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SAIRAM
DIGITAL RESOURCES

UNIT NO 1 ANALOG MODULATION



EC8394

1.2.1 THEORY OF AMPLITUDE MODULATION

ANALOG AND DIGITAL COMMUNICATION

ELECTRONICS & COMMUNICATION ENGINEERING



MODULATION

➤ Defined as

“ The process by which some characteristics of a signal called carrier varied in accordance with the instantaneous value of another signal called modulating signal “

- The information bearing signal is called modulating signal
- The signal resulting from process of modulation is known as modulated signal

TYPES OF MODULATION

- Sine wave (carrier) described by 3 parameters: amplitude, frequency and phase.
- Let carrier signal be:

$$v(t) = A \sin (\omega t + \phi)$$

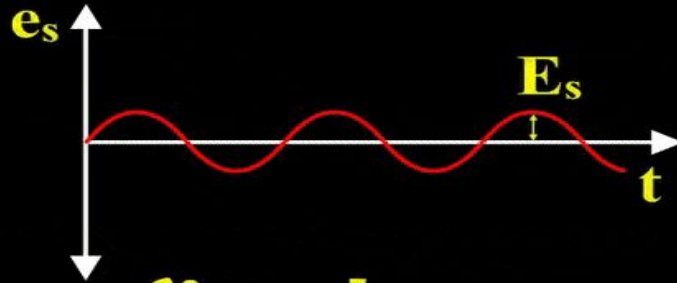
So can have

- ❖ – **Amplitude modulation (AM)**
- ❖ – **Frequency modulation (FM)**
- ❖ – **Phase modulation (PM)**

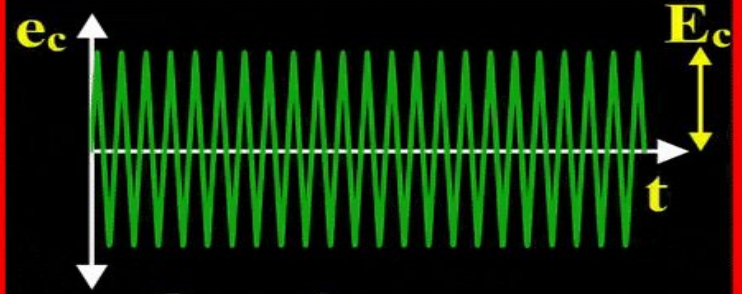
Frequency and phase combined are known as Angle Modulation

AMPLITUDE MODULATION

- The amplitude of the carrier is changed in accordance with the instantaneous value of modulating signal
- Carrier : $c(t) = V_c \cos(2\pi f_c t + \varphi)$
modulating signal $v(t) = V_m \cos(2\pi f_m t)$
- Information is contained in the envelop



Signal wave

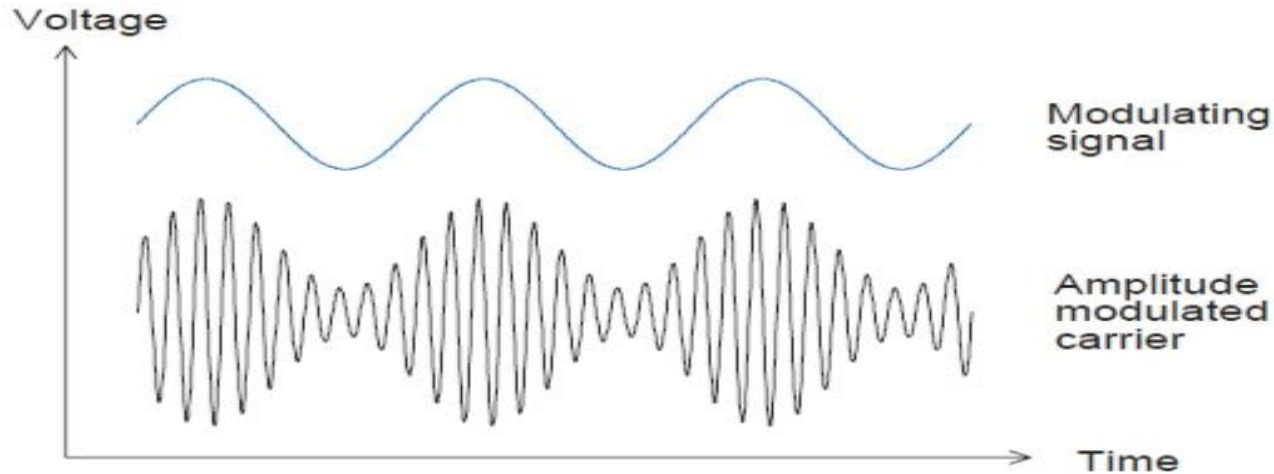


Carrier wave



AM Wave

AMPLITUDE MODULATION



Frequency representation of AM wave: (Double sideband – full carrier)

Upper sideband:

- The band of the frequency range between f_c and $f_c + f_m$ is called as upper sideband(USB).

Lower sideband:

- The band of the frequency range between f_c and $f_c - f_m$ is called as lower sideband(LSB).

Upper sideband frequency:

- Any of the frequency that lies between f_c and $f_c + f_m$ is called an upper sideband frequency.

Lower sideband frequency:

- Any of the frequency that lies between f_c and $f_c - f_m$ is called a lower sideband frequency.

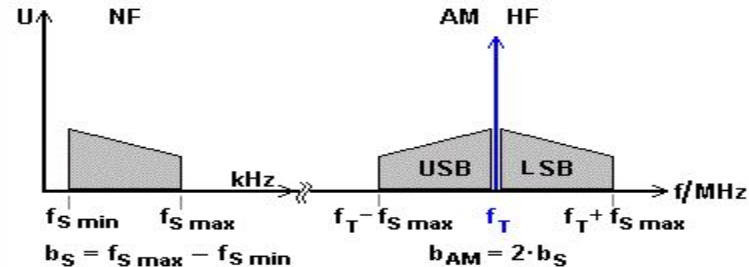
Bandwidth:

- It is the difference between upper sideband frequency to the lower sideband frequency.
- Upper side band frequency = $f_c + f_m$
- Lower side band frequency = $f_c - f_m$

$$BW = (f_c + f_m) - (f_c - f_m)$$

Therefore,

$$BW = 2f_m$$



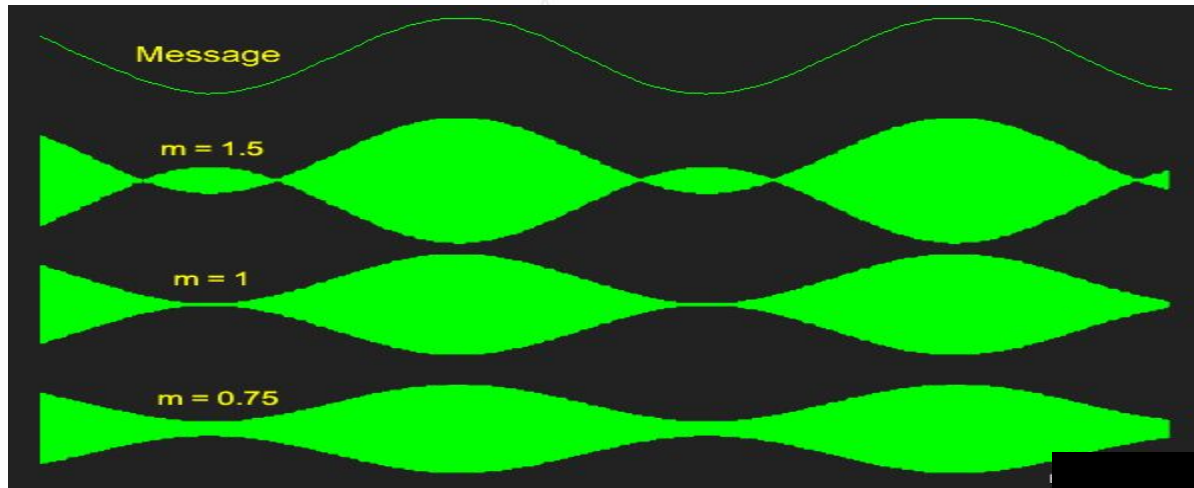
Coefficient of modulation or modulation index:

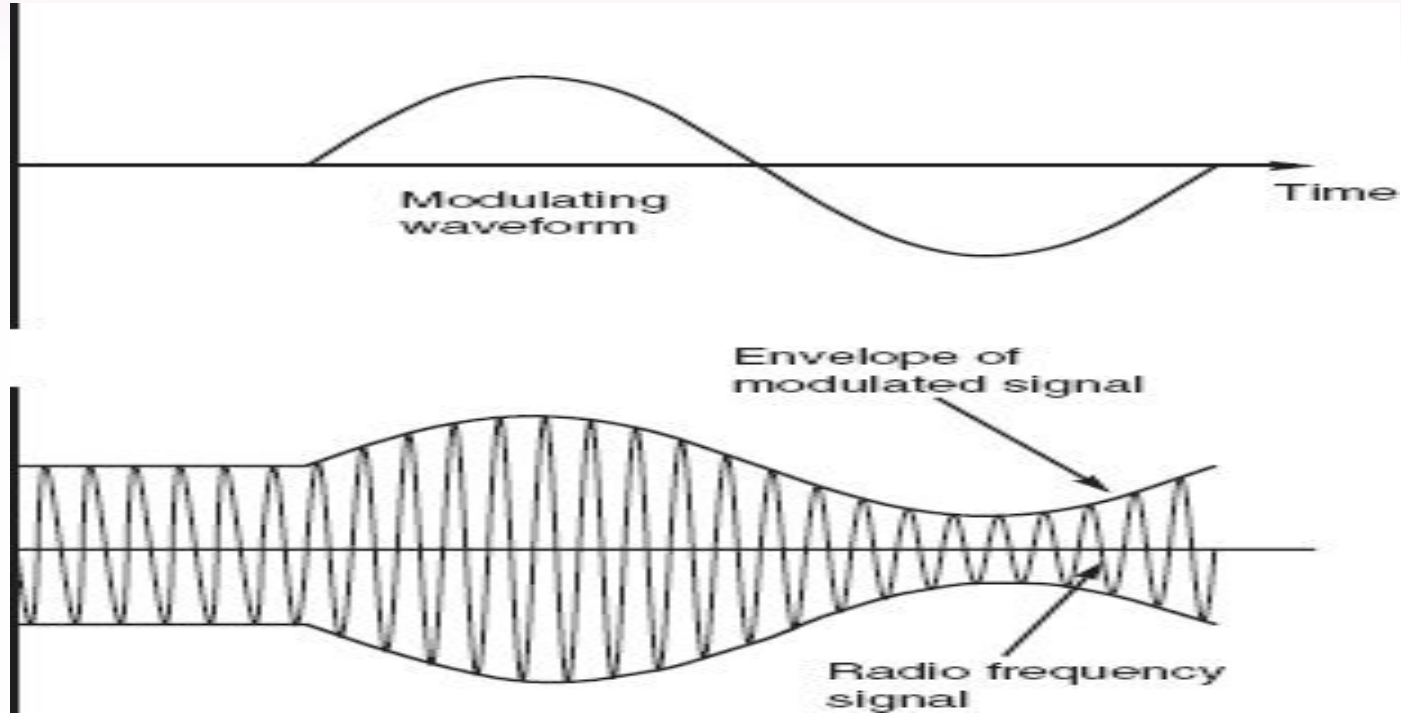
- The ratio between the maximum amplitude of the modulating signal to the maximum amplitude of the carrier signal is called a modulation index.
- Modulation index, $m = V_m / V_c$
- Where V_c be the maximum amplitude of the modulating signal.
- Value of V_m must be less than the value of V_c
- Hence the maximum value of the modulation index will be equal to 1 when $V_m = V_c$
- The minimum value will be zero.
- If the modulation index is higher than 1, then it is called overmodulation.

modulation index of an amplitude modulated signal is defined as the measure or extent of amplitude variation about an un-modulated carrier

Percentage of modulation:

- Whenever the coefficient of a modulation index is expressed in terms of percentage then it is called a percentage of modulation.
- $M = (V_m / V_c) * 100$





- Consider the upper highest peak value as $V_{\max} = E_m + E_c$
- Upper lowest peak value as $V_{\min} = E_m - E_c$
- Downward highest peak value as $-V_{\max} = -E_m - E_c$

Downward lowest peak value as $-V_{\min} = -E_m + E_c$

$$V_{\max} + V_{\min} = E_m + E_c + E_m - E_c$$

$$V_{\max} + V_{\min} = 2 E_m$$

$$E_m = (V_{\max} + V_{\min}) / 2$$

Similarly,

$$V_{\max} - V_{\min} = E_m + E_c - E_m + E_c$$

$$V_{\max} - V_{\min} = 2 E_c$$

$$E_c = (V_{\max} - V_{\min}) / 2$$

Therefore,

$$m = V_m / V_c = E_m / E_c$$

Therefore,

$$m = (V_{\max} + V_{\min}) / (V_{\max} - V_{\min})$$

$$M = ((V_{\max} + V_{\min}) / (V_{\max} - V_{\min})) * 100$$

Voltage representation of AM wave: (Equation of double sideband- full carrier)

From the diagram we can observe the following:

$$v_m(t) = E_m \sin \omega_m t$$

where, $v_m(t)$ be the instantaneous value of the modulating signal.

E_m be the maximum amplitude of the modulating signal.

ω_m be the angular frequency of the modulating signal.

$$v_c(t) = E_c \sin \omega_c t$$

where, $v_c(t)$ be the instantaneous value of the carrier signal.

E_c be the maximum amplitude of the carrier signal.

ω_c be the angular frequency of the carrier signal.

Therefore for amplitude modulated signal,

$$VAM(t) = (E_c + E_m \sin \omega_m t) \sin \omega_c t$$

$$VAM(t) = E_c \sin \omega_c t + E_m \sin \omega_m t \sin \omega_c t$$

$$VAM(t) = E_c \sin \omega_c t + m E_c \sin \omega_m t \sin \omega_c t \quad [\text{since } m = E_m / E_c]$$

$$VAM(t) = E_c \{ \sin \omega_c t + m \sin \omega_m t \sin \omega_c t \}$$

$$VAM(t) = E_c \{ \sin \omega_c t + m/2 \{ \cos (\omega_c - \omega_m)t - \cos (\omega_c + \omega_m)t \} \}$$

$$[\text{since } \sin A \sin B = 1/2 (\cos (A-B) - \cos (A+B))]$$

$$VAM(t) = E_c \{ \sin 2\pi f_c t + m/2 \{ \cos 2\pi (f_c - f_m)t - \cos 2\pi (f_c + f_m)t \} \}$$

$$VAM(t) = E_c \sin 2\pi f_c t - m E_c / 2 \{ \cos 2\pi (f_c + f_m)t - \cos 2\pi (f_c - f_m)t \}$$

- E_c be the amplitude of the carrier signal.
- $m E_c / 2$ be the amplitude of the USB signal.
- $m E_c / 2$ be the amplitude of the LSB signal.
- f_c be the frequency of the carrier signal.
- $f_c + f_m$ be the frequency of the USB signal.
- $f_c - f_m$ be the frequency of the LSB signal

Power distribution of AM wave: $P_c = V_{rms}^2 / \text{load resistor}$

$$\text{i.e., } P_c = V_{rms}^2 / R$$

where, V_{rms} be the root mean square voltage.

P_c be the power of the carrier signal.

$$V_{rms} = V_m / \sqrt{2} = E_c / \sqrt{2}$$

$$P_c = (E_c / \sqrt{2})^2 / R$$

$$P_c = E_c^2 / 2R$$

$$P_{LSB} = P_{USB} = (m E_c / 2)^2 / 2R$$

$$P_{LSB} = P_{USB} = m^2 E_c^2 / 8R$$

$$P_{LSB} = P_{USB} = (m^2 / 4) * (E_c^2 / 2R)$$

$$P_{LSB} = P_{USB} = (m^2 / 4) * P_c$$

Total power $PT = P_c + P_{LSB} + P_{USB}$

$$PT = P_c + (m^2 / 4) * P_c + (m^2 / 4) * P_c$$

$$PT = P_c + 2(m^2 / 4) * P_c$$

$$PT = P_c + (m^2 / 2) * P_c$$

$$PT = P_c (1 + m^2 / 2)$$

Where, m is the modulation index.

PT is the total power.

P_c is the power of the carrier signal.

MULTIPLE CHOICE QUESTIONS

<https://forms.gle/vWCyETgxrySpcjAW7>

VIDEO LINK OF AMPLITUDE MODULATION

https://www.youtube.com/watch?v=fGf_ng7qljl&list=RDCMUCXvKiwWVq5mvrflCSfzmyug&index=1