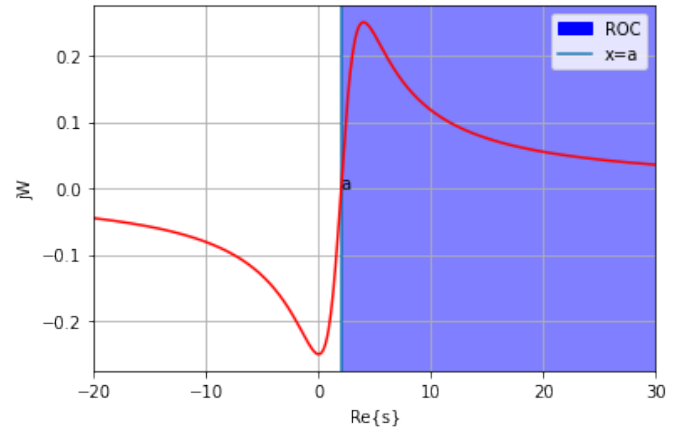


Fig. 1: ROC plot