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| Question Paper Code | 11077 |
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B.E / B.Tech. DEGREE EXAMINATIONS, APRIL/MAY 2021

Fourth Semester

Computer Science and Engineering

(Common to Information Technology)

CS8451 - Design and Analysis of Algorithm

(Regulations 2017)

Duration: 3 Hours

Max. Marks 100

Answer ALL Questions

PART-A (10 × 2 = 20 Marks)

| | | | |
|-----|--|----|-----|
| 1. | Give Euclid algorithm to compute GCD | K1 | CO1 |
| 2. | Compare the order of growth of $n(n-1)/2$ and n^2 | K4 | CO1 |
| 3. | State convex hull problem | K1 | CO1 |
| 4. | Give the general plan of divide and conquer algorithms | K1 | CO3 |
| 5. | What are memory functions? | K1 | CO4 |
| 6. | Define principle of optimality | K1 | CO3 |
| 7. | What do you mean by perfect matching in bipartite graphs | K2 | CO6 |
| 8. | When a linear program is said to be unbounded | K1 | CO6 |
| 9. | How NP-Hard problems are different from NP-Complete | K4 | CO5 |
| 10. | What are tractable and non-tractable problems | K1 | CO5 |

PART – B (5 × 13 = 65 marks)

11. a) (i) Find the closest asymptotic tight bound by solving the recurrence equation $T(n)=8T(n/2)+n^2$ with $T(1)=1$ using the recurrence tree method. 7 K3 CO2
- (ii) Derive the recurrence relation for Fibonacci series algorithm; also carry out the time complexity analysis. 6 K3 CO2

OR

- b) Use the most appropriate notation to indicate the time efficiency class of the sequential search algorithm in the worst case, best case, and the average case. 13 K3 CO2
12. a) (i) Sort the following set of elements using merge sort : 12, 24, 8, 71, 4, 23, 6, 89, 56. 6 K3 CO3
- (ii) Write an algorithm for Quick sort and write its time complexity with example list 5,3,1,9,8,2,4,7. 7 K3 CO3

OR

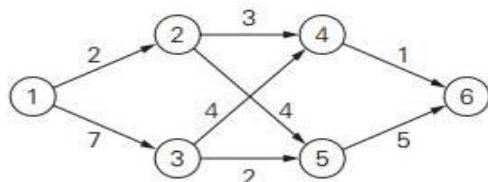
- b) (i) There are 4 people who need to be assigned to execute 4 jobs(one person per job) and the problem is to find an assignment with the minimum total cost. The assignment cost is given below, Solve the assignment problem by exhaustive search.
- | | Job 1 | Job 2 | Job 3 | Job 4 |
|----------|-------|-------|-------|-------|
| Person 1 | 9 | 2 | 7 | 8 |
| Person 2 | 6 | 4 | 3 | 7 |
| Person 3 | 5 | 8 | 1 | 8 |
| Person 4 | 7 | 6 | 9 | 4 |
- (ii) Explain the concept of Closest pair and Convex Hull problem and solve the problems using Brute force approach. 7 K2 CO1
13. a) How memory functions are used in dynamic knapsack? Write the algorithm and analyze its efficiency class. 13 K3 CO4

OR

- b) Analyze the algorithm of Optimal Binary Search Tree with suitable examples. 13 K4 CO4

14. a) Find Max-flow and Min-cut value for the problem given below.

13 K3 CO6



OR

- b) (i) For the given ranking matrix, Solve stable marriage problem

6 K3 CO6

| | <i>A</i> | <i>B</i> | <i>C</i> | <i>D</i> |
|----------|----------|----------|----------|----------|
| α | 1, 3 | 2, 3 | 3, 2 | 4, 3 |
| β | 1, 4 | 4, 1 | 3, 4 | 2, 2 |
| γ | 2, 2 | 1, 4 | 3, 3 | 4, 1 |
| δ | 4, 1 | 2, 2 | 3, 1 | 1, 4 |

- (ii) Maximize $p=2x+3y+z$ using Simplex method.

7 K3 CO6

Subject to $x+y+z \leq 40$, $2x+y-z \geq 10$, $-y+z \geq 10$, $x \geq 0$, $y \geq 0$

15. a) Find the optimal jobs assigned for a person with the following cost matrix using Branch and Bound methods.

13 K4 CO4

| | Job 1 | Job 2 | Job 3 | Job 4 |
|----------|-------|-------|-------|-------|
| Person 1 | 9 | 2 | 7 | 8 |
| Person 2 | 6 | 4 | 3 | 7 |
| Person 3 | 5 | 8 | 1 | 8 |
| Person 4 | 7 | 6 | 9 | 4 |

OR

- b) Solve the following instance of Knapsack problem by branch and bound algorithm.

13 K4 CO4

$W=15$

| ITEM | WEIGHT | PROFIT |
|------|--------|--------|
| 1 | 5 | 40 |
| 2 | 7 | 35 |
| 3 | 2 | 18 |
| 4 | 4 | 4 |
| 5 | 5 | 10 |
| 6 | 1 | 2 |

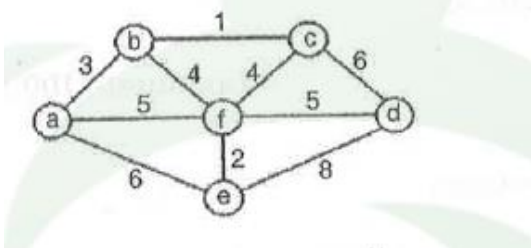
PART C (1 × 15 = 15)

16. a) Give the pseudo code for Prim's Algorithm and apply the same to

15

K3

CO3



find MST.

OR

- b) Solve the following recurrence relations :

15

K3

CO2

$$X(n) = x(n-1) + 5 \text{ for } n > 1, x(1) = 0$$

$$X(n) = 3x(n-1) \text{ for } n > 1, x(1) = 4$$

$$X(n) = x(n/2) + n \text{ for } n > 1, x(1) = 1 \text{ [solve for } n = 2^k]$$